

Reverse Polish Notation

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Reverse Polish Notation

- Most math expressions you have seen were written in “in-fix” notation
- Example:

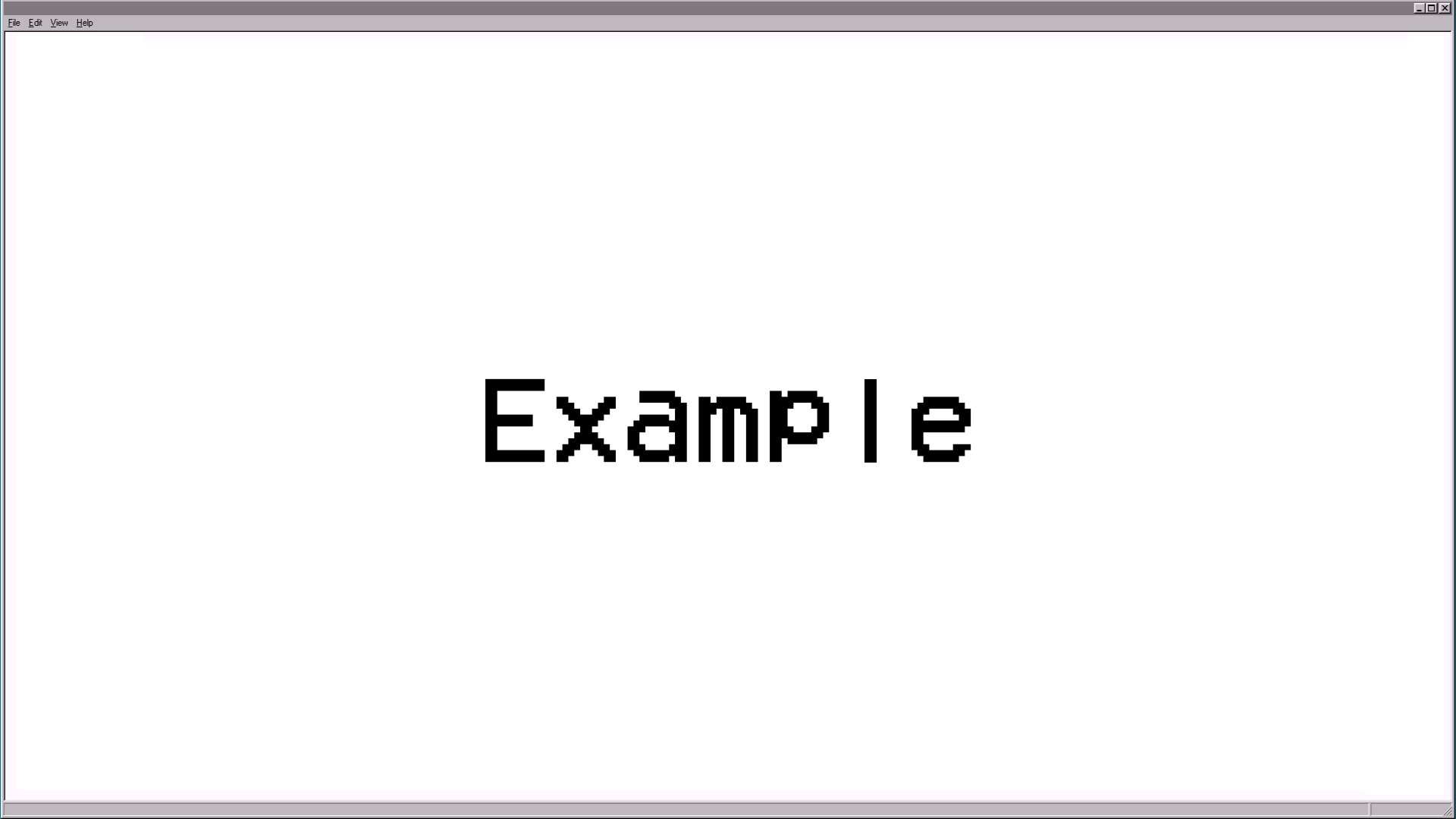
$$3 + 5$$

- However, there is another notation called “post-fix” or “Reverse Polish Notation” where the operator is at the end
- Example

$$3\ 5\ +$$

Big Idea

- Use a stack to solve reverse polish notation
- You push onto the stack when there's a number
- When there's an operator (+, -, *, /) then
 - Pop off two items from the stack
 - Evaluate the two numbers with that operation
 - Push the result back to the stack
- Once it has completed the expression there should only be one item left on the stack



Example

Reverse Polish Example

- Here the user has inputted the string 3 2 +

3 2 +

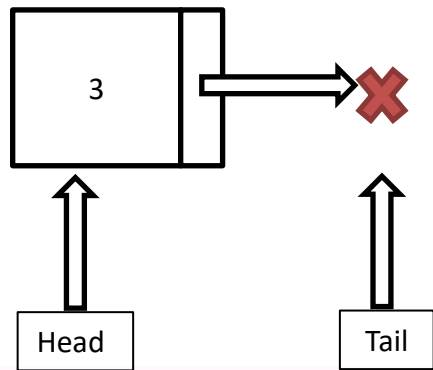
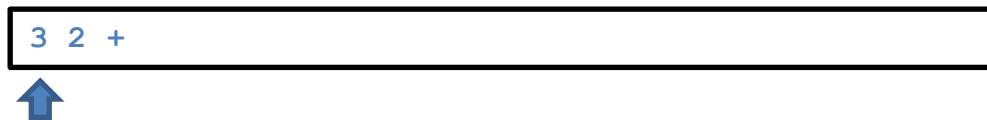


