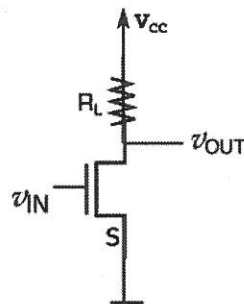


Solution attached

# CSU0007 Basic Electronics, Final Exam

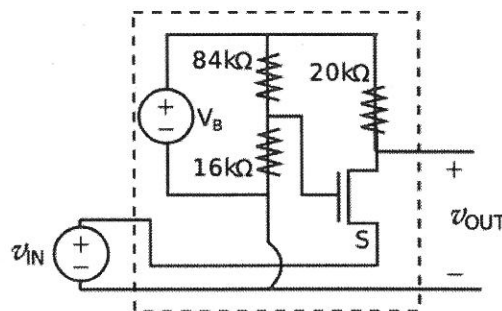
- Exam time: 3:30PM-5:30pm, Jan. 15th, 2021.
- 110 points in total.
- MOSFET parameters:  $K=1\text{mA/V}^2$  and  $V_T=1\text{V}$ . For difference amplifiers, we assume identical MOSFETs.

- (20 points) Consider this specification: The noise margin is 0.5V for logical 0 and 0.5V for logical 1. The forbidden region is from 0.9V to 1.5V. In order to build a MOSFET inverter (shown in the following figure) to meet this specification, what would be the maximum feasible value of ratio  $\frac{L}{W}$ ? Suppose  $R_N=5\text{k}\Omega$ ,  $R_L=8\text{k}\Omega$ , and  $V_{cc}=3.3\text{V}$ , and consider the SR model:

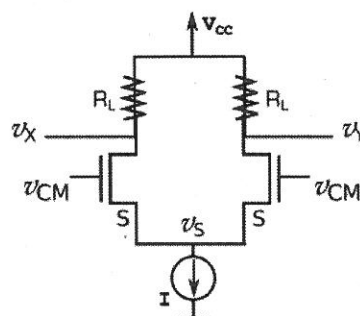


- (30 points) For the MOSFET circuit in Question 1, now consider the SCS model.

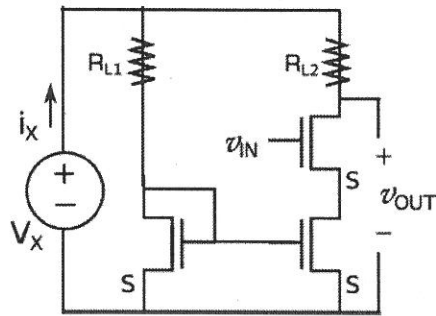
- (20 points) We know that for the MOSFET to operate in the saturation region, input voltage  $v_{IN}$  should be constrained to a certain range. Given a constant  $V_{CC}$ , would the size of this range increase or decrease if we increase  $R_L$ ? Explain your analysis.
- (10 points) Compute  $\frac{V_{OUT}}{V_{IN}}$  the large-signal voltage gain, given  $V_{IN} = 2\text{V}$ . Suppose  $R_L = 5\text{k}\Omega$  and  $V_{cc}=5\text{V}$ .
- (20 points) For the following non-inverting amplifier circuit, to make a small-signal ~~output~~ <sup>input</sup> resistance smaller than  $50\Omega$ , what should be the minimum value of  $V_B$ ?



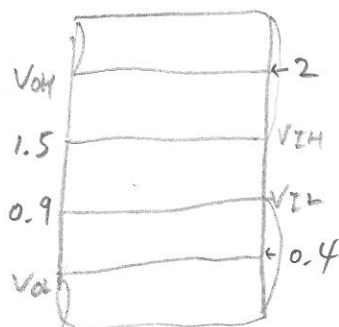
- (20 points) For the following difference amplifier in the common mode, suppose that  $I = 0.64\text{mA}$ ,  $V_{CC}=3\text{V}$ ,  $R_L=2\text{k}\Omega$ , and  $v_{CM}=2\text{V}$ . Does  $v_{CM}=3.5\text{V}$  violate the saturation discipline? Explain.



5. (20 points) For the following circuit, suppose  $R_{L1}=10\text{k}\Omega$  and  $R_{L2}=5\text{k}\Omega$ , and  $V_X=5\text{V}$ . If  $v_{IN}=0\sim 20\text{V}$ , what would be the range of  $i_x$ ?



① From Homework 4:



To make  $V_{OL} > V_{CC} \times \frac{R_{ON}}{R_{ON} + R_L}$

$$\Rightarrow 0.4 > 3.3 \times \frac{R_{ON}}{R_{ON} + 8}$$

$$\Rightarrow R_{ON} < \frac{8}{7.25}$$

$$\Rightarrow 5 \times \frac{L}{W} < \frac{8}{7.25} \Rightarrow \frac{L}{W} < 0.22 \left( \frac{8}{36.25} \right)$$

$$\frac{32}{145}$$

②.1 From Homework 5: Decrease. See Question 3.1 in Homework 5 for detail.

②.2  $i_D = \frac{1}{2} k (V_{IN} - V_T)^2 = \frac{V_{CC} - V_{OUT}}{R_L}$

$$\Rightarrow \frac{1}{2} = \frac{5 - V_{OUT}}{5} \Rightarrow V_{OUT} = 2.5 \Rightarrow \frac{V_{OUT}}{V_{IN}} = \frac{2.5}{2} = 1.25$$

③ From Homework 6, Question 3:

$$r_{\pi} = \frac{1}{g_m} = \frac{1}{k(V_{GS} - V_T)} < 50 \Rightarrow V_{GS} - V_T > 20$$

$$\Rightarrow V_B \times \frac{16}{100} - V_{IN} > 21$$

$$\Rightarrow V_B > \frac{100}{16} (V_{IN} + 21)$$

④ From Homework 7, Question 1.2:

We should have

$$V_{CM} < V_T + V_{CC} - \frac{I}{2} R_L = 3.36 \text{ V}$$

$\Rightarrow V_{CM} = 3.5 \text{ V}$  violates the discipline.

(This time you will still receive score if you didn't put  $V_{IN}$  in the formula, because I think people might be misled by my mistake in the answer of Question 4.3 in Homework 6 (which I corrected now).)

⑤ This configuration is like:

where the current source is driven by



In any case, there will be some current flowing through  $R_L$ .

$$\frac{1}{2} k (V_{DS} - V_T)^2 = \frac{V_X - V_{DS}}{R_{L1}}$$

$$\Rightarrow \frac{1}{2} (V_{DS} - 1)^2 = \frac{5 - V_{DS}}{10}$$

$$\Rightarrow V_{DS} = 1.8 \text{ V} \Rightarrow I = 0.32 \text{ mA}$$

Now, the MOSFET at the lower-right corner ensure that the current flowing through  $R_{L2}$  will never be larger than  $0.32 \text{ mA}$ .

To ensure  $M_1$  works in saturation, we must make  $v_T \geq 0.8 \text{ V}$

To ensure  $M_1$  works in saturation, we must make  $V_{GS1} \leq 3.4 - 0.8 = 2.6 \text{ V}$

Finally, we can determine  $V_{IN}$  to make everything work:  $\frac{1}{2} k (V_{IN} - 0.8 - 1)^2 = 0.32$

$$\Rightarrow V_{IN} = 2.6 \text{ V}$$

$$\text{and } V_{GS1} = 1.8 \text{ V} < 2.6 \text{ V}$$

Therefore,  $V_{IN} = 0 \sim 20 \text{ V}$

3 would make  $i_X = 0.32 \sim 0.64 \text{ mA}$