

# Aufgabenbeschreibung für die Hausarbeit im Modul MP2

First step, the necessary packages will be imported. Numpy and Pandas for editing the data; Import the dataset from sklearn; Seaborn and Matplotlib for plotting; StandardScaler and MinMaxScaler for processing data.

```
In [ ]: import pandas as pd
        from sklearn.datasets import fetch_california_housing
        import seaborn as sns
        import matplotlib.pyplot as plt
        from sklearn.preprocessing import StandardScaler, MinMaxScaler
```

## 1, Beschreibung der Bestandteile des Datensatzes

- Das Data wird von sklearn.dasets heruntergeladen.
- Die Daten stammen aus der US-Volkszählung von 1990 für Blockgruppen in Kalifornien. Die Daten wurden von Forschern verarbeitet und zur Verfügung gestellt, die sie in einem statistischen Analysepapier verwendeten: „Sparse Spatial Autoregressions“ von Pace und Barry (1997).  
<https://www.kaggle.com/datasets/camnugent/california-housing-prices>
- Es gibt insgesamt 20640 Datensätze und 8 Attribute: ['MedInc', 'HouseAge', 'AveRooms', 'AveBedrms', 'Population', 'AveOccup', 'Latitude', 'Longitude']
  - Medianeinkommen (Median Income)
  - Medianes Alter der Wohnbevölkerung (Median Age of Housing Units)
  - Durchschnittliche Anzahl der Zimmer (Average Number of Rooms)
  - Durchschnittliche Anzahl der Schlafzimmer (Average Number of Bedrooms)
  - Bevölkerung pro Hektar (Population per Acre)
  - Anteil an Haushalten, die nicht Eigentümer sind (Percentage of Households Not Owner Occupied);
  - Latitude;
  - Longitude
- Jedes Attribute hat 20640 Ausprägungen; Die Data ist type float64. Die Werte von Latitude und Longitude können nicht nur positive sondern auch negative sein. Es gibt auch eine option von diesem Data. Das heißt, dass das 'target' column auch zu zeigen ist, wenn es nötig ist.

Import data and define it as HOUSING, then to show original data shape and columns names to have better compact overview.

```
In [ ]: housing = fetch_california_housing()
        print(housing.data.shape, housing.target.shape)
```

```
print(housing.feature_names[:])
```

```
(20640, 8) (20640,)
['MedInc', 'HouseAge', 'AveRooms', 'AveBedrms', 'Population', 'AveOccup', 'Latitude', 'Longitude']
```

Change original data to dataframe type then modify it and add a target column in it, also showing the attribute dtype and new shape.

(target feature here means price: Jeder Datensatz repräsentiert ein Haus in Kalifornien. Die Zielvariable ist der Medianwert des Hauses in 100.000 USD-Einheiten.)

```
In [ ]: df = pd.DataFrame(housing.data, columns=housing.feature_names)
# Add the target variable (if applicable)
if hasattr(housing, 'target'):
    df['target'] = housing.target
df_new = df
print(df_new.dtypes, df_new.shape)
```

```
MedInc      float64
HouseAge    float64
AveRooms    float64
AveBedrms   float64
Population  float64
AveOccup    float64
Latitude    float64
Longitude   float64
target      float64
dtype: object (20640, 9)
```

## 2, Deskriptive Analyse des Datensatzes

Es gibt insgesamt 9 Attribute in df\_new:

- MedInc
- HouseAge
- AveRooms
- AveBedrms
- Population
- AveOccup
- Latitude
- Longitude
- target

Let us have a short view of data

```
In [ ]: df_new.head()
```

Out [ ]:

	MedInc	HouseAge	AveRooms	AveBedrms	Population	AveOccup	Latitude	L
0	8.3252	41.0	6.984127	1.023810	322.0	2.555556	37.88	
1	8.3014	21.0	6.238137	0.971880	2401.0	2.109842	37.86	
2	7.2574	52.0	8.288136	1.073446	496.0	2.802260	37.85	
3	5.6431	52.0	5.817352	1.073059	558.0	2.547945	37.85	
4	3.8462	52.0	6.281853	1.081081	565.0	2.181467	37.85	

Check if there is any zero value inside, in this data there is no error.

In [ ]:

df\_new.info()

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 20640 entries, 0 to 20639
Data columns (total 9 columns):
#   Column      Non-Null Count  Dtype
---  -
0   MedInc      20640 non-null  float64
1   HouseAge    20640 non-null  float64
2   AveRooms    20640 non-null  float64
3   AveBedrms   20640 non-null  float64
4   Population  20640 non-null  float64
5   AveOccup    20640 non-null  float64
6   Latitude    20640 non-null  float64
7   Longitude   20640 non-null  float64
8   target      20640 non-null  float64
dtypes: float64(9)
memory usage: 1.4 MB
```

Use built-in function '.describe()' to check many kinds of characters of data.

- attribute: MedInc HouseAge AveRooms AveBedrms Population AveOccup Latitude Longitude target
- max: 15.000100 52.000000 141.909091 34.066667 35682.000000 1243.333333 41.950000 -114.310000 5.000010
- min: 0.499900 1.000000 0.846154 0.333333 3.000000 0.692308 32.540000 -124.350000 0.149990
- mean: 3.870671 28.639486 5.429000 1.096675 1425.476744 3.070655 35.631861 -119.569704 2.068558
- std: 1.899822 12.585558 2.474173 0.473911 1132.462122 10.386050 2.135952 2.003532 1.153956

In [ ]:

df\_new.describe()

Out[ ]:

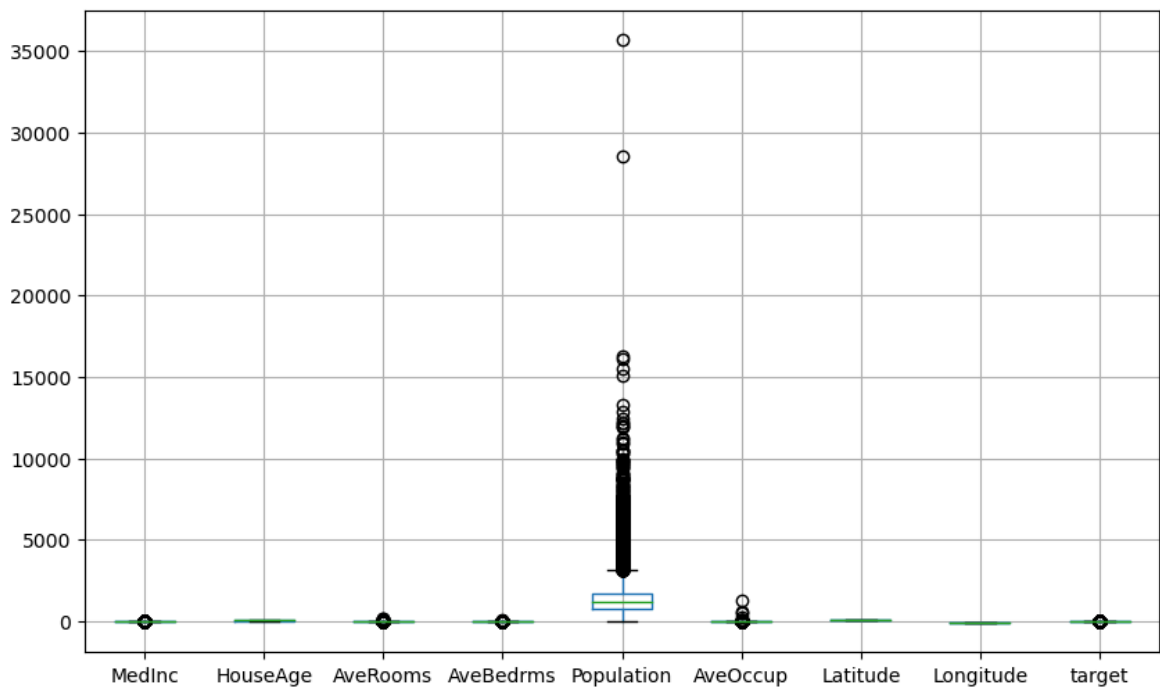
	MedInc	HouseAge	AveRooms	AveBedrms	Population	
count	20640.000000	20640.000000	20640.000000	20640.000000	20640.000000	20640.000000
mean	3.870671	28.639486	5.429000	1.096675	1425.476744	
std	1.899822	12.585558	2.474173	0.473911	1132.462122	
min	0.499900	1.000000	0.846154	0.333333	3.000000	
25%	2.563400	18.000000	4.440716	1.006079	787.000000	
50%	3.534800	29.000000	5.229129	1.048780	1166.000000	
75%	4.743250	37.000000	6.052381	1.099526	1725.000000	
max	15.000100	52.000000	141.909091	34.066667	35682.000000	12

For the distribution two methodes are used here: boxplot and histplot

- Box plots are an effective way to visualize the distribution of data, helping you quickly understand the general characteristics of your data and identify potential outliers. In this case, there are several outliers values in attribut Population.
- Histplot is a function used to create histograms. It is often used to visualize data distribution. A histogram is a statistical graph that divides data into intervals (often called bins) and shows the number of data points in each bin.
- KDE option is setted as True. The kde parameter controls whether or not a kernel density estimation (KDE) plot is overlaid on the histogram. While histograms provide a good starting point, they can be blocky, especially with a small number of data points. KDE helps visualise the smoother, continuous distribution behind the histogram. Identify potential outliers: Deviations from the smooth KDE curve might indicate outliers in your data. Essentially, using kde=True in sns.histplot enhances the visualization by providing a more complete picture of the data's distribution. It combines the clarity of the histogram with the smoothness of the KDE plot.

In [ ]:

