

Edge detection



[Winter in Kraków photographed by Marcin Ryczek](#)

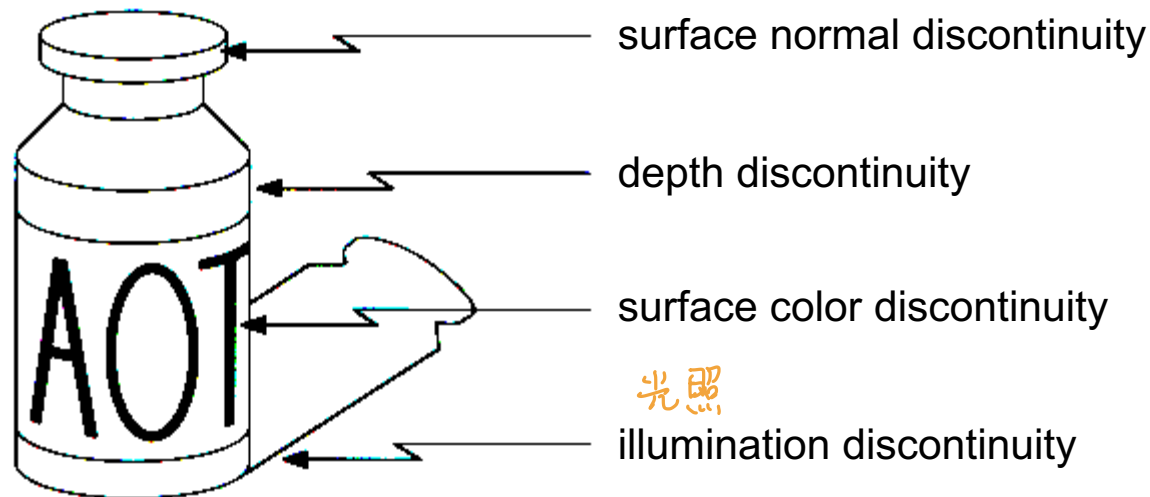
Edge detection

- **Goal:** Identify sudden changes (discontinuities) in an image.
 - Intuitively, most semantic and shape information from the image can be encoded in the edges
 - More compact than pixels
- **Ideal:** artist's line drawing (but artist is also using object-level knowledge)



