

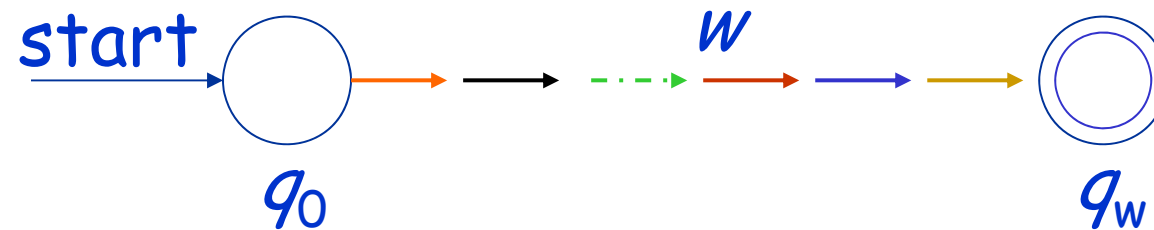
# Nondeterministic Finite Automata(NFA)

1. Definition
2. Notation
3. Construction
4. Language accepted by a NFA
5. Equivalence with DFA

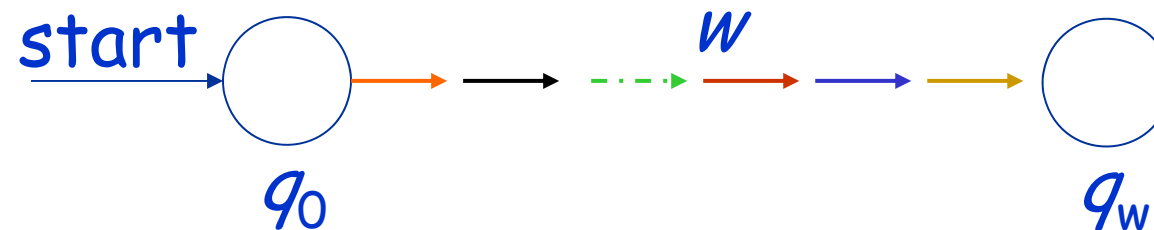
Example 3.1 Construct a DFA to accept

$$L_{x01} = \{x01 \mid x \text{ is any strings of 0's and 1's}\}$$

If  $w \in L_{x01}$ , then



If  $w \notin L_{x01}$ , then

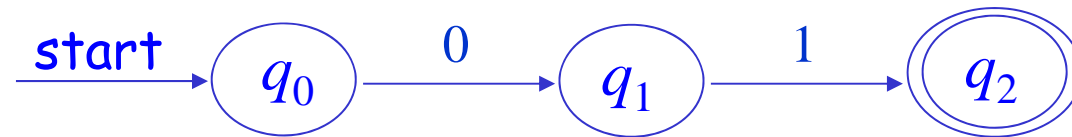


**Example 3.1** Construct a DFA to accept

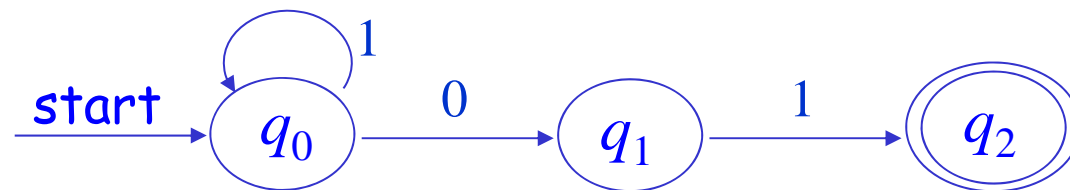
$$L_{x01} = \{x01 \mid x \text{ is any strings of 0's and 1's}\}$$

We start from the most simple string

For  $w=01$ ,



For  $w=1^n01$ ,  
(  $n \geq 0$  )