```
fig, ax = plt.subplots(figsize=(10, 6))
df_new.boxplot(ax=ax)
plt.show()
```

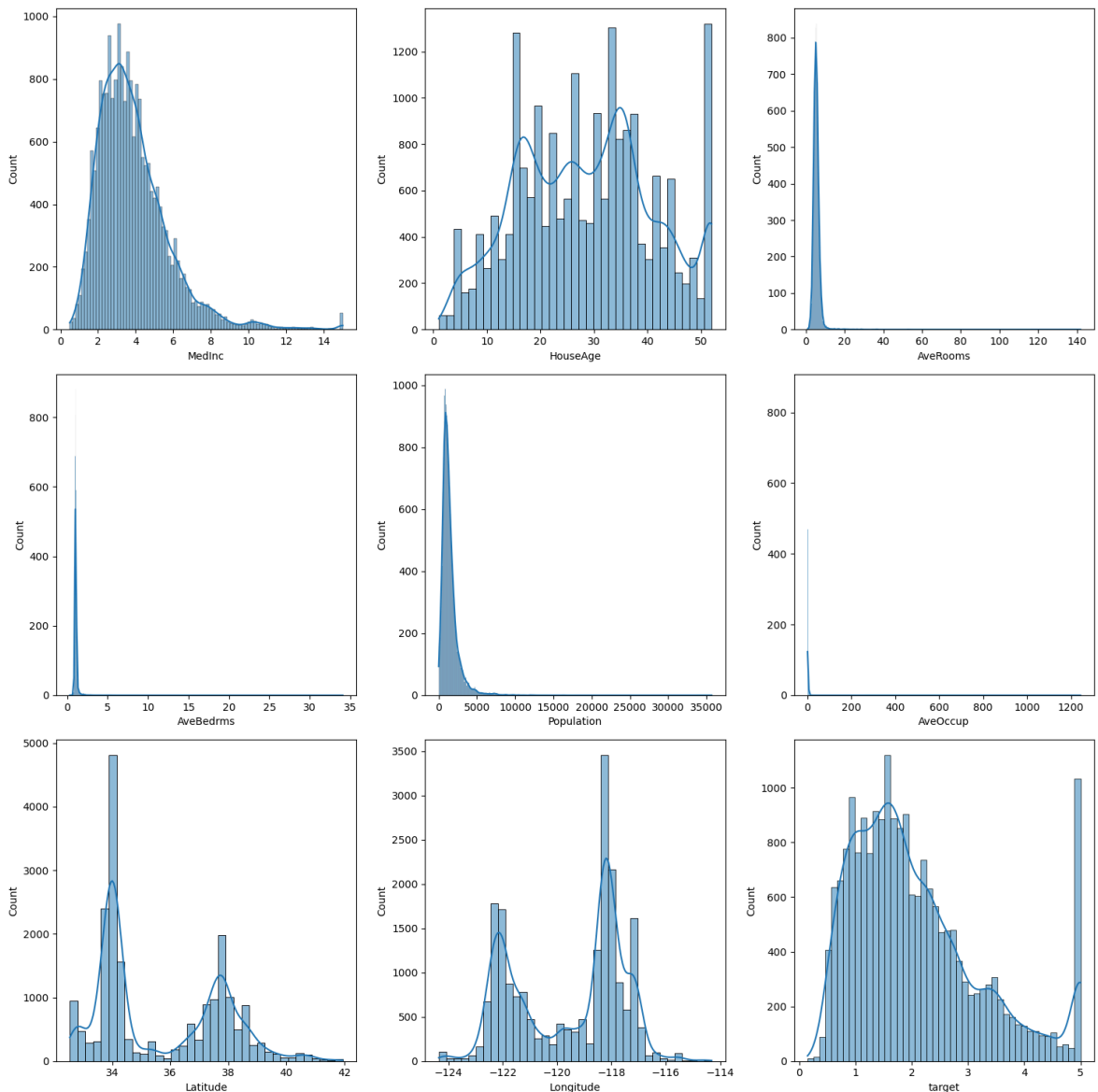


```
In [ ]: ##### columns: MedInc    HouseAge    AveRooms    AveBedrms    Populati
nrows= 3
ncols= 3
fig, axes = plt.subplots(3, 3, figsize=(15, 15)) # set up the plots layout

data1= df_new['MedInc']
data2= df_new['HouseAge']
data3= df_new['AveRooms']
data4= df_new['AveBedrms']
data5= df_new['Population']
data6= df_new['AveOccup']
data7= df_new['Latitude']
data8= df_new['Longitude']
data9= df_new['target']

#Use sns.distplot() on each subplot to plot histograms and kernel density estima
sns.histplot(data1, ax=axes[0, 0], kde=True)
sns.histplot(data2, ax=axes[0, 1], kde=True)
sns.histplot(data3, ax=axes[0, 2], kde=True)
sns.histplot(data4, ax=axes[1, 0], kde=True)
sns.histplot(data5, ax=axes[1, 1], kde=True)
sns.histplot(data6, ax=axes[1, 2], kde=True)
sns.histplot(data7, ax=axes[2, 0], kde=True)
sns.histplot(data8, ax=axes[2, 1], kde=True)
sns.histplot(data9, ax=axes[2, 2], kde=True)
"""longitude
latitude
housing_median_age
total_rooms
total_bedrooms
population
households
median_income
median_house_value
ocean_proximity"""
plt.tight_layout()
# here the path needs to be changed to local path
```

```
plt.savefig('house_x_train_features_histplot.png')
plt.show()
```



### 3, Beziehungen zwischen Variablen

The Correlation Plots showed below.

The methode here, which used in the lecture will be downloaded and imported.

```
In [ ]: from os.path import basename, exists

def download(url):
    filename = basename(url)
    if not exists(filename):
        from urllib.request import urlretrieve

        local, _ = urlretrieve(url, filename)
        print("Downloaded " + local)

download("https://github.com/AllenDowney/ThinkStats2/raw/master/code/thinkstats2")
download("https://github.com/AllenDowney/ThinkStats2/raw/master/code/thinkplot.p")
```

```
download("https://github.com/AllenDowney/ThinkStats2/raw/master/code/brfss.py")
download("https://github.com/AllenDowney/ThinkStats2/raw/master/code/CDBRFS08.AS
```

Import just downloaded packages

```
In [ ]: import numpy as np
import thinkstats2
import thinkplot
import brfss
# -Medianeinkommen (Median Income)
# -Medianes Alter der Wohnbevölkerung (Median Age of Housing Units)
# -Durchschnittliche Anzahl der Zimmer (Average Number of Rooms)
# -Durchschnittliche Anzahl der Schlafzimmer (Average Number of Bedrooms)
# -Bevölkerung pro Hektar (Population per Acre)
# -Anteil an Haushalten, die nicht Eigentümer sind (Percentage of Households Not
# -Latitude;
# -Longitude
```

Then write a function to use build in .corr function to caculate the correlation.

## Spearman Correlation Coefficient: A Comprehensive Overview

### Introduction

The Spearman correlation coefficient, also known as the rank correlation coefficient, is a non-parametric statistical measure that assesses the strength and direction of the association between two variables. It is similar to Pearson's correlation coefficient, but it does not require the assumption of normally distributed data and is less sensitive to outliers.

### Calculation of Spearman Correlation Coefficient

The Spearman correlation coefficient is calculated using the following formula:

$$r_s = 1 - \frac{6 \sum d_i^2}{n(n^2 - 1)}$$

where:

- $r_s$  is the Spearman correlation coefficient
- $d$  is the difference in ranks for each data point
- $n$  is the number of data points

The Spearman correlation coefficient ranges from -1 to 1:

- $r_s > 0$  indicates a positive correlation, meaning the ranks of the two variables change in the same direction.
- $r_s = 0$  indicates no correlation, meaning there is no linear relationship between the ranks of the two variables.
- $r_s < 0$  indicates a negative correlation, meaning the ranks of the two variables change in opposite directions.

The reason to choose spearman correlation for this data?

- Pearson's correlation coefficient: Measures the strength and direction of the linear relationship between two continuous variables. Requires that the data are normally distributed, meaning both variables should be approximately normally distributed. Sensitive to outliers, meaning extreme values can significantly impact the results.
- Spearman's rank correlation coefficient: Measures the monotonic relationship between two variables, regardless of whether this relationship is linear. Does not require the data to be normally distributed, only that the ranks of the data are comparable. Less sensitive to outliers compared to Pearson's correlation coefficient.

Because we could see that that most data dont fit normal distribution, therefore Spearman's rank correlation coefficient would be more suitable.