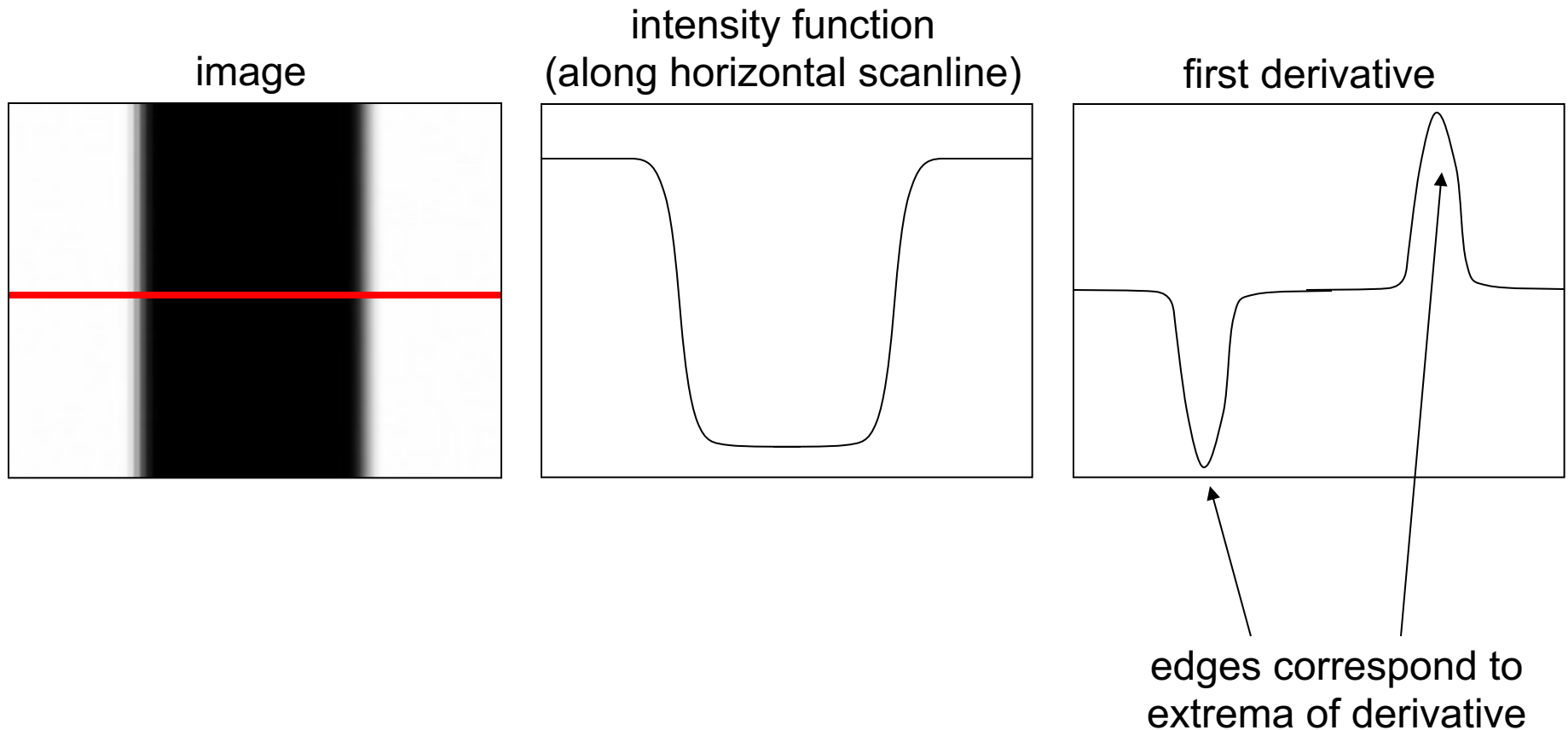
Origin of edges

Edges are caused by a variety of factors:



Edge detection

- An edge is a place of rapid change in the image intensity function



Derivatives with convolution

For 2D function $f(x,y)$, the partial derivative is:

$$\frac{\partial f(x, y)}{\partial x} = \lim_{\varepsilon \rightarrow 0} \frac{f(x + \varepsilon, y) - f(x, y)}{\varepsilon}$$

For discrete data, we can approximate using finite differences:

$$\frac{\partial f(x, y)}{\partial x} \approx \frac{f(x + 1, y) - f(x, y)}{1}$$

To implement the above as convolution, what would be the associated filter?

Partial derivatives of an image

水平方向差分

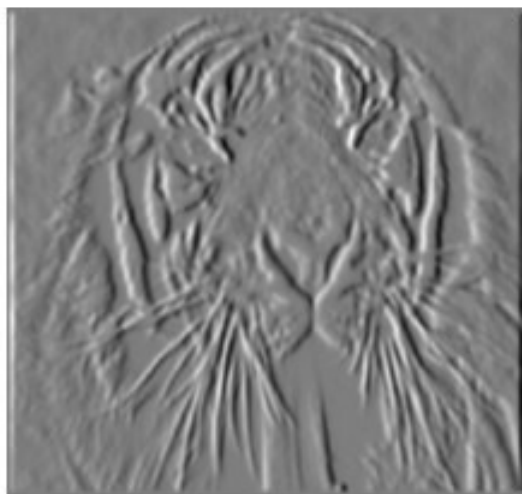


$$\frac{\partial f(x, y)}{\partial x}$$

$$\partial x$$



-1	1
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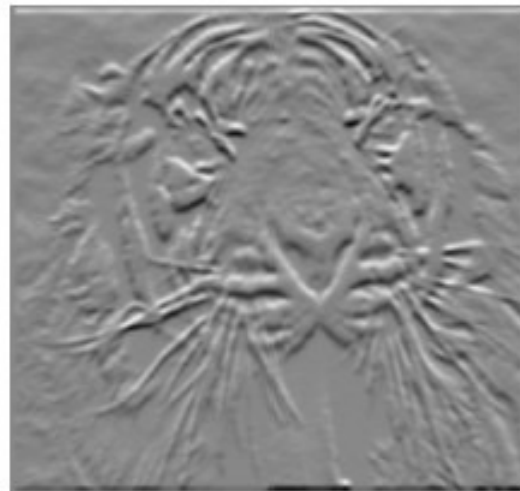


$$\frac{\partial f(x, y)}{\partial y}$$

$$\partial y$$

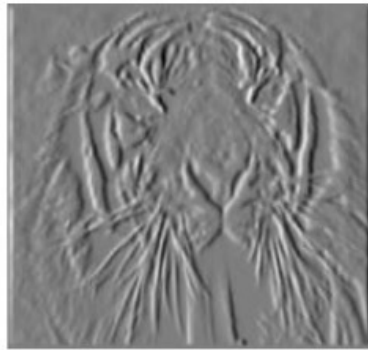


-1	or	1
1		-1

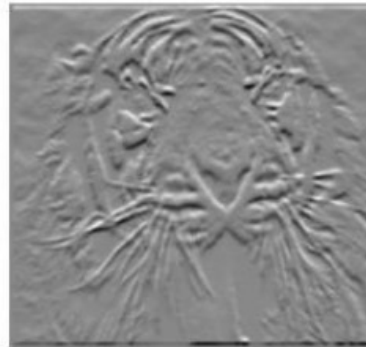


Which shows changes with respect to x?