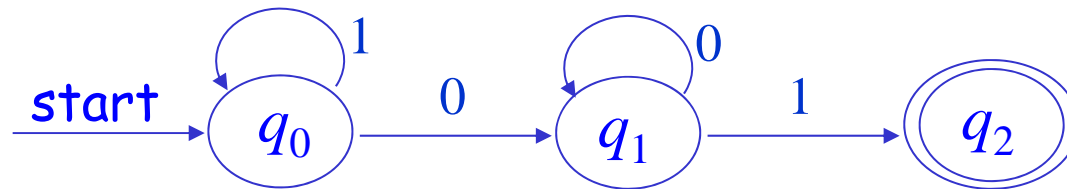


**Example 3.1** Construct a DFA to accept

$$L_{x01} = \{x01 \mid x \text{ is any strings of 0's and 1's}\}$$

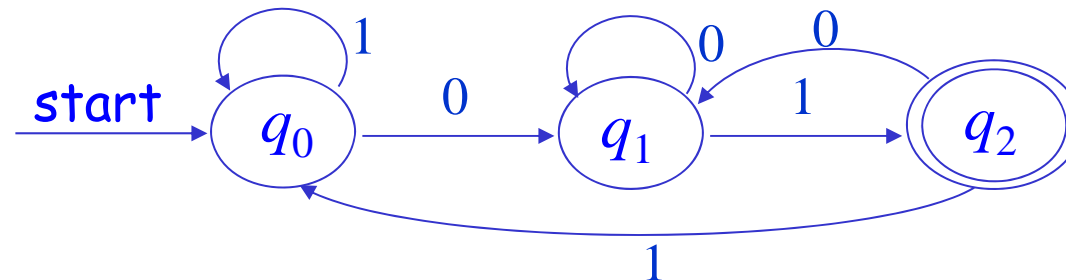
Then to more complex strings

For  $w=1^n00^n1$ ,  
( $n \geq 0$ )



Finally to the most complex strings

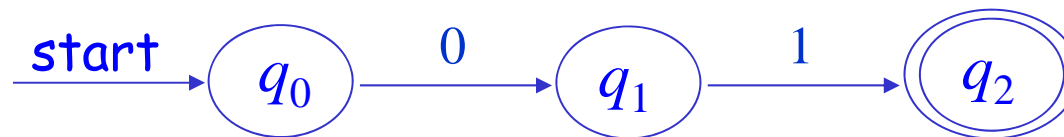
For  $w=x01$ ,



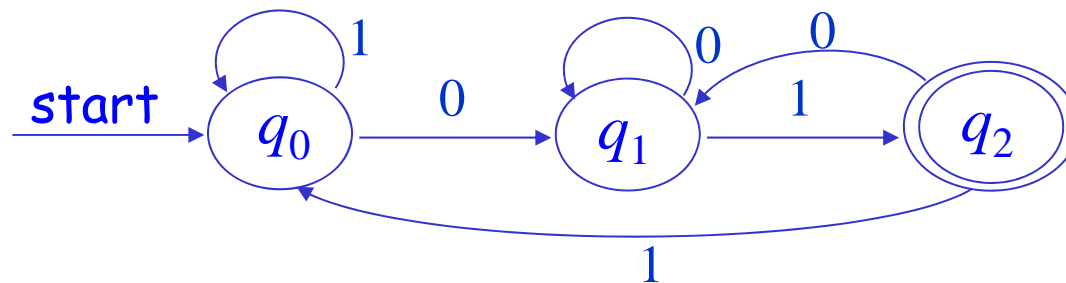
**Example 3.1** Construct a DFA to accept