Head

Tail

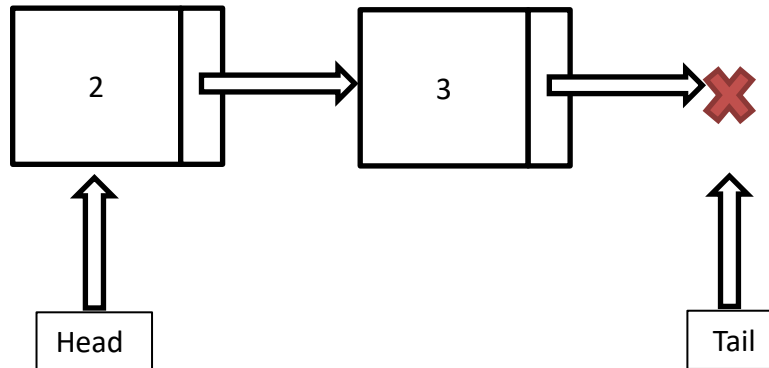
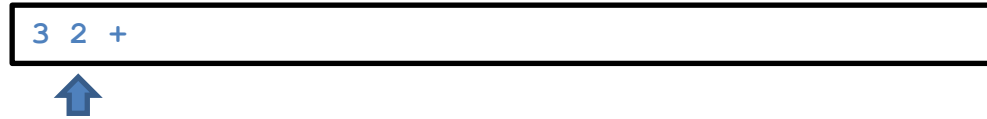
Reverse Polish Example

- 3 is a number so push it on the stack



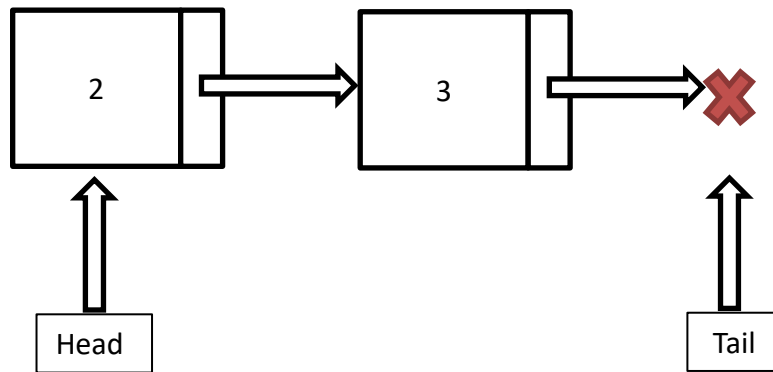
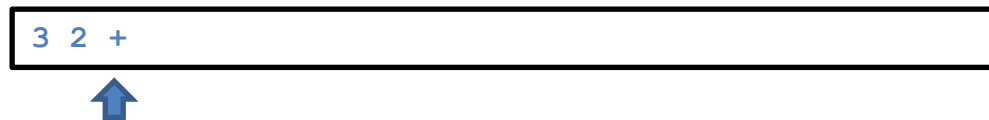
Reverse Polish Example

