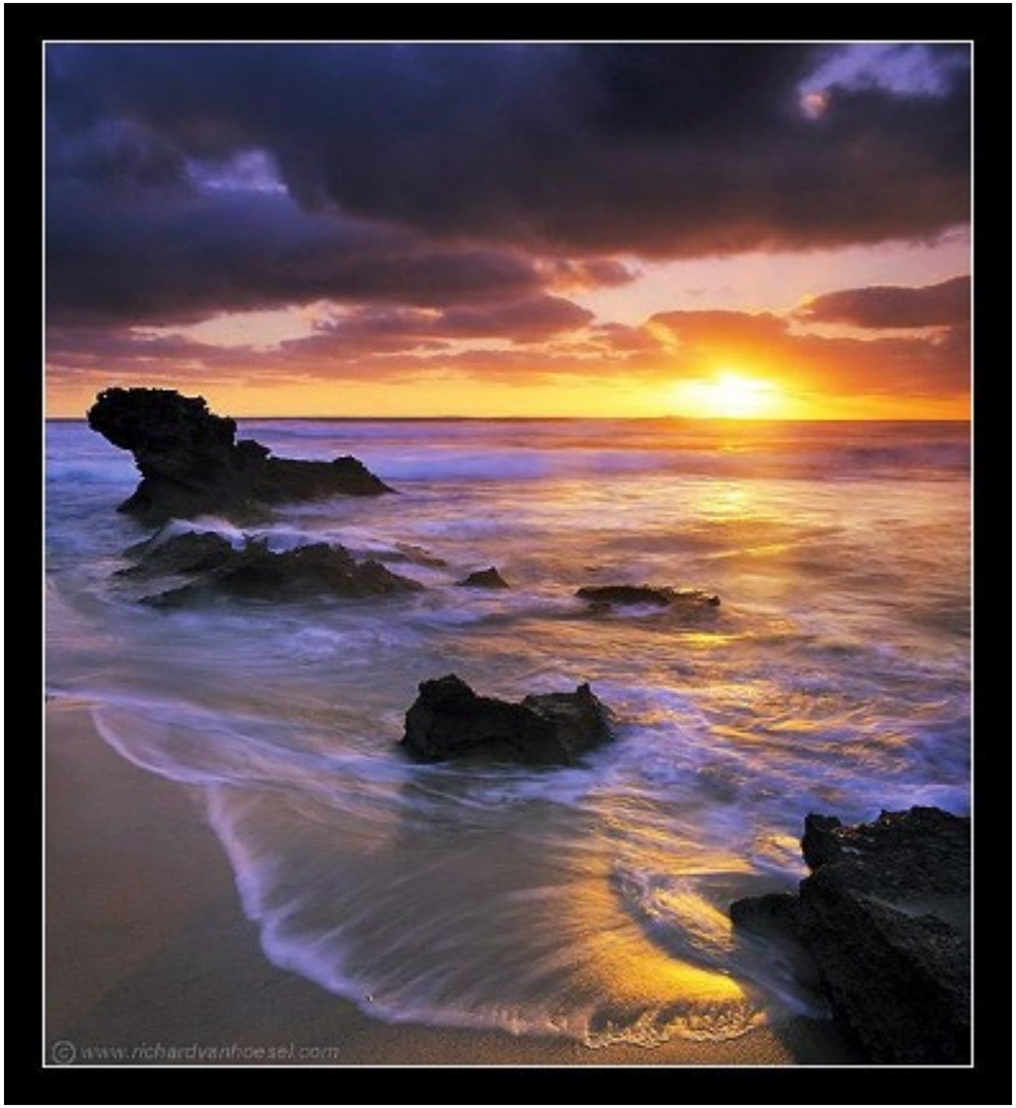
Light and shading



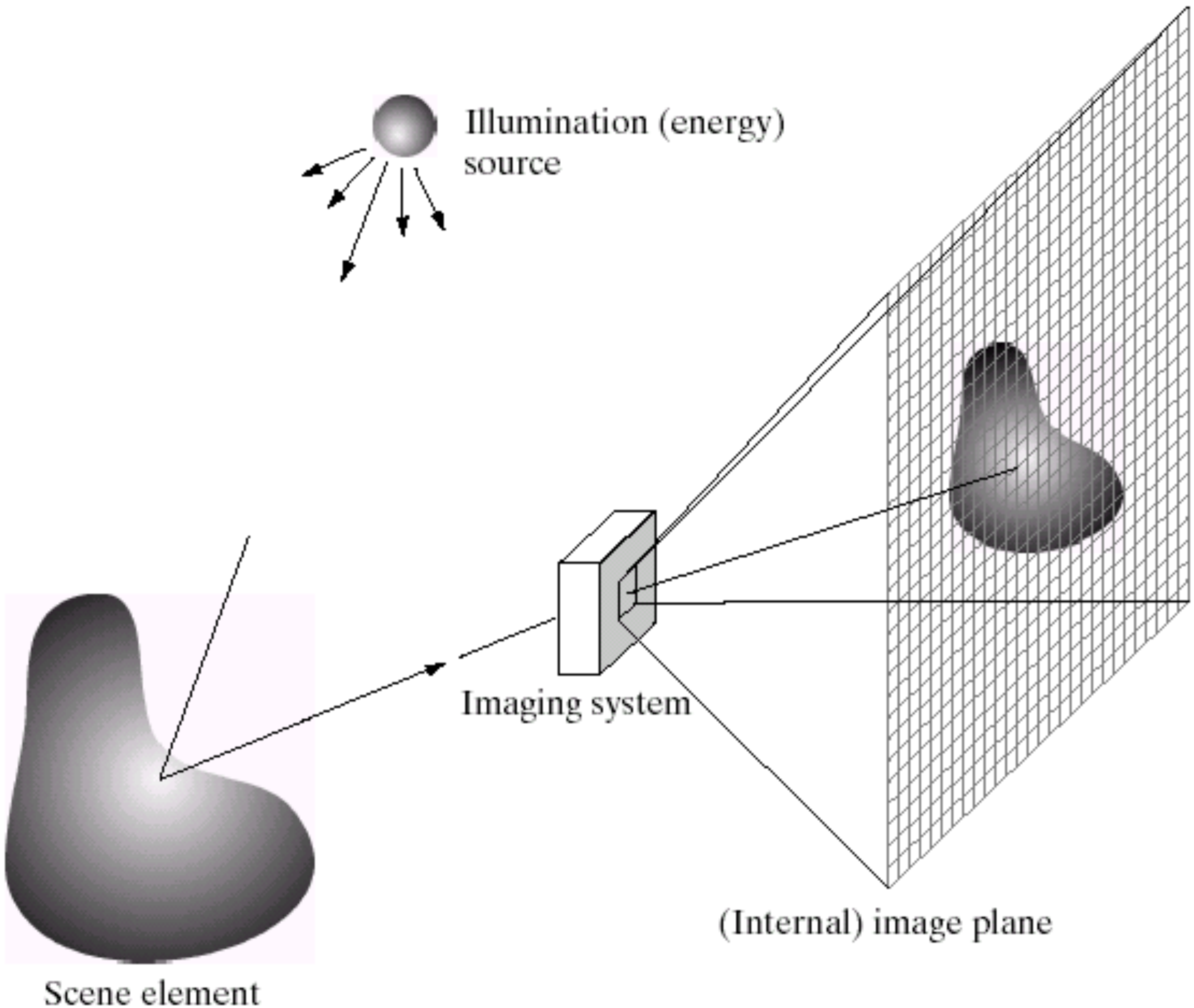
What determines a pixel's intensity?

What can we infer about the scene from pixel intensities?

Image Source: A. Efros

Some slides credited to James Hays@Brown University, Kristen Grauman@UT Austin and Svatalana Lazebnik@UIUC

How light is recorded



Digital camera 光学信号→电信号

A digital camera replaces film with a sensor array

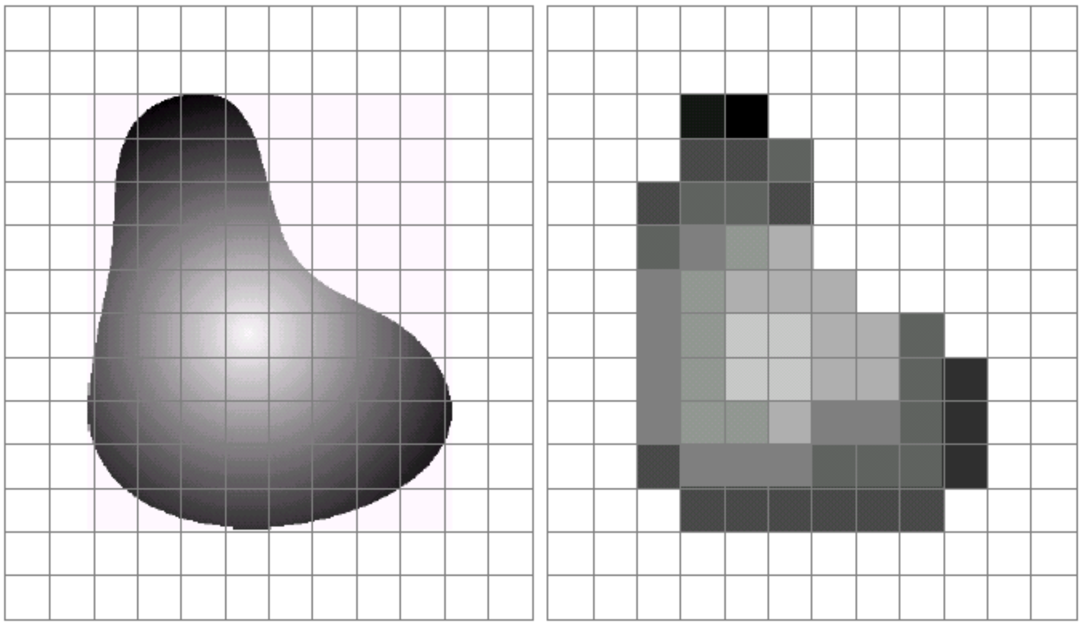
Each cell in the array is light-sensitive diode that converts photons to electrons

Two common types: Charge Coupled Device (CCD) and CMOS

http://electronics.howstuffworks.com/digital-camera.htm

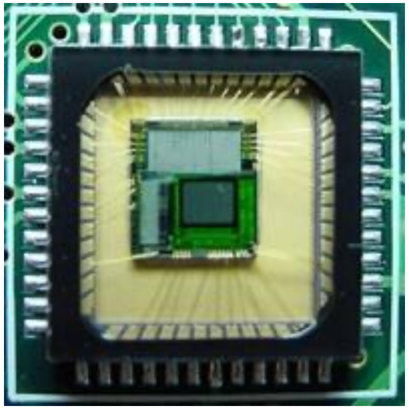
Sensor Array

每个像素 → 电信号



a b

FIGURE 2.17 (a) Continuos image projected onto a sensor array. (b) Result of image sampling and quantization.