```
In [ ]: def SpearmanCorr(xs, ys):
        xs = pd.Series(xs) #use pd.Series() to label each input
        ys = pd.Series(ys)
        return xs.corr(ys, method='spearman')
```

```
In [ ]: target= df_new['target'] #target feature here means price: Jeder Datensatz reprä
```

Because the data is about the house price, so i will calculate the correaltion between price and everz other attribute. Y axis is price and X axis is other attribute.

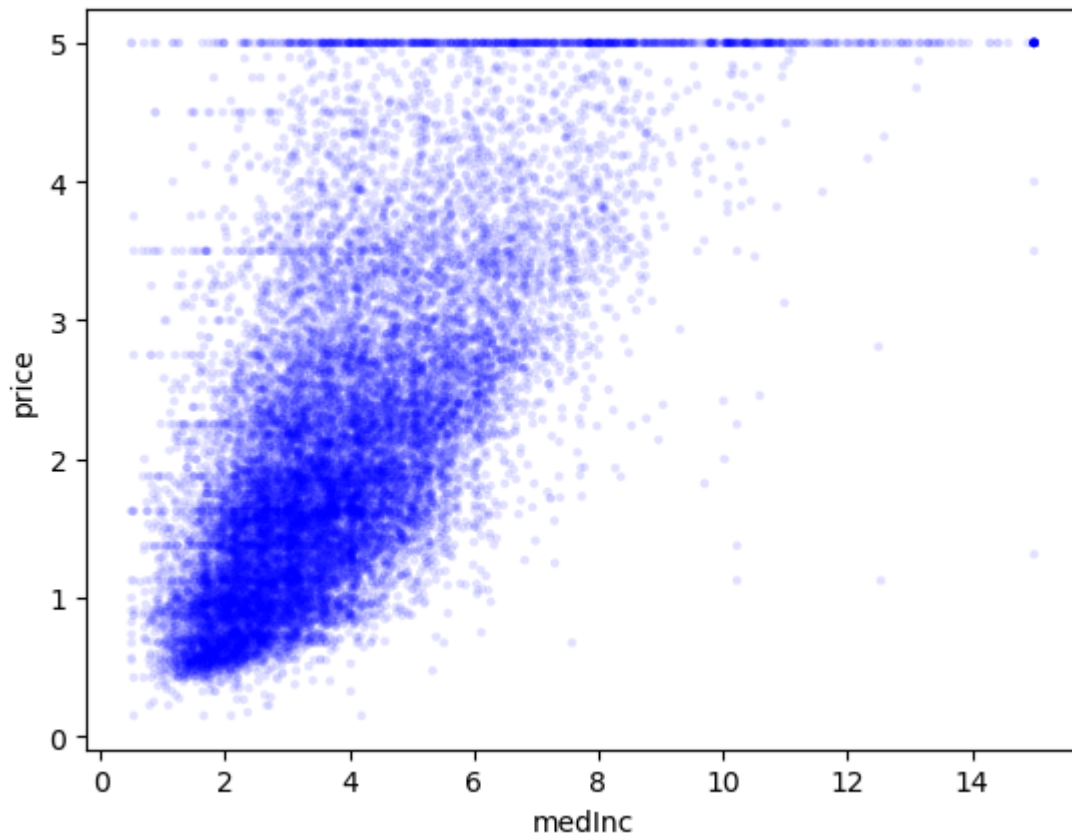
And i will use the build in plot function from 'thinkplot' package.

```
In [ ]: medinc= df_new['MedInc']
        thinkplot.Scatter(medinc, target, alpha=0.1, s=10)
        thinkplot.Config(xlabel='medInc',
                          ylabel='price',
                          legend=False)

        SpearmanCorr(target, medinc)
```

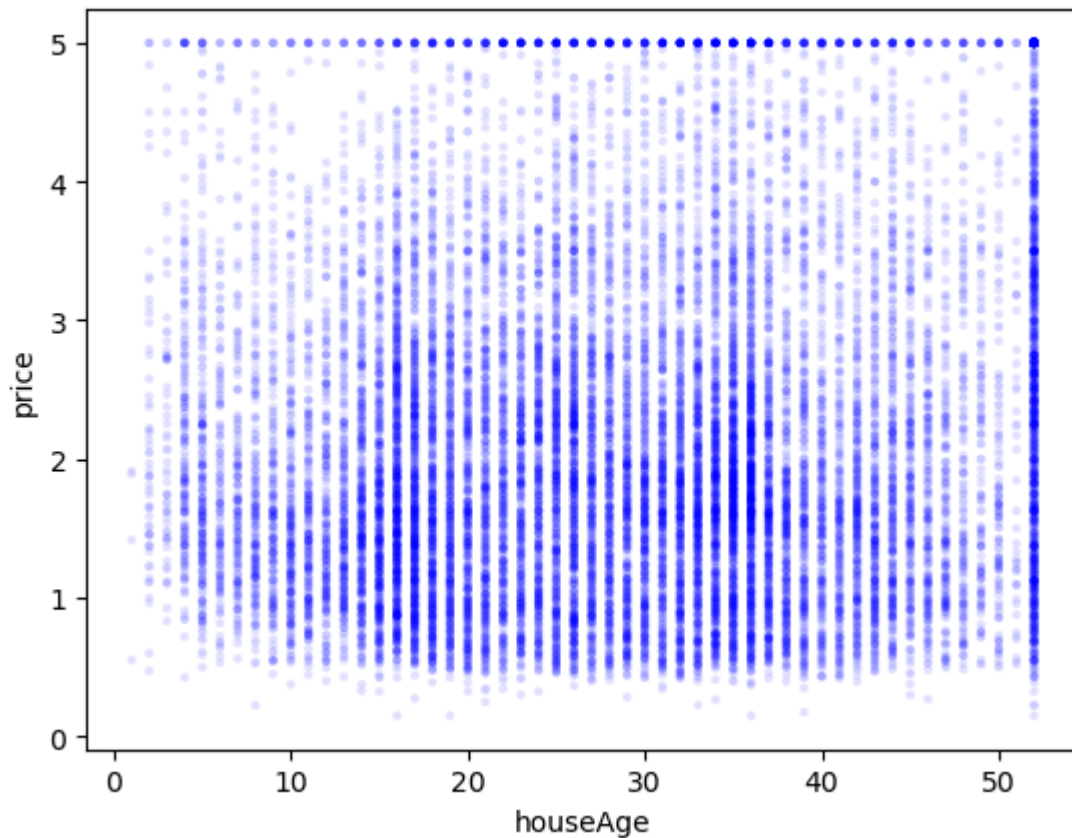
```
Out[ ]: 0.6767781095942506
```





```
In [ ]: houseage= df_new['HouseAge']  
thinkplot.Scatter(houseage, target, alpha=0.1, s=10)  
thinkplot.Config(xlabel='houseAge',  
                  ylabel='price',  
                  legend=False)  
  
SpearmanCorr(target, houseage)
```

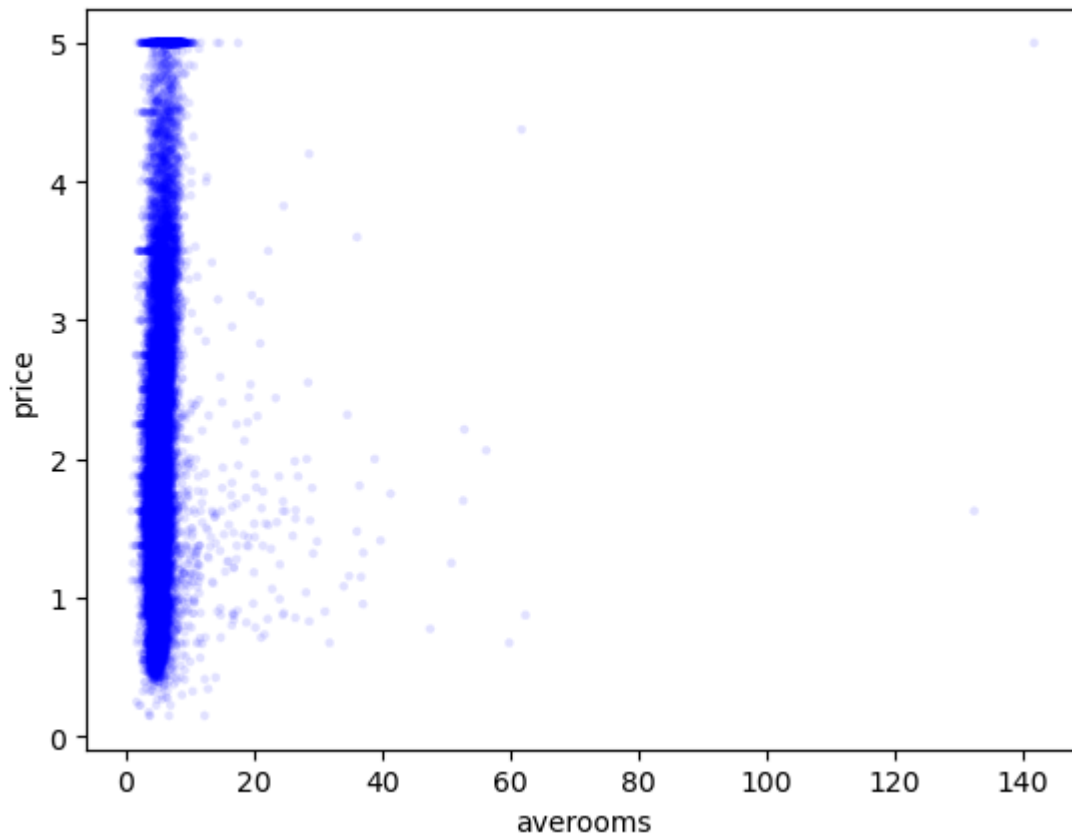
```
Out[ ]: 0.07485485302251019
```