Gradient Magnitude



$$\frac{\partial f(x,y)}{\partial x}$$



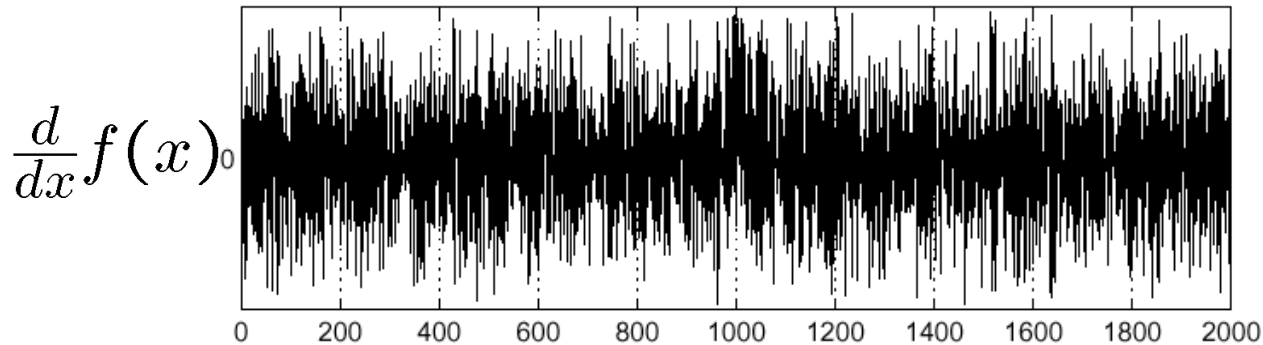
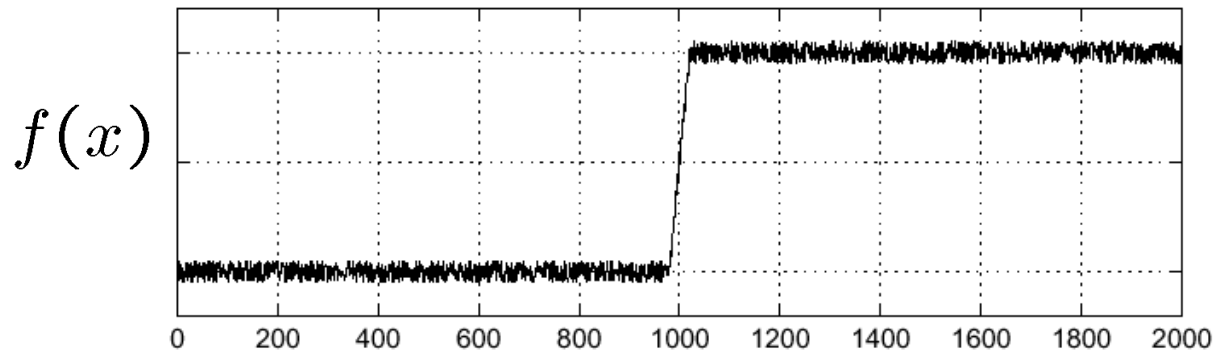
$$\frac{\partial f(x,y)}{\partial y}$$