- 2 is a number so push it on the stack



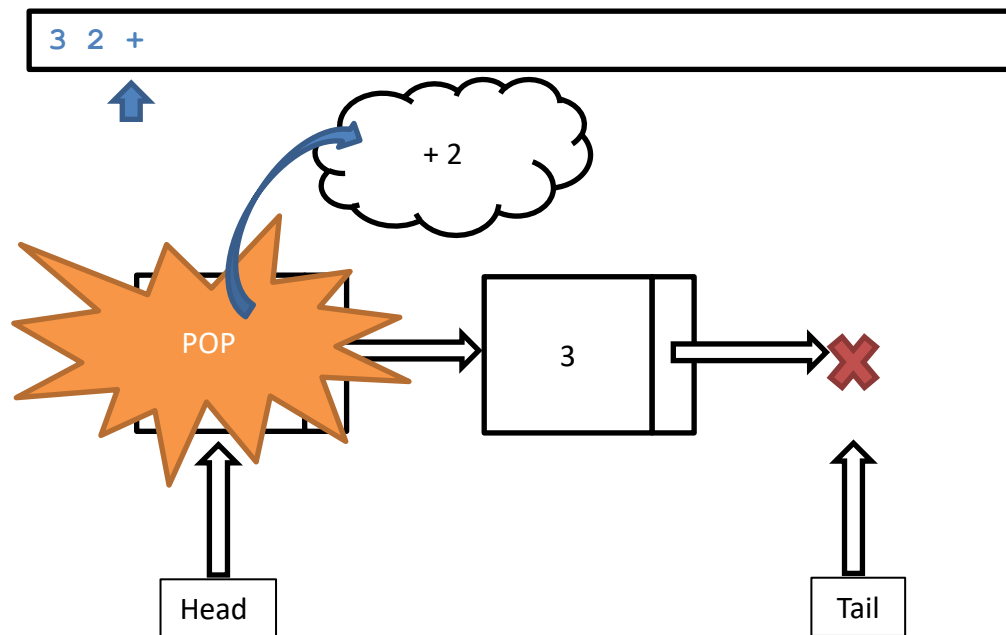
Reverse Polish Example

- + is an operator so pop of two



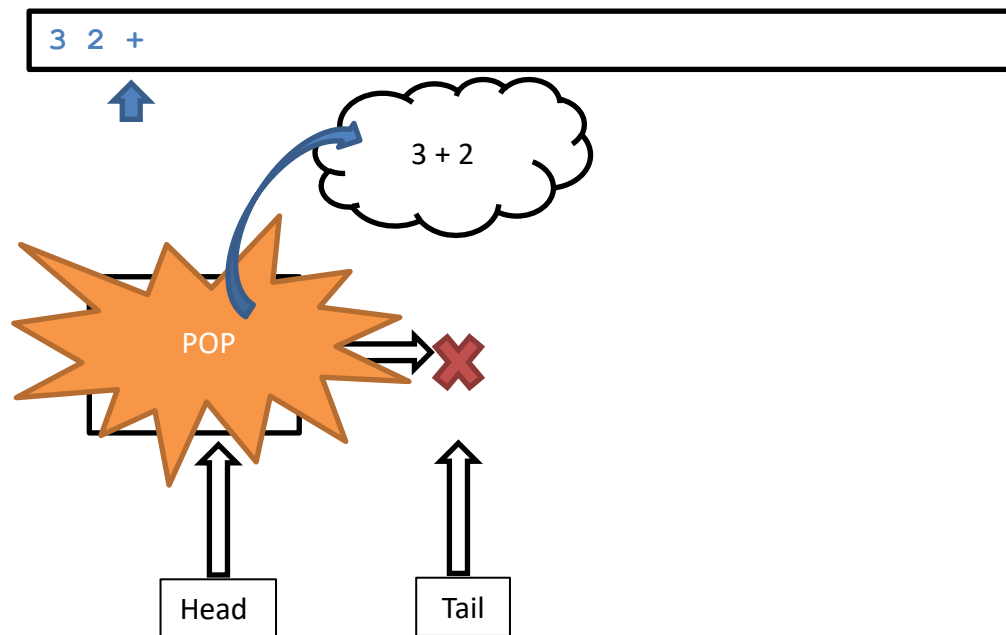
Reverse Polish Example

- + is an operator so pop of two



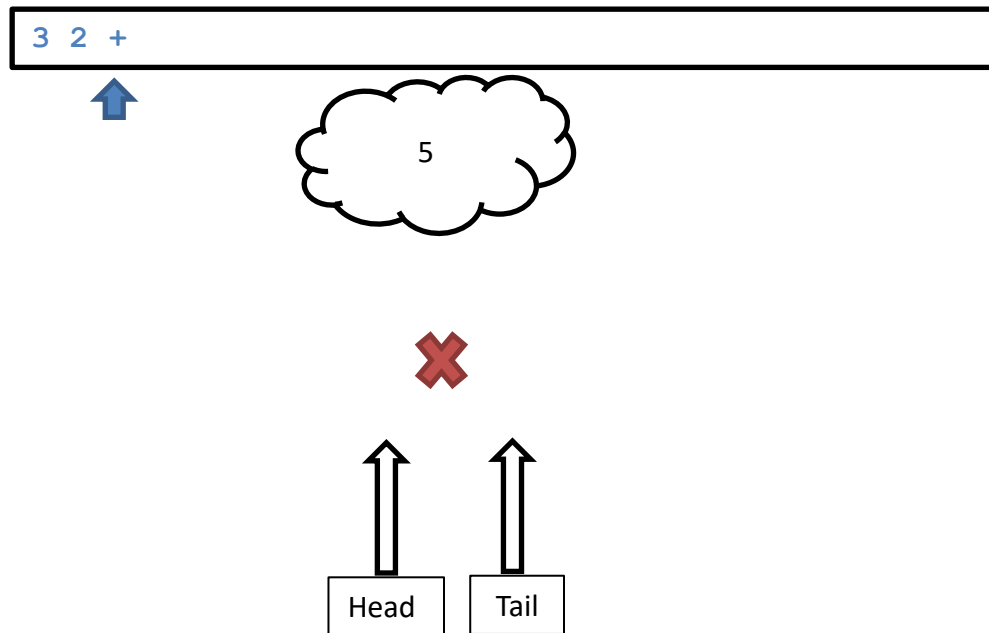
