

Name: Solution

Student ID: \_\_\_\_\_

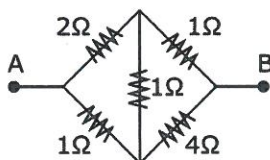
*Solution attached*

National Taiwan Normal University  
Department of Computer Science and Information Engineering  
**CSU0007 - Basic Electronics**  
**Midterm Exam (Nov. 13, 2020)**

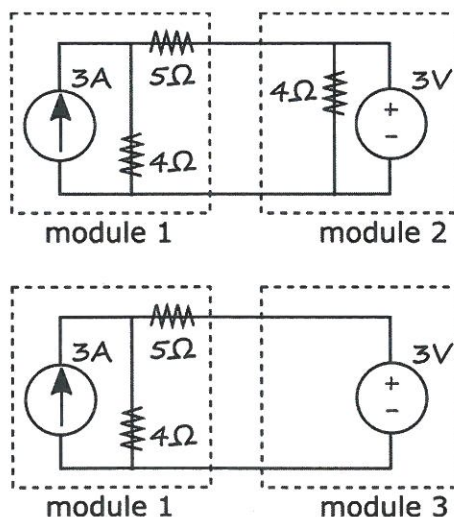
Exam time: 2 hours (3:30pm-5:30pm)

Clearly label your answer, and clearly state each step of your answer.

1. (20 points) **KCL and KVL.** For the following circuit, determine the equivalent resistance from the view of A-B. (Hint: attach a testing voltage source).



2. (30 points) **Circuit Transformation.** For the following circuits, answer two questions.
- 2a. (20 points) Is it true that module 2 and module 3 are equivalent from the view of module 1? Explain your answer.
- 2b. (10 points) In Homework 3, we have discussed a plausible approach of determining the Thévenin equivalent resistance by using only a multimeter. Now, think about the circuits given here and give one reason why in reality we may still choose to use a potentiometer (i.e., a variable resistor) to determine the Thévenin equivalent resistance.

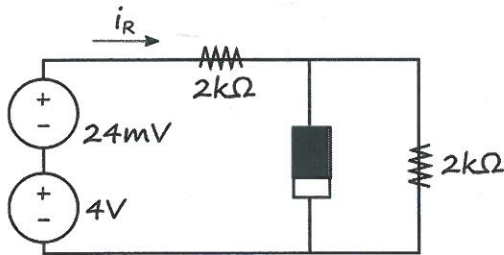


3. (15 points) **Static Discipline.** Consider the following specification:  $V_{IL}=1.8V$ ,  $V_{IH}=3.3V$ ,  $V_{OL}=1.2V$ , and  $V_{OH}=4.3V$ . Answer two questions.
- 3a. (5 points) What is the noise margin for a logic 1?
- 3b. (10 points) Can the following electronic module meet the above specification? Why or why not? The module produces voltage level  $V_{OUT}=1V$  for sending a logic 0 and  $V_{OUT}=4.5V$  for sending a logic 1. The module can interpret input signals between 0V and 2V as a logic 0 and input signals higher than 3V as a logic 1.

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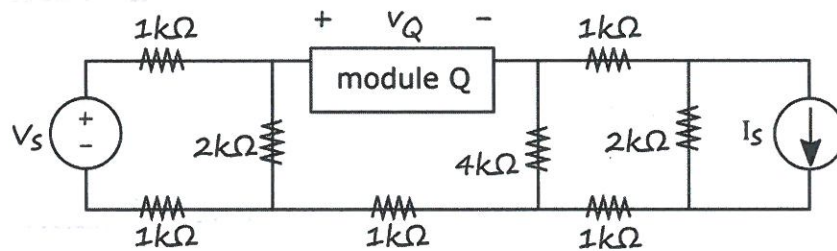
4. (15 points) **Small-Signal Analysis.** For the following circuit,
- 4a. (5 points) Compute the small-signal linear resistance  $r_d$ .
- 4b. (10 points) Compute current  $i_R$ .



$$i_D = \begin{cases} K \cdot v_D^2 & \text{for } v_D > 0 \\ 0 & \text{otherwise} \end{cases}$$