```
In [ ]: averooms= df_new['AveRooms']
thinkplot.Scatter(averooms, target, alpha=0.1, s=10)
thinkplot.Config(xlabel='averooms',
                  ylabel='price',
                  legend=False)

SpearmanCorr(target, averooms)
```

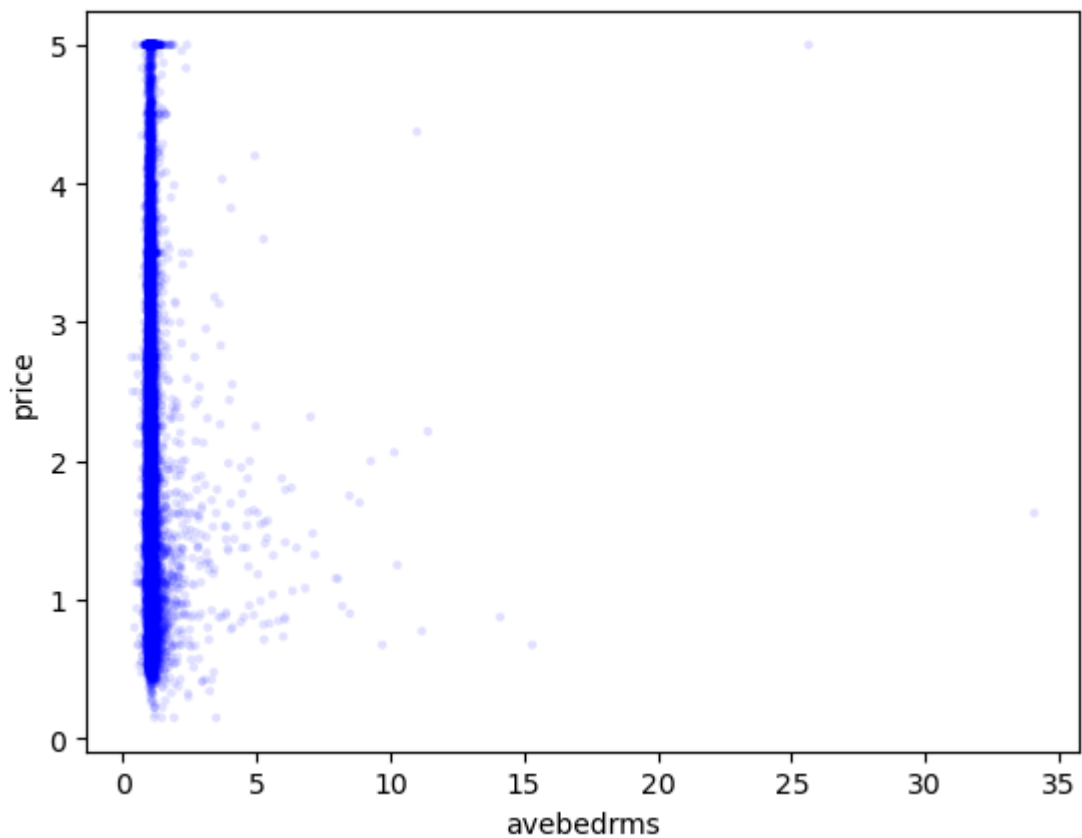
```
Out[ ]: 0.26336668772954447
```



```
In [ ]: avebedrms= df_new['AveBedrms']
thinkplot.Scatter(avebedrms, target, alpha=0.1, s=10)
thinkplot.Config(xlabel='avebedrms',
                  ylabel='price',
                  legend=False)

SpearmanCorr(target, avebedrms)
```

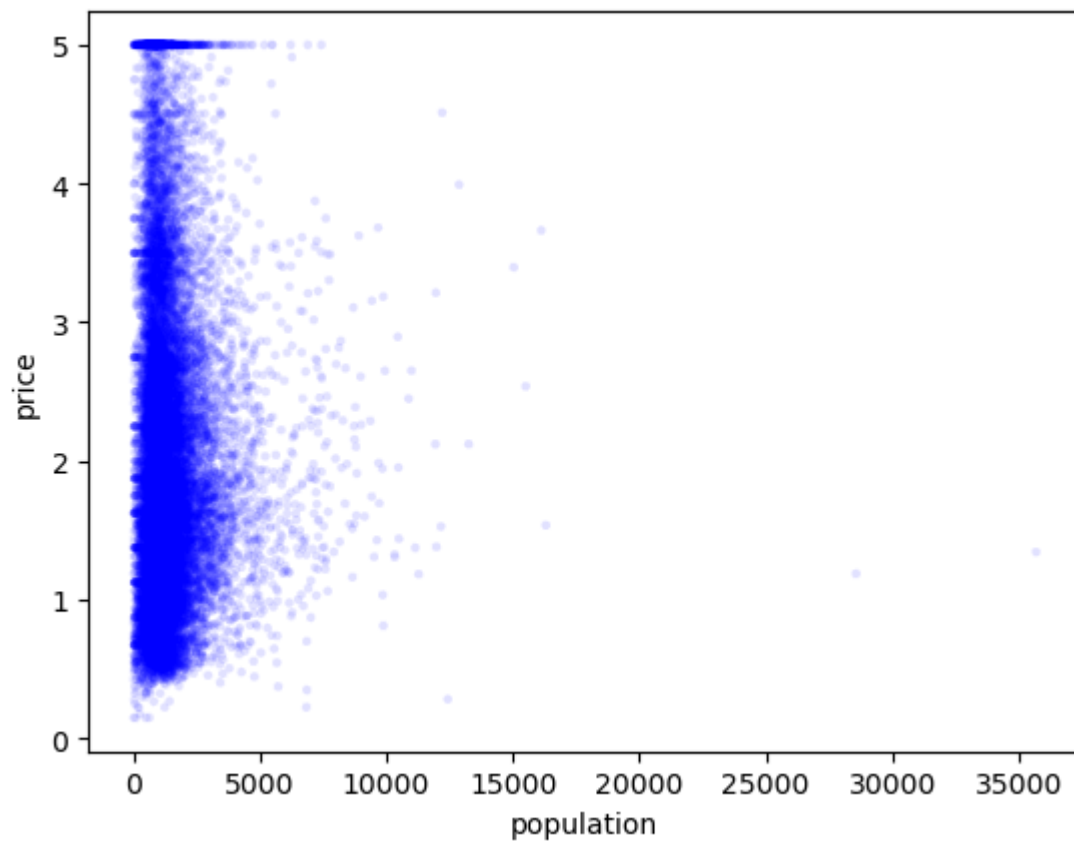
```
Out[ ]: -0.12518706503579644
```



```
In [ ]: population= df_new['Population']
thinkplot.Scatter(population, target, alpha=0.1, s=10)
thinkplot.Config(xlabel='population',
                  ylabel='price',
                  legend=False)