Reverse Polish Example

- + is an operator so pop of two



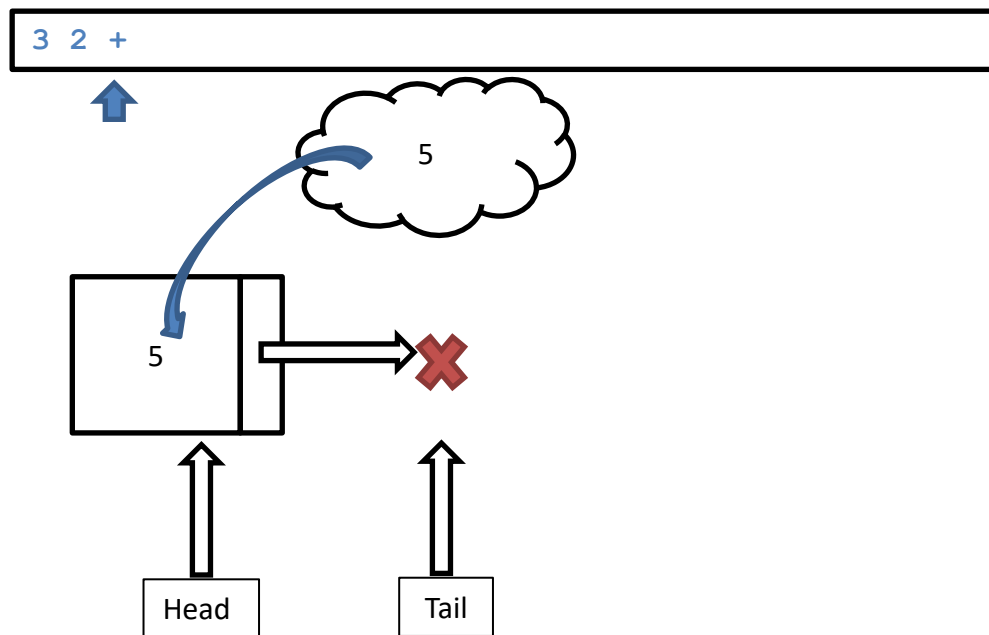
Reverse Polish Example

- Evaluate



Reverse Polish Example

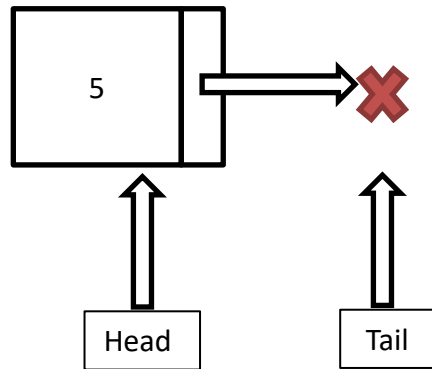
- Push the value back

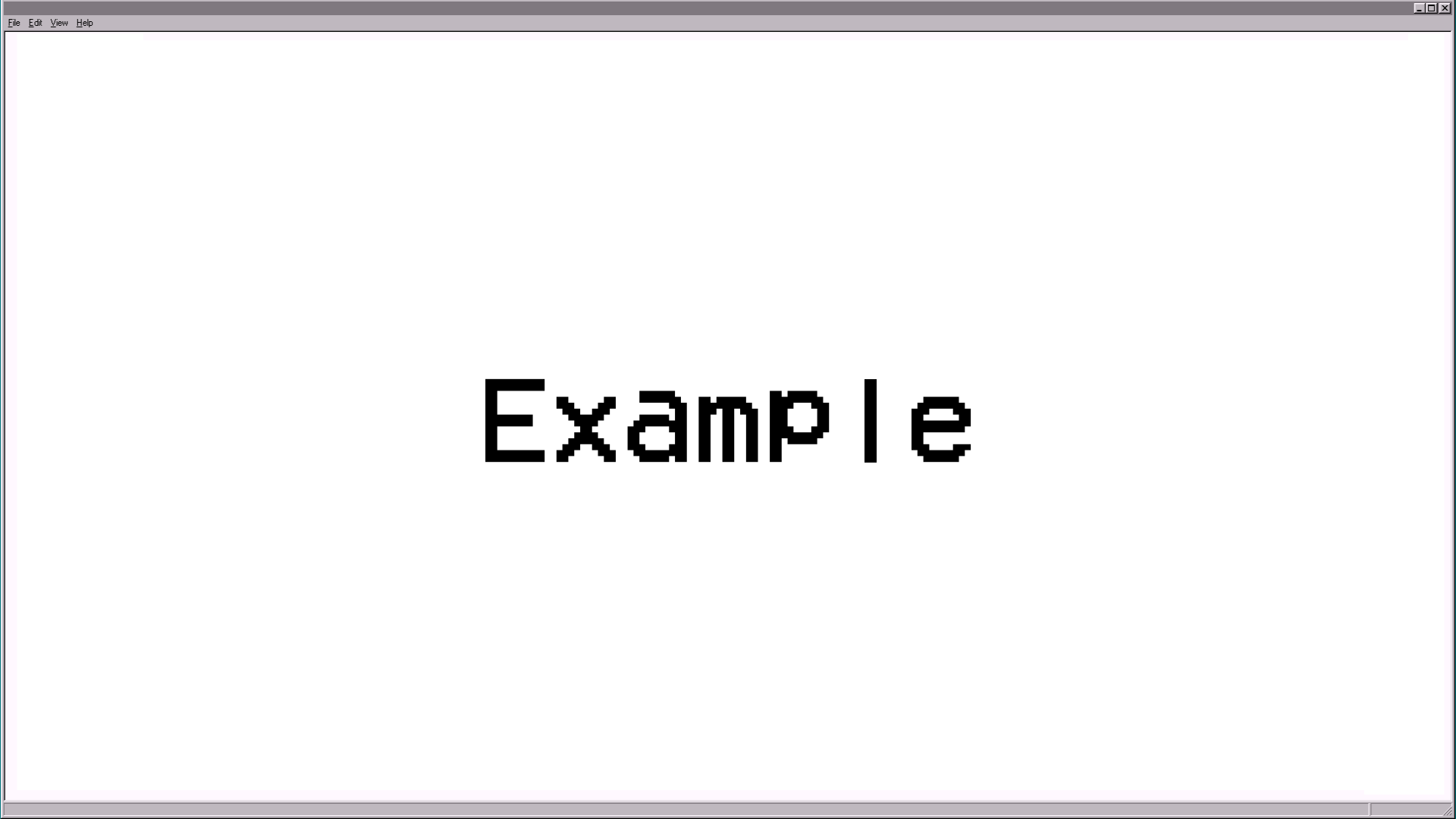


Reverse Polish Example

- DONE!

