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1. Social Planner's problem.

$$\max_{C_{1},C_{2}} \left\{ \left( C_{1}^{0.5}C_{2}^{0.5} - \frac{l^{2}}{2} \right)^{2} + 0.96 \times V(Z',A',k') \right\} = V(Z,A,k)$$

$$C_{1},C_{2},\left\{ \left( C_{1}^{0.5}C_{2}^{0.5} - \frac{l^{2}}{2} \right)^{2} + 0.96 \times V(Z',A',k') \right\} = V(Z,A,k)$$

$$k' \quad S.t. \quad C_{1} + k' = e^{Z} k^{0.33} l_{1}^{0.67} + 0.9k$$

$$C_{2} = A l_{2}$$

$$l = l_{1} + l_{2}$$

2. Steady state. - Solved by FOC of the Bellman Equation In the deterministic state where z=0 and A=1,

$$V(k) = \max_{l_1, l_2, k'} \left\{ \left( k^{0.33} l_1^{0.67} + 0.9k - k' \right)^{0.5} l_2^{0.5} - \frac{\left( l_1 + l_2 \right)^2}{2} + 0.96 V(k') \right\}$$

 $F.o.c[li] li+li=0.5 \times 0.67 \times li \times (k^{0.33}li^{0.67}+0.9k-k')^{-0.5}$   $[li] li+li=0.5 \times (k^{0.33}li^{0.67}+0.9k-k')^{0.5}$   $(k^{0.33}li^{0.67}+0.9k-k')^{0.5}$ 

$$[k]$$
  $I = 0.96 \times (0.9 + 1.0.67 \cdot 0.33 k^{-0.67})$ 

By Fsolve of Matlab, we get Rss = 0.83  $L_1ss = 0.23$   $L_2ss = 0.27$   $C_1ss = 0.27$   $C_2ss = 0.27$ Vss = 0.14