Generative Adversarial Networks (GANs)

So far in CS231N, all the applications of neural networks that we have explored have been **discriminative models** that take an input and are trained to produce a labeled output. This has ranged from straightforward classification of image categories to sentence generation (which was still phrased as a classification problem, our labels were in vocabulary space and we'd learned a recurrence to capture multi-word labels). In this notebook, we will expand our repetoire, and build **generative models** using neural networks. Specifically, we will learn how to build models which generate novel images that resemble a set of training images.

What is a GAN?

In 2014, Goodfellow et al. presented a method for training generative models called Generative Adversarial Networks (GANs for short). In a GAN, we build two different neural networks. Our first network is a traditional classification network, called the **discriminator**. We will train the discriminator to take images, and classify them as being real (belonging to the training set) or fake (not present in the training set). Our other network, called the **generator**, will take random noise as input and transform it using a neural network to produce images. The goal of the generator is to fool the discriminator into thinking the images it produced are real.

We can think of this back and forth process of the generator (G) trying to fool the discriminator (D), and the discriminator trying to correctly classify real vs. fake as a minimax game:

$$\min_{G} \max_{D} \mathbb{E}_{x \sim p_{ ext{data}}} \left[\log D(x)
ight] + \mathbb{E}_{z \sim p(z)} \left[\log (1 - D(G(z)))
ight]$$

where $z\sim p(z)$ are the random noise samples, G(z) are the generated images using the neural network generator G, and D is the output of the discriminator, specifying the probability of an input being real. In Goodfellow et al., they analyze this minimax game and show how it relates to minimizing the Jensen-Shannon divergence between the training data distribution and the generated samples from G.

To optimize this minimax game, we will attenute between taking gradient *descent* steps on the objective for G, and gradient *ascent* steps on the objective for D:

- 1. update the **generator** (G) to minimize the probability of the **discriminator making the** correct choice.
- 2. update the **discriminator** (D) to maximize the probability of the **discriminator making** the correct choice.

While these updates are useful for analysis, they do not perform well in practice. Instead, we will use a different objective when we update the generator: maximize the probability of the **discriminator making the incorrect choice**. This small change helps to allevaiate problems with the generator gradient vanishing when the discriminator is confident. This is the

standard update used in most GAN papers, and was used in the original paper from Goodfellow et al..

In this assignment, we will alternate the following updates:

1. Update the generator (G) to maximize the probability of the discriminator making the incorrect choice on generated data:

$$\mathop{\text{maximize}}_{G} \mathbb{E}_{z \sim p(z)} \left[\log D(G(z)) \right]$$

2. Update the discriminator (D), to maximize the probability of the discriminator making the correct choice on real and generated data:

$$ext{maximize } \mathbb{E}_{x \sim p_{ ext{data}}} \left[\log D(x)
ight] + \mathbb{E}_{z \sim p(z)} \left[\log (1 - D(G(z)))
ight]$$

What else is there?

Since 2014, GANs have exploded into a huge research area, with massive workshops, and hundreds of new papers. Compared to other approaches for generative models, they often produce the highest quality samples but are some of the most difficult and finicky models to train (see this github repo that contains a set of 17 hacks that are useful for getting models working). Improving the stabiilty and robustness of GAN training is an open research question, with new papers coming out every day! For a more recent tutorial on GANs, see here. There is also some even more recent exciting work that changes the objective function to Wasserstein distance and yields much more stable results across model architectures: WGAN, WGAN-GP.

GANs are not the only way to train a generative model! For other approaches to generative modeling check out the deep generative model chapter of the Deep Learning book. Another popular way of training neural networks as generative models is Variational Autoencoders (co-discovered here and here). Variational autoencoders combine neural networks with variational inference to train deep generative models. These models tend to be far more stable and easier to train but currently don't produce samples that are as pretty as GANs.

Here's an example of what your outputs from the 3 different models you're going to train should look like... note that GANs are sometimes finicky, so your outputs might not look exactly like this... this is just meant to be a *rough* guideline of the kind of quality you can expect:



Setup

```
import torch
import torch.nn as nn
from torch.nn import init
import torchvision
import torchvision.transforms as T
import torch.optim as optim
from torch.utils.data import DataLoader
from torch.utils.data import sampler
```

```
%matplotlib inline
         plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
         plt. rcParams['image.interpolation'] = 'nearest'
         plt.rcParams['image.cmap'] = 'gray'
         # for auto-reloading external modules
         # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
         %load ext autoreload
         %autoreload 2
         def show images (images):
             images = np. reshape(images, [images. shape[0], -1]) # images reshape to (batch_s
             sqrtn = int(np. ceil(np. sqrt(images. shape[0])))
             sqrtimg = int(np. ceil(np. sqrt(images. shape[1])))
             fig = plt. figure (figsize=(sqrtn, sqrtn))
             gs = gridspec. GridSpec(sqrtn, sqrtn)
             gs. update (wspace=0.05, hspace=0.05)
             for i, img in enumerate (images):
                 ax = plt. subplot(gs[i])
                 plt. axis ('off')
                 ax. set_xticklabels([])
                 ax. set_yticklabels([])
                 ax. set aspect ('equal')
                 plt. imshow(img. reshape([sqrtimg, sqrtimg]))
             return
In [ ]: # Colab users only
         %cd drive/My\ Drive/$FOLDERNAME/
         %cp -r gan-checks-tf.npz /content/
         %cd /content/
In [2]: from cs231n.gan pytorch import preprocess img, deprocess img, rel error, count para
```

import torchvision. datasets as dset

import matplotlib.gridspec as gridspec

import matplotlib.pyplot as plt

import numpy as np

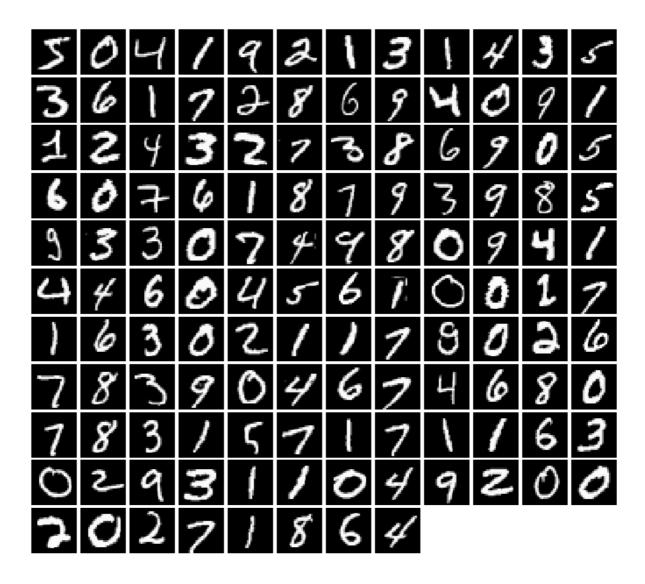
Dataset

answers = dict(np. load('gan-checks-tf.npz'))

GANs are notoriously finicky with hyperparameters, and also require many training epochs. In order to make this assignment approachable without a GPU, we will be working on the MNIST dataset, which is 60,000 training and 10,000 test images. Each picture contains a centered image of white digit on black background (0 through 9). This was one of the first datasets used to train convolutional neural networks and it is fairly easy -- a standard CNN model can easily exceed 99% accuracy.

