

MAE5009: Continuum Mechanics B

Assignment 01: Stress

Due September 23, 2020

1. Given $\sigma_x = -14$ MPa, $\sigma_y = 6$ MPa, and $\tau_{xy} = -17$ MPa, determine both by formulas and by the Mohr's circle,
 - (a) the principal stresses and their directions,
 - (b) the direction having the maximum shear stress and the corresponding shear and normal stress magnitudes,
 - (c) the stress components on the x' and y' planes when $\alpha = 45^\circ$
2. Given a three-dimensional stress state with
$$\sigma_x = 10 \text{ MPa}, \sigma_y = 20 \text{ MPa}, \sigma_z = -10 \text{ MPa}$$
$$\tau_{xy} = 5 \text{ MPa}, \tau_{xz} = -10 \text{ MPa}, \tau_{yz} = -15 \text{ MPa}$$
 - (a) find the magnitude and direction of the stress vector p on the x' plane where the x' direction is defined by
$$\cos(x', x) = 1/2, \cos(x', y) = 1/\sqrt{2} \text{ and } \cos(x', z) \text{ is positive}$$
 - (b) find σ and τ on this plane
 - (c) determine the angle between p and σ
 - (d) solve for $\tau_{x'y'}$ and $\tau_{x'z'}$, if $\cos(x, y') = 1/2$ and $\cos(z, y')$ is negative.
 - (e) evaluate all of the stress components acting on the x' , y' and z' planes
 - (f) determine the principal stresses and the direction cosines of the principal axes

3. Given the following stress functions,

$$\begin{aligned}\sigma_x &= 3x^2 + 3y^2 - z & \tau_{xy} &= z - 6xy - \frac{3}{4} \\ \sigma_y &= 3y^2 & \tau_{xz} &= x + y - \frac{3}{2} \\ \sigma_z &= 3x + y - z + \frac{5}{4} & \tau_{yz} &= 0\end{aligned}$$

(a) show that the above stress state is in equilibrium

(b) for the stress state at point $x = 1/2$, $y = 1$, and $z = 3/4$, determine the principal stresses.