

1. Sort the sequence 3, 1, 4, 7, 5, 9, 2, 6, 8 using Insertion Sort (Please present the sorting procedure as shown on page 15 in slides of Course\_09) and calculate the number of swaps.

The procedure:

- Insertion sort consists of 8 passes.
- For pass P = 1 through 8, insertion sort ensures that the elements in position 0 to P are in sorted order.

Original	3	<u>1</u>	4	7	5	9	2	6	8	Swap	Comparison
After P = 1	1	3	<u>4</u>	7	5	9	2	6	8	1	2
After P = 2	1	3	4	<u>7</u>	5	9	2	6	8	0	1
After P = 3	1	3	4	7	<u>5</u>	9	2	6	8	0	1
After P = 4	1	3	4	5	7	<u>9</u>	2	6	8	1	2
After P = 5	1	3	4	5	7	9	<u>2</u>	6	8	0	1
After P = 6	1	2	3	4	5	7	9	<u>6</u>	8	5	6
After P = 7	1	2	3	4	5	6	7	9	<u>8</u>	2	3
After P = 8	1	2	3	4	5	6	7	8	9	1	2
<b>Sum</b>	-	-	-	-	-	-	-	-	-	<b>10</b>	<b>18</b>

2. Sort the sequence 9, 8, 7, 6, 5, 4, 3, 2, 1 using Shell Sort with the increments {7, 3, 1} (Please present the sorting procedure as shown on page 34 in slides of Course\_09) and calculate the number of swaps.

The procedure:

$h_1 = 1$

$h_2 = 3$

$h_3 = 7$

Sub-Arrays

**Original**

9	8	7	6	5	4	3	2	1
---	---	---	---	---	---	---	---	---

Distance = 7



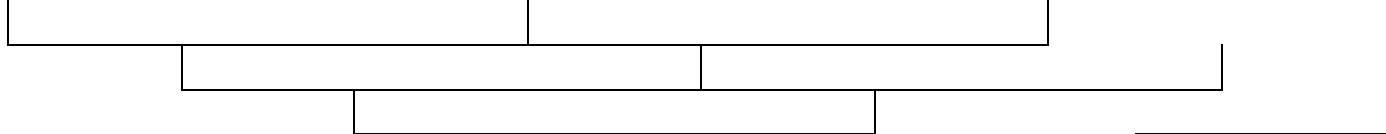
{9, 2}

{8, 1}

**After 7-sort**

2	1	7	6	5	4	3	9	8
---	---	---	---	---	---	---	---	---

Distance = 3



{2, 6, 3}

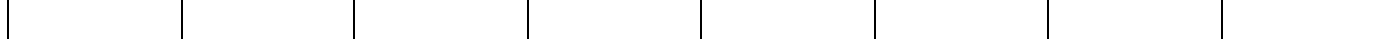
{1, 5, 9}

{7, 4, 8}

**After 3-sort**

2	1	4	3	5	7	6	9	8
---	---	---	---	---	---	---	---	---

Distance = 1



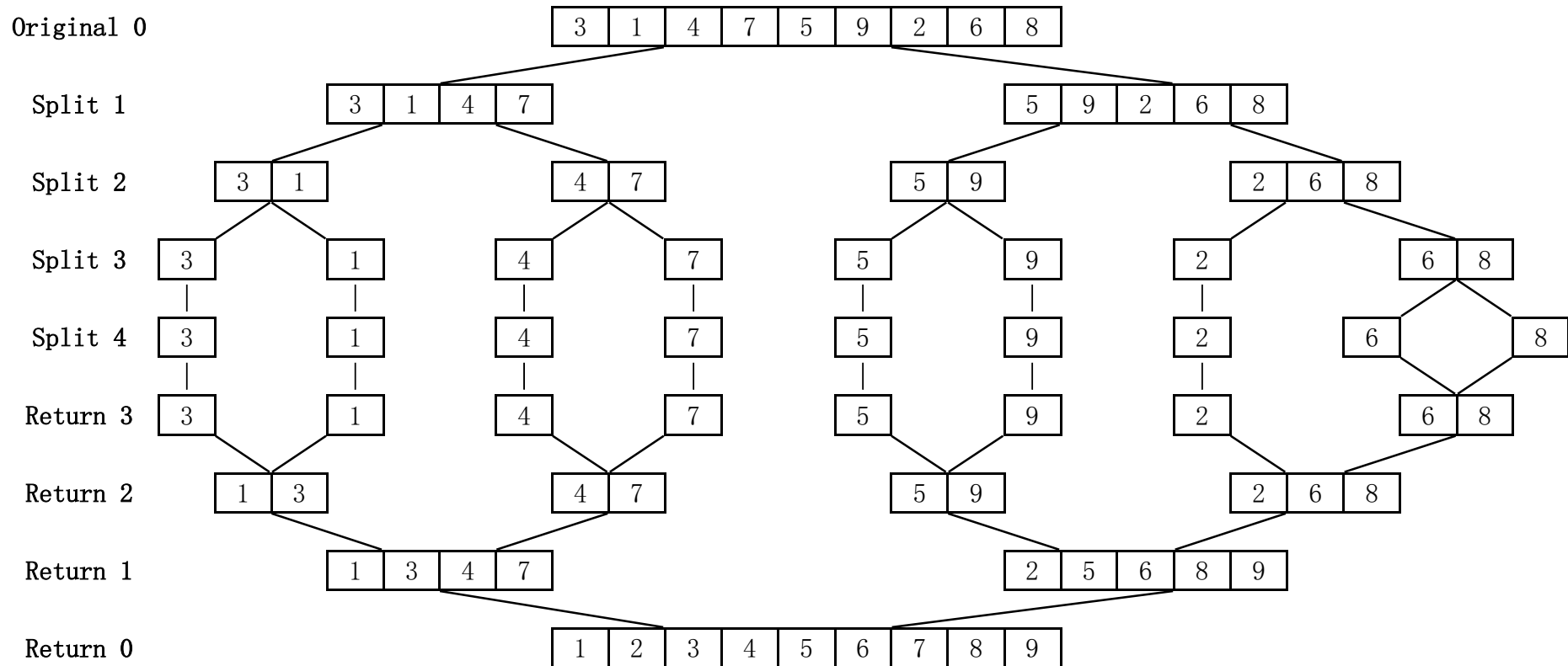
**After 1-sort**

1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---

Number of swaps =  $(1 + 1) + (1 + 0 + 1) + (1 + 1 + 1 + 1) = 8$

3. Sort 3, 1, 4, 7, 5, 9, 2, 6, 8 using Merge Sort (Please present the sorting procedure as shown on page 45 in slides of Course\_09).

The procedure:



4. Sort 3, 1, 4, 7, 5, 9, 2, 6, 8 using Quick Sort with median-of-three pivot selection and the partitioning strategy (Please present the sorting procedure as shown in pages 67 and 68 in slides of Course\_09).

The procedure: (ppt 67 页的 while 边界有问题, 导致 n=2 时出现错误, 因次以下答案将 while 边界改为了“i <= j”)

**Original A[9]**

3	1	4	7	5	9	2	6	8
---	---	---	---	---	---	---	---	---

**1st Partition :**

$\text{median}(A[0], A[4], A[8]) = \text{median}(3, 5, 8) = 5 = A[4]$

$\text{pivot} = A[4]; \text{left} = 0; \text{right} = 9; \text{swap}(A[4], A[9]);$

$i = \text{left}; j = \text{right} - 1;$

3	1	4	7	8	9	2	6	5
---	---	---	---	---	---	---	---	---

i j

Before 1st swap

3	1	4	7	8	9	2	6	5
---	---	---	---	---	---	---	---	---

i j

After 1st swap

3	1	4	2	8	9	7	6	5
---	---	---	---	---	---	---	---	---

i j

Before 2nd swap

3	1	4	2	8	9	7	6	5
---	---	---	---	---	---	---	---	---

j i

$\text{swap}(A[i], A[\text{right}])$

3	1	4	2	5	9	7	6	8
---	---	---	---	---	---	---	---	---

j i

**After 1st Partition**

3	1	4	2	5	9	7	6	8
---	---	---	---	---	---	---	---	---

**2-1st Partition :**

$\text{median}(A[0], A[1], A[3]) = \text{median}(3, 1, 2) = 2 = A[3]$

$\text{pivot} = A[3]; \text{left} = 0; \text{right} = 3$

3	1	4	2
---	---	---	---

i = left; j = right -1;

Before 1st swap

After 1st swap

Before 2nd swap

swap(A[i], A[right])

**After 2-1st Partition**

**2-2nd Partition :**

median(A[5], A[6],A[8]) = median(9,7,8) = 8 = A[8]

pivot = A[8]; left = 5; right = 8

i = left; j = right -1;

Before 1st swap

After 1st swap

Before 2nd swap

swap(A[i], A[right])

3	1	4	2
---	---	---	---

i                  j

3	1	4	2
---	---	---	---

i                  j

1	3	4	2
---	---	---	---

i                  j

1	3	4	2
---	---	---	---

j                  i

1	2	4	3
---	---	---	---

j                  i

1	2	4	3
---	---	---	---

9	7	6	8
---	---	---	---

9	7	6	8
---	---	---	---

i                  j

9	7	6	8
---	---	---	---

i                  j

6	7	9	8
---	---	---	---

i                  j

6	7	9	8
---	---	---	---

j                  i

6	7	8	9
---	---	---	---

		j	i	
6	7	8	9	

**After 2-2nd Partition**

**3-1st Partition :**  
 $\text{median}(A[2], A[2], A[3]) = \text{median}(4, 4, 3) = 4 = A[2]$   
 $\text{pivot} = A[2]; \text{left} = 2; \text{right} = 3; \text{swap}(A[2], A[3])$   
 $i = \text{left}; j = \text{right} - 1;$

4	3
---	---

Before 1st swap

3	4
---	---

$\text{swap}(A[i], A[\text{right}]) // \text{swap}(A[3], A[3])$

ij

3	4
---	---

j i

3	4
---	---

j i

3	4
---	---

**After 3-1st Partition**

**3-2nd Partition :**  
 $\text{median}(A[5], A[5], A[6]) = \text{median}(6, 6, 7) = 6 = A[5]$   
 $\text{pivot} = A[5]; \text{left} = 5; \text{right} = 6; \text{swap}(A[5], A[6])$   
 $i = \text{left}; j = \text{right} - 1;$

6	7
---	---

Before 1st swap

7	6
---	---

ij

7	6
---	---

j i

6	7
---	---

j i

**After 3-2nd Partition**

6	7
---	---

**Final Sorted Output**

1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---