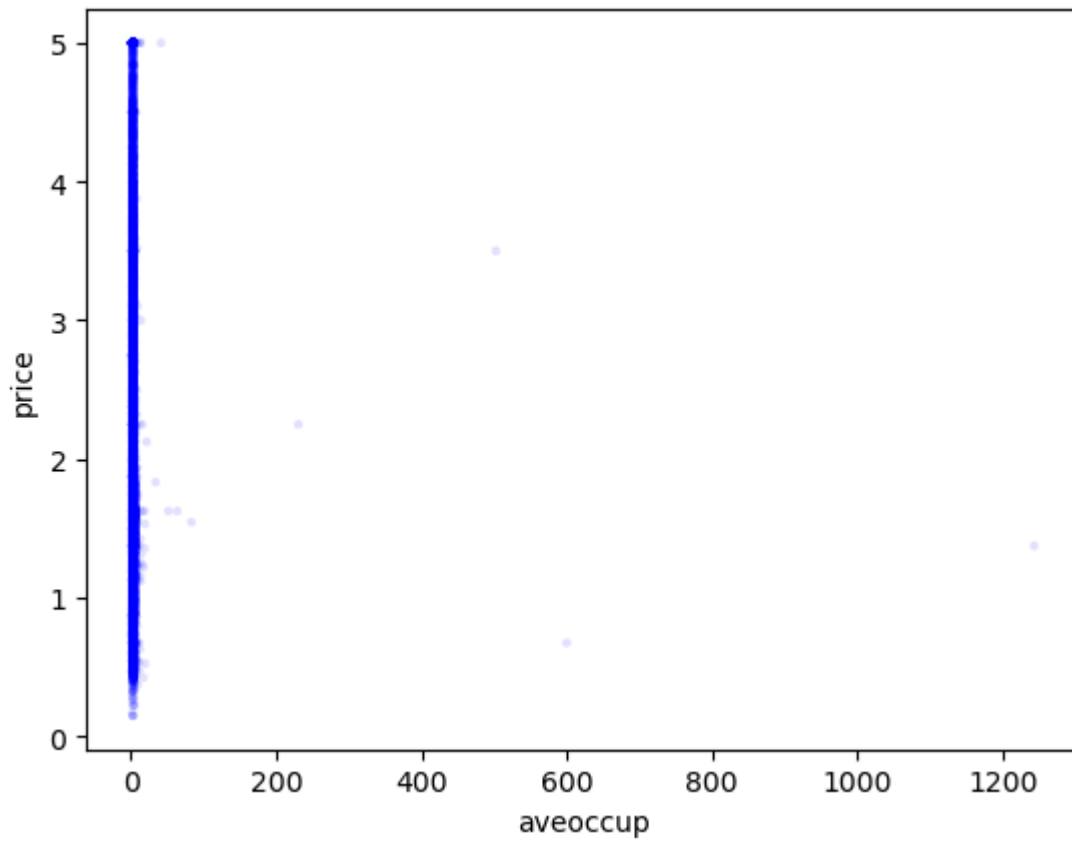
SpearmanCorr(target, population)
```

```
Out[ ]: 0.0038387551282557182
```



```
In [ ]: aveoccup= df_new['AveOccup']  
thinkplot.Scatter(aveoccup, target, alpha=0.1, s=10)  
thinkplot.Config(xlabel='aveoccup',  
                  ylabel='price',  
                  legend=False)  
  
SpearmanCorr(target, aveoccup)
```

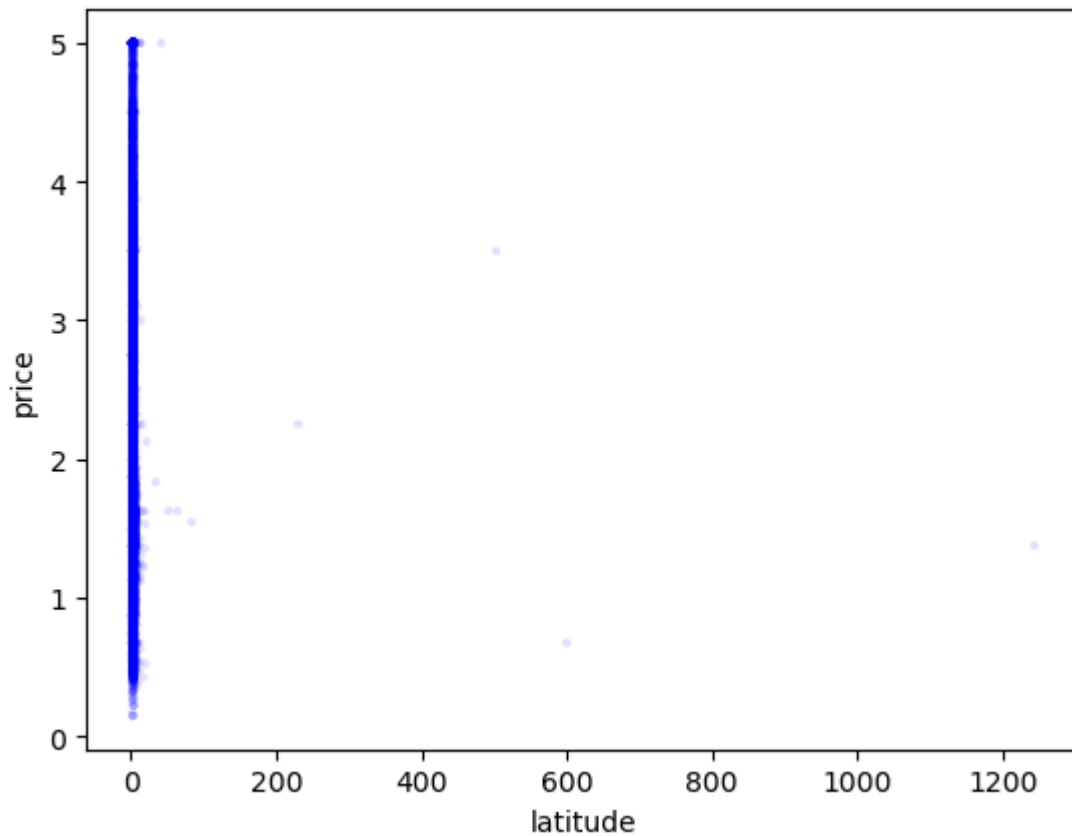
```
Out[ ]: -0.2565937646638933
```



```
In [ ]: latitude= df_new['Latitude']
thinkplot.Scatter(aveoccup, target, alpha=0.1, s=10)
thinkplot.Config(xlabel='latitude',
                  ylabel='price',
                  legend=False)

SpearmanCorr(target, latitude)
```

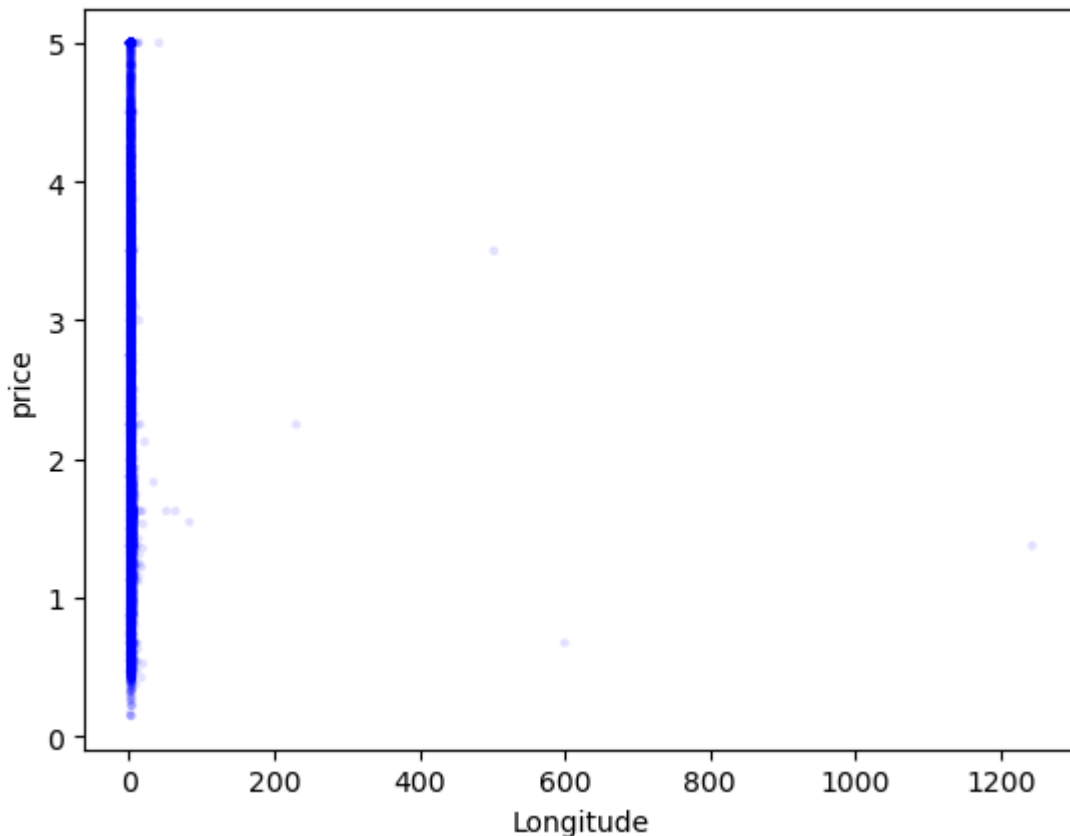
```
Out[ ]: -0.1657388374452999
```



```
In [ ]: longitude= df_new['Longitude']
thinkplot.Scatter(aveoccup, target, alpha=0.1, s=10)
thinkplot.Config(xlabel='Longitude',
                  ylabel='price',
                  legend=False)