$$L_{x01} = \{x01 \mid x \text{ is any strings of 0's and 1's}\}$$

Let us look at the most simple

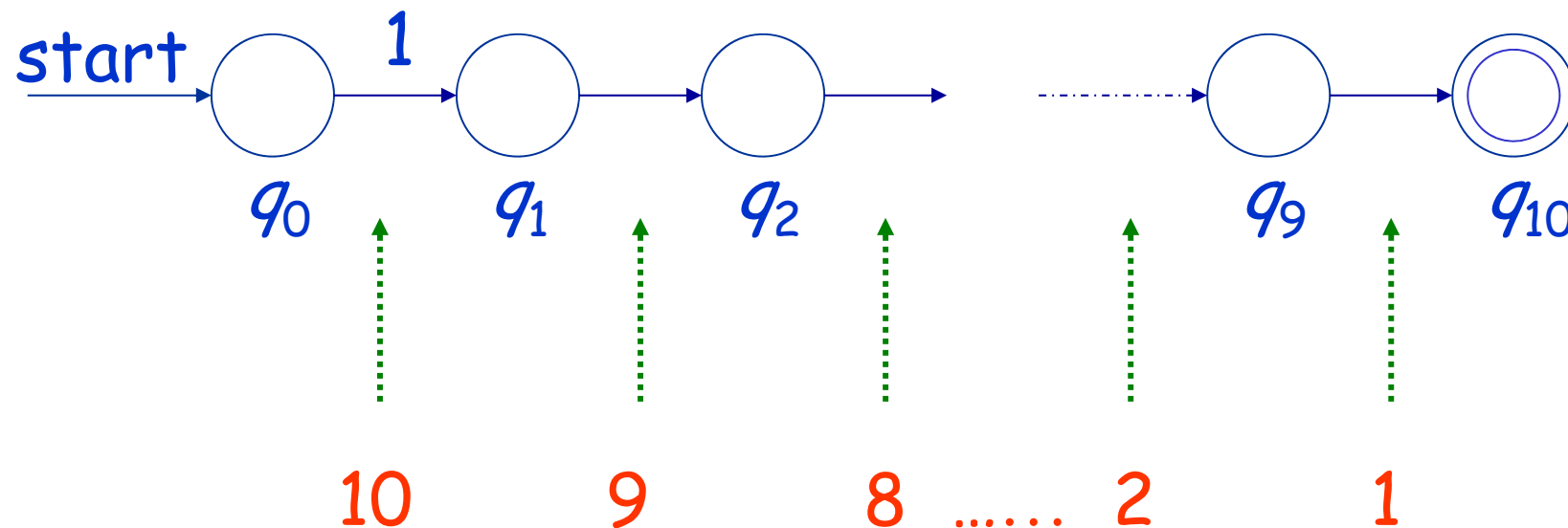


and most complex



## Case for which DFA not suitable

$L = \{w \mid w \text{ consists of 0's and 1's, and the tenth symbol from the right end is 1} \}$