$$||\nabla f|| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

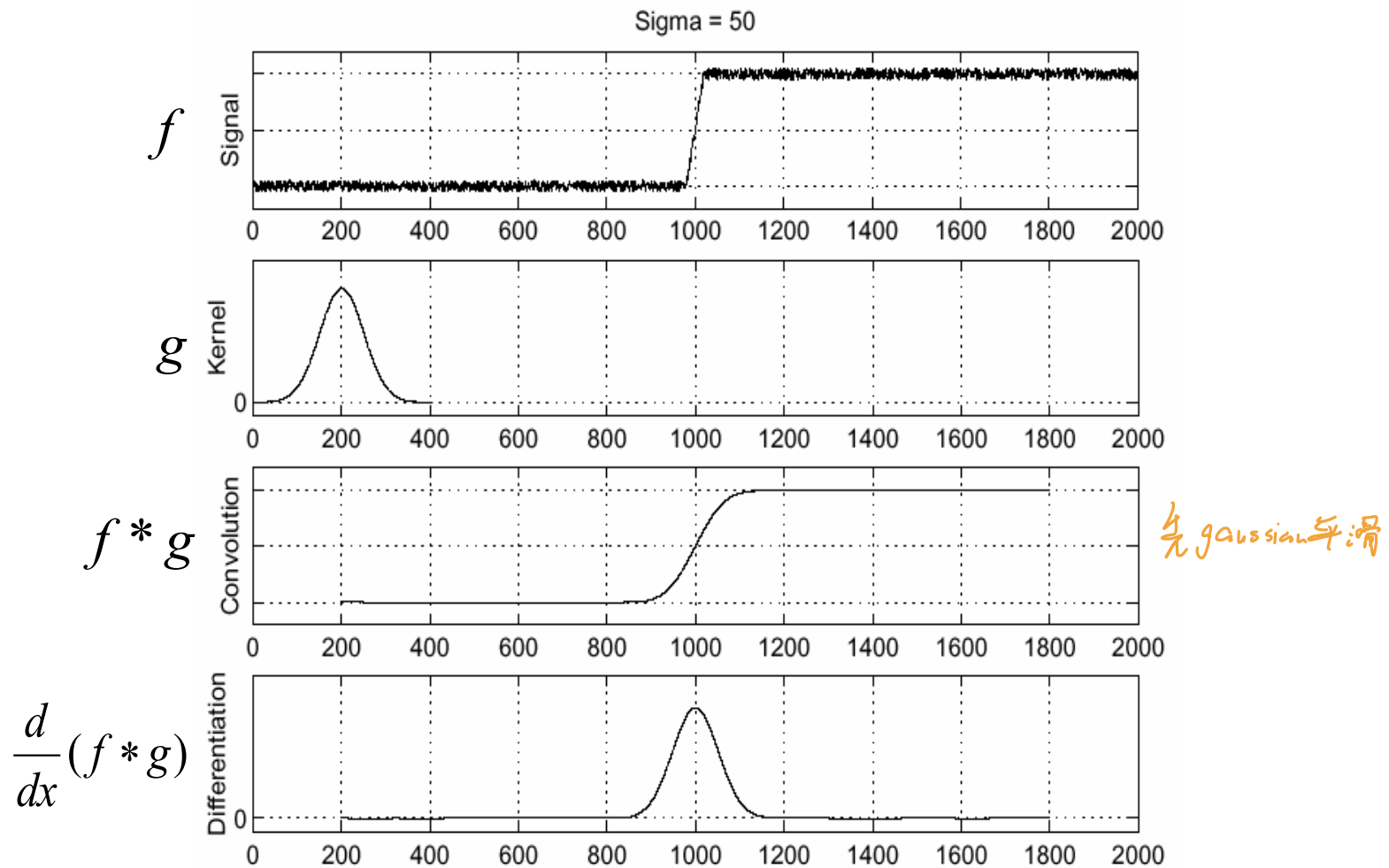
Effects of noise

Consider a single row or column of the image



Where is the edge?

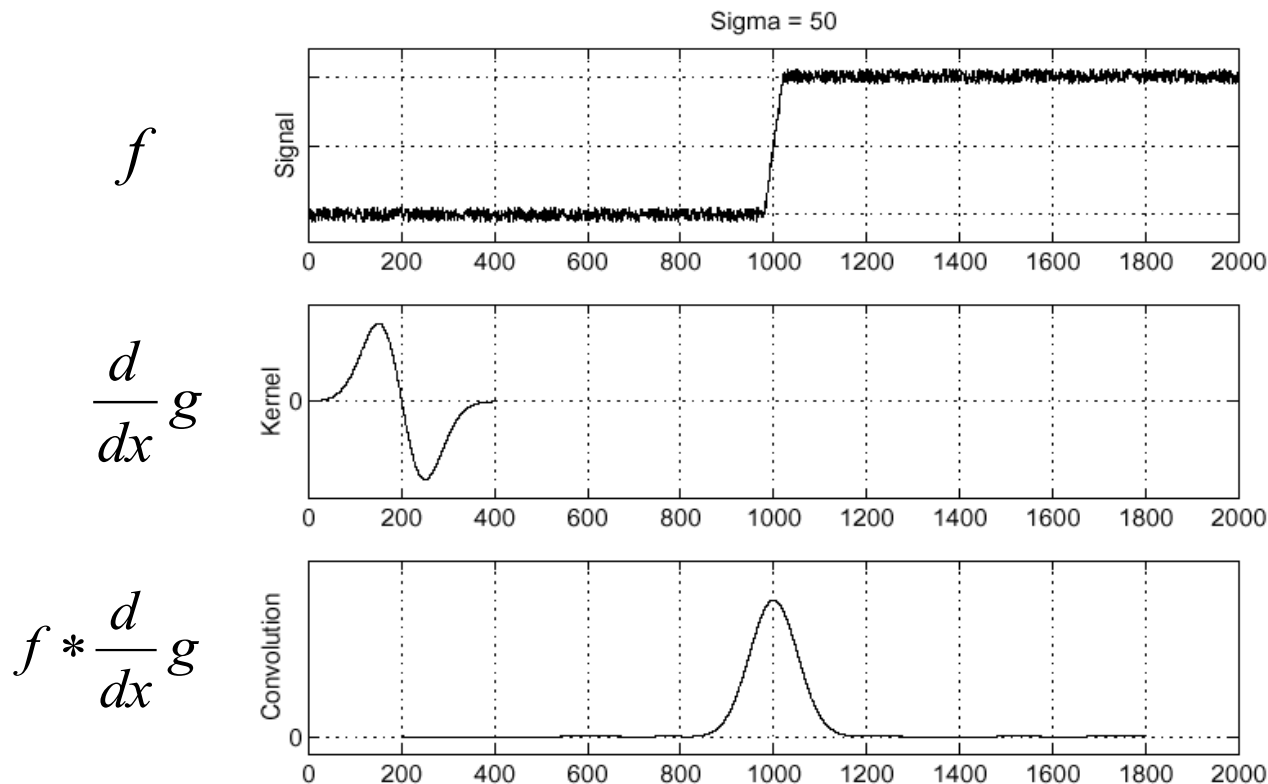
Solution: smooth first



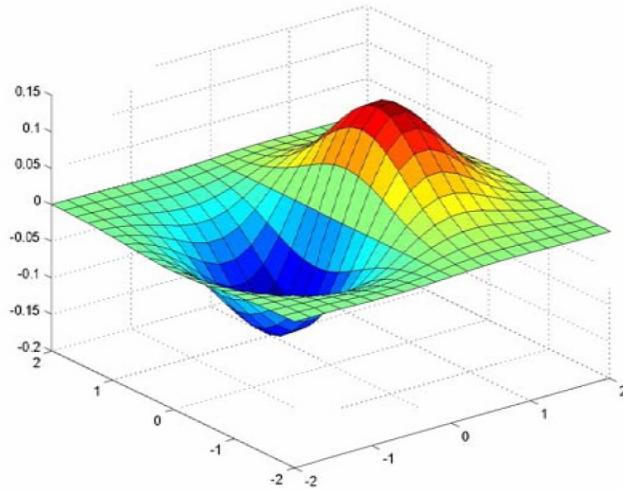
- To find edges, look for peaks in $\frac{d}{dx}(f * g)$