To simplify our code here, we will use the PyTorch MNIST wrapper, which downloads and loads the MNIST dataset. See the documentation for more information about the interface. The default parameters will take 5,000 of the training examples and place them into a validation dataset. The data will be saved into a folder called MNIST_data.

```
In [3]: NUM_TRAIN = 50000
        NUM_VAL = 5000
         NOISE DIM = 96
         batch_size = 128
         mnist train = dset. MNIST('./cs231n/datasets/MNIST data', train=True, download=True,
                                    transform=T. ToTensor())
         loader train = DataLoader (mnist train, batch size=batch size,
                                   sampler=ChunkSampler(NUM TRAIN, 0))
         mnist_val = dset.MNIST('./cs231n/datasets/MNIST_data', train=True, download=True,
                                    transform=T. ToTensor())
         loader_val = DataLoader(mnist_val, batch_size=batch_size,
                                 sampler=ChunkSampler(NUM VAL, NUM TRAIN))
         imgs = loader train. iter ().next()[0].view(batch size, 784).numpy().squeeze()
         show_images(imgs)
        Downloading http://yann.lecun.com/exdb/mnist/train-images-idx3-ubyte.gz
        Failed to download (trying next):
        HTTP Error 403: Forbidden
        Downloading https://ossci-datasets.s3.amazonaws.com/mnist/train-images-idx3-ubyte.gz
        Downloading https://ossci-datasets.s3.amazonaws.com/mnist/train-images-idx3-ubyte.gz
        to ./cs231n/datasets/MNIST_data\MNIST\raw\train-images-idx3-ubyte.gz
                        0/9912422 [00:00<?, ?it/s]
        Extracting ./cs231n/datasets/MNIST_data\MNIST\raw\train-images-idx3-ubyte.gz to ./cs
        231n/datasets/MNIST data\MNIST\raw
        Downloading http://yann.lecun.com/exdb/mnist/train-labels-idxl-ubyte.gz
        Failed to download (trying next):
        HTTP Error 403: Forbidden
        Downloading https://ossci-datasets.s3.amazonaws.com/mnist/train-labels-idx1-ubyte.gz
        Downloading https://ossci-datasets.s3.amazonaws.com/mnist/train-labels-idxl-ubyte.gz
        to ./cs231n/datasets/MNIST data\MNIST\raw\train-labels-idx1-ubyte.gz
                        0/28881 [00:00<?, ?it/s]
        Extracting ./cs231n/datasets/MNIST_data\MNIST\raw\train-labels-idx1-ubyte.gz to ./cs
        231n/datasets/MNIST data\MNIST\raw
        Downloading http://yann.lecun.com/exdb/mnist/t10k-images-idx3-ubyte.gz
        Failed to download (trying next):
        HTTP Error 403: Forbidden
        Downloading https://ossci-datasets.s3.amazonaws.com/mnist/t10k-images-idx3-ubyte.gz
        Downloading https://ossci-datasets.s3.amazonaws.com/mnist/t10k-images-idx3-ubyte.gz
        to ./cs231n/datasets/MNIST_data\MNIST\raw\t10k-images-idx3-ubyte.gz
          0%
                        | 0/1648877 [00:00<?, ?it/s]
        Extracting ./cs231n/datasets/MNIST_data\MNIST\raw\t10k-images-idx3-ubyte.gz to ./cs2
        31n/datasets/MNIST_data\MNIST\raw
        Downloading http://yann.lecun.com/exdb/mnist/t10k-labels-idx1-ubyte.gz
        Failed to download (trying next):
        HTTP Error 403: Forbidden
        Downloading https://ossci-datasets.s3.amazonaws.com/mnist/t10k-labels-idx1-ubyte.gz
        Downloading https://ossci-datasets.s3.amazonaws.com/mnist/t10k-labels-idx1-ubyte.gz
        to ./cs231n/datasets/MNIST data\MNIST\raw\t10k-labels-idx1-ubyte.gz
                        | 0/4542 [00:00<?, ?it/s]
          0%
        Extracting ./cs231n/datasets/MNIST_data\MNIST\raw\t10k-labels-idx1-ubyte.gz to ./cs2
        31n/datasets/MNIST data\MNIST\raw
```



Random Noise

```
Generate uniform noise from -1 to 1 with shape [batch_size, dim].
```

Implement sample_noise in cs231n/gan_pytorch.py .

Hint: use torch.rand.

Make sure noise is the correct shape and type:

```
In [4]: from cs231n.gan_pytorch import sample_noise

def test_sample_noise():
    batch_size = 3
    dim = 4
    torch.manual_seed(231)
    z = sample_noise(batch_size, dim)
    np_z = z.cpu().numpy()
    assert np_z.shape == (batch_size, dim)
    assert torch.is_tensor(z)
    assert np. all(np_z >= -1.0) and np. all(np_z <= 1.0)
    assert np. any(np_z < 0.0) and np. any(np_z > 0.0)
    print('All tests passed!')

test_sample_noise()
```

Flatten

Recall our Flatten operation from previous notebooks... this time we also provide an Unflatten, which you might want to use when implementing the convolutional generator. We also provide a weight initializer (and call it for you) that uses Xavier initialization instead of PyTorch's uniform default.

```
In [5]: from cs231n.gan_pytorch import Flatten, Unflatten, initialize_weights
```

CPU / GPU

By default all code will run on CPU. GPUs are not needed for this assignment, but will help you to train your models faster. If you do want to run the code on a GPU, then change the dtype variable in the following cell. If you are a Colab user, it is recommeded to change colab runtime to GPU.

```
In [15]: #dtype = torch.FloatTensor
dtype = torch.cuda.FloatTensor ## UNCOMMENT THIS LINE IF YOU'RE ON A GPU!
```

Discriminator

Our first step is to build a discriminator. Fill in the architecture as part of the nn.Sequential constructor in the function below. All fully connected layers should include bias terms. The architecture is:

- Fully connected layer with input size 784 and output size 256
- LeakyReLU with alpha 0.01
- Fully connected layer with input_size 256 and output size 256
- LeakyReLU with alpha 0.01
- Fully connected layer with input size 256 and output size 1

Recall that the Leaky ReLU nonlinearity computes $f(x) = \max(\alpha x, x)$ for some fixed constant α ; for the LeakyReLU nonlinearities in the architecture above we set $\alpha = 0.01$.

