STATEMENT OF PURPOSE

Yanshu Wang

Under the supervision of Professor Vasily Dolgushev, I conducted the research that introduced a more streamlined version of the groupoid GTSh of GT-shadows and contributed to the SageMath package for working with GT-shadows. The groupoid GTSh is a 'computable' approximation to the gentle version of the Grothendieck-Teichmüller group \widetilde{GT} with the set of objects of GTSh is the poset $\operatorname{NFI}^B_3(F_2)$ of B_3 -invariant finite index normal subgroups of the free group F_2 on two generators. This object is worth studying because it is very 'likely' that in most cases, the morphism of GTSh lifts to the absolute Galois group $G_{\mathbb{Q}}$. And it is already known that for a specific subposet Dih_2 of dihedral posets, if K is an element of Dih_2 , every morphism of the connected component of K in GTSh lifts to an element of $G_{\mathbb{Q}}$.

Mentored by Professor Maxence Mayrand, I participated in a research internship that constructed new GKP code from the Abelian varieties on the cyclotomic field $K = \mathbb{Q}(\zeta_n)$. The construction $(K \otimes_{\mathbb{Q}} \mathbb{R})/\mathcal{O}_K$ is an abelian variety of CM-type. We defined a skew-symmetric form E and extended it to a hermitian inner product E on E on E on the extended it to a hermitian inner product E on E on the extended it to a hermitian inner product E on E on the extended it to a hermitian inner product E on the extended it is a hermitian inner product E on the extended it is a hermitian inner product E on the extended it is a hermitian inner product E on the extended it is a hermitian inner product E on the extended it is a hermitian inner product E on the extended it is a hermitian inner product E on the exten

Under the supervision of Professor Lisa Berger, Ajmain Yamin and Connor Stewart, I participated in an online collaborative research to obtain equations for K_9 dessin, that is the bipartification dessin of the complete regular map from K_9 graph. We proved that the Riemann surface of the K_9 dessin is a degree 9 cover of the Bolza surface $y^2 = x(x^4 - 1)$ with covering group $(\mathbb{Z}/3\mathbb{Z})^2$. We used the fact that any unramified abelian cover of a Riemann surface S is obtained from pulling back S along an unramified abelian cover of

the Jacobian $\mathrm{Jac}(S)$ of S. So, we computed the equation for the Abel-Jacobi map of the Bolza surface S_B and constructed a degree 9 cover of the Jacobian $\mathrm{Jac}(S_B)$ and obtained the equation.

These research experiences let me explore a wide range of mathematics and significantly improve my self-learning, writing, programming and speaking skills. It is these research experiences that boost my determination to seek admission to a graduate program and do mathematical research.

I think University of Pisa is a great place to study Number theory. My undergraduate advisor recommended University of Pisa to me.