SpearmanCorr(target, longitude)
```

```
Out[ ]: -0.069666666665067331
```



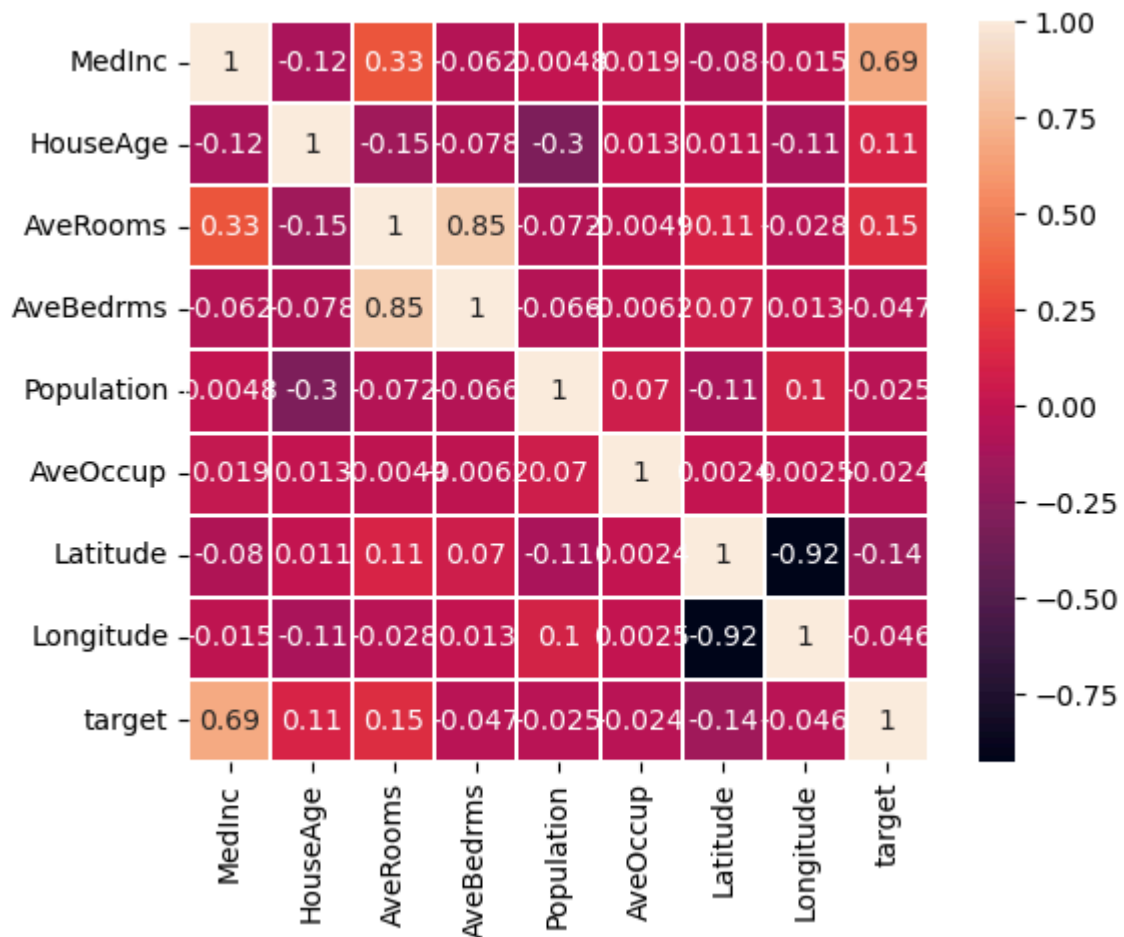
The observation of plots:

- In the relationship graph between Price and MedianIncome, there are some cases where their MedianIncome has nothing to do with property prices. (The prices of some houses are very high, but MedianIncome's values cover the entire range.)
- Houseage has a weak effect on house prices
- There are some samples that have a lot of rooms. Most are under 10.
- There are some samples that have a lot of bedrooms. Most are under 10.
- The population per hectare is below 5000, there are many houses with prices between 1 and 2, but still a few at 5.
- Nothing much in particular found
- Most correlation values of Longitude and Latitude are very low.

```
In [ ]: #Here i just used another function to show the whole correlations between each t
sns.heatmap(df_new.corr(),linewidths=0.1,vmax=1.0, square=True,linecolor='white')
```

```
Out[ ]: <Axes: >
```





From plots above, there could be have some questions to this data:

- Does this data need more attributes? Because in the first plot, some houses with high prices have almost nothing to do with the MedIncome. (For example, the ratio of heirs)
- Is it possible to visualize the data of longitude and latitude so that one can easily understand the data of them?

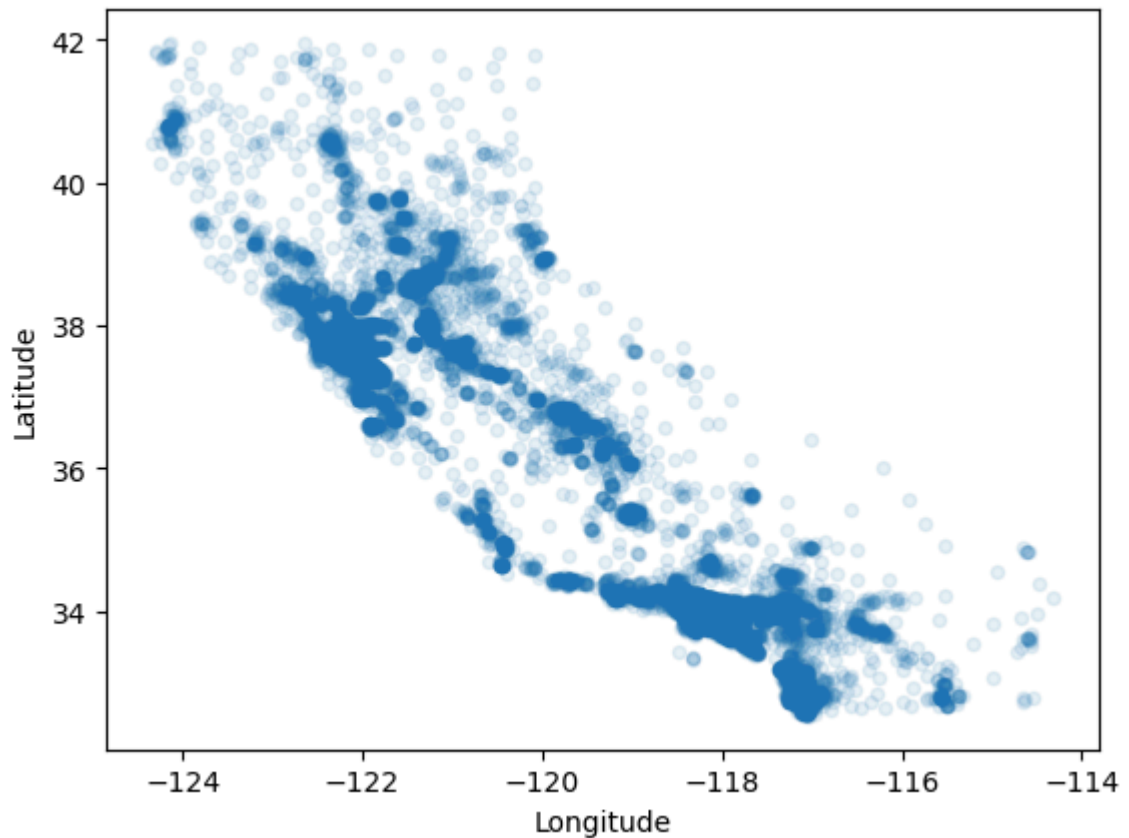
## 4, Induktive Analyse

Here we use `df_new.plot()` to visualte the Longituden and Latituden. Because the longitude and latitude datacontains the spital information, there fore to show them out in plot is reasonable.

The density of samples can be seen from the lontitudes and latitudes. It's almost like a visualization of Carlifonia! (L.A, S.F, eg)