CMOS sensor

0~255

多少光学传感器 → 分辨率

Each sensor cell record a small range of orientations amount of light coming in

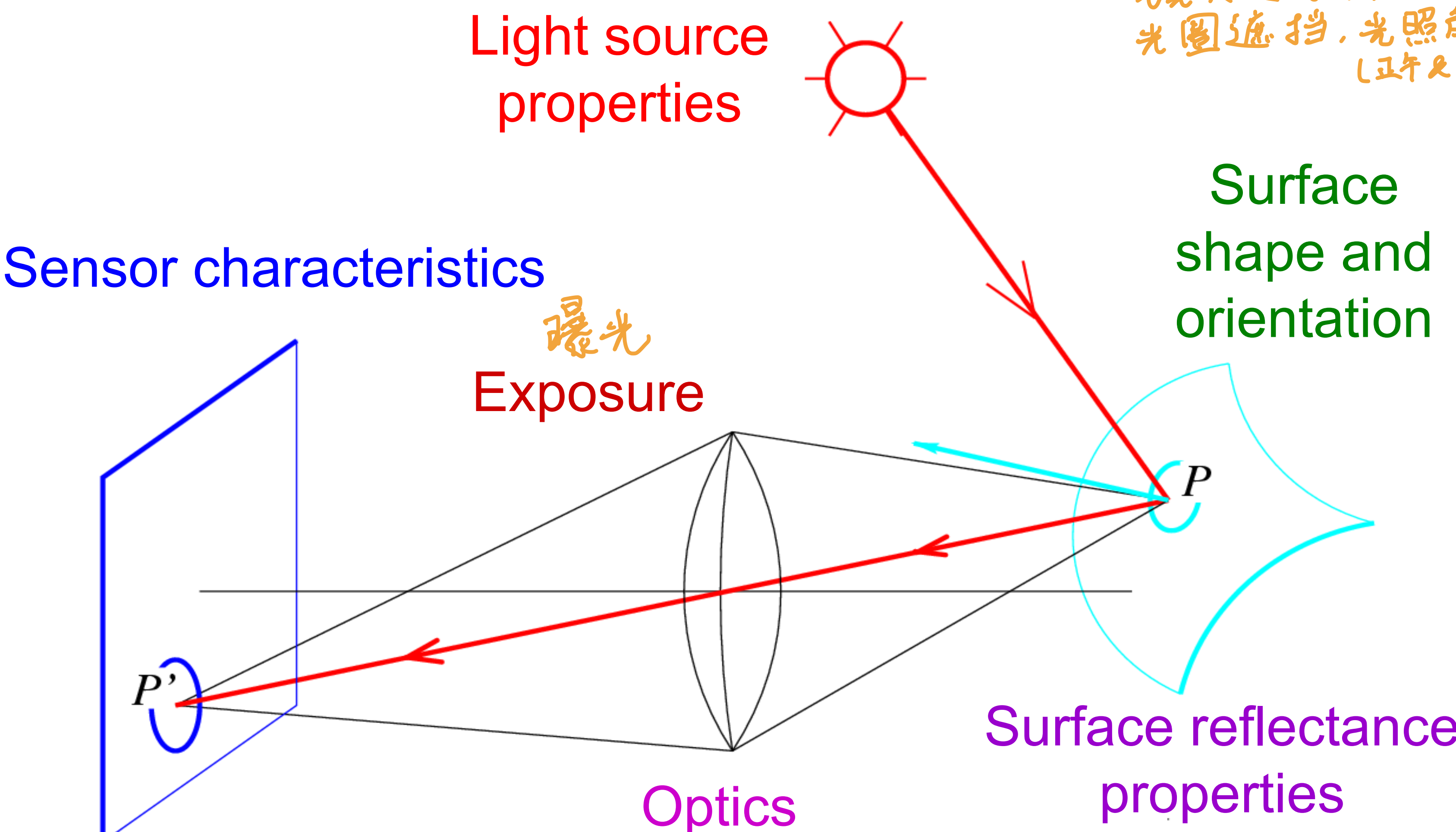
CCD: 高感光度, 低噪

CMOS: 快 (video)

Image formation

What determines the brightness of an image pixel?

光源强度，surface折射率，
镜头透光率，
光圈遮挡，光照角度
（正午及日出）



Slide by L. Fei-Fei

Intensity and Surface Orientation

Intensity depends on illumination angle because less light comes in at oblique angles.