Derivative theorem of convolution

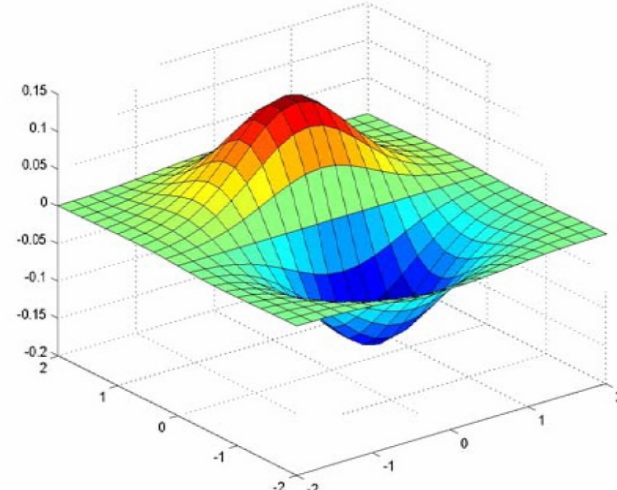
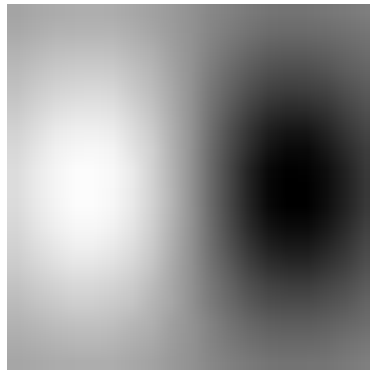
- Differentiation is convolution, and convolution is associative: $\frac{d}{dx}(f * g) = f * \frac{d}{dx}g$
- This saves us one operation:



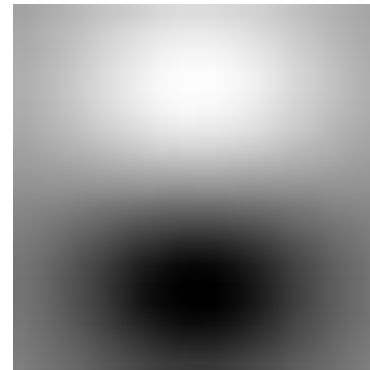
Derivative of Gaussian filters



x-direction

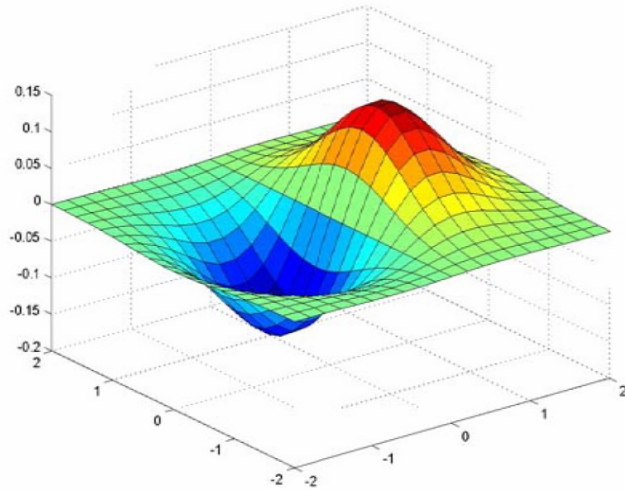


y-direction

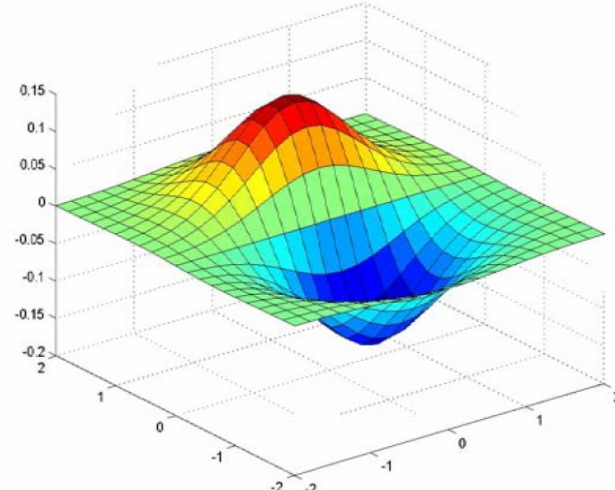
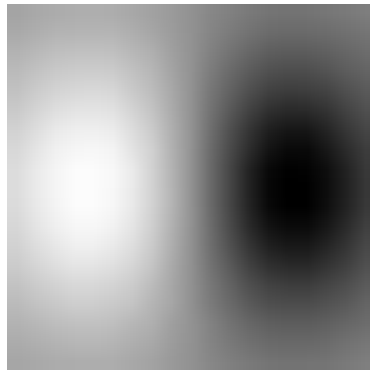


Which one finds horizontal/vertical edges?