```
In [ ]: df_new.plot(kind="scatter",x="Longitude",y="Latitude",alpha=0.1)
```

```
Out[ ]: <Axes: xlabel='Longitude', ylabel='Latitude'>
```

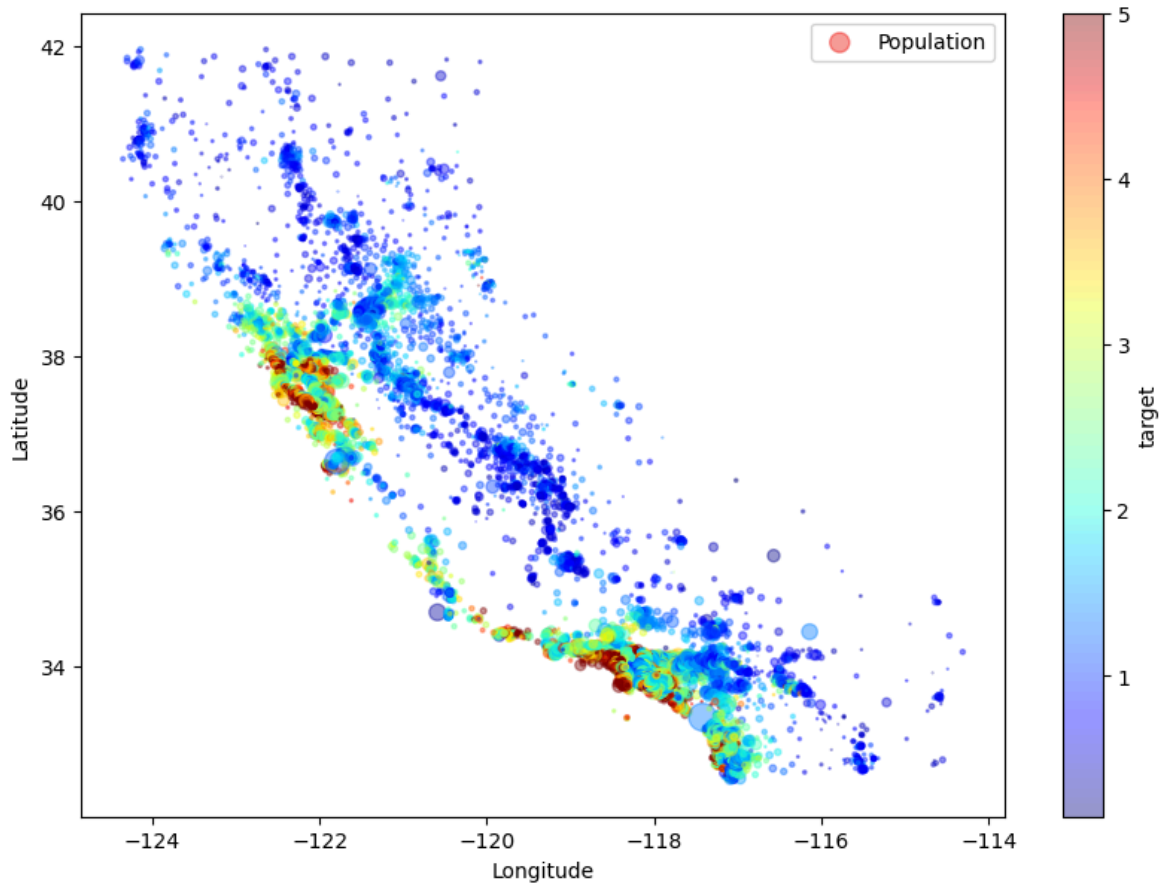


The plot also shows the population and prices. From this plot, we can see that areas with higher house price have big population.

```
In [ ]: df_new.plot(kind='scatter',x='Longitude',y='Latitude',alpha=0.4,s=df_new['Popula
        label='Population',figsize=(10,7),
        c='target',cmap= plt.cm.get_cmap('jet'),colorbar=True) #target is the
```

```
/tmp/ipykernel_419892/3168257586.py:3: MatplotlibDeprecationWarning: The get_cmap
function was deprecated in Matplotlib 3.7 and will be removed two minor releases
later. Use ``matplotlib.colormaps[name]`` or ``matplotlib.colormaps.get_cmap(obj)
`` instead.
        c='target',cmap= plt.cm.get_cmap('jet'),colorbar=True) #target is the price
```

```
Out[ ]: <Axes: xlabel='Longitude', ylabel='Latitude'>
```



For a deeper analyse i would like to have: inheritance can be easily defined with the binary value (true/false).

## 5, Diskussion

Because this carlifonia house price data is often used to do regression. So the scale of attribute has to be considered! So the data should be further modified.

There are two typical kinds of scaling: z score scaling and minmax scaling.

### StandardScaler

Principle:

`StandardScaler` transforms each feature to have zero mean and unit variance, often necessary for the proper functioning of many machine learning algorithms, particularly those involving distance calculations like k-nearest neighbors and support vector machines. The transformation is defined by:

$$z = \frac{(x - \mu)}{\sigma}$$

where (  $x$  ) is the original value, (  $\mu$  ) is the mean of the feature, and (  $\sigma$  ) is the standard deviation of the feature.

Applications:

- Ideal for algorithms that assume data is normally distributed and features have equal scales.
- Useful in optimization algorithms, which are sensitive to the scales of input.

Advantages:

- Maintains useful data about outliers and does not bound values to a specific range.

Disadvantages:

- Not suitable for data with outliers as they will influence the mean and standard deviation.

## MinMaxScaler

Principle:

`MinMaxScaler` scales each feature to a given range, typically 0 to 1, or -1 to 1 if there are negative values. The transformation is calculated using:

$$x_{\text{scaled}} = \frac{(x - \min(x))}{(\max(x) - \min(x))} \times (\text{new\_max} - \text{new\_min}) + \text{new\_min}$$

where (  $x$  ) is an original value,  $\min(x)$  and  $\max(x)$  are the minimum and maximum values of the feature, respectively.  $\text{new\_min}$  and  $\text{new\_max}$  are the desired scaling range.

Applications:

- Often used when the data needs to be bounded within a scale like 0 to 1.
- Useful for feature scaling for algorithms that weigh inputs like neural networks and algorithms using distance measures like k-nearest neighbors.

Advantages:

- Transforms features to a specific scale.
- Useful when you know the approximate minimum and maximum values that the data can take.

Disadvantages:

- Sensitive to outliers, as they can compress most of the data into a narrow range.
- Does not handle outliers as well as `StandardScaler`.

```
In [ ]: ##### Z score normalization #####
scaler = StandardScaler()

df_new_copy= df_new.copy()
df_scaled = scaler.fit_transform(df_new_copy.drop(columns=['target'])) # Assume
normalized_df = pd.DataFrame(df_scaled, columns=df_new_copy.drop(columns=['target
```

```

normalized_df['target'] = df_new['target']
#print(normalized_df.head())
means = normalized_df.mean()
stds = normalized_df.std()

print("Means after standardization:\n", means)
print("\nStandard deviations after standardization:\n", stds)

fig, axes = plt.subplots(3, 3, figsize=(15, 15)) # Resize to a larger size to p

sns.histplot(normalized_df['MedInc'], ax=axes[0, 0], kde=True)
sns.histplot(normalized_df['HouseAge'], ax=axes[0, 1], kde=True)
sns.histplot(normalized_df['AveRooms'], ax=axes[0, 2], kde=True)
sns.histplot(normalized_df['AveBedrms'], ax=axes[1, 0], kde=True)
sns.histplot(normalized_df['Population'], ax=axes[1, 1], kde=True)
sns.histplot(normalized_df['AveOccup'], ax=axes[1, 2], kde=True)
sns.histplot(normalized_df['Latitude'], ax=axes[2, 0], kde=True)
sns.histplot(normalized_df['Longitude'], ax=axes[2, 1], kde=True)
sns.histplot(normalized_df['target'], ax=axes[2, 2], kde=True)

plt.tight_layout()
plt.savefig('house_x_train_features_histplot_Z_normalization.png')
plt.show()

```

Means after standardization:

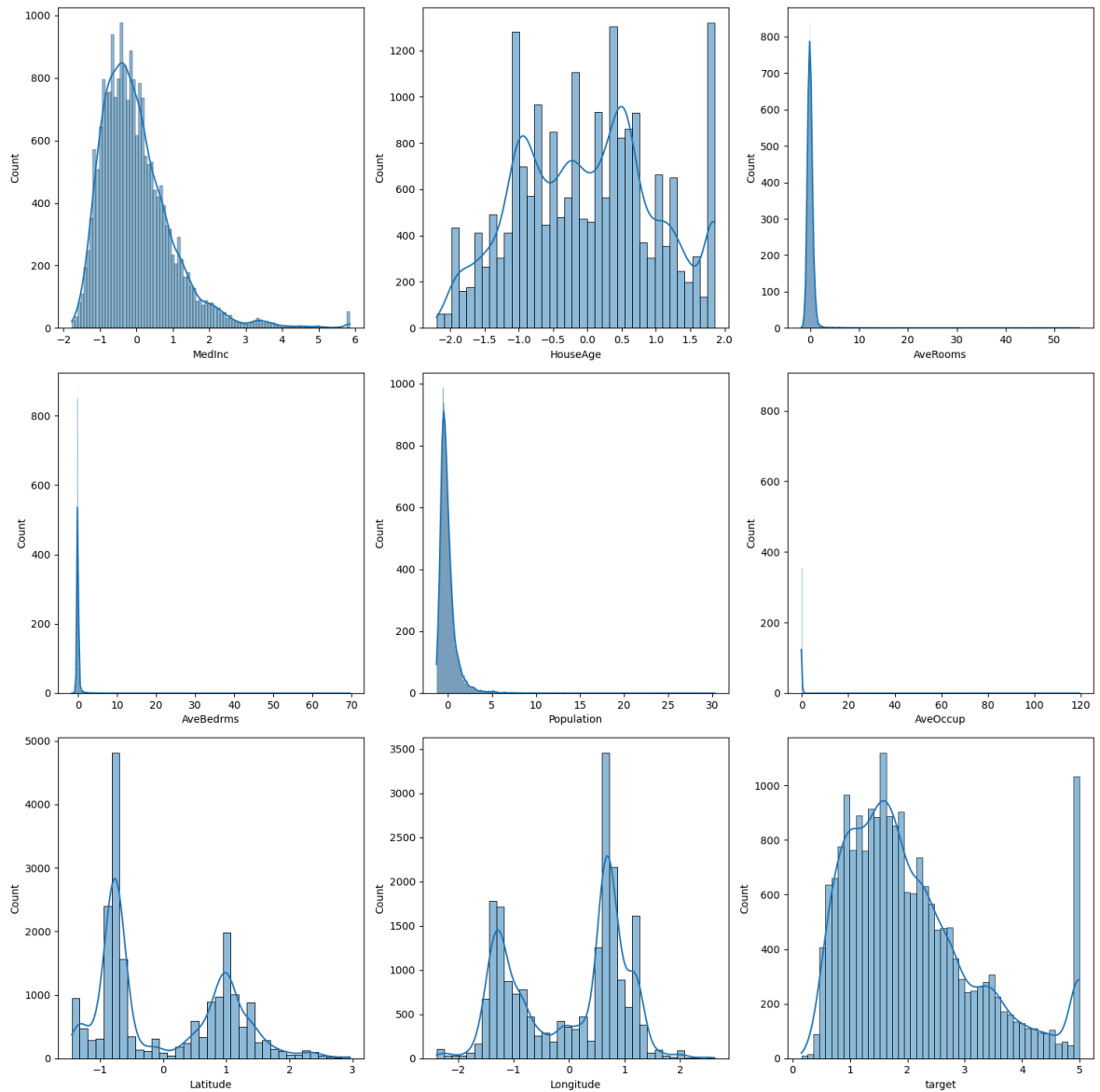
MedInc	6.609700e-17
HouseAge	5.508083e-18
AveRooms	6.609700e-17
AveBedrms	-1.060306e-16
Population	-1.101617e-17
AveOccup	3.442552e-18
Latitude	-1.079584e-15
Longitude	-8.526513e-15
target	2.068558e+00

dtype: float64

Standard deviations after standardization:

MedInc	1.000024
HouseAge	1.000024
AveRooms	1.000024
AveBedrms	1.000024
Population	1.000024
AveOccup	1.000024
Latitude	1.000024
Longitude	1.000024
target	1.153956

dtype: float64