Assuming  $K = 1 \text{ mA/V}^2$

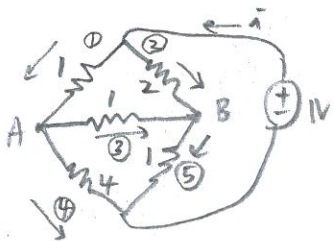
5. (20 points) **Comprehensive Analysis.** Consider the following electronic module, called module Q. Module Q will work correctly only if the voltage across it is higher than or equal to 2V. When it is working, module Q is equivalent to a linear resistor with resistance  $4k\Omega$  from the view of the rest of the circuit. Now, in the following configuration, given  $V_S = 2V$ , what is the minimum value of  $I_S$  to make module Q work correctly?



This is the end of the exam questions.

Start your answer here:

### ① Solution 1: Symbolic Computation



$$\begin{cases} \hat{i}_1 = \hat{i}_3 + \hat{i}_4 \\ \hat{i}_2 = \hat{i}_5 - \hat{i}_3 \\ \hat{i}_1 + 4\hat{i}_4 = 2\hat{i}_2 + \hat{i}_5 \\ 4\hat{i}_4 = \hat{i}_3 + \hat{i}_5 \\ 2\hat{i}_2 = \hat{i}_1 + \hat{i}_3 \end{cases}$$

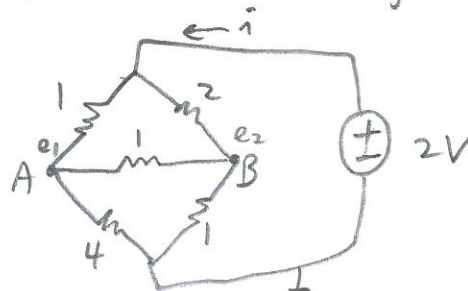
$$R_{eq} = \frac{1V}{i} = \frac{\hat{i}_1 + 4\hat{i}_4}{i}$$

$$\begin{bmatrix} 1 & 0 & -1 & -1 & 0 & 0 \\ 0 & 1 & 1 & 0 & -1 & 0 \\ 1 & -2 & 0 & 4 & -1 & 0 \\ 0 & 0 & 1 & -4 & 1 & 0 \\ 1 & -2 & 1 & 0 & 0 & 0 \end{bmatrix}$$

dependent

Solve the matrix using  
Gaussian's elimination method

### Solution 2: Node Analysis



$$\text{node A: } \frac{2 - e_1}{1} = \frac{e_1 - e_2}{1} + \frac{e_1 - 0}{4}$$

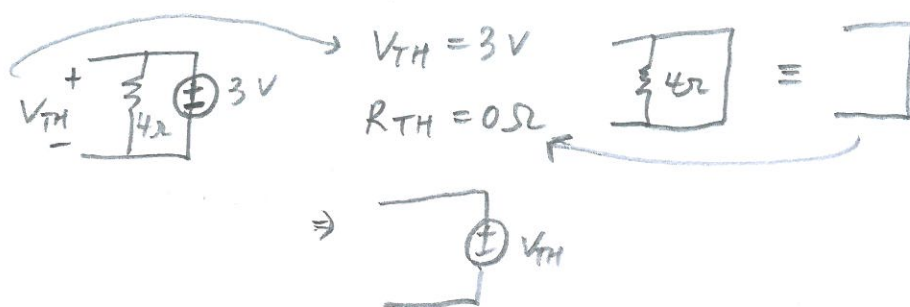
$$\text{node B: } \frac{2 - e_2}{2} = \frac{-(e_1 - e_2)}{1} + \frac{e_2 - 0}{1}$$

$$\Rightarrow e_1 = \frac{48}{37}, e_2 = \frac{34}{37}$$

$$\Rightarrow i = \frac{2 - e_1}{1} + \frac{2 - e_2}{2} = \frac{46}{37}$$

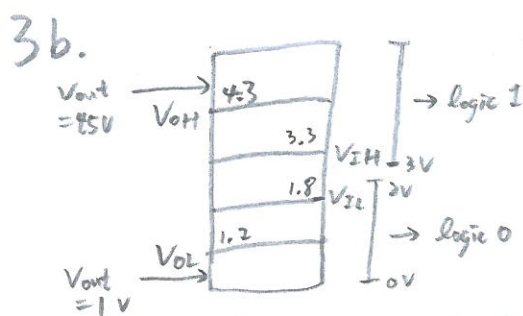
$$\Rightarrow R_{eq} = \frac{2V}{i} = \frac{37}{23} \Omega$$