## Formal Definition of NFA

Nondeterministic finite automaton is a five-tuple ,

such as  $M = (Q, \Sigma, \delta, q_0, F)$

Where  $Q$  is a finite set of *states* ,

$\Sigma$  is a finite set of *input symbols* ,

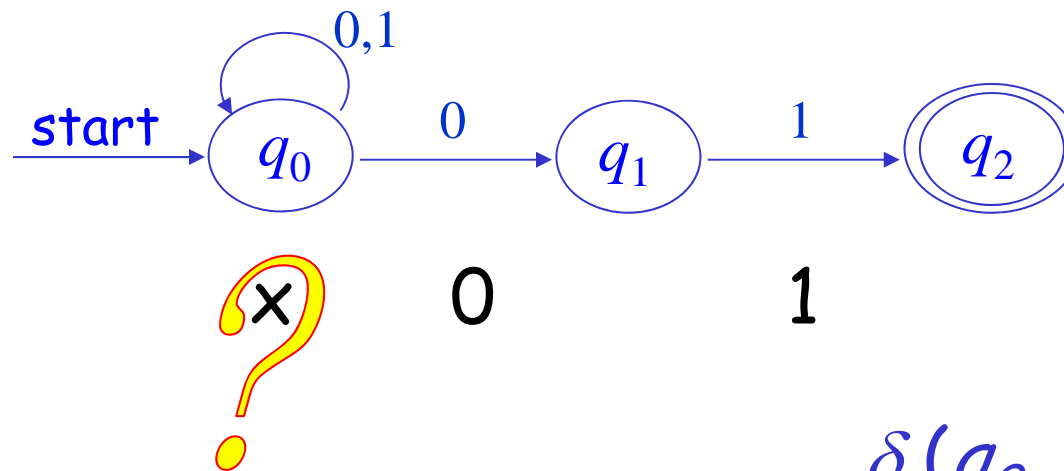
$q_0$  is *start state* ,

$F$  is *a set of final state* ,

$\delta$  is *transition function* , which is a mapping  
from  $Q \times \Sigma$  to  $2^Q$  .

## Example 3.2 Construct an NFA to accept

$$L_{x01} = \{x01 \mid x \text{ is any strings of 0's and 1's}\}$$



$$\delta(q_0, 0) = \{q_0, q_1\}$$

Note  $\delta : Q \times \Sigma \Rightarrow 2^Q$

That  $\delta(q, a) = \{q_1, q_2, \dots, q_n\}$



**Example 3.2** Construct an NFA to accept

$$L_{x01} = \{x01 \mid x \text{ is any strings of 0's and 1's}\}$$

$$N = (\{q_0, q_1, q_2\}, \{0, 1\}, \delta, q_0, \{q_2\})$$

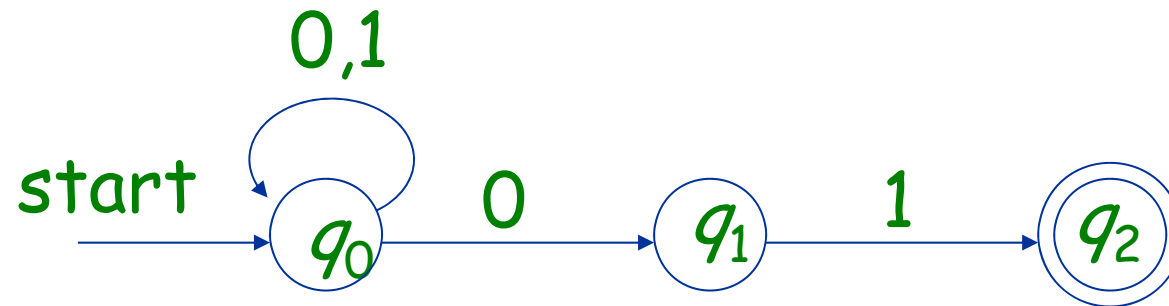
$\delta$  :