The output of the discriminator should have shape [batch_size, 1], and contain real numbers corresponding to the scores that each of the batch_size inputs is a real image.

```
Implement discriminator in cs231n/gan_pytorch.py
```

Test to make sure the number of parameters in the discriminator is correct:

```
In [7]: from cs231n.gan_pytorch import discriminator

def test_discriminator(true_count=267009):
    model = discriminator()
    cur_count = count_params(model)
    if cur_count != true_count:
        print('Incorrect number of parameters in discriminator. Check your achitecturelse:
```

```
print('Correct number of parameters in discriminator.')
test_discriminator()
```

Correct number of parameters in discriminator.

Generator

Now to build the generator network:

- Fully connected layer from noise_dim to 1024
- ReLU
- Fully connected layer with size 1024
- ReLU
- Fully connected layer with size 784
- TanH (to clip the image to be in the range of [-1,1])

Implement generator in cs231n/gan_pytorch.py

Test to make sure the number of parameters in the generator is correct:

```
In [8]: from cs231n.gan_pytorch import generator

def test_generator(true_count=1858320):
    model = generator(4)
    cur_count = count_params(model)
    if cur_count != true_count:
        print('Incorrect number of parameters in generator. Check your achitecture.'
    else:
        print('Correct number of parameters in generator.')

test_generator()
```

Correct number of parameters in generator.

GAN Loss

Compute the generator and discriminator loss. The generator loss is:

$$\ell_G = -\mathbb{E}_{z \sim p(z)} \left[\log D(G(z))
ight]$$

and the discriminator loss is:

$$\ell_D = -\mathbb{E}_{x \sim p_{ ext{data}}} \left[\log D(x)
ight] - \mathbb{E}_{z \sim p(z)} \left[\log (1 - D(G(z)))
ight]$$

Note that these are negated from the equations presented earlier as we will be *minimizing* these losses.

HINTS: You should use the <code>bce_loss</code> function defined below to compute the binary cross entropy loss which is needed to compute the log probability of the true label given the logits output from the discriminator. Given a score $s \in \mathbb{R}$ and a label $y \in \{0,1\}$, the binary cross entropy loss is

$$bce(s, y) = -y * \log(s) - (1 - y) * \log(1 - s)$$

A naive implementation of this formula can be numerically unstable, so we have provided a numerically stable implementation for you below.

You will also need to compute labels corresponding to real or fake and use the logit arguments to determine their size. Make sure you cast these labels to the correct data type using the global dtype variable, for example:

```
true_labels = torch.ones(size).type(dtype)
```

Instead of computing the expectation of $\log D(G(z))$, $\log D(x)$ and $\log(1 - D(G(z)))$, we will be averaging over elements of the minibatch, so make sure to combine the loss by averaging instead of summing.

```
Implement bce_loss, discriminator_loss, generator_loss in
cs231n/gan_pytorch.py
```

Test your generator and discriminator loss. You should see errors < 1e-7.

test_generator_loss(answers['logits_fake'], answers['g_loss_true'])

Maximum error in g_loss: 4.4518e-09

Optimizing our loss

Make a function that returns an optim.Adam optimizer for the given model with a 1e-3 learning rate, beta1=0.5, beta2=0.999. You'll use this to construct optimizers for the generators and discriminators for the rest of the notebook.

```
Implement get_optimizer in cs231n/gan_pytorch.py
```

Training a GAN!

We provide you the main training loop... you won't need to change run_a_gan in cs231n/gan_pytorch.py , but we encourage you to read through and understand it.