② 2a. Yes. According to Thevenin's Theorem,



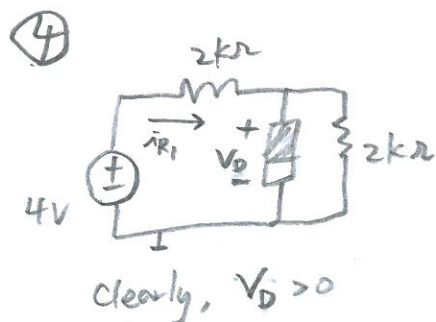
2b. The internal resistance could be very small, and therefore the current flowing through the multimeter could be very large and could burn out the multimeter. ★

③ 3a. Noise margin is  $4.3 - 3.3 = 1V$ , from 3.3V to 4.3V

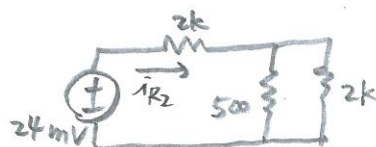


Also, refer to Example 5.1 in the textbook ~

- Yes.  $\therefore$
- ①  $V_{out}$  for logic 1 is higher than  $V_{OH}$
  - ②  $V_{out}$  for logic 0 is lower than  $V_{OL}$
  - ★ ③  $V_{in}$  higher than  $V_{IH}$  can be interpreted as logic 1
  - ★ ④  $V_{in}$  lower than  $V_{IL}$  can be interpreted as a logic 0.



$$r_d = \frac{1}{f(V_D)|_{V_D=V_D}} = \frac{1}{2kV_D} = 500\Omega$$



$$\hat{I}_{R2} = \frac{24}{2 + \frac{0.5 \times 2}{0.5 + 2}} = 10\mu A$$

$$KCL \Rightarrow \frac{4 - V_D}{2} = 1kV_D + \frac{V_D}{2}$$

$$\Rightarrow 2V_D + 2V_D - 4 = 0$$

$$\Rightarrow V_D = 1V \Rightarrow \hat{I}_{R1} = \frac{3}{2} = 1.5mA$$

$$\Rightarrow \hat{I} = \hat{I}_{R1} + \hat{I}_{R2} = 1.51mA$$

Also, refer to the exercise ② on P57 in the lecture note ~

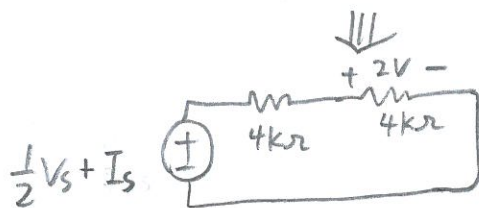
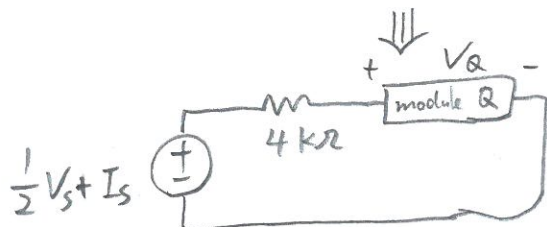
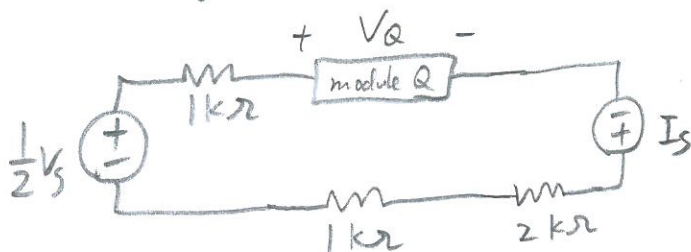


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⑤ The original circuit is equivalent to the following:

(Use Thévenin's Theorem)



$$\frac{1}{2}V_s + I_s = 4$$

given  $V_s = 2V \Rightarrow I_s = 3 \text{ mA}$

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Important take-home message from this problem is the "load effect", as we've discussed last week in class.