

Corrections of *GEE Analysis of Clustered Binary Data with Diverging Number of Covariates*

I thank Drs. Xianbin Chen and Juliang Yin for pointing out some typos and small errors in the supplement of the paper. Please find the corrections below.

1. In evaluating J_{n1} , there is a missing \mathbf{X}_{ij} . We should have

$$\begin{aligned} & \sup_{\|\boldsymbol{\beta}_n - \boldsymbol{\beta}_{n0}\| \leq \Delta \sqrt{\frac{p_n}{n}}} \sup_{\|\mathbf{b}_n\|=1} J_{n1}(\boldsymbol{\beta}_n) \\ & \leq CO_p(\sqrt{p_n/n}) O_p(\sqrt{p_n/n}) \lambda_{max} \left(\sum_{i=1}^n \mathbf{X}_i^T \mathbf{X}_i \right) \sup_{i,j} \|\mathbf{X}_{ij}\| = O_p(p_n^{3/2}) = O_p(\sqrt{np_n}), \end{aligned}$$

by assumptions (A1) and (A3). So the original upper bound $O_p(\sqrt{np_n})$ in the proof remains the same, as it is assumed in Theorem 5.1 that $n^{-1}p_n^2 = o(1)$.

2. In the evaluation of $J_{n5}(\boldsymbol{\beta}_{n0})$, instead of taking the expectation, the order can be evaluated directly by applying the Cauchy-Schwartz inequality.

$$\begin{aligned} \|J_{n5}(\boldsymbol{\beta}_{n0})\| & \leq \sqrt{\sup_{\|\mathbf{b}_n\|=1} \sum_{i=1}^n \|b_n^T \mathbf{X}_i^T \mathbf{A}_i^{1/2}(\boldsymbol{\beta}_{n0})(\hat{\mathbf{R}}^{-1} - \bar{\mathbf{R}}^{-1})\|^2} \\ & \quad \times \sqrt{\sup_{\|\mathbf{b}_n\|=1} \sum_{i=1}^n \|\mathbf{A}_i^{-3/2}(\boldsymbol{\beta}_{n0}) \mathbf{C}_{i2}(\boldsymbol{\beta}_{n0}) \mathbf{F}_i(\boldsymbol{\beta}_{n0}) \mathbf{X}_i b_n\|^2}. \end{aligned}$$

This eliminates the problem of the dependence between $\hat{\mathbf{R}}^{-1}$ and \mathbf{Y}_i . It is easy to see that the first term is of order $O_p(\sqrt{p_n})$ and the second term is of order $O_p(\sqrt{n})$. Hence, we have $\|J_{n5}(\boldsymbol{\beta}_{n0})\| = O_p(\sqrt{np_n})$. The same order as the original claim.

3. Regarding Remark 2 of the paper, We note that the matrix $\mathbf{D}_n(\boldsymbol{\beta}_n) - \bar{\mathbf{D}}_n(\boldsymbol{\beta}_n)$ is not necessarily symmetric in general. However, this will not influence the proof. What one really need in the proof is just Lemma 3.3, which does not require $\mathbf{D}_n(\boldsymbol{\beta}_n) - \bar{\mathbf{D}}_n(\boldsymbol{\beta}_n)$ to be symmetric (it just does not have the eigenvalue interpretation). Remark 2 can in fact be eliminated from the paper. When evaluating terms such as $(\boldsymbol{\beta}_n - \boldsymbol{\beta}_{n0})^T [\mathbf{D}_n(\boldsymbol{\beta}_n^*) - \bar{\mathbf{D}}_n(\boldsymbol{\beta}_n^*)](\boldsymbol{\beta}_n - \boldsymbol{\beta}_{n0})$, we will just get rid of the eigenvalue notation and apply Lemma 3.3 directly.