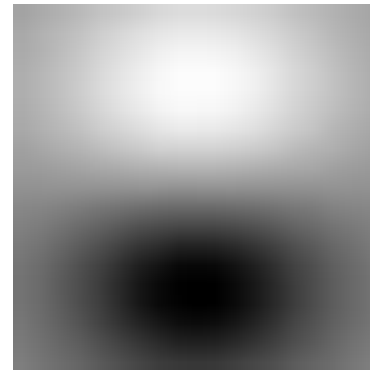
Derivative of Gaussian filters



x-direction

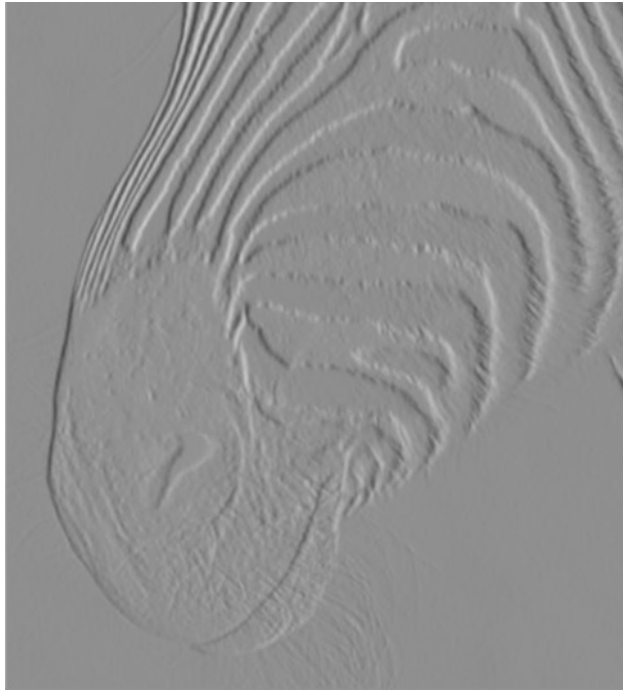


y-direction

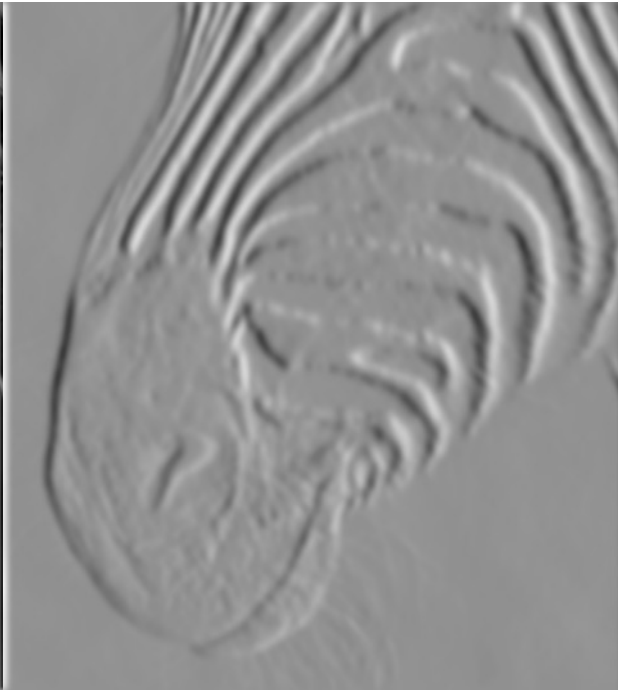


Are these filters separable?

Scale of Gaussian derivative filter



1 pixel



3 pixels



7 pixels

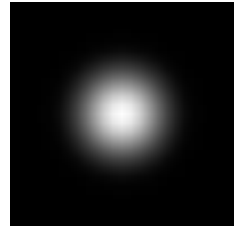
Smoothed derivative removes noise, but blurs edge. Also finds edges at different “scales”

Review: Smoothing vs. derivative filters

Smoothing filters

- Gaussian: remove “high-frequency” components; “low-pass” filter
- Can the values of a smoothing filter be negative? No
- What should the values sum to?
 - **One**: constant regions are not affected by the filter

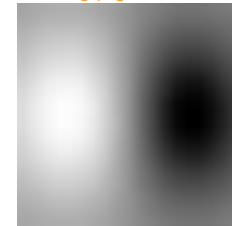
低通



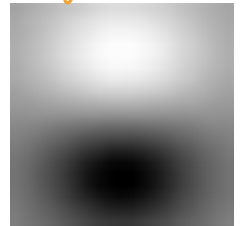
Derivative filters

- Derivatives of Gaussian
- Can the values of a derivative filter be negative?
- What should the values sum to?
 - **Zero**: no response in constant regions