ρ = albedo 反照率

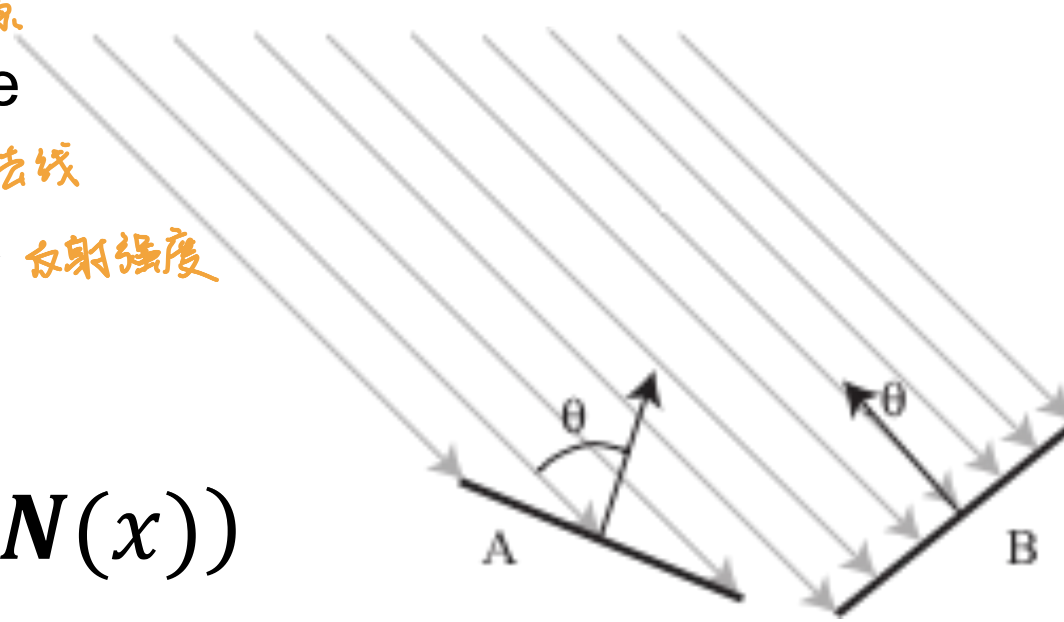
光源

$\boldsymbol{S}$ = directional source

$\boldsymbol{N}$ = surface normal 法线

I = reflected intensity 反射强度

$$I(x) = \rho(x)(\boldsymbol{S} \cdot \boldsymbol{N}(x))$$



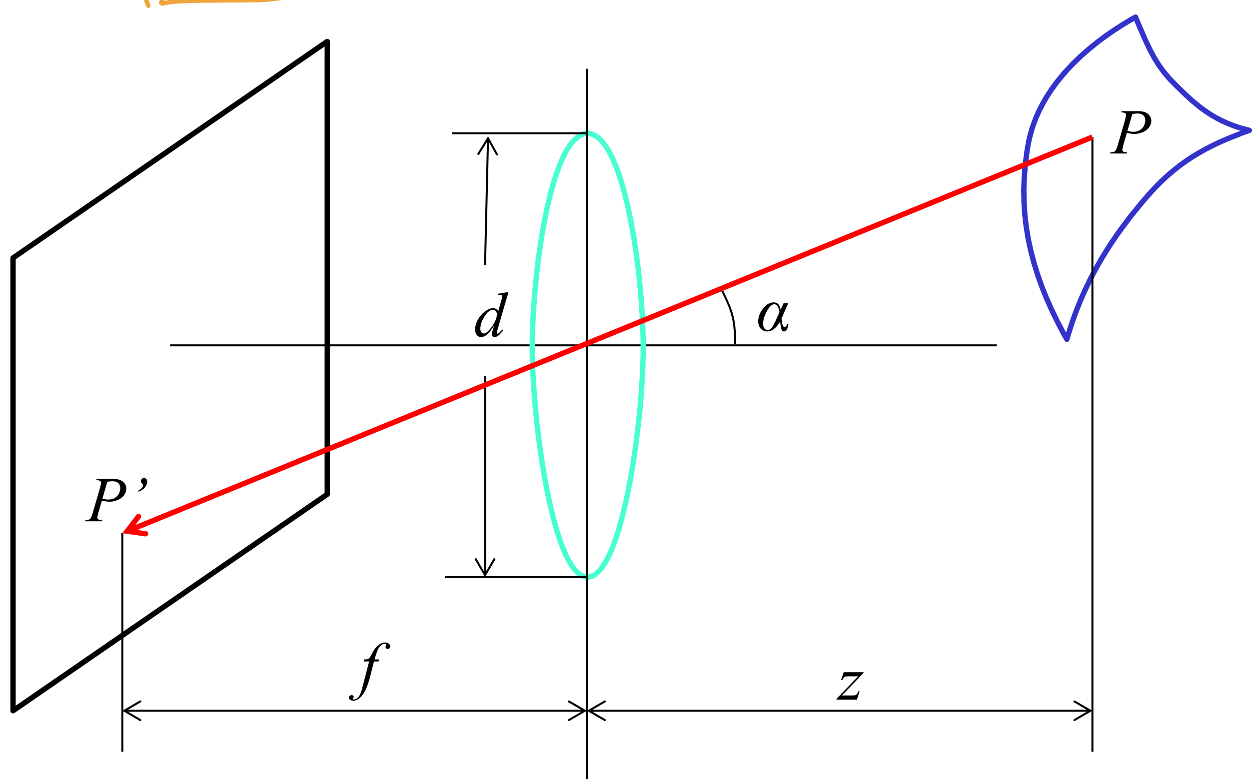
Fundamental radiometric relation

L: *Radiance* emitted from *P* toward *P'* (辐射度) 垂直于方向 recieve最多

- Energy carried by a ray (Watts per sq. meter per steradian)

E: *Irradiance* falling on *P'* from the lens (辐照度) 自己能感受

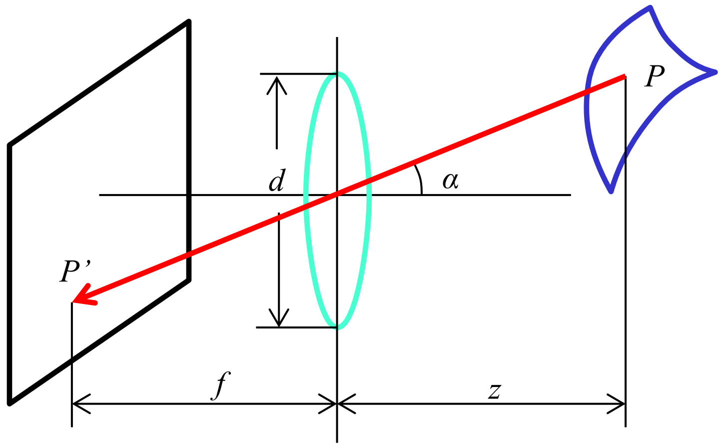
- Energy arriving at a surface (Watts per sq. meter)



What is the relationship between *E* and *L*?

Szeliski 2.2.3

Fundamental radiometric relation



$$E = \left[\frac{\pi}{4} \left(\frac{d}{f} \right)^2 \cos^4 \alpha \right] L$$

- Image irradiance is linearly related to scene radiance
- Irradiance is proportional to the area of the lens and inversely proportional to the squared distance between the lens and the image plane
- The irradiance falls off as the angle between the viewing ray and the optical axis increases (natural vignetting)

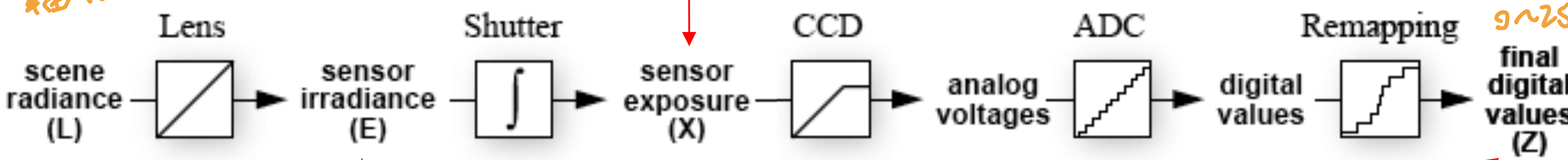
Szeliski 2.2.3

From light rays to pixel values

$$X = E \cdot \Delta t$$

辐射度

0~255



辐照度

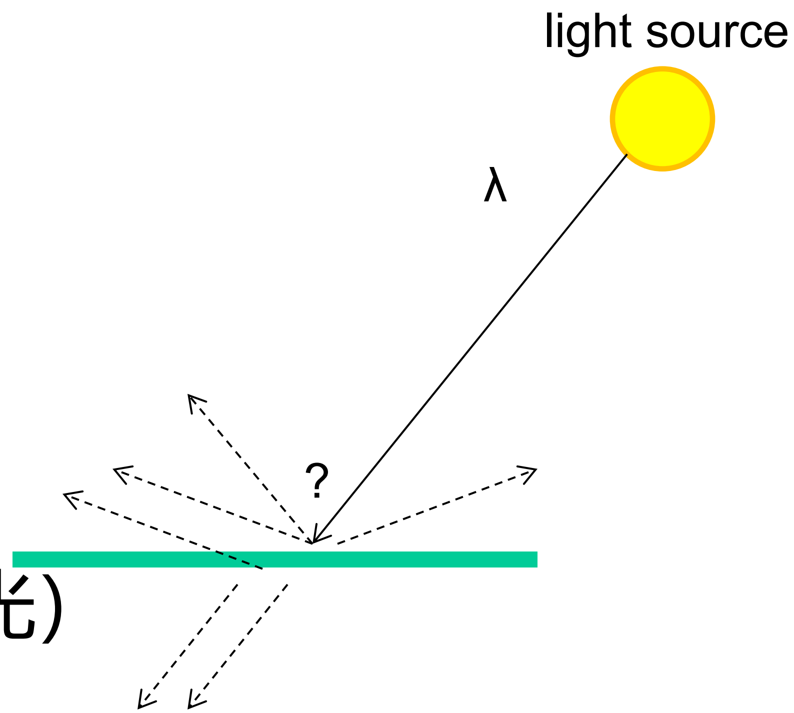
$$E = \left[\frac{\pi}{4} \left(\frac{d}{f} \right)^2 \cos^4 \alpha \right] L$$

$$Z = f(E \cdot \Delta t)$$

- Camera response function: the mapping f from irradiance to pixel values
  - Useful if we want to estimate material properties
  - Enables us to create high dynamic range images
  - For more info: P. E. Debevec and J. Malik, [Recovering High Dynamic Range Radiance Maps from Photographs](), *SIGGRAPH 97*

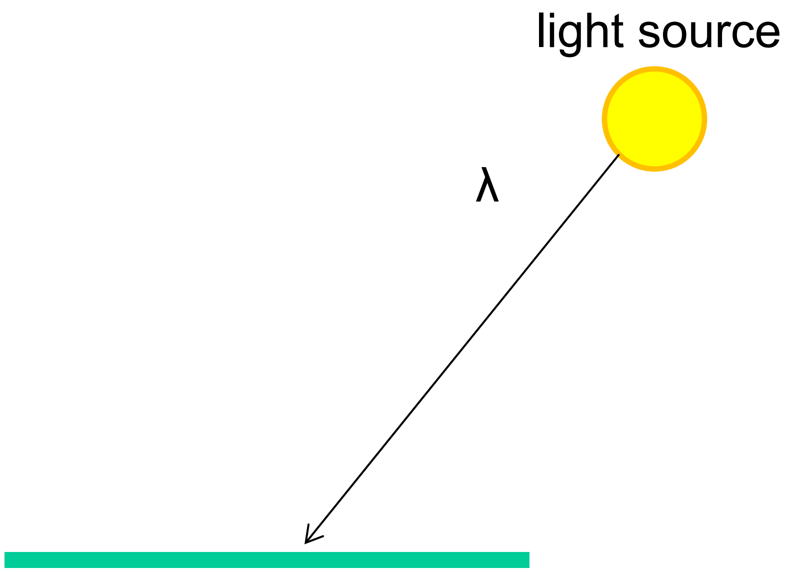
A photon's life choices 光线特性

- Absorption 吸收
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence （荧光）
- Subsurface scattering
- Phosphorescence （磷光）
- Interreflection



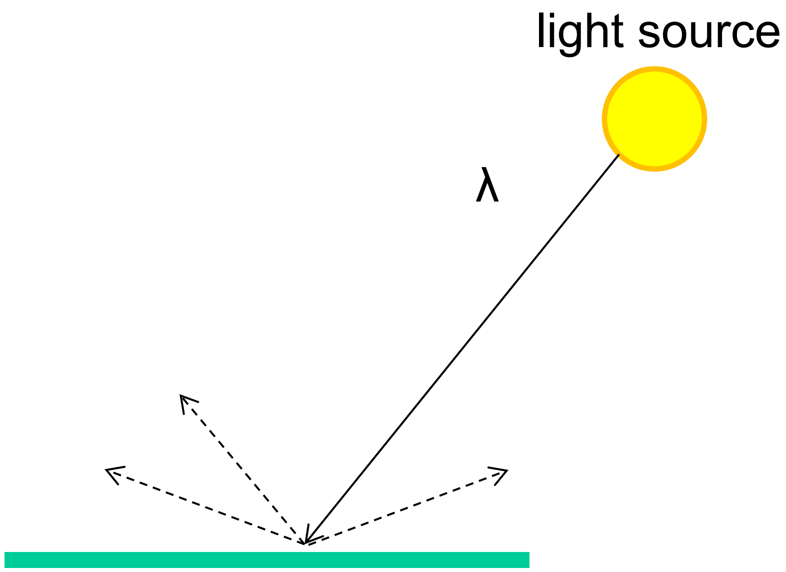
A photon's life choices

- **Absorption**
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



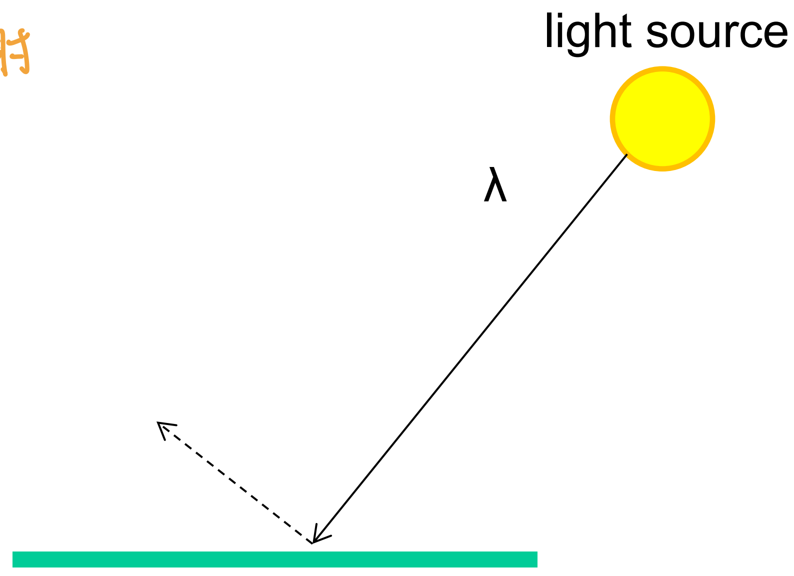
A photon's life choices

- Absorption
- **Diffuse Reflection** 散射
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



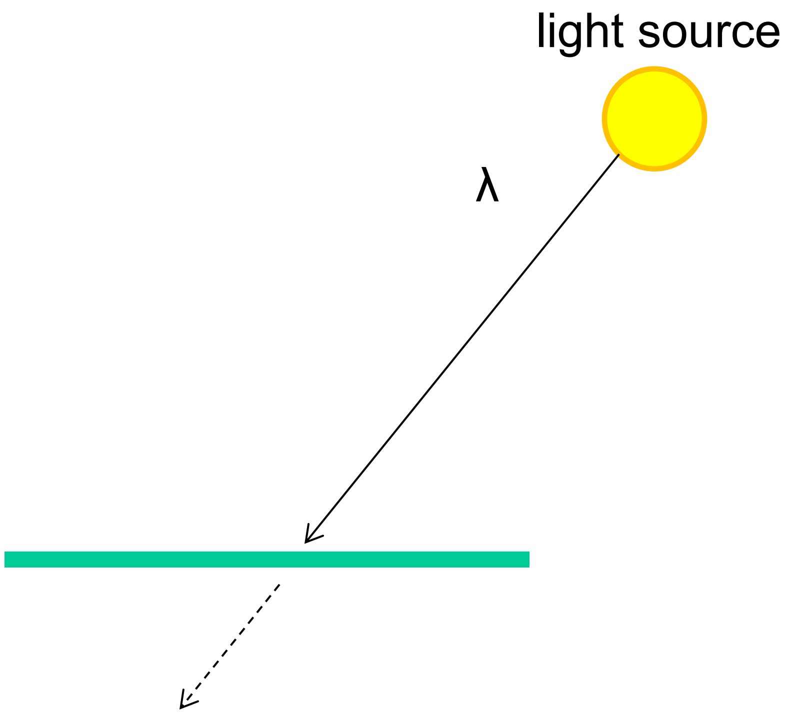
A photon's life choices

- Absorption
- Diffusion
- **Specular Reflection** 反射
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



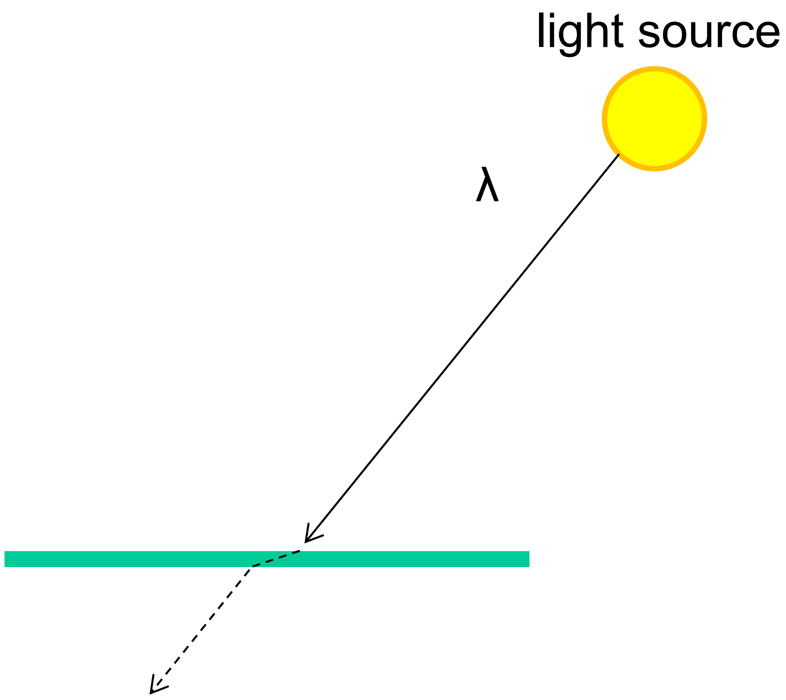
A photon's life choices

- Absorption
- Diffusion
- Reflection
- **Transparency** 透明
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



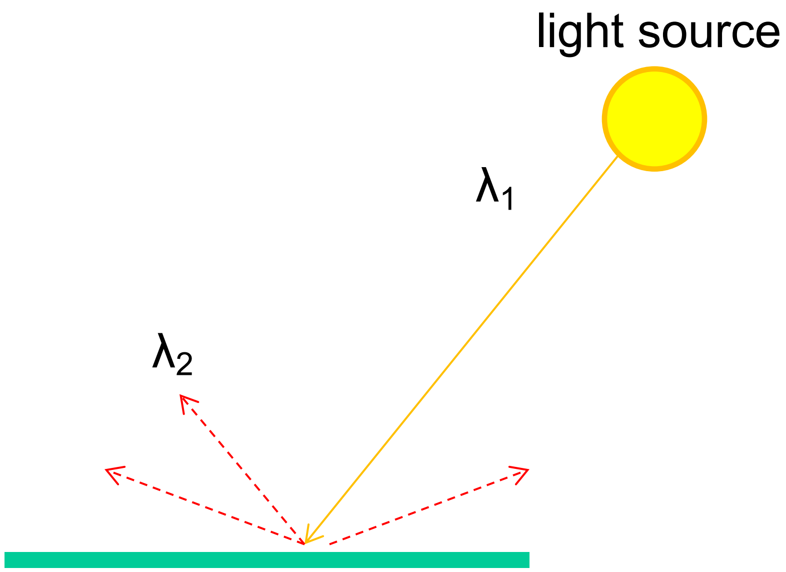
A photon's life choices

- Absorption
- Diffusion
- Reflection
- Transparency
- **Refraction** 折射
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



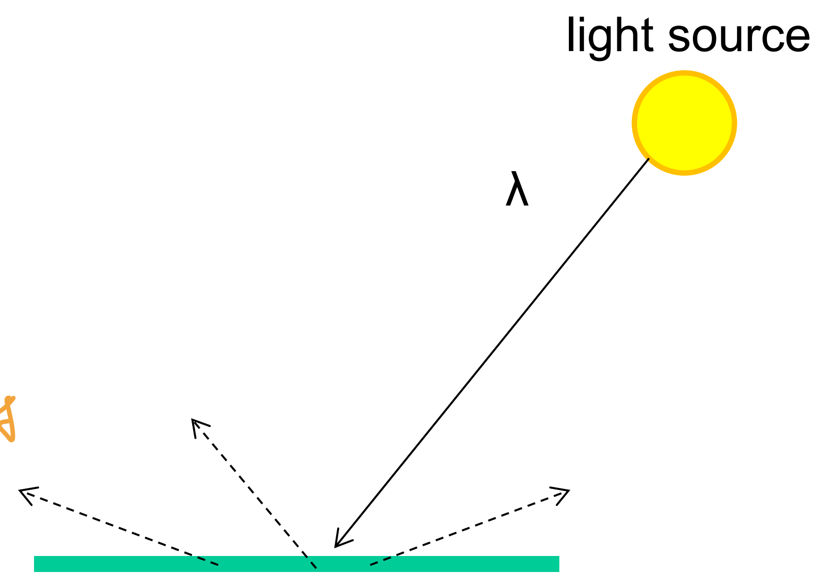
A photon's life choices

- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- **Fluorescence** 荧光
- Subsurface scattering
- Phosphorescence
- Interreflection



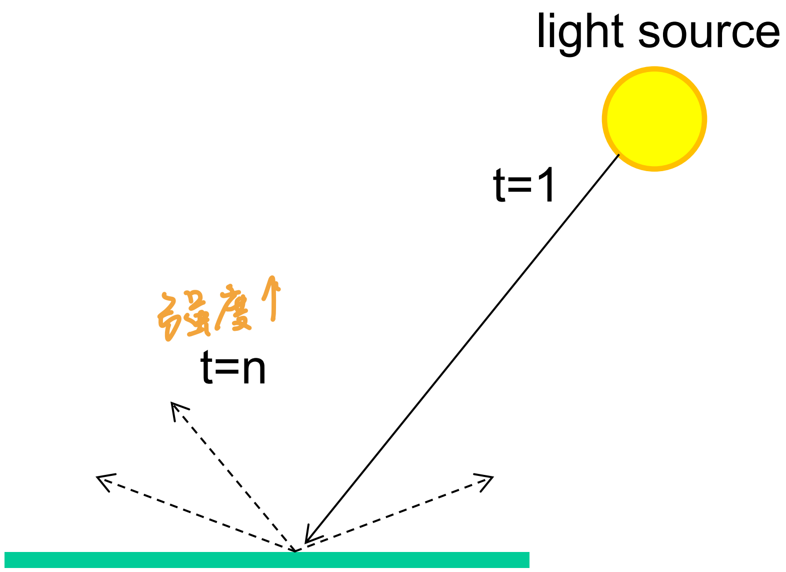
A photon's life choices

- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- **Subsurface scattering** 次表面散射
- Phosphorescence
- Interreflection



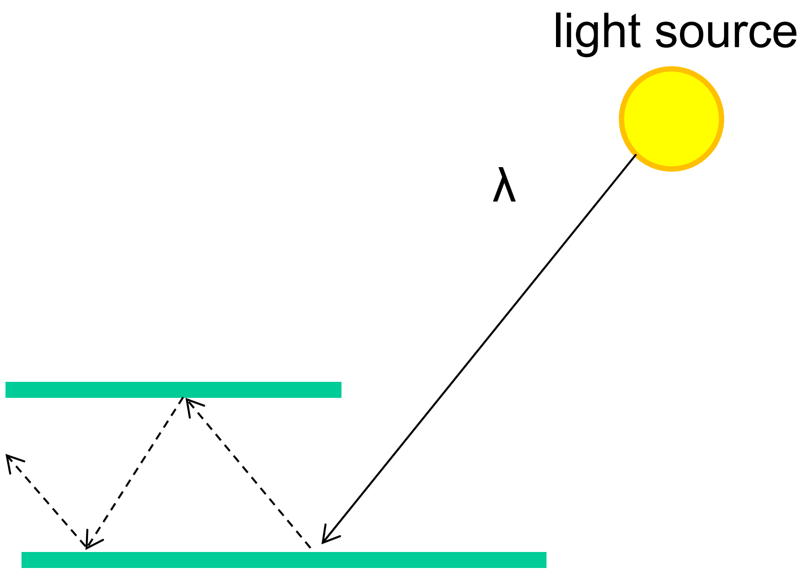
A photon’s life choices

- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- **Phosphorescence** 磷光
- Interreflection



A photon's life choices

- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- **Interreflection** 固反射

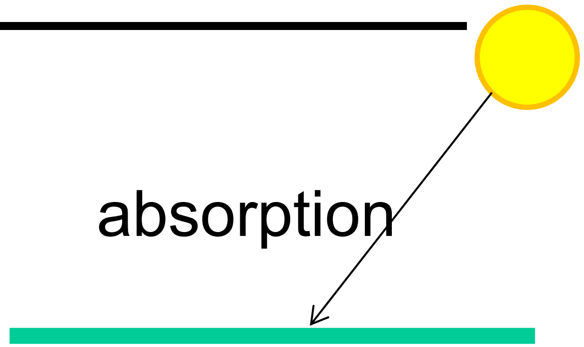


(Specular Interreflection)

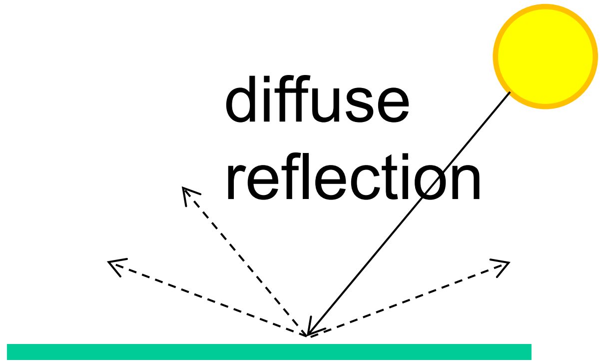
Some common effects

When light hits a typical surface

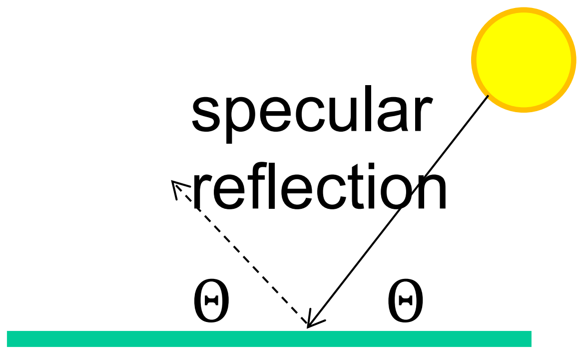
- Some light is absorbed (1-ρ) 吸收率
  - More absorbed for low albedos



- Some light is reflected diffusely
  - Independent of viewing direction

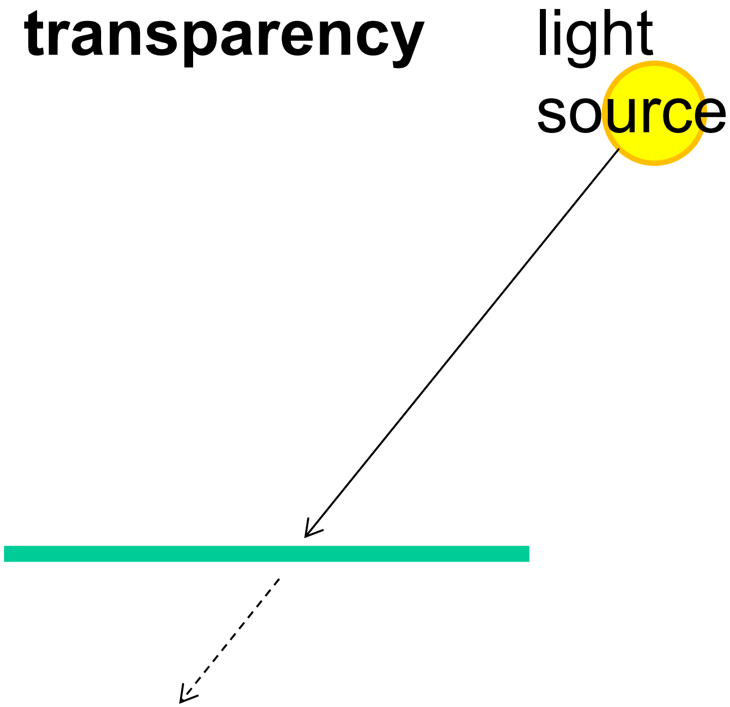


- Some light is reflected specularly
  - Light bounces off (like a mirror), depends on viewing direction

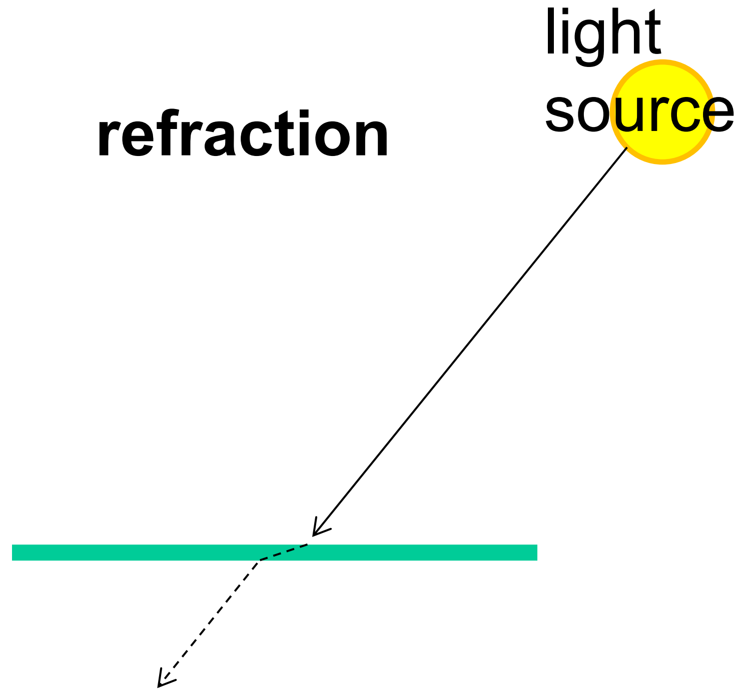


Other possible effects

transparency



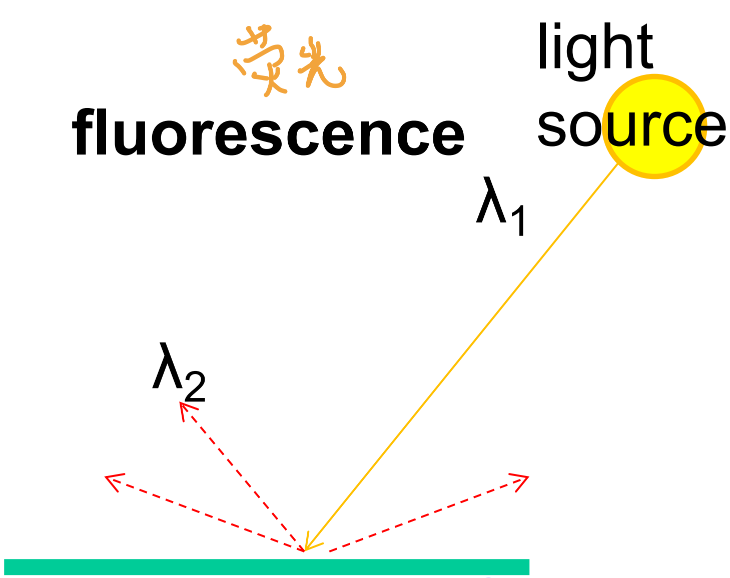
refraction



(光加强)

荧光

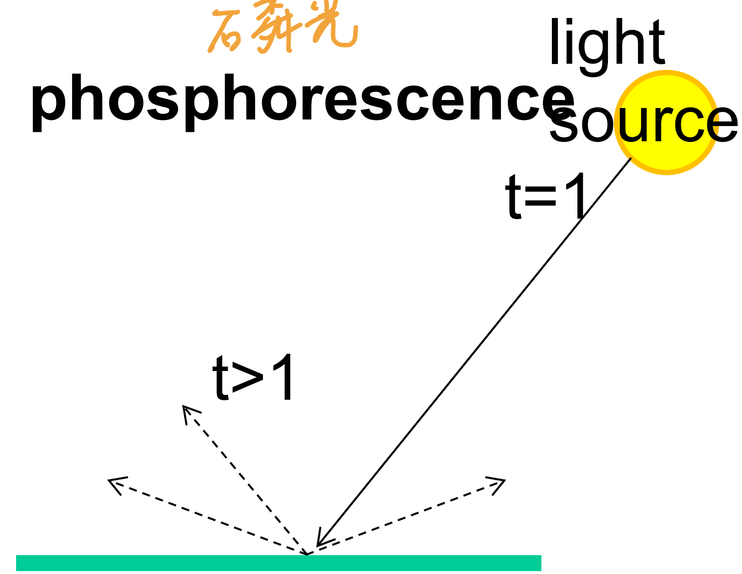
fluorescence



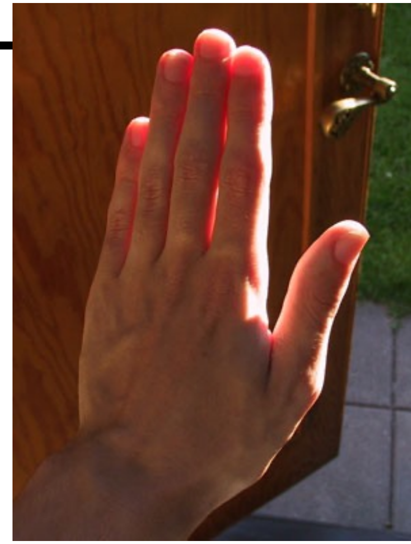
may 吸收一些光，夜间发出

磷光

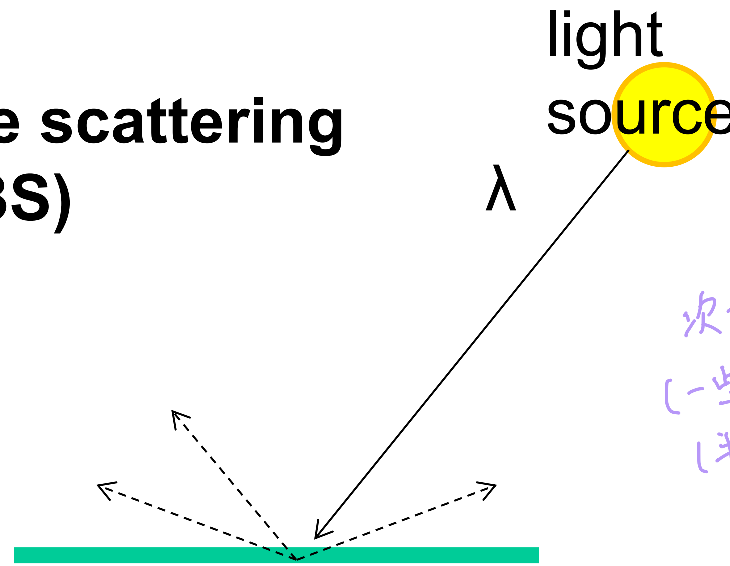
phosphorescence



冷发光



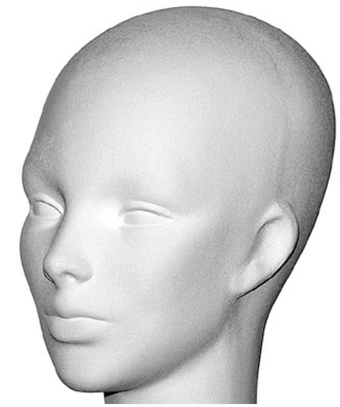
subsurface scattering
(3S)

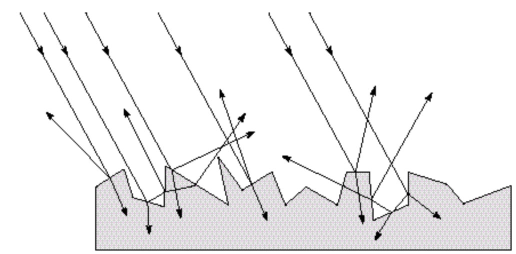


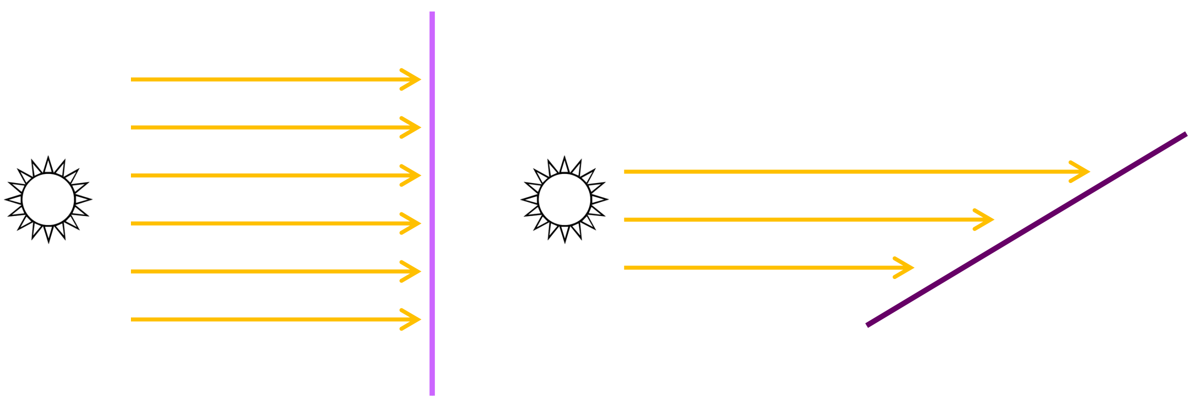
次表面反射
(一些材质)
(半透明难渲染

Diffuse reflection 漫反射

- Light is reflected equally in all directions
  - Dull, matte surfaces like chalk or latex paint
  - Microfacets scatter incoming light randomly
  - Effect is that light is reflected equally in all directions
- Brightness of the surface depends on the incidence of illumination







brighter darker

Photometric stereo (shape from shading)

- Can we reconstruct the shape of an object based on shading cues?

Luca della Robbia,
Cantoria, 1438

Photometric stereo

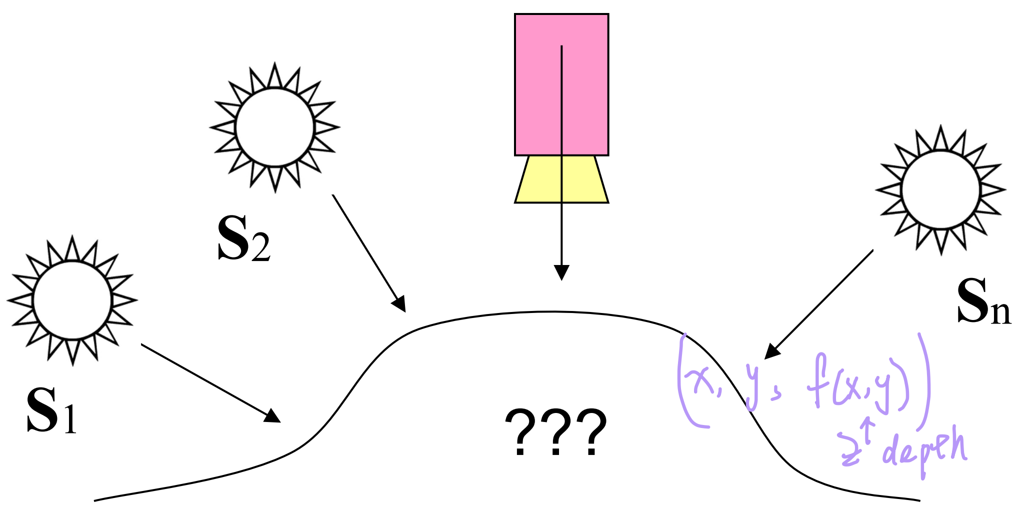
Assume:

必须亚光物体

- A Lambertian object
- A *local shading model* (each point on a surface receives light only from sources visible at that point)
- A set of *known* light source directions
- A set of pictures of an object, obtained in exactly the same camera/object configuration but using different sources

Goal: reconstruct object shape and albedo

重建物体形状与反照率ρ



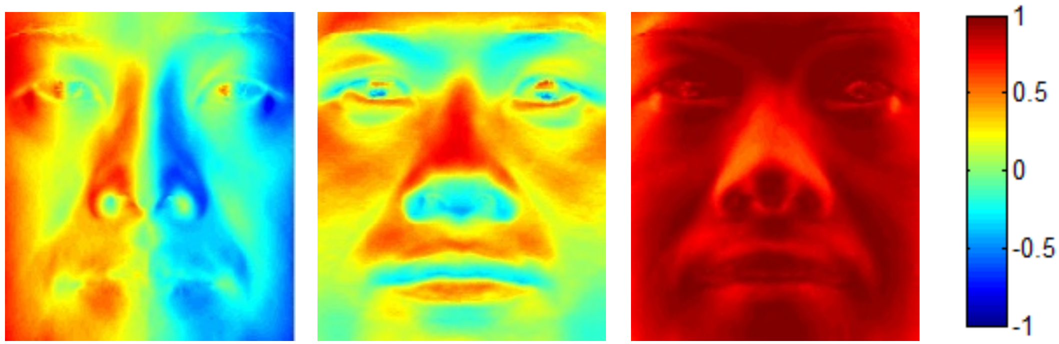
F&P 2nd ed., sec. 2.2.4

Example

Input

Recovered albedo

Recovered normal field



x y z

Recovered surface model

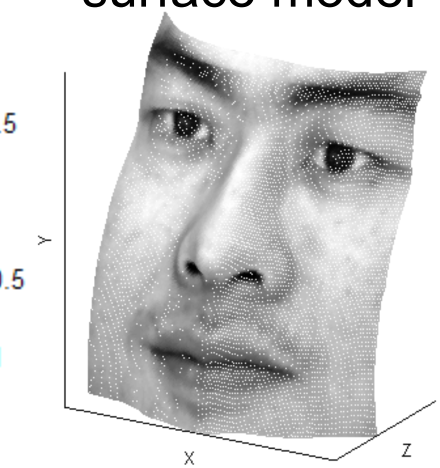
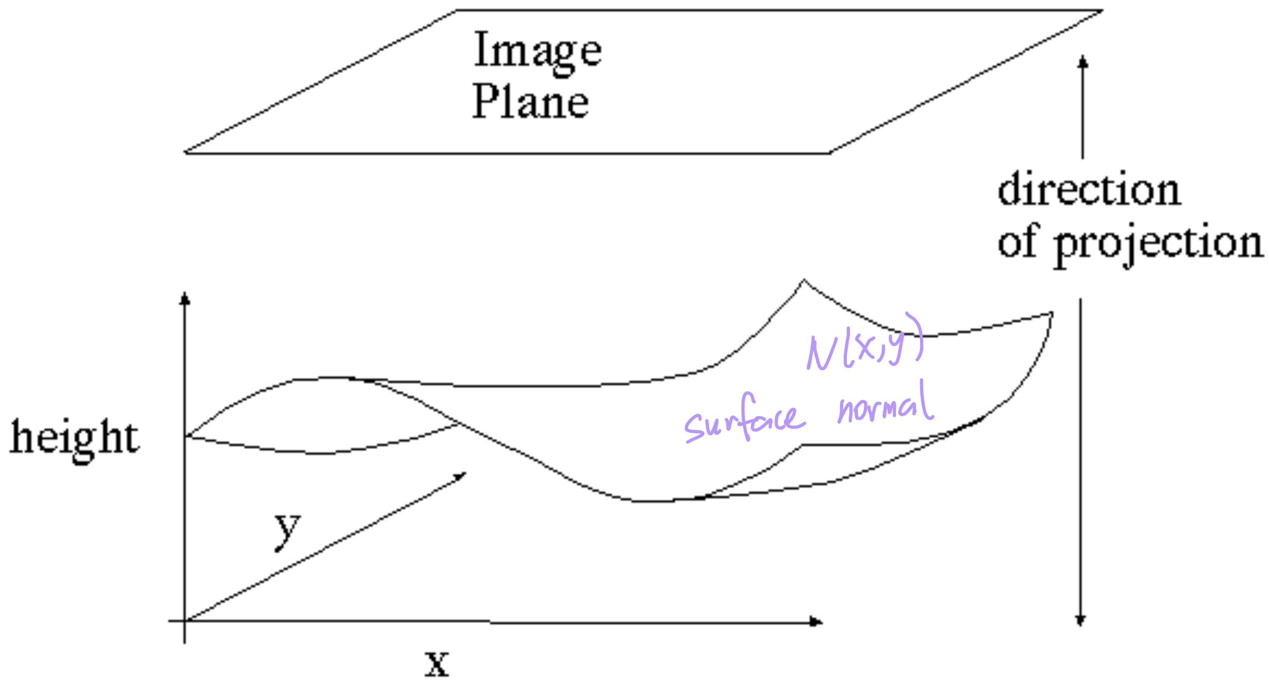


Image model

- **Known:** source vectors $\mathbf{S}_j$ and pixel values $I_j(x,y)$
- **Unknown:** surface normal $\mathbf{N}(x,y)$ and albedo 反照率 $\rho(x,y)$



F&P 2nd ed., sec. 2.2.4

Image model

- **Known:** source vectors $\mathbf{S}_j$ and pixel values $I_j(x,y)$
- **Unknown:** surface normal $\mathbf{N}(x,y)$ and albedo 反照率 $\rho(x,y)$
- Assume that the response function of the camera is a linear scaling by a factor of k
- Lambert's law:

$$
\begin{aligned}
I_j(x,y) &= k\,\rho(x,y)\big(\mathbf{N}(x,y)\cdot\mathbf{S}_j\big) \\
&= \big(\rho(x,y)\overset{\text{求解}}{\mathbf{N}(x,y)}\big)\cdot\overset{\text{已知}}{(k\mathbf{S}_j)} \\
&= \mathbf{g}(x,y)\cdot\mathbf{V}_j
\end{aligned}
$$

F&P 2nd ed., sec. 2.2.4

Least squares problem

- For each pixel, set up a linear system:

$$\underbrace{\begin{bmatrix} I_1(x,y) \\ I_2(x,y) \\ \vdots \\ I_n(x,y) \end{bmatrix}}_{\substack{(n \times 1) \\ \text{known}}} = \underbrace{\begin{bmatrix} \mathbf{V}_1^T \\ \mathbf{V}_2^T \\ \vdots \\ \mathbf{V}_n^T \end{bmatrix}}_{\substack{(n \times 3) \\ \text{known}}} \underbrace{\mathbf{g}(x,y)}_{\substack{(3 \times 1) \\ \text{unknown}}}$$

$Y = ax$

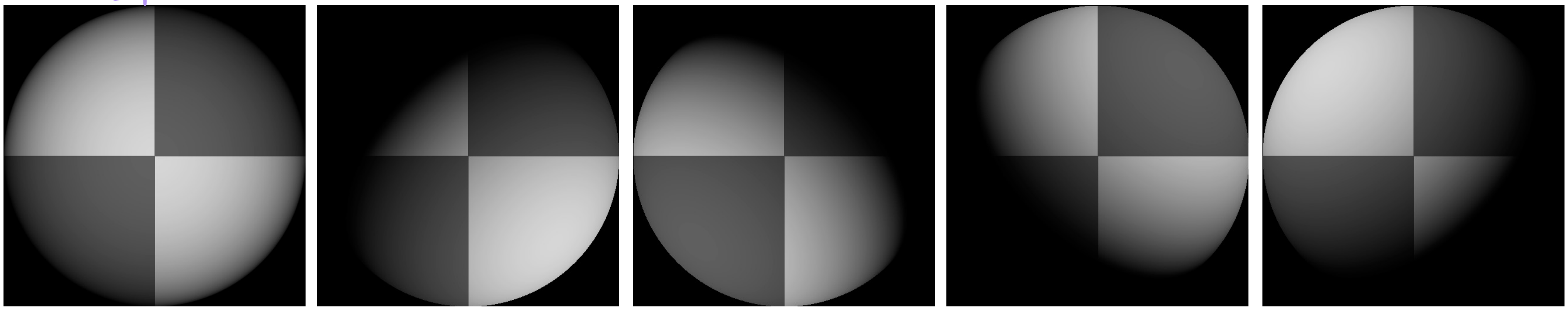
$\|Ax - Y\|^2$

- Obtain least-squares solution for $\mathbf{g}(x,y)$ (which we defined as $\mathbf{N}(x,y)\ \rho(x,y)$)
- Since $\mathbf{N}(x,y)$ is the unit normal, $\rho(x,y)$ is given by the magnitude of $\mathbf{g}(x,y)$
- Finally, $\mathbf{N}(x,y) = \mathbf{g}(x,y) \,/\, \rho(x,y)$