3 2 +





Example

Reverse Polish Example

- Here the user has inputted the string 8 2 – 3 *

8 2 – 3 *



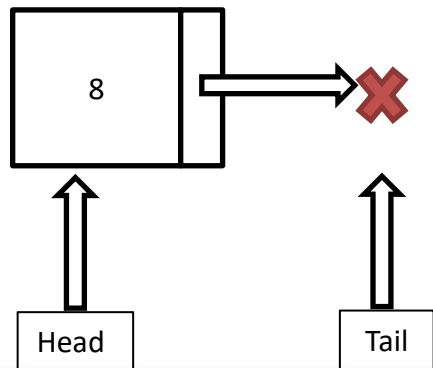

Head

Tail

Reverse Polish Example

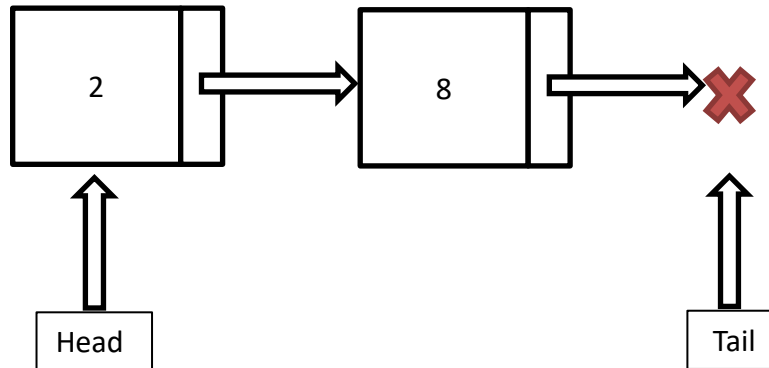
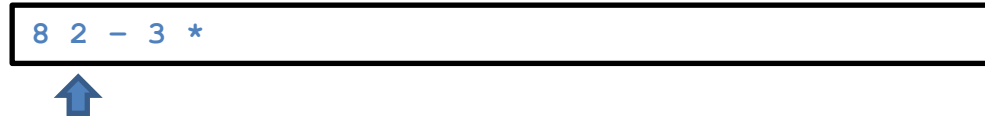
- 8 is a number so push it on the stack

8 2 - 3 *



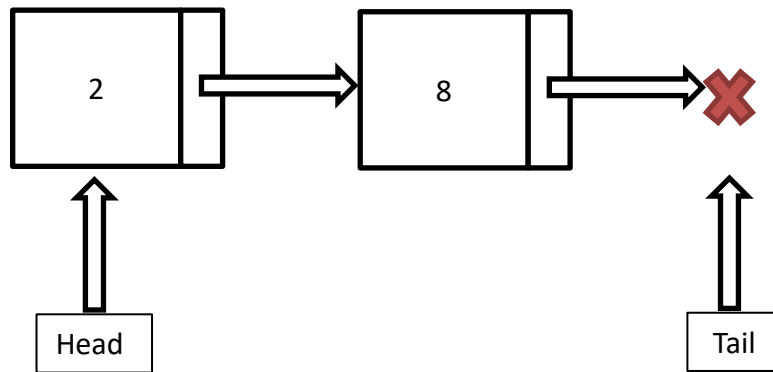
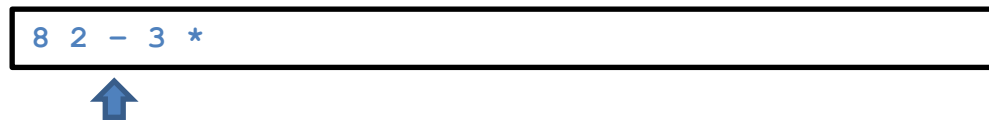
Reverse Polish Example