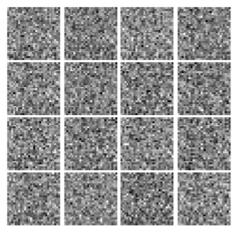
```
In [13]: from cs231n.gan_pytorch import get_optimizer, run_a_gan
```

```
In [16]: # Make the discriminator
         D = discriminator().type(dtype)
          # Make the generator
          G = generator(). type(dtype)
          # Use the function you wrote earlier to get optimizers for the Discriminator and the
          D_solver = get_optimizer(D)
          G_solver = get_optimizer(G)
          # Run it!
          images = run_a_gan(D, G, D_solver, G_solver, discriminator_loss, generator_loss, loa
          Iter: 0, D: 1.366, G:0.7204
          Iter: 250, D: 1.33, G:0.9184
         Iter: 500, D: 0.8938, G:1.03
         Iter: 750, D: 1.262, G:1.474
         Iter: 1000, D: 1.2, G:0.7694
         Iter: 1250, D: 1.137, G:1.465
         Iter: 1500, D: 1.243, G:0.9016
         Iter: 1750, D: 1.31, G:0.7951
         Iter: 2000, D: 1.504, G:1.249
         Iter: 2250, D: 1.319, G:0.9127
         Iter: 2500, D: 1.346, G:0.7864
         Iter: 2750, D: 1.228, G:0.8248
         Iter: 3000, D: 1.31, G:0.7513
         Iter: 3250, D: 1.264, G:0.7869
         Iter: 3500, D: 1.281, G:0.7632
         Iter: 3750, D: 1.346, G:0.8384
```

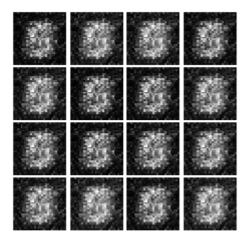
Run the cell below to show the generated images.

```
In [17]: numIter = 0
for img in images:
    print("Iter: {}". format(numIter))
    show_images(img)
    plt. show()
    numIter += 250
    print()
```

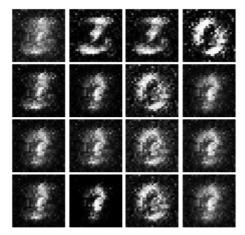
Iter: 0



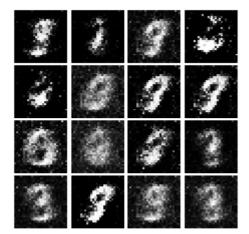
Iter: 250



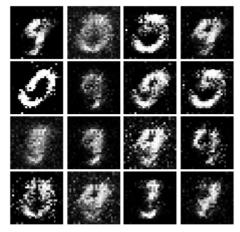
Iter: 500



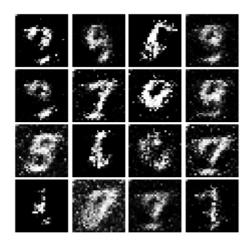
Iter: 750



Iter: 1000



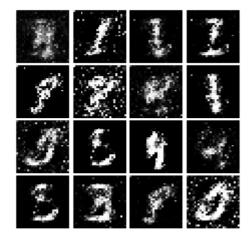
Iter: 1250



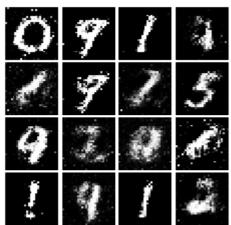
Iter: 1500



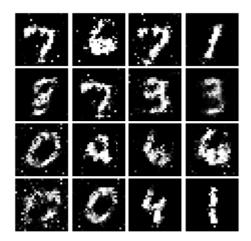
Iter: 1750



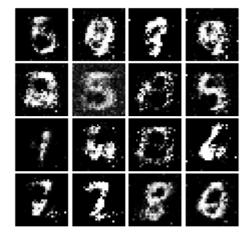
Iter: 2000



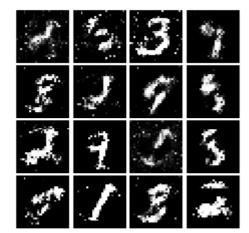
Iter: 2250



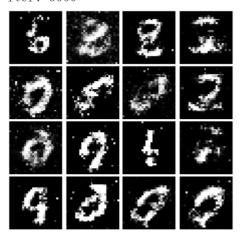
Iter: 2500



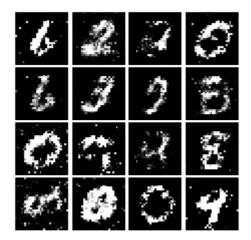
Iter: 2750



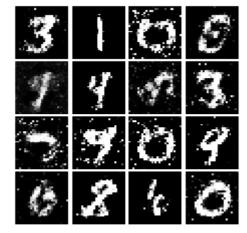
Iter: 3000



Iter: 3250



Iter: 3500



Iter: 3750



Please tag the cell below on Gradescope while submitting.

```
In [18]: print("Vanilla GAN Fianl image:")
    show_images(images[-1])
    plt. show()
```

Vanilla GAN Fianl image:



Well that wasn't so hard, was it? In the iterations in the low 100s you should see black backgrounds, fuzzy shapes as you approach iteration 1000, and decent shapes, about half of which will be sharp and clearly recognizable as we pass 3000.

Least Squares GAN

We'll now look at Least Squares GAN, a newer, more stable alernative to the original GAN loss function. For this part, all we have to do is change the loss function and retrain the model. We'll implement equation (9) in the paper, with the generator loss:

$$\ell_G = rac{1}{2}\mathbb{E}_{z\sim p(z)}\left[\left(D(G(z))-1
ight)^2
ight]$$

and the discriminator loss:

$$\ell_D = rac{1}{2}\mathbb{E}_{x \sim p_{ ext{data}}}\left[\left(D(x) - 1
ight)^2
ight] + rac{1}{2}\mathbb{E}_{z \sim p(z)}\left[\left(D(G(z))
ight)^2
ight]$$

HINTS: Instead of computing the expectation, we will be averaging over elements of the minibatch, so make sure to combine the loss by averaging instead of summing. When plugging in for D(x) and D(G(z)) use the direct output from the discriminator (scores_real and scores_fake).

Implement ls_discriminator_loss , ls_generator_loss in
cs231n/gan_pytorch.py

Before running a GAN with our new loss function, let's check it:

```
Maximum error in d_loss: 1.53171e-08
Maximum error in g_loss: 2.7837e-09
```

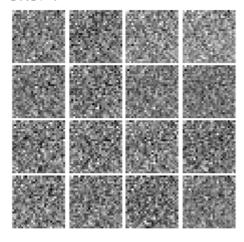
Run the following cell to train your model!

```
In [20]:
          D_LS = discriminator(). type(dtype)
          G_LS = generator(). type(dtype)
          D_LS_solver = get_optimizer(D_LS)
          G_LS_solver = get_optimizer(G_LS)
          images = run_a_gan(D_LS, G_LS, D_LS_solver, G_LS_solver, ls_discriminator_loss, ls_g
         Iter: 0, D: 0.5481, G:0.47
         Iter: 250, D: 0.7852, G:0.2117
         Iter: 500, D: 0.1683, G:1.45
         Iter: 750, D: 0.1184, G:0.2799
          Iter: 1000, D: 0.1239, G:0.42
         Iter: 1250, D: 0.1647, G:0.2519
         Iter: 1500, D: 0.1699, G:0.3553
         Iter: 1750, D: 0.1592, G:0.2309
         Iter: 2000, D: 0.215, G:0.189
         Iter: 2250, D: 0.2317, G:0.1713
         Iter: 2500, D: 0.1908, G:0.1298
         Iter: 2750, D: 0.2244, G:0.1654
         Iter: 3000, D: 0.2387, G:0.1595
         Iter: 3250, D: 0.2227, G:0.1946
         Iter: 3500, D: 0.2347, G:0.1694
         Iter: 3750, D: 0.2174, G:0.1575
```

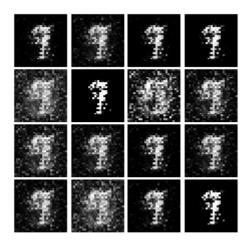
Run the cell below to show generated images.

```
In [21]: numIter = 0
    for img in images:
        print("Iter: {}". format(numIter))
        show_images(img)
        plt. show()
        numIter += 250
        print()
```