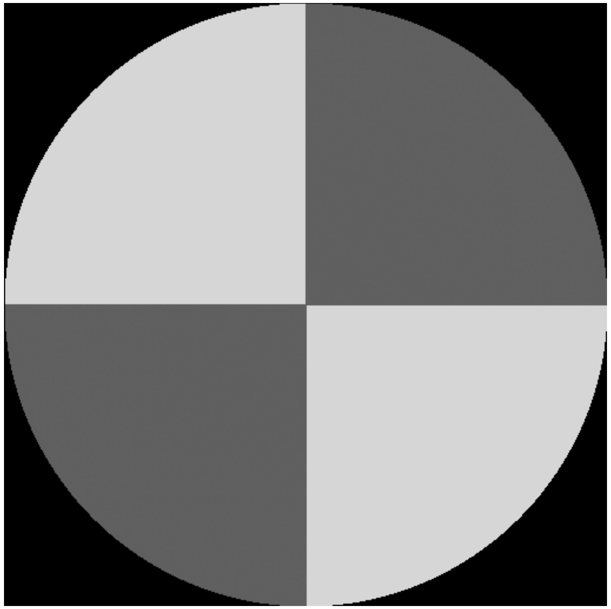
F&P 2nd ed., sec. 2.2.4

Synthetic example

Input



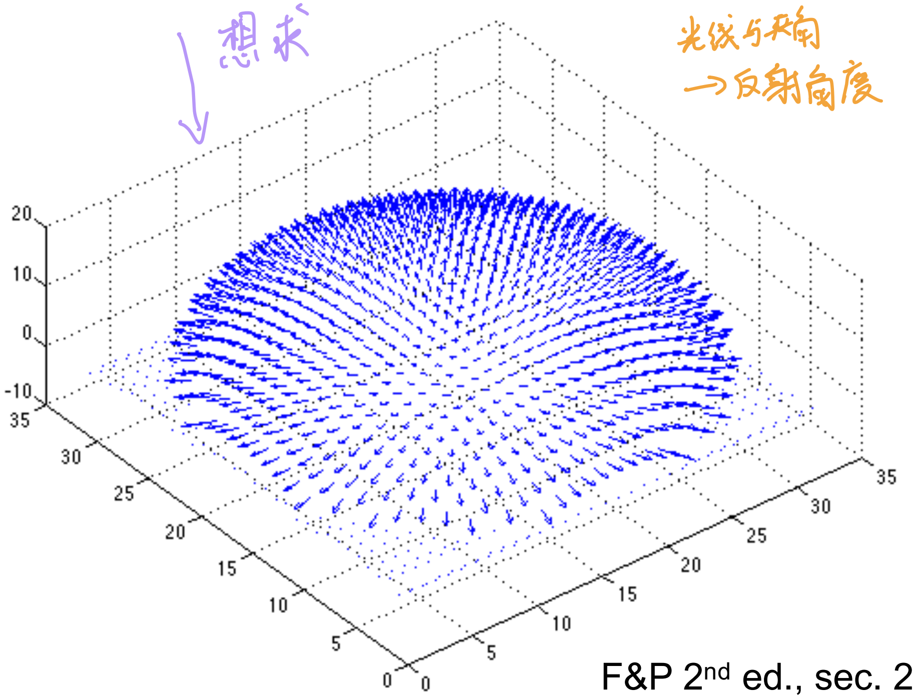
Recovered albedo



Recovered normal field

想求

光线与夹角
→ 反射角度



F&P 2nd ed., sec. 2.2.4

Recovering a surface from normals

Recall the surface is written as

$z = f(x, y)$

$$(x, y, f(x, y))$$

This means the normal has the form:

偏导 + 标准化

$$\mathbf{N}(x, y) = \frac{1}{\sqrt{f_x^2 + f_y^2 + 1}} \begin{pmatrix} f_x \\ f_y \\ 1 \end{pmatrix}$$

$$= \frac{1}{p(x,y)} g(x,y)$$

$$= \frac{1}{p(x,y)} \begin{pmatrix} g_1(x,y) \\ g_2(x,y) \\ g_3(x,y) \end{pmatrix} = \frac{g_3(x,y)}{p(x,y)} \begin{pmatrix} g_1/g_3 \\ g_2/g_3 \\ 1 \end{pmatrix}$$

If we write the estimated vector *g* as

$$\mathbf{g}(x, y) = \begin{pmatrix} g_1(x, y) \\ g_2(x, y) \\ g_3(x, y) \end{pmatrix}$$

Then we obtain values for the partial derivatives of the surface:

$$f_x(x, y) = g_1(x, y) / g_3(x, y)$$

$$f_y(x, y) = g_2(x, y) / g_3(x, y)$$

F&P 2nd ed., sec. 2.2.4

Recovering a surface from normals

We can now recover the surface height at any point by integration along some path, e.g.

$$f(x,y) = \int_0^x f_x(s,0)\,ds + \int_0^y f_y(x,t)\,dt + C$$

(for robustness, should take integrals over many different paths and average the results)

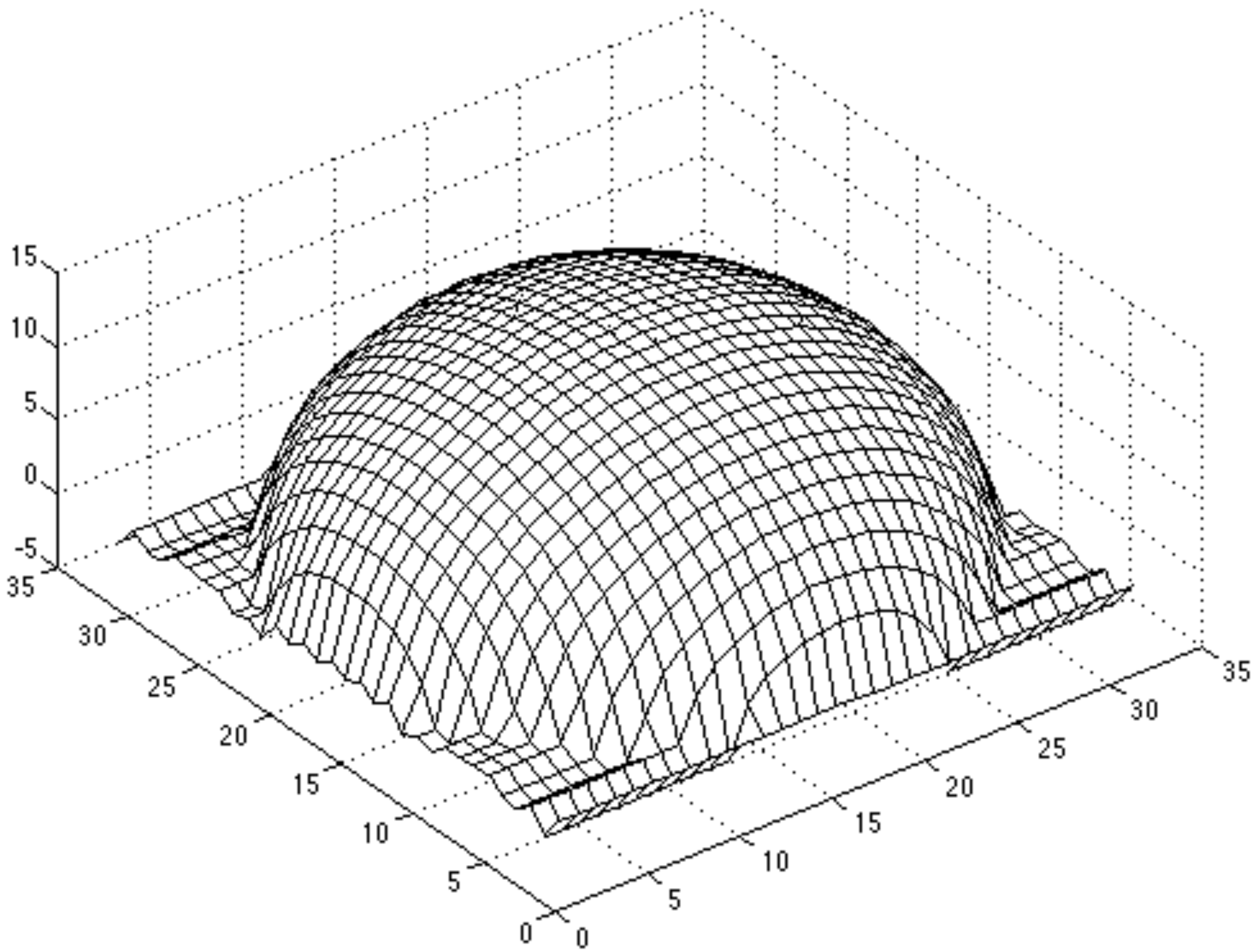
Integrability: for the surface f to exist, the mixed second partial derivatives must be equal:

$$\frac{\partial}{\partial y}(g_1(x,y)/g_3(x,y)) = \frac{\partial}{\partial x}(g_2(x,y)/g_3(x,y))$$

(in practice, they should at least be similar)

F&P 2nd ed., sec. 2.2.4

Surface recovered by integration



F&P 2nd ed., sec. 2.2.4

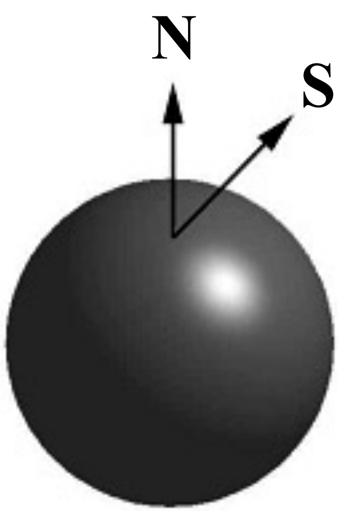
Limitations

- Simplistic reflectance and lighting model
- No shadows
- No interreflections
- No missing data
- Integration is tricky

表面已知计算光源

Finding the direction of the light source

$$\boxed{I(x,y) = \mathbf{N}(x,y) \cdot \mathbf{S}(x,y)}$$



Full 3D case:

$$\begin{pmatrix} N_x(x_1,y_1) & N_y(x_1,y_1) & N_z(x_1,y_1) \\ N_x(x_2,y_2) & N_y(x_2,y_2) & N_z(x_2,y_2) \\ \vdots & \vdots & \vdots \\ N_x(x_n,y_n) & N_y(x_n,y_n) & N_z(x_n,y_n) \end{pmatrix} \begin{pmatrix} S_x \\ S_y \\ S_z \end{pmatrix} = \begin{pmatrix} I(x_1,y_1) \\ I(x_2,y_2) \\ \vdots \\ I(x_n,y_n) \end{pmatrix}$$

For points on the *occluding contour*:

$$\begin{pmatrix} N_x(x_1,y_1) & N_y(x_1,y_1) \\ N_x(x_2,y_2) & N_y(x_2,y_2) \\ \vdots & \vdots \\ N_x(x_n,y_n) & N_y(x_n,y_n) \end{pmatrix} \begin{pmatrix} S_x \\ S_y \end{pmatrix} = \begin{pmatrix} I(x_1,y_1) \\ I(x_2,y_2) \\ \vdots \\ I(x_n,y_n) \end{pmatrix}$$

P. Nillius and J.-O. Eklundh, “Automatic estimation of the projected light source direction,” CVPR 2001

Finding the direction of the light source

P. Nillius and J.-O. Eklundh, “Automatic estimation of the projected light source direction,” CVPR 2001

Application: Detecting composite photos

Fake photo

Real photo

M. K. Johnson and H. Farid, [Exposing Digital Forgeries by Detecting Inconsistencies in Lighting](), ACM Multimedia and Security Workshop, 2005.