- 2 is a number so push it on the stack



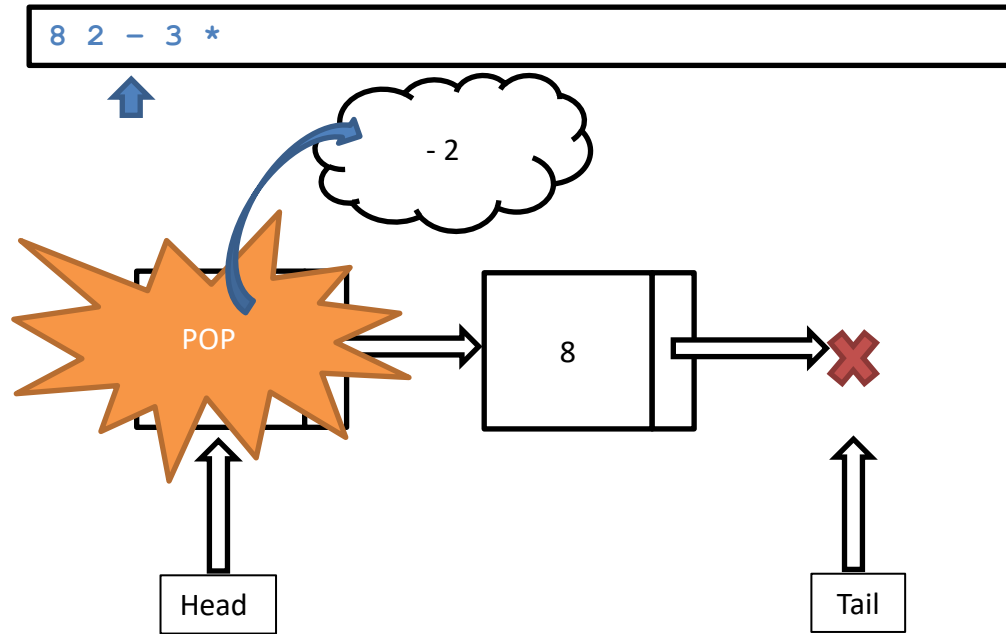
Reverse Polish Example

- - is an operator so pop of two



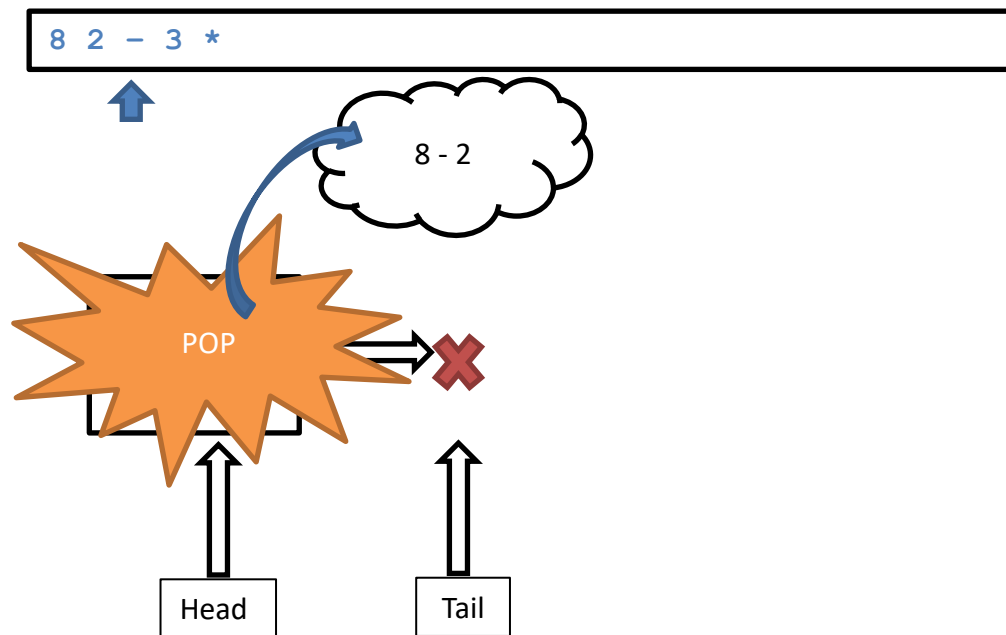
Reverse Polish Example

- + is an operator so pop of two



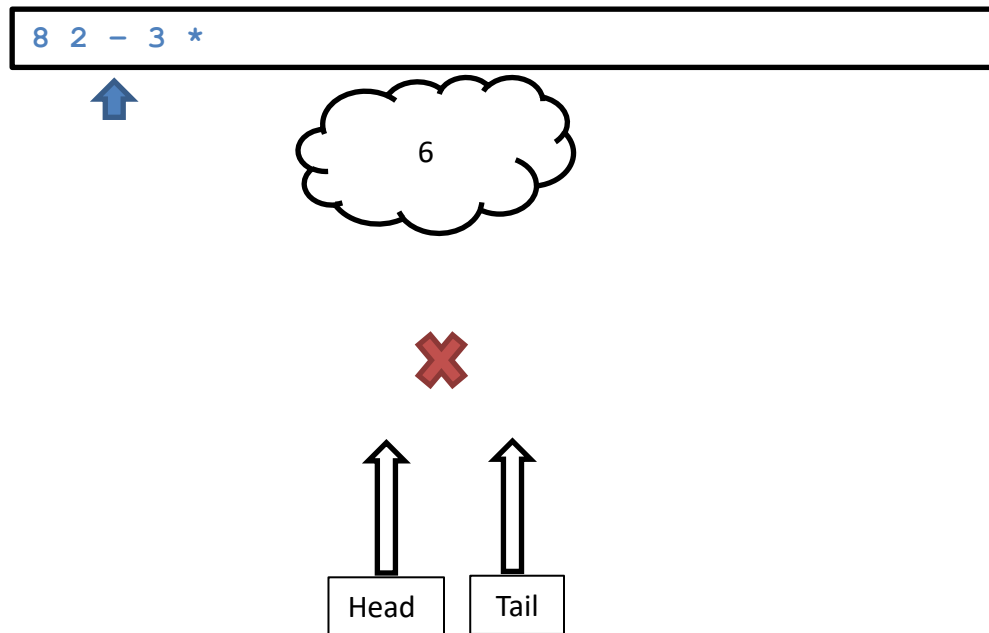
Reverse Polish Example

- + is an operator so pop of two



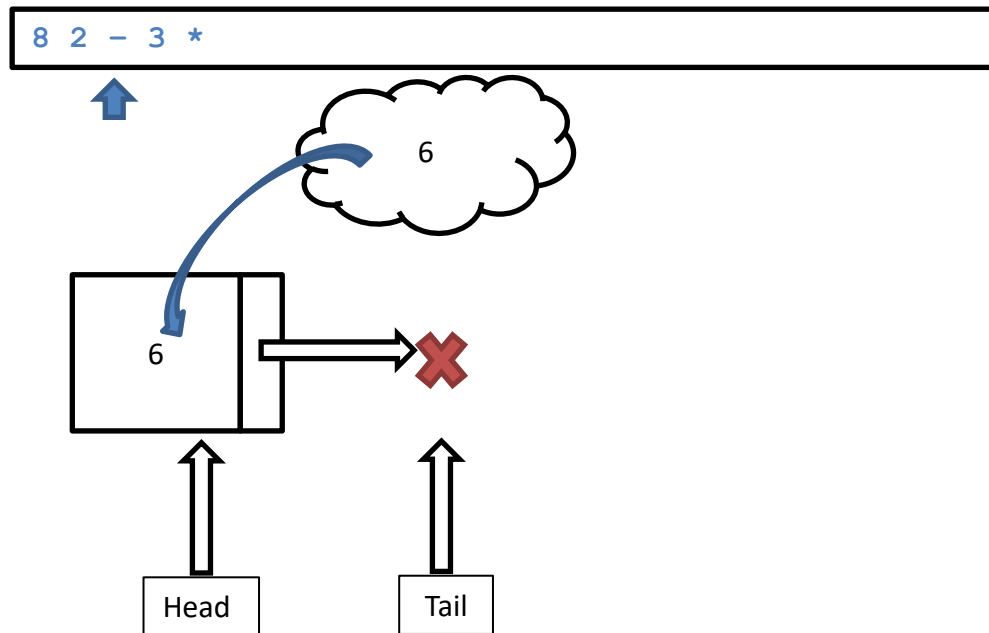
Reverse Polish Example

- Evaluate



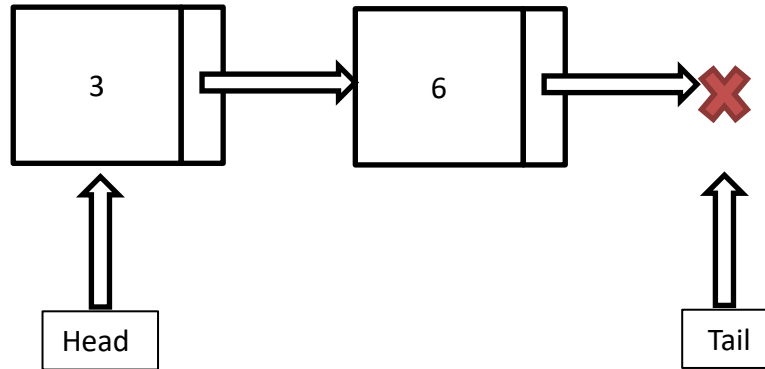
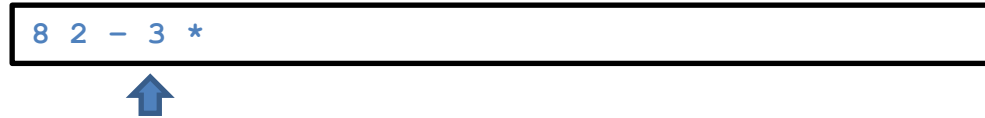
Reverse Polish Example

- Push the value back



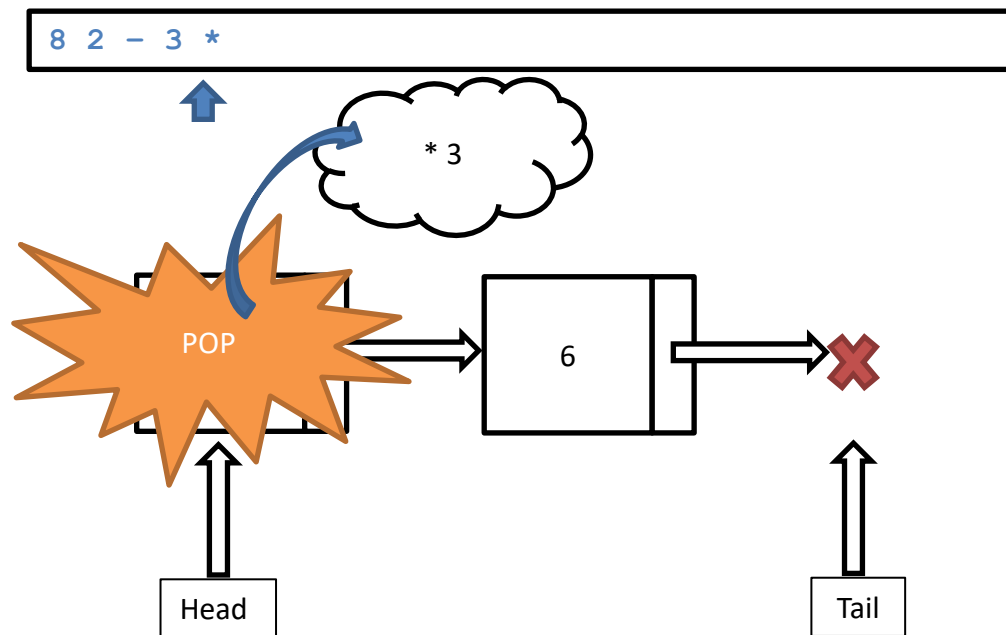
Reverse Polish Example

- 3 is a number so push it onto the stack



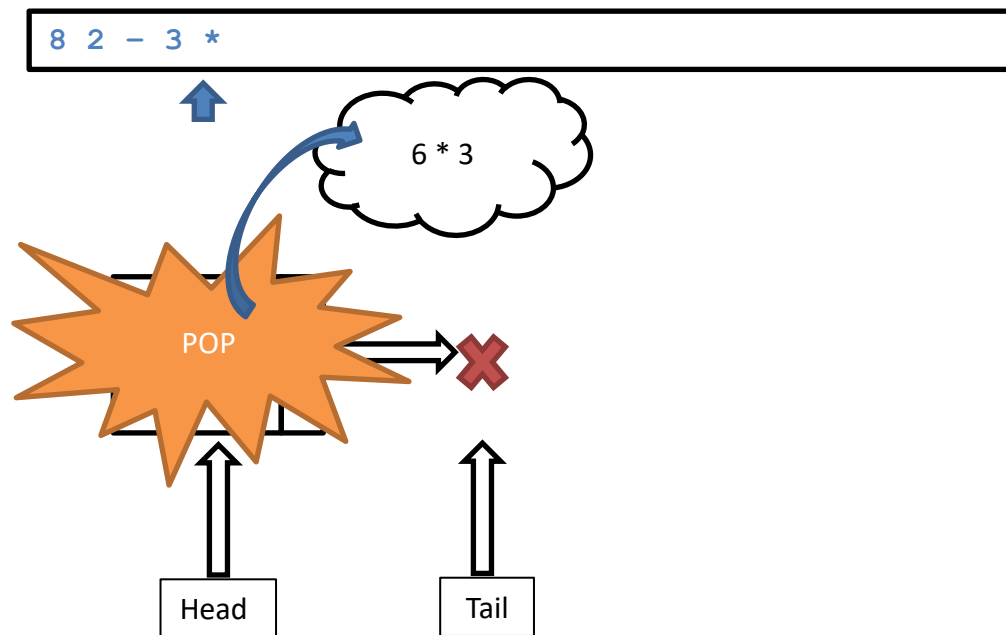
Reverse Polish Example

- * is an operator so pop of two



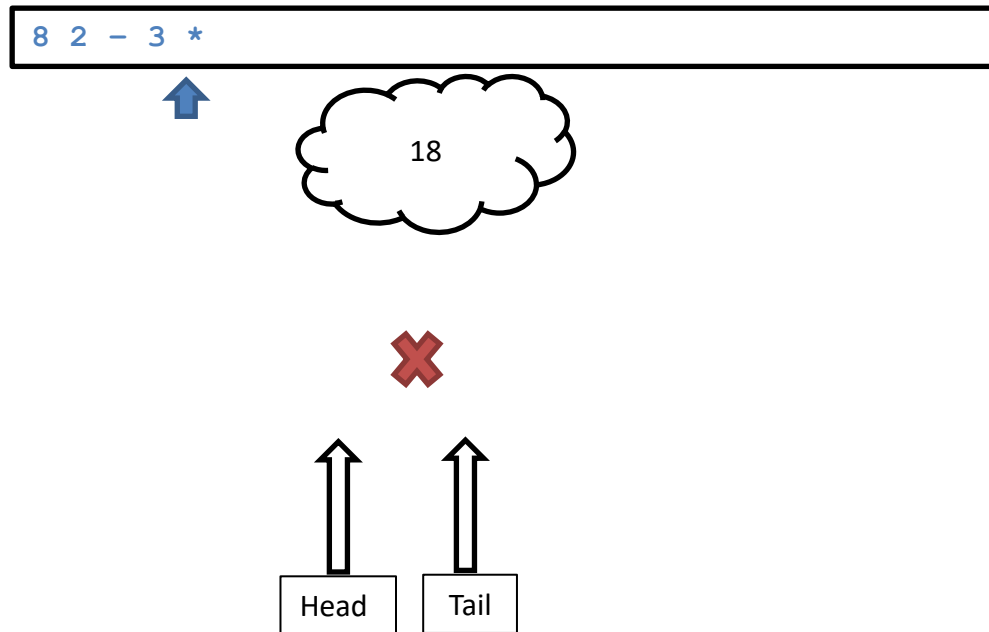
Reverse Polish Example

- * is an operator so pop of two



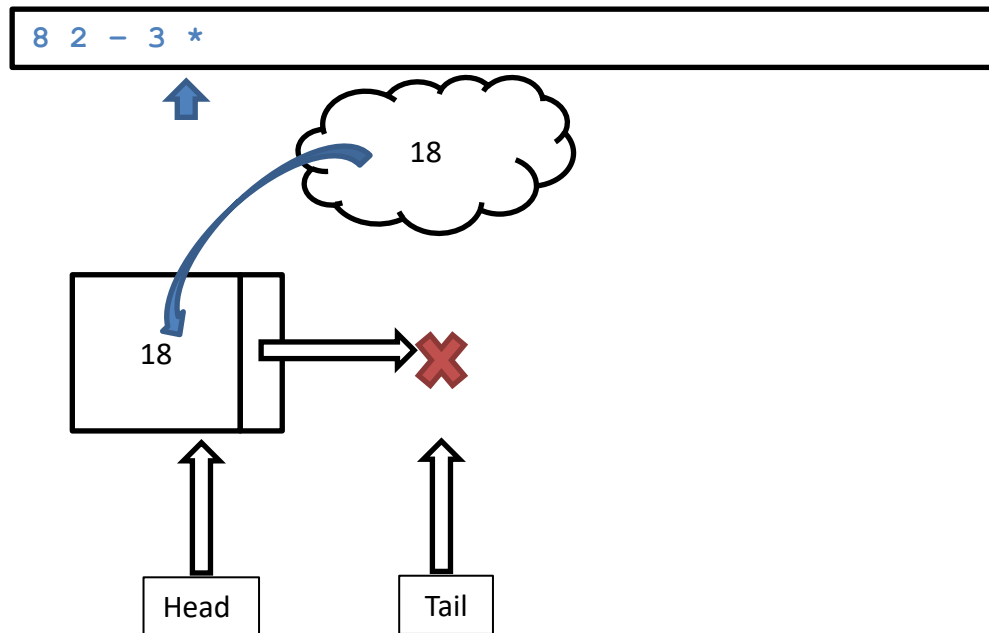
Reverse Polish Example

- Evaluate



Reverse Polish Example

- Push the value back



Reverse Polish Example

- DONE!