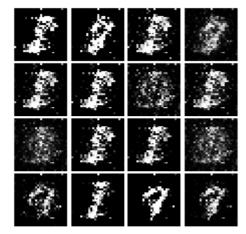
Iter: 0



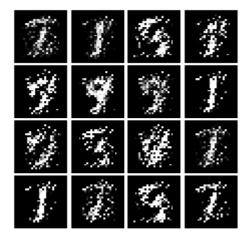
Iter: 250



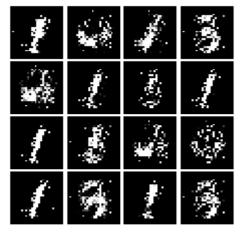
Iter: 500



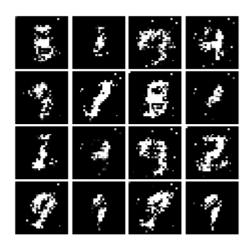
Iter: 750



Iter: 1000



Iter: 1250



Iter: 1500



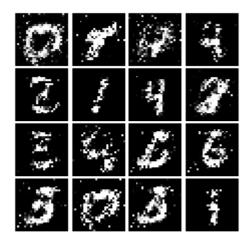
Iter: 1750



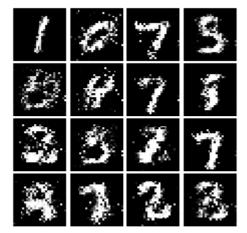
Iter: 2000



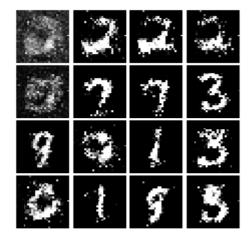
Iter: 2250



Iter: 2500



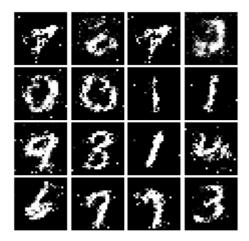
Iter: 2750



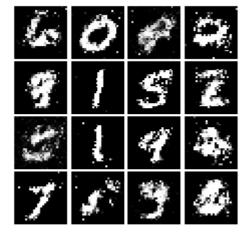
Iter: 3000



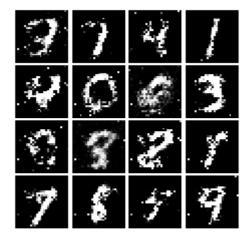
Iter: 3250



Iter: 3500



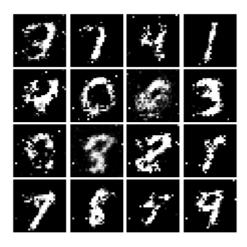
Iter: 3750



Please tag the cell below on Gradescope while submitting.

```
In [22]: print("LSGAN Fianl image:")
    show_images(images[-1])
    plt. show()
```

LSGAN Fianl image:



Deeply Convolutional GANs

In the first part of the notebook, we implemented an almost direct copy of the original GAN network from Ian Goodfellow. However, this network architecture allows no real spatial reasoning. It is unable to reason about things like "sharp edges" in general because it lacks any convolutional layers. Thus, in this section, we will implement some of the ideas from DCGAN, where we use convolutional networks

Discriminator

We will use a discriminator inspired by the TensorFlow MNIST classification tutorial, which is able to get above 99% accuracy on the MNIST dataset fairly quickly.

- Reshape into image tensor (Use Unflatten!)
- Conv2D: 32 Filters, 5x5, Stride 1
- Leaky ReLU(alpha=0.01)
- Max Pool 2x2, Stride 2
- Conv2D: 64 Filters, 5x5, Stride 1
- Leaky ReLU(alpha=0.01)
- Max Pool 2x2, Stride 2
- Flatten
- Fully Connected with output size 4 x 4 x 64
- Leaky ReLU(alpha=0.01)
- Fully Connected with output size 1

Implement build_dc_classifier in cs231n/gan_pytorch.py

```
In [25]: from cs231n.gan_pytorch import build_dc_classifier

data = next(enumerate(loader_train))[-1][0].type(dtype)
b = build_dc_classifier(batch_size).type(dtype)
out = b(data)
print(out.size())

torch.Size([128, 1])
```

Check the number of parameters in your classifier as a sanity check:

```
In [26]: def test_dc_classifer(true_count=1102721):
    model = build_dc_classifier(batch_size)
    cur_count = count_params(model)
    if cur_count != true_count:
        print('Incorrect number of parameters in generator. Check your achitecture.')
    else:
        print('Correct number of parameters in generator.')

test_dc_classifer()
```

Correct number of parameters in generator.

Generator

For the generator, we will copy the architecture exactly from the InfoGAN paper. See Appendix C.1 MNIST. See the documentation for tf.nn.conv2d_transpose. We are always "training" in GAN mode.

- Fully connected with output size 1024
- ReLU
- BatchNorm
- Fully connected with output size 7 x 7 x 128
- ReLU
- BatchNorm
- Reshape into Image Tensor of shape 7, 7, 128
- Conv2D^T (Transpose): 64 filters of 4x4, stride 2, 'same' padding (use padding=1)
- ReLU
- BatchNorm
- Conv2D^T (Transpose): 1 filter of 4x4, stride 2, 'same' padding (use padding=1)
- TanH
- Should have a 28x28x1 image, reshape back into 784 vector

Implement build_dc_generator in cs231n/gan_pytorch.py

```
In [27]: from cs231n.gan_pytorch import build_dc_generator
    test_g_gan = build_dc_generator().type(dtype)
    test_g_gan.apply(initialize_weights)
    fake_seed = torch.randn(batch_size, NOISE_DIM).type(dtype)
    fake_images = test_g_gan.forward(fake_seed)
    fake_images.size()

Out[27]: torch.Size([128, 784])
```

Check the number of parameters in your generator as a sanity check:

```
In [28]: def test_dc_generator(true_count=6580801):
    model = build_dc_generator(4)
    cur_count = count_params(model)
    if cur_count != true_count:
        print('Incorrect number of parameters in generator. Check your achitecture.')
    else:
        print('Correct number of parameters in generator.')

test_dc_generator()
```

Correct number of parameters in generator.