```
In [ ]: ##### Min-Max normalization #####
scaler = MinMaxScaler()

df_new_copy_minmax= df_new.copy()
df_scaled = scaler.fit_transform(df_new_copy_minmax.drop(columns=['target'])) #
normalized_minmax_df = pd.DataFrame(df_scaled, columns=df_new_copy_minmax.drop(c
normalized_df['target'] = df_new['target']
normalized_minmax_df['target'] = df_new['target']
#print(normalized_minmax_df.head())
means = normalized_minmax_df.mean()
stds = normalized_minmax_df.std()
print("Means after standardization:\n", means)
print("\nStandard deviations after standardization:\n", stds)

fig, axes = plt.subplots(3, 3, figsize=(15, 15)) # Resize to a larger size to p

sns.histplot(normalized_minmax_df['MedInc'], ax=axes[0, 0], kde=True)
sns.histplot(normalized_minmax_df['HouseAge'], ax=axes[0, 1], kde=True)
sns.histplot(normalized_minmax_df['AveRooms'], ax=axes[0, 2], kde=True)
sns.histplot(normalized_minmax_df['AveBedrms'], ax=axes[1, 0], kde=True)
sns.histplot(normalized_minmax_df['Population'], ax=axes[1, 1], kde=True)
sns.histplot(normalized_minmax_df['AveOccup'], ax=axes[1, 2], kde=True)
sns.histplot(normalized_minmax_df['Latitude'], ax=axes[2, 0], kde=True)
sns.histplot(normalized_minmax_df['Longitude'], ax=axes[2, 1], kde=True)
```

```
sns.histplot(normalized_minmax_df['target'], ax=axes[2, 2], kde=True)

plt.tight_layout()
plt.savefig('house_x_train_features_histplot_minmax_normalization.png')
plt.show()
```

Means after standardization:

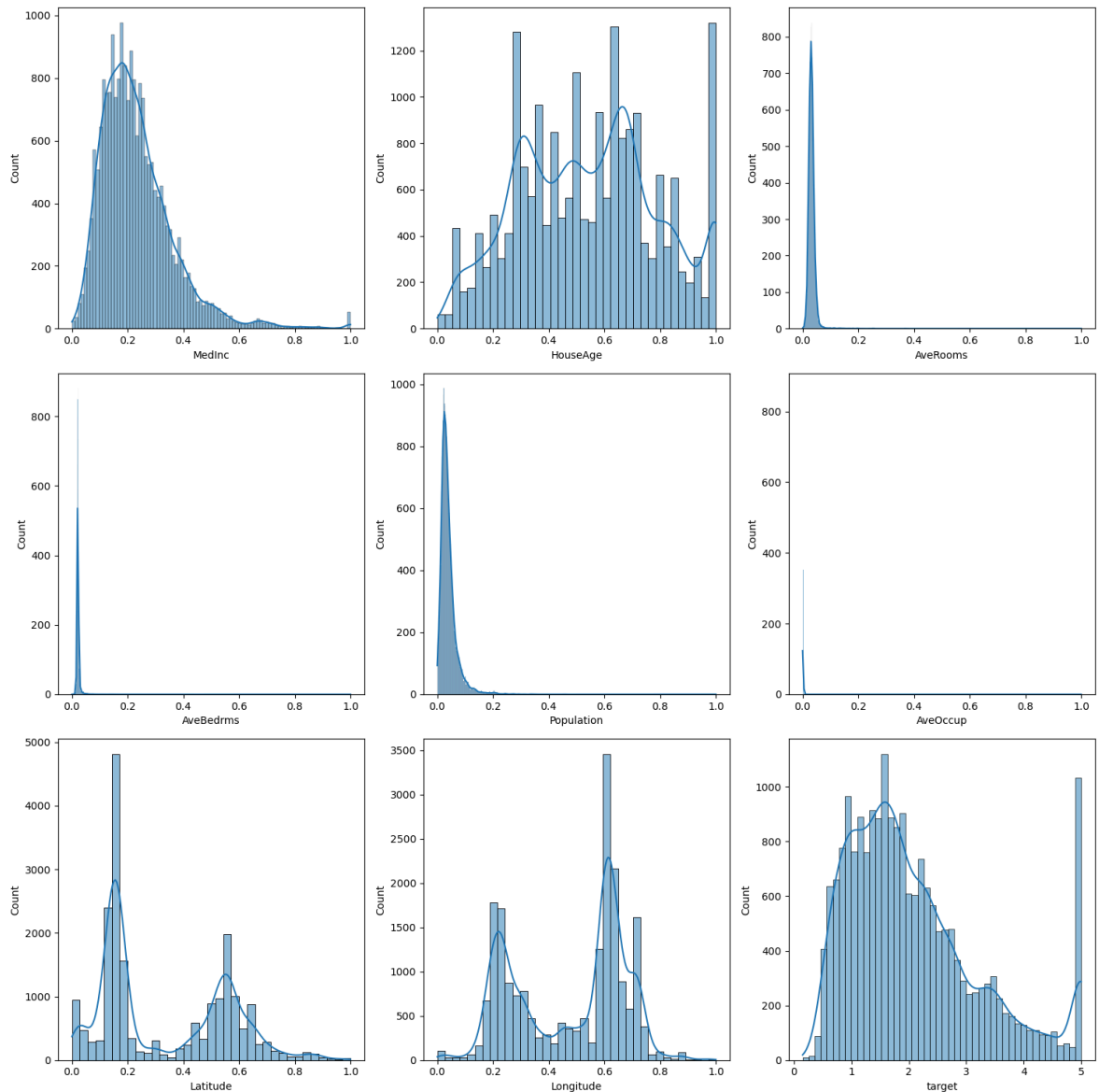
MedInc	0.232464
HouseAge	0.541951
AveRooms	0.032488
AveBedrms	0.022629
Population	0.039869
AveOccup	0.001914
Latitude	0.328572
Longitude	0.476125
target	2.068558

dtype: float64

Standard deviations after standardization:

MedInc	0.131020
HouseAge	0.246776
AveRooms	0.017539
AveBedrms	0.014049
Population	0.031740
AveOccup	0.008358
Latitude	0.226988
Longitude	0.199555
target	1.153956

dtype: float64



After scaling, we can compare the statistical properties (like mean and standard deviation) of the scaled features to understand the effect of each scaling method.

- StandardScaler will transform the features so they have mean close to 0 and standard deviation close to 1.
- MinMaxScaler will transform the features so their values are bounded between 0 and 1.

Both scaling methods prepare data for machine learning algorithms that might perform better if features are on similar scales or are normalized. This is especially true for algorithms that depend on the magnitude of features, such as k-nearest neighbors and gradient descent-based algorithms.

## 6, Bonus

- Falls möglich, versuchen Sie ihren Datensatz mit weiteren Daten anzureichern oder einen weiteren, denselben Sachverhalt beschreibenden, Datensatz zu besorgen. Erweitern Sie danach Ihre Analyse um die angereicherten Daten.



In [ ]:

In [ ]: