Case Study 2

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Explication of abbreviations: https://s3.amazonaws.com/dl.ncsbe.gov/data/layout_ncvoter.txt

```
# contains info about the aggregate counts of voters who actually voted by demographic variables
votes <- read.table("history_stats_20201103.txt", header = TRUE, fill = TRUE, sep = '\t')</pre>
# contains info about the aggregate counts of registered voters by demographic variables
registers <- read.table("voter_stats_20201103.txt", header = TRUE, fill = TRUE, sep = '\t')
# set "" or " " to NA
registers[registers == ""] <- NA
registers[registers == " "] <- NA
votes[votes == " "] <- NA</pre>
# unique(registers$election_date) # "11/03/2020" NA
# unique(registers$stats type) # "history" NA
# unique(registers$update_date) # "01/13/2021" NA
# remove above three columns
registers <- registers %>%
  select(-election_date, -stats_type, -update_date)
votes <- votes %>%
  select(-election_date, -stats_type, -update_date)
votes <- votes %>%
  mutate(total_voters = as.numeric(total_voters))
registers <- registers %>%
  mutate(total_voters2 = as.numeric(total_voters))
votes <- votes %>%
  group_by(county_desc, age, party_cd, race_code, ethnic_code, sex_code) %>%
  summarize(total_vot = sum(total_voters, na.rm =T))
```

'summarise()' has grouped output by 'county_desc', 'age', 'party_cd', 'race_code', 'ethnic_code'. You

```
data <- registers %>%
  group_by(county_desc, party_cd, race_code, ethnic_code, sex_code, age) %>%
  summarize(total_reg = sum(total_voters2, na.rm= T)) %>%
  left_join(votes, by = c("county_desc", "age", "party_cd", "race_code",
                      "ethnic_code", "sex_code"))
## 'summarise()' has grouped output by 'county_desc', 'party_cd', 'race_code', 'ethnic_code', 'sex_code
data <- data %>%
  mutate(total_vot = as.numeric(total_vot),
         total_reg = as.numeric(total_reg))
         # county_desc = as.factor(county_desc),
         # party_cd = as.factor(party_cd),
         # race_code = as.factor(race_code),
         # sex code = as.factor(sex code),
         # ethnic_code = as.factor(ethnic_code),
         # age = as.factor(age))
#data <- data %>%
# filter(!is.na(total_req))
data$total_vot <- ifelse(is.na(data$total_vot), 0, data$total_vot)</pre>
data$total_vot <- ifelse(data$total_vot <= data$total_reg, data$total_vot, data$total_reg)</pre>
data <- data %>%
 drop_na()
# 13066 rows
set.seed(10)
counties <- sample(unique(data$county_desc), 30)</pre>
data <- data %>%
 filter(county_desc %in% counties)
data$race_code <- recode_factor(data$race_code, M = "Multiracial", U = "Undesignated")</pre>
data2 <- data %>%
  drop na() %>%
 mutate(total_not_vote = total_reg - total_vot) %>%
 pivot_longer(cols = c("total_vot", "total_not_vote"), names_to = "vote_or_not", values_to = "prob") %
 mutate(vote_or_not = ifelse(vote_or_not == "total_vot", 1, 0)) %>%
  mutate(row_expand = map(prob, ~rep_len(1, .x))) %>%
  unnest(cols = c(row_expand)) %>%
  select(-prob, -row_expand)
```

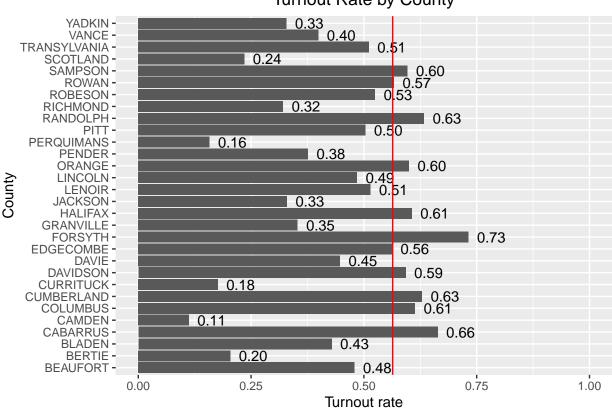
EDA

```
table(data2$vote_or_not)
```

turnout rate

```
turnout_rate <- sum(data$total_vot) / sum(data$total_reg)</pre>
data.frame(group = "Total", turnout_rate = turnout_rate)
## group turnout_rate
## 1 Total 0.5637756
data %>%
  group_by(county_desc) %>%
  summarise(total_reg = sum(total_reg),
            total_vot = sum(total_vot), .groups = "drop") %>%
  mutate(turnout_rate = total_vot / total_reg) %>%
  ggplot( aes(x = county_desc, y = turnout_rate)) +
  geom_bar(stat = "identity") +
  ylim(0,1) +
  xlab("County") + ylab("Turnout rate") +
  geom_text(aes(label=format(turnout_rate, digits = 2)), hjust = -0.3) +
  ggtitle("Turnout Rate by County") +
   theme(plot.title = element_text(hjust = 0.5)) +
  geom_hline(yintercept = turnout_rate, color = 'red') +
  coord_flip()
```

Turnout Rate by County



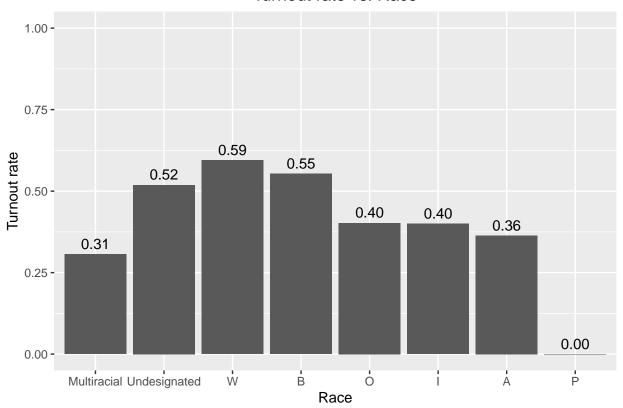
```
data %>%
  group_by(county_desc) %>%
  summarize(n = n())
```

```
## # A tibble: 30 x 2
##
      county desc
                       n
##
      <chr>
                   <int>
    1 BEAUFORT
##
                     105
    2 BERTIE
                      44
##
##
    3 BLADEN
                      74
                     295
##
    4 CABARRUS
##
    5 CAMDEN
                      23
##
    6 COLUMBUS
                      103
##
    7 CUMBERLAND
                     437
    8 CURRITUCK
                      65
##
    9 DAVIDSON
##
                     208
## 10 DAVIE
                      75
## # ... with 20 more rows
```

no extremely small sample size

race

Turnout rate vs. Race



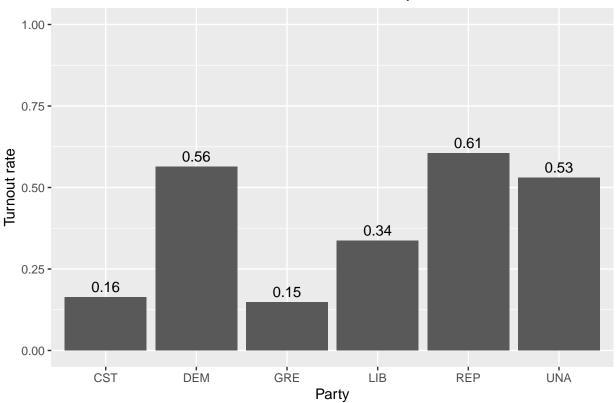
```
data %>%
  group_by(race_code) %>%
  summarize(n = n())
```

```
## # A tibble: 8 x 2
## race_code n
## 

fct> <int>
fct> <int>
## 1 Multiracial 275
## 2 Undesignated 859
## 3 W 1274
## 4 B 769
```

party





```
data %>%
  group_by(party_cd) %>%
  summarize(n = n())
```

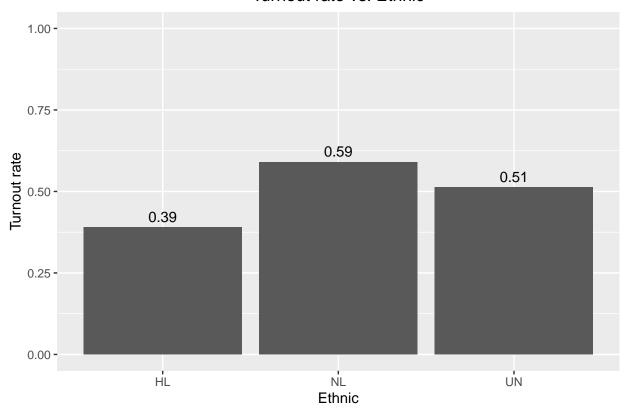
```
## # A tibble: 6 x 2
##
     party_cd
                  n
     <chr>
              <int>
## 1 CST
                 50
## 2 DEM
               1387
## 3 GRE
                 25
## 4 LIB
                194
## 5 REP
               1073
## 6 UNA
               1465
```

```
# "CST", "GRE" have small smaple size (50,25) and similar turnout rate (0.16,0.15) data$party_cd <- ifelse(data$party_cd %in% c("CST", "GRE"), "CST_GRE", data$party_cd)
```

ethnic groups

```
select(group = ethnic_code, turnout_rate) %>%
ggplot( aes(x = group, y = turnout_rate)) +
geom_bar(stat = "identity") +
ylim(0,1) +
xlab("Ethnic") + ylab("Turnout rate") +
geom_text(aes(label=format(turnout_rate, digits = 2)), vjust = -0.5) +
ggtitle("Turnout rate vs. Ethnic") +
    theme(plot.title = element_text(hjust = 0.5))
```

Turnout rate vs. Ethnic

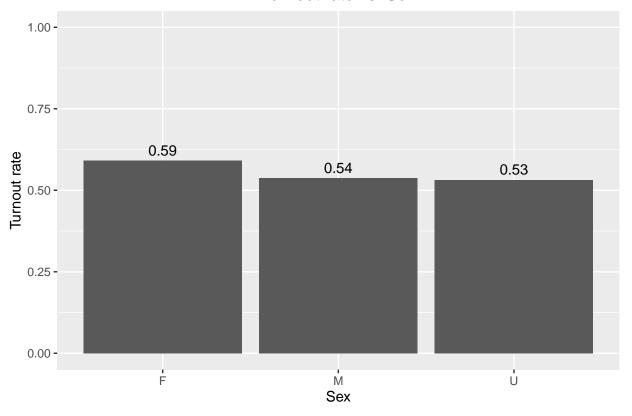


```
data %>%
  group_by(ethnic_code) %>%
  summarize(n = n())
```

\mathbf{Sex}

```
data %>%
group_by(sex_code) %>%
```

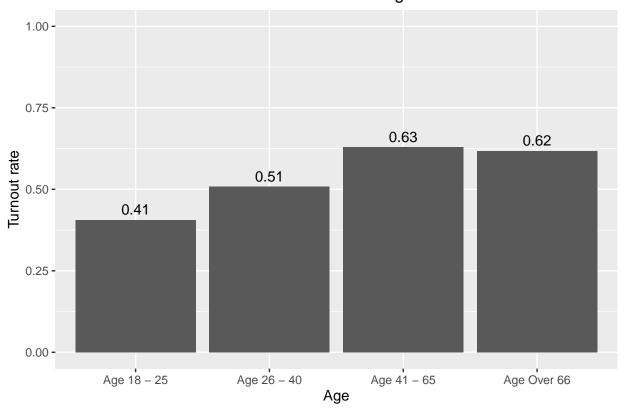
Turnout rate vs. Sex



```
data %>%
  group_by(sex_code) %>%
  summarize(n = n())
```

```
## # A tibble: 3 x 2
## sex_code n
## <chr> int>
## 1 F 1835
## 2 M 1780
## 3 U 579
```

Turnout rate vs. Age

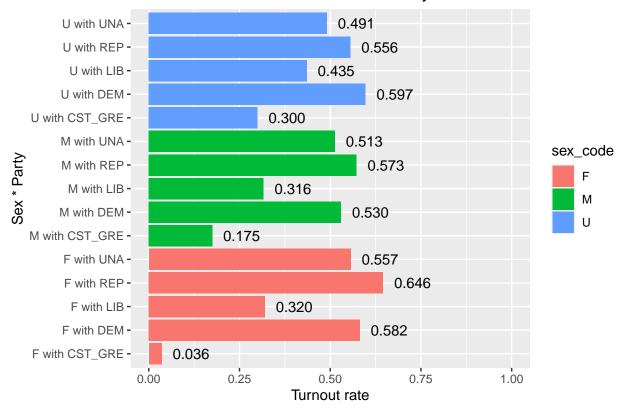


```
data %>%
  group_by(age) %>%
  summarize(n = n())
```

```
## 3 Age 41 - 65 1248
## 4 Age Over 66 743
```

sex & party

Turnout rate vs. Sex*Party



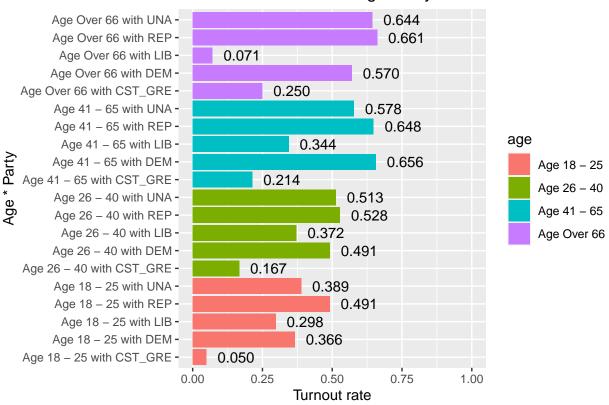
```
data %>%
  group_by(sex_code, party_cd) %>%
  summarize(n = n())
```

'summarise()' has grouped output by 'sex_code'. You can override using the '.groups' argument.

```
## # A tibble: 15 x 3
## # Groups:
              sex_code [3]
##
      sex_code party_cd
##
      <chr>
              <chr>
                        <int>
##
  1 F
              CST_GRE
                           26
## 2 F
              DEM
                          628
## 3 F
              LIB
                          81
## 4 F
              REP
                          450
## 5 F
              UNA
                          650
              CST_GRE
                          34
## 6 M
## 7 M
              DEM
                          572
## 8 M
                          79
              LIB
## 9 M
              REP
                          480
## 10 M
              UNA
                          615
## 11 U
              CST_GRE
                          15
## 12 U
              DEM
                          187
## 13 U
              LIB
                          34
## 14 U
              REP
                          143
## 15 U
              UNA
                          200
```

age & party

Turnout rate vs. Age*Party



```
data %>%
  group_by(age, party_cd) %>%
  summarize(n = n())
```

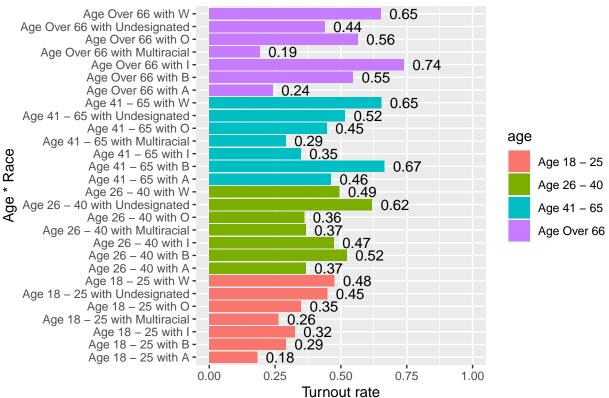
'summarise()' has grouped output by 'age'. You can override using the '.groups' argument.

```
## # A tibble: 20 x 3
## # Groups:
               age [4]
##
      age
                  party_cd
      <chr>
                   <chr>>
                            <int>
##
    1 Age 18 - 25 CST_GRE
                               18
##
    2 Age 18 - 25 DEM
                              329
    3 Age 18 - 25 LIB
                               60
    4 Age 18 - 25 REP
                              237
    5 Age 18 - 25 UNA
                              388
##
    6 Age 26 - 40 CST_GRE
                               28
   7 Age 26 - 40 DEM
                              383
    8 Age 26 - 40 LIB
                               70
    9 Age 26 - 40 REP
                              277
## 10 Age 26 - 40 UNA
                              413
## 11 Age 41 - 65 CST_GRE
                               25
## 12 Age 41 - 65 DEM
                              402
## 13 Age 41 - 65 LIB
                               53
                              348
## 14 Age 41 - 65 REP
## 15 Age 41 - 65 UNA
                              420
## 16 Age Over 66 CST_GRE
                                4
```

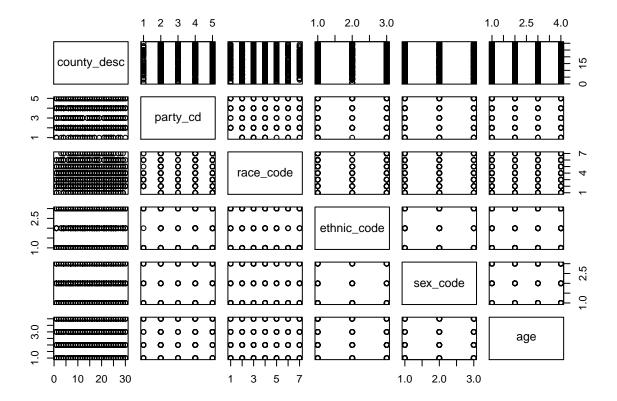
```
## 17 Age Over 66 DEM 273
## 18 Age Over 66 LIB 11
## 19 Age Over 66 REP 211
## 20 Age Over 66 UNA 244
```

age & race

Turnout rate vs. Age*Race



```
data %>%
  group_by(age, race_code) %>%
  summarize(n = n())
## 'summarise()' has grouped output by 'age'. You can override using the '.groups' argument.
## # A tibble: 28 x 3
## # Groups: age [4]
##
      age
                 race\_code
                                  n
##
      <chr>
                 <fct>
                               <int>
## 1 Age 18 - 25 Multiracial
                                 84
## 2 Age 18 - 25 Undesignated
                                214
                                308
## 3 Age 18 - 25 W
## 4 Age 18 - 25 B
                                182
## 5 Age 18 - 25 O
                                149
## 6 Age 18 - 25 I
                                 46
## 7 Age 18 - 25 A
                                 49
## 8 Age 26 - 40 Multiracial
                                 95
## 9 Age 26 - 40 Undesignated
                                235
## 10 Age 26 - 40 W
                                 351
## # ... with 18 more rows
data <- data %>%
  mutate(total_vot = as.numeric(total_vot),
        total_reg = as.numeric(total_reg),
         county_desc = as.factor(county_desc),
        party_cd = as.factor(party_cd),
        race_code = as.factor(race_code),
         sex_code = as.factor(sex_code),
         ethnic_code = as.factor(ethnic_code),
         age = as.factor(age))
pairs(data[,1:6])
```



Model

```
mod1 <- glmer(cbind(total_vot, total_reg - total_vot) ~</pre>
                      party_cd + race_code + ethnic_code + sex_code + age + (1|county_desc),
                    data = data, family = binomial,
              control=glmerControl(optimizer = "bobyqa"))
BIC(mod1)
## [1] 40615.93
mod2 <- glmer(cbind(total_vot, total_reg - total_vot) ~</pre>
                       -1 + race_code + ethnic_code + sex_code + age + (1 | county_desc),
                    data = data, family = binomial,
              control=glmerControl(optimizer = "bobyqa", optCtrl=list(maxfun=2e5)))
BIC(mod2)
## [1] 40712.29
mod3 <- glmer(cbind(total_vot, total_reg - total_vot) ~</pre>
                  party_cd + race_code + ethnic_code + sex_code + age +
                  sex_code:party_cd + age:party_cd + (1|county_desc),
                data = data, family = binomial,
              control=glmerControl(optimizer = "bobyqa", optCtrl=list(maxfun=2e5)))
BIC(mod3)
```

[1] 40298.74

[1] 39476.9

Table 1: Forward model selection

Model	LRT.p.value	BIC
Base model		40615.93
Without intercept	0	40712.29
Add the interaction of sex and party_cd, and age and party	0	40298.74
Add the interaction of sex and party_cd, age and party, and age and race	0	39476.90

In order to answer the questions of interest, we require the following features in our model:

- 1. Fixed effects for various demographic subgroups (race, ethnicity, age, sex)
- 2. Random effects for county
- 3. Sex-Party interaction
- 4. Age-Party interaction

summary(mod4)

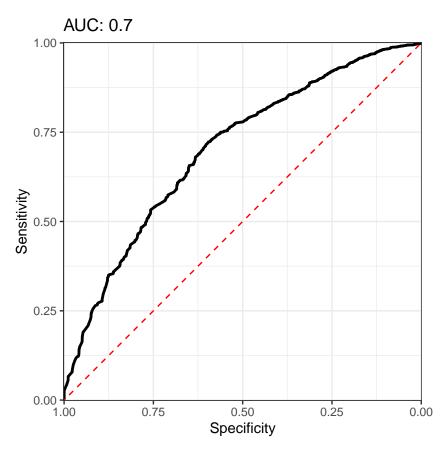
```
## Generalized linear mixed model fit by maximum likelihood (Laplace
## Approximation) [glmerMod]
## Family: binomial ( logit )
## Formula:
## cbind(cbind(total_vot, total_reg - total_vot)) ~ party_cd + race_code +
## ethnic_code + sex_code + age + sex_code:party_cd + age:party_cd +
## age:race_code + (1 | county_desc)
## Data: data
## Control: glmerControl(optimizer = "bobyqa", optCtrl = list(maxfun = 2e+05))
```

```
##
##
                 BIC
                       logLik deviance df.resid
        AIC
##
   39115.4 39476.9 -19500.7 39001.4
##
## Scaled residuals:
##
       \mathtt{Min}
                  1Q
                      Median
                                    3Q
                                             Max
  -19.8597 -0.9768 -0.2823
                                1.4499
##
## Random effects:
   Groups
                Name
                            Variance Std.Dev.
   county_desc (Intercept) 0.7272
## Number of obs: 4194, groups: county_desc, 30
## Fixed effects:
##
                                         Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                         -4.10771
                                                     1.03678 -3.962 7.43e-05 ***
                                                               2.498 0.012484 *
## party_cdDEM
                                         2.53214
                                                     1.01360
## party cdLIB
                                         1.84816
                                                     1.05097
                                                               1.759 0.078657 .
                                                     1.01358
                                                               2.595 0.009470 **
## party_cdREP
                                         2.62985
## party cdUNA
                                         2.42949
                                                     1.01313
                                                               2.398 0.016485 *
## race_codeUndesignated
                                         0.75694
                                                     0.18951
                                                               3.994 6.49e-05 ***
## race_codeW
                                                     0.18421
                                                               5.039 4.67e-07 ***
                                         0.92827
## race_codeB
                                                              -0.365 0.715430
                                         -0.06776
                                                     0.18587
                                                     0.20512
                                                               2.714 0.006655 **
## race code0
                                         0.55664
## race_codeI
                                         0.19965
                                                     0.22622
                                                               0.883 0.377485
## race codeA
                                         -0.77203
                                                     0.28168 -2.741 0.006129 **
## ethnic_codeHL
                                         -0.71634
                                                     0.05638 -12.706 < 2e-16 ***
## ethnic_codeUN
                                         -0.34210
                                                     0.02179 -15.698 < 2e-16 ***
                                                     1.09263 -1.442 0.149213
## sex_codeF
                                        -1.57591
## sex_codeU
                                         0.89680
                                                     0.73415
                                                               1.222 0.221876
## ageAge 41 - 65
                                         1.01423
                                                     1.10640
                                                               0.917 0.359306
## ageAge Over 66
                                         1.23936
                                                     1.60972
                                                               0.770 0.441348
## ageAge 26 - 40
                                         0.88208
                                                     1.06869
                                                               0.825 0.409156
## party_cdDEM:sex_codeF
                                         1.80057
                                                     1.09299
                                                               1.647 0.099480
## party cdLIB:sex codeF
                                         1.65679
                                                     1.12124
                                                               1.478 0.139505
## party_cdREP:sex_codeF
                                         1.76578
                                                               1.615 0.106204
                                                     1.09303
## party cdUNA:sex codeF
                                         1.70029
                                                     1.09305
                                                               1.556 0.119815
## party_cdDEM:sex_codeU
                                        -0.36358
                                                     0.73556 -0.494 0.621103
## party_cdLIB:sex_codeU
                                        -0.22507
                                                     0.80290
                                                              -0.280 0.779236
## party_cdREP:sex_codeU
                                                              -0.895 0.370841
                                        -0.65764
                                                     0.73488
## party cdUNA:sex codeU
                                                              -1.207 0.227375
                                        -0.88629
                                                     0.73420
## party_cdDEM:ageAge 41 - 65
                                         -0.98003
                                                     1.07549
                                                              -0.911 0.362165
## party_cdLIB:ageAge 41 - 65
                                        -1.75963
                                                     1.12155
                                                              -1.569 0.116665
## party_cdREP:ageAge 41 - 65
                                                     1.07549
                                                             -1.188 0.235001
                                        -1.27722
## party_cdUNA:ageAge 41 - 65
                                        -1.15928
                                                     1.07495 -1.078 0.280830
## party_cdDEM:ageAge Over 66
                                                     1.52278
                                                              -1.331 0.183179
                                         -2.02686
## party_cdLIB:ageAge Over 66
                                        -4.22539
                                                     1.88115
                                                              -2.246 0.024693 *
## party_cdREP:ageAge Over 66
                                        -1.90879
                                                     1.52305
                                                              -1.253 0.210108
## party_cdUNA:ageAge Over 66
                                         -1.31378
                                                     1.52280
                                                              -0.863 0.388281
## party_cdDEM:ageAge 26 - 40
                                         -0.76260
                                                     1.04724
                                                              -0.728 0.466493
## party_cdLIB:ageAge 26 - 40
                                                              -0.475 0.635136
                                        -0.51396
                                                     1.08314
## party cdREP:ageAge 26 - 40
                                        -0.44149
                                                     1.04735
                                                              -0.422 0.673365
## party_cdUNA:ageAge 26 - 40
                                        -0.35145
                                                     1.04660 -0.336 0.737021
## race codeUndesignated:ageAge 41 - 65 0.50540
                                                     0.28385
                                                               1.780 0.074994 .
```

```
## race_codeW:ageAge 41 - 65
                                         0.93852
                                                    0.27987
                                                              3.353 0.000798 ***
                                                    0.28132
                                                              6.567 5.15e-11 ***
## race_codeB:ageAge 41 - 65
                                         1.84728
## race code0:ageAge 41 - 65
                                        0.39488
                                                    0.30552 1.292 0.196186
## race_codeI:ageAge 41 - 65
                                                    0.31629
                                                             0.190 0.849274
                                         0.06011
## race_codeA:ageAge 41 - 65
                                         1.52298
                                                    0.36870
                                                             4.131 3.62e-05 ***
## race codeUndesignated:ageAge Over 66 0.67358
                                                    0.54479
                                                             1.236 0.216312
## race codeW:ageAge Over 66
                                                    0.53707 2.473 0.013407 *
                                         1.32806
## race_codeB:ageAge Over 66
                                                    0.53894 3.736 0.000187 ***
                                         2.01324
## race_codeO:ageAge Over 66
                                         1.19009
                                                    0.57100 2.084 0.037141 *
## race_codeI:ageAge Over 66
                                         2.41249
                                                    0.59132 4.080 4.51e-05 ***
## race_codeA:ageAge Over 66
                                         0.86591
                                                    0.65675 1.318 0.187340
## race_codeUndesignated:ageAge 26 - 40 0.58624
                                                    0.24576
                                                              2.385 0.017058 *
## race_codeW:ageAge 26 - 40
                                        -0.39687
                                                    0.24006 -1.653 0.098289 .
## race_codeB:ageAge 26 - 40
                                                             3.246 0.001172 **
                                         0.78775
                                                    0.24271
## race_codeO:ageAge 26 - 40
                                                    0.27118 -1.219 0.222859
                                        -0.33055
## race_codeI:ageAge 26 - 40
                                        0.33277
                                                    0.30020
                                                              1.109 0.267638
## race_codeA:ageAge 26 - 40
                                                    0.35115
                                        0.58063
                                                             1.653 0.098230 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Correlation matrix not shown by default, as p = 56 > 12.
## Use print(x, correlation=TRUE) or
##
      vcov(x)
                      if you need it
chart_fixef <- function(model) {</pre>
  summary(model)$coefficients %>%
    as.data.frame() %>%
    mutate(`95% CI` = paste0(
      '[',
      round(Estimate - 1.96 * `Std. Error`, 3), ', '
     round(Estimate + 1.96 * `Std. Error`, 3), ']' )
   ) %>%
   select(Estimate, `95% CI`) %>%
   kable(digits=3) %>%
   kable_styling(full_width=FALSE) %>%
   kable classic()
}
# expand data from aggregated format
data_expand <- data %>%
  mutate(resp = map2(total_vot, total_reg, ~ c(
   rep(1, .x), rep(0, .y - .x)
  ))) %>%
  unnest(cols = c(resp)) %>%
  select(-c(total_reg, total_vot))
# split into train and test
sample <- sample(c(TRUE, FALSE), nrow(data_expand), replace=TRUE, prob=c(0.7,0.3))</pre>
train <- data expand[sample,]</pre>
test <- data_expand[!sample,]</pre>
# fit model on train data
```

```
### fit any model you like on unaggregated train data
### will take a while...
# mod2 <- glmer(resp ~ 1 + party_cd + (1 | county_desc),</pre>
                data = train, family = binomial)
# ROC + AUC
predicted <- predict(mod2, test, type="response")</pre>
rocobj <- roc(test$resp, predicted)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
ggroc(rocobj, size=1) +
  coord_fixed() +
  scale_x_reverse(
   name = "Specificity",
   limits = c(1,0),
   expand = c(0.001, 0.001)
  ) +
  scale_y_continuous(
  name = "Sensitivity",
   limits = c(0,1),
   expand = c(0.001, 0.001)
  geom_abline(intercept=1, slope=1, linetype="dashed", color="red") +
  labs(title=paste("AUC:", round(rocobj$auc, 3))) +
 theme_bw()
```

Scale for 'x' is already present. Adding another scale for 'x', which will ## replace the existing scale.

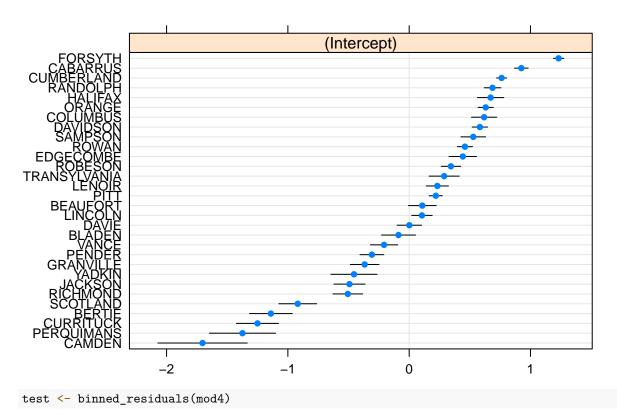


	Estimate	95% CI
(Intercept)	-1.988	[-2.859, -1.117]
party_cdDEM	1.633	[0.801, 2.466]
party_cdLIB	0.667	[-0.224, 1.559]
party_cdREP	1.821	[0.988, 2.653]
party_cdUNA	1.609	[0.777, 2.442]
party_cdCST_GRE:sex_codeF	-1.812	[-3.96, 0.336]
party_cdDEM:sex_codeF	0.238	[0.186, 0.291]
party_cdLIB:sex_codeF	0.043	[-0.433, 0.52]
party_cdREP:sex_codeF	0.243	[0.184, 0.302]
party_cdUNA:sex_codeF	0.179	[0.12, 0.237]
party_cdCST_GRE:sex_codeU	0.507	[-0.776, 1.79]
party_cdDEM:sex_codeU	0.178	[0.06, 0.297]
party_cdLIB:sex_codeU	0.616	[-0.001, 1.233]
party_cdREP:sex_codeU	-0.119	[-0.225, -0.014]
party_cdUNA:sex_codeU	-0.292	[-0.378, -0.206]

Random Effects dotplot(ranef(mod4))

\$county_desc

county_desc



Warning: Probably bad model fit. Only about 9% of the residuals are inside the error bounds.

```
as.data.frame() %>%
#
   mutate(`95% CI` = paste0(
#
      "[", round(Q2.5, 3), ",", round(Q97.5, 3), "]"
  )) %>%
#
  select(-c(Est.Error, Q2.5, Q97.5)) %>%
#
  kable(digits=3) %>%
#
  kable_classic() %>%
#
  kable\_styling(full\_width=FALSE)
# ranef(mod)$county_desc %>%
# as.data.frame() %>%
  tibble::rownames_to_column(var="County") %>%
#
#
  ggplot(aes(y=reorder(County, Estimate.Intercept), x=Estimate.Intercept)) +
#
    geom_point(color="blue", size=2) +
#
     geom_linerange(aes(
      xmin=Q2.5.Intercept, xmax=Q97.5.Intercept
#
#
     )) +
#
     labs(
#
       x="Intercept",
       y="County"
#
#
     theme_bw()
```