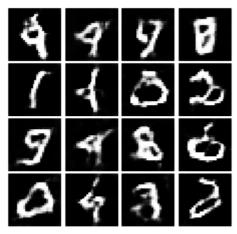
Run the cell below to show generated images.

```
In [30]: numIter = 0
    for img in images:
        print("Iter: {}". format(numIter))
        show_images(img)
        plt. show()
        numIter += 250
        print()
```

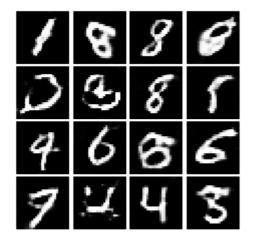
Iter: 0



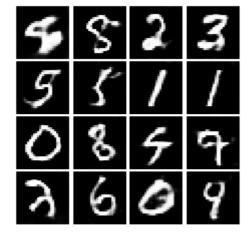
Iter: 250



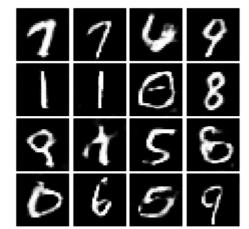
Iter: 500



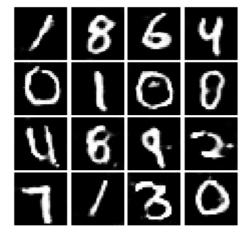
Iter: 750



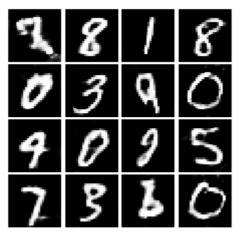
Iter: 1000



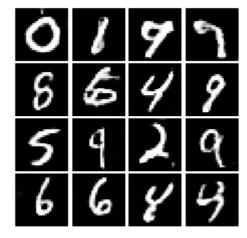
Iter: 1250



Iter: 1500



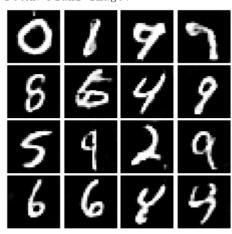
Iter: 1750



Please tag the cell below on Gradescope while submitting.

```
In [31]: print("DCGAN Fianl image:")
    show_images(images[-1])
    plt. show()
```

DCGAN Fianl image:



INLINE QUESTION 1

We will look at an example to see why alternating minimization of the same objective (like in a GAN) can be tricky business.

Consider f(x,y)=xy. What does $\min_x \max_y f(x,y)$ evaluate to? (Hint: minmax tries to minimize the maximum value achievable.)

Now try to evaluate this function numerically for 6 steps, starting at the point (1,1), by using alternating gradient (first updating y, then updating x using that updated y) with step size 1. Here step size is the learning_rate, and steps will be learning_rate * gradient. You'll find that writing out the update step in terms of $x_t, y_t, x_{t+1}, y_{t+1}$ will be useful.

Breifly explain what $\min_x \max_y f(x, y)$ evaluates to and record the six pairs of explicit values for (x_t, y_t) in the table below.

Your answer:

y_0	y_1	y_2	y_3	y_4	y_5	y_6	
1	2	1	-1	-2	-1	1	
x_0	x_1	x_2	x_3	x_4	x_5	x_6	
1	-1	-2	-1	1	2	1	

INLINE QUESTION 2

Using this method, will we ever reach the optimal value? Why or why not?

Your answer:

NO, we will never reach the optimal value. From question 1, we can easily find the values of two are oscillating.

INLINE QUESTION 3

If the generator loss decreases during training while the discriminator loss stays at a constant high value from the start, is this a good sign? Why or why not? A qualitative answer is sufficient.

Your answer:

Usually not a good sign. Constantly high discriminator loss suggests that the discriminator is not learning effectively and is likely unable to differentiate between real and generated data. This means that maybe the discriminator is not complex enough or the training settings are not suitable for the discriminator. Decreasing generator loss in this context might indicate that the generator is optimizing against a poorly performing discriminator, rather than genuinely improving the quality of the generated data. The generator might be exploiting the discriminator's weaknesses without producing realistic outputs. Therefore, all these signals are not good signs.