$$\delta(q_0, 0) = \{q_0, q_1\}, \quad \delta(q_0, 1) = \{q_1\},$$

$$\delta(q_1, 1) = \{q_2\}$$

# Diagram and Table Notation

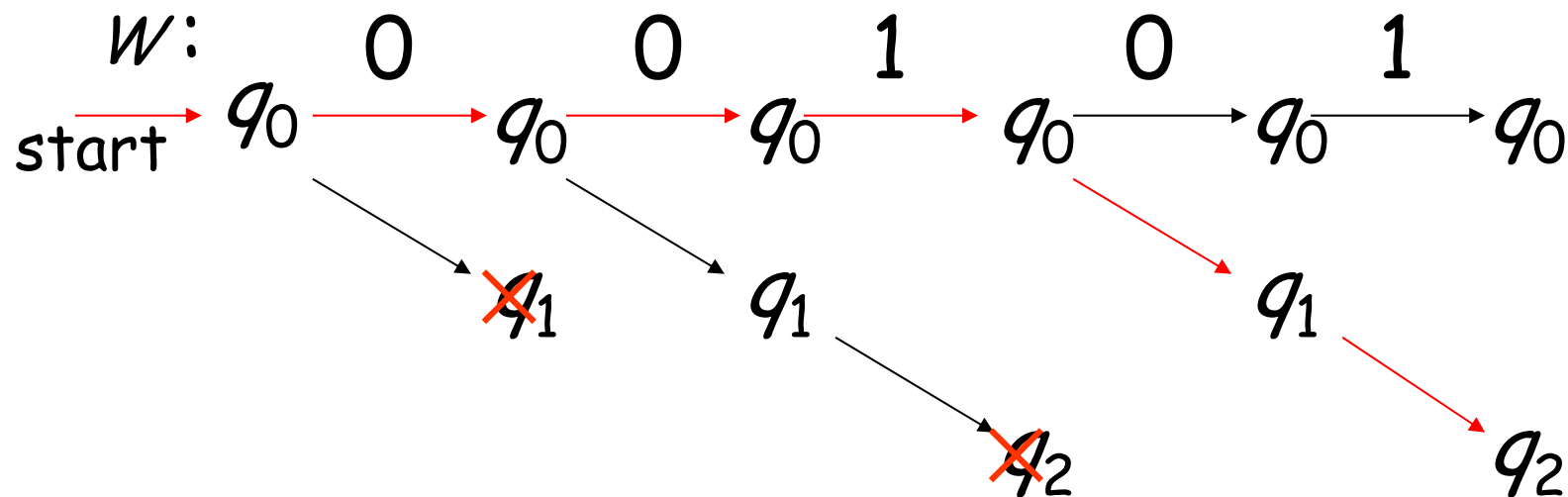
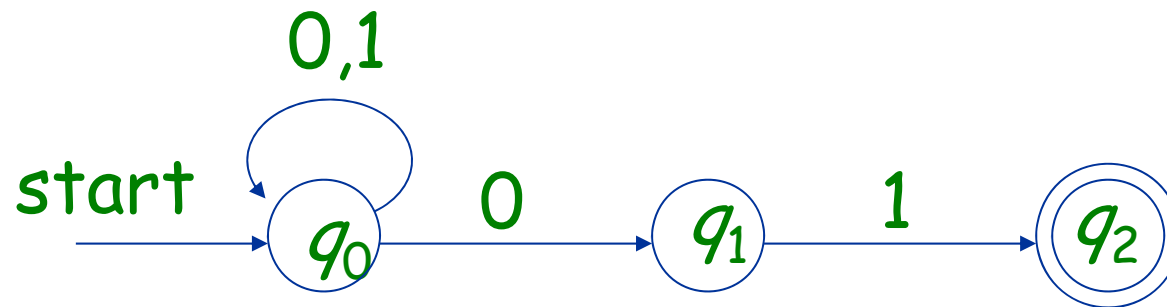
## Diagram



## Table

	0	1
→ $q_0$	$\{q_0, q_1\}$	$\{q_1\}$
$q_1$	$\{\}$	$\{q_2\}$
* $q_2$	$\{\}$	$\{\}$