x方向

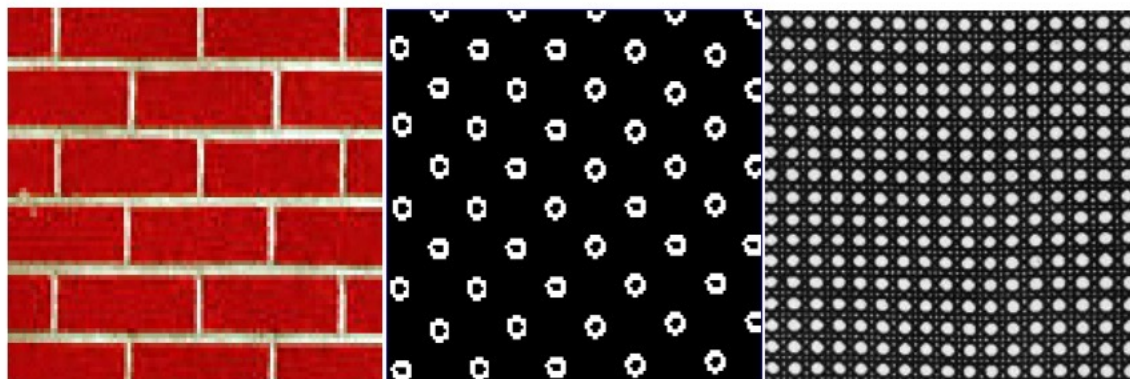


y方向

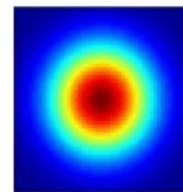
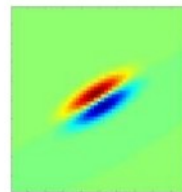
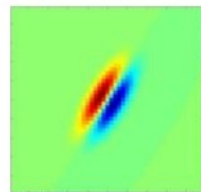
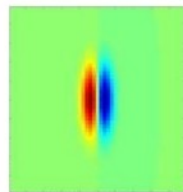
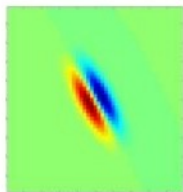
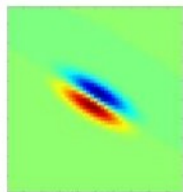
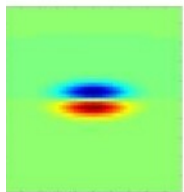


Texture

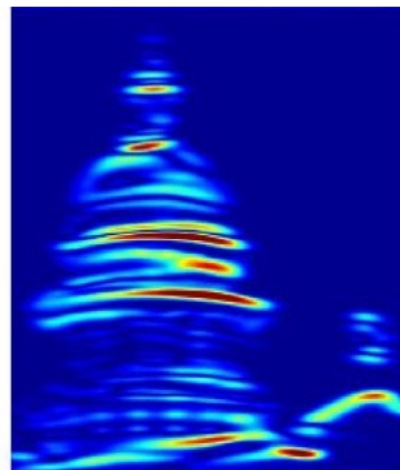
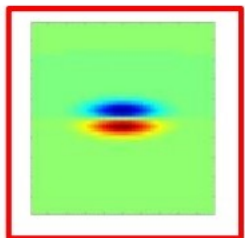


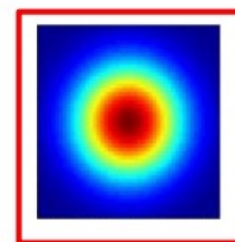


卷积核组

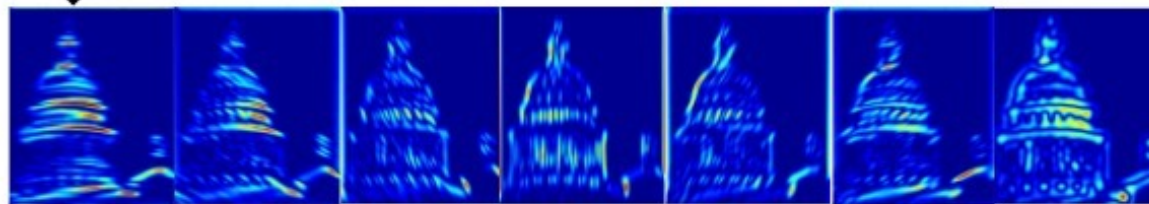
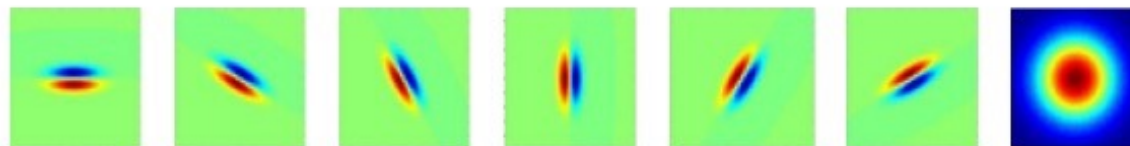


边缘检测





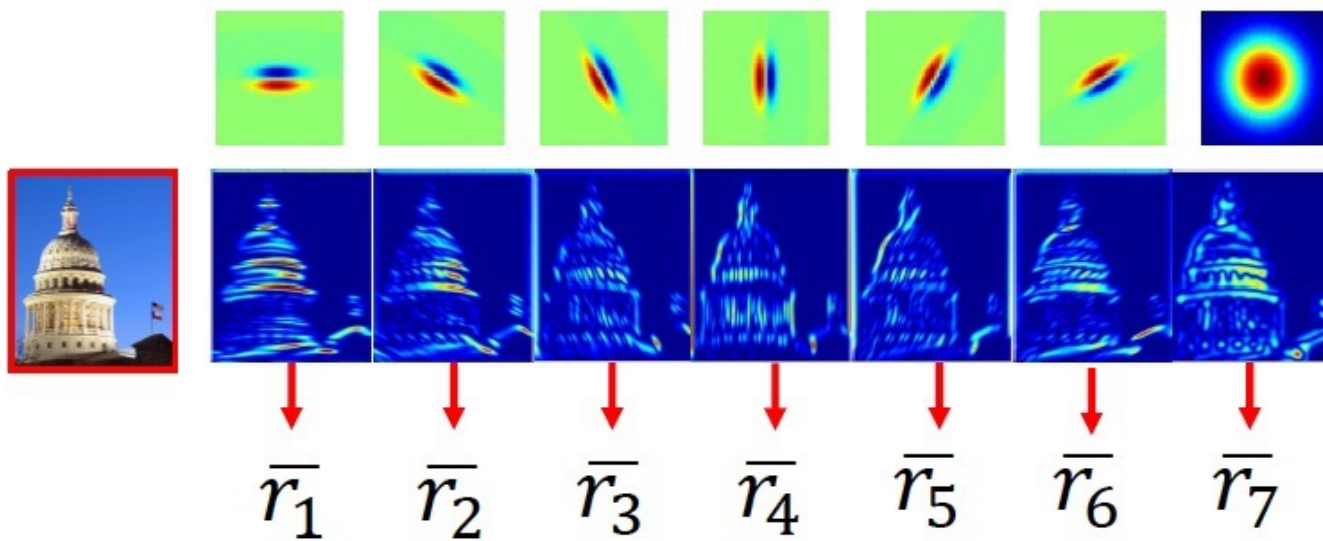
200

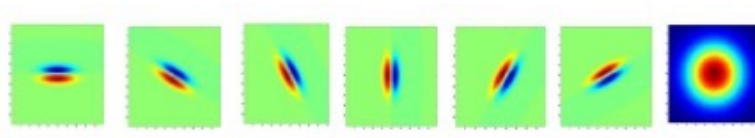
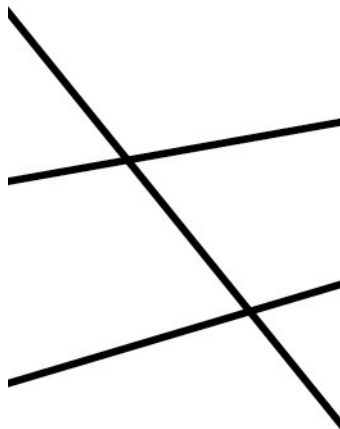
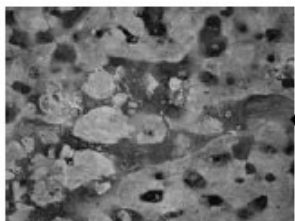


响应图组

$$r_1 = [r_{11}, r_{12}, \dots, r_{1 \times n}]$$

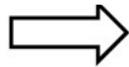
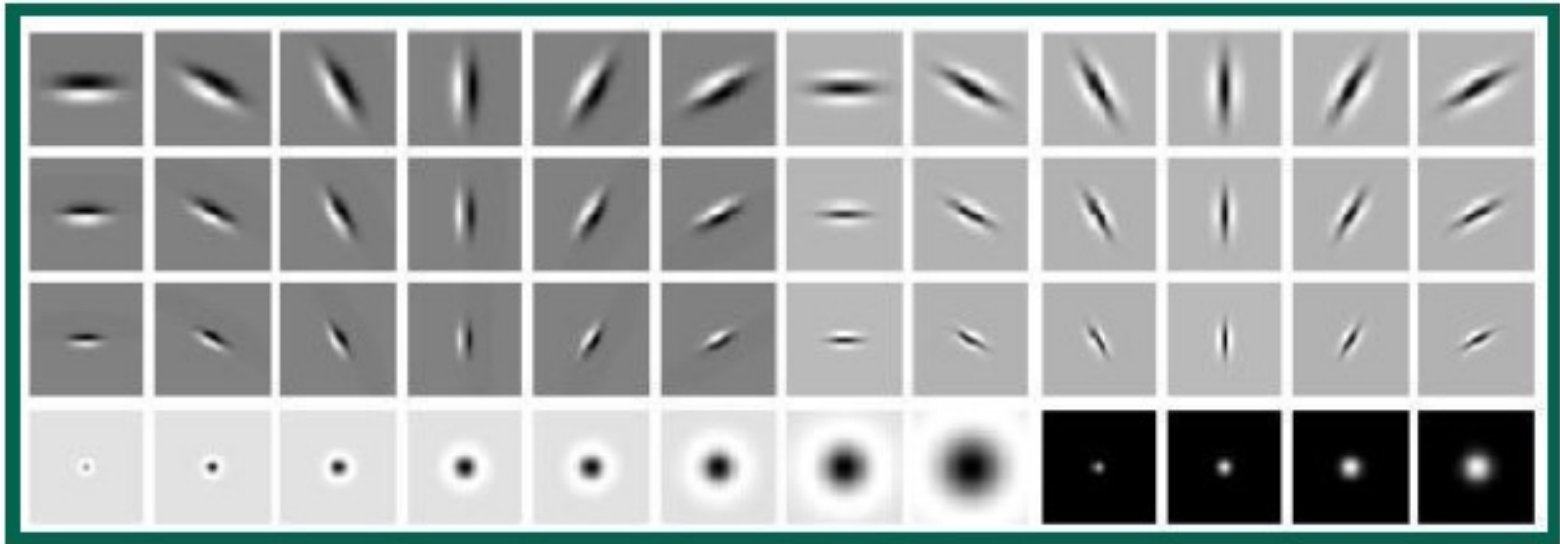
200x100x



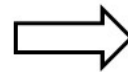


白色
↓
响应值最高

How to design?



...



$[\bar{r}_1 \quad \dots \quad \bar{r}_{48}]$