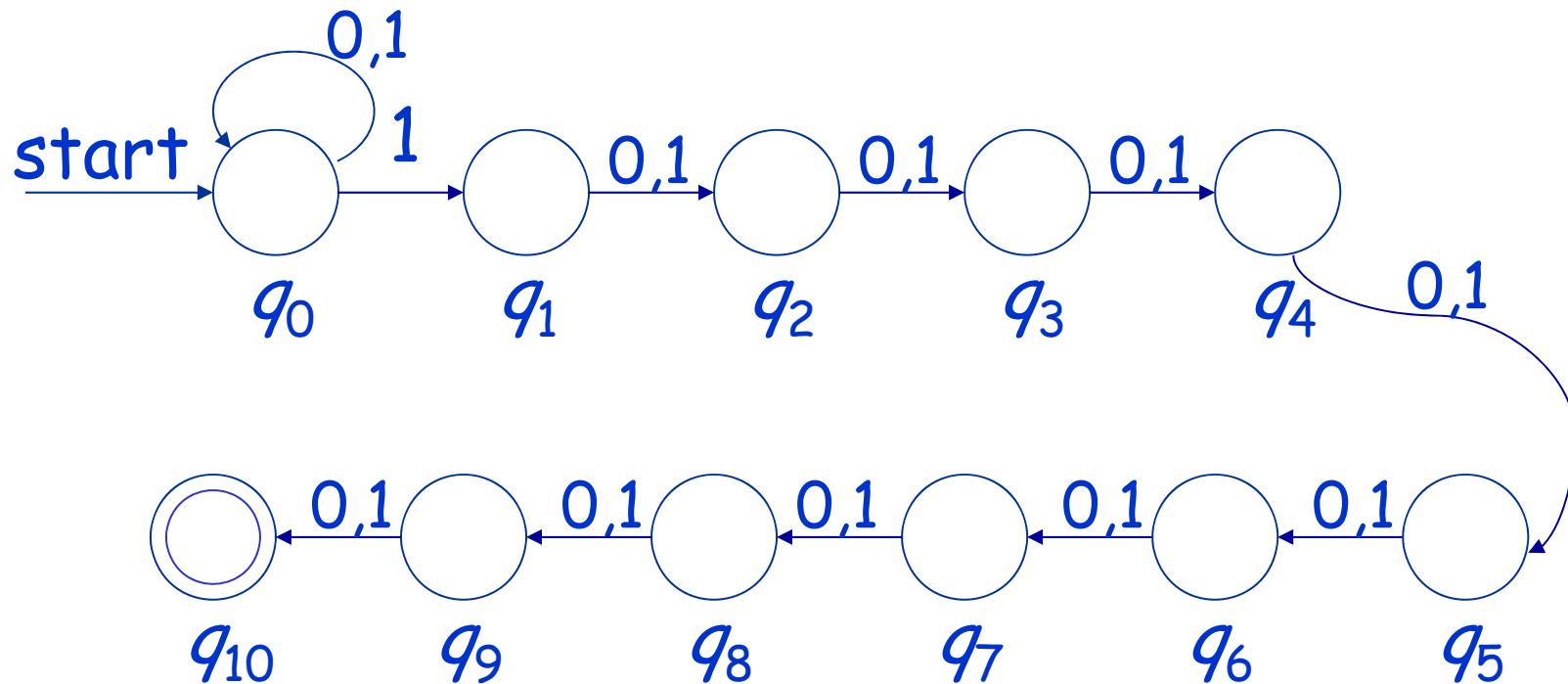
## Description



*There is a path, labeled with a sequence of symbols one by one, from start state to final state.*

### Example 3.3 Construct an NFA to accept

$L = \{w \mid w \text{ consists of 0's and 1's, and the tenth symbol from the right end is 1} \}$



# Extending transition function to string

## BASIS

$$\hat{\delta}(q, \varepsilon) = q.$$

## INDUCTION

Suppose  $w = xa$ ,  $\hat{\delta}(q, x) = \{p_1, p_2, \dots, p_k\}$

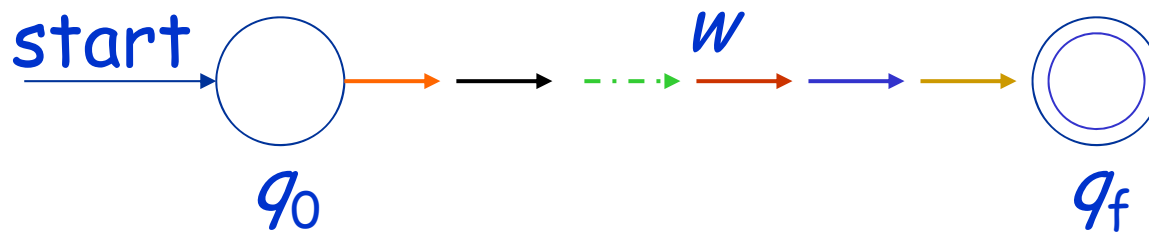
Let  $\bigcup_{i=1}^k \delta(p_i, a) = \{r_1, r_2, \dots, r_m\}$

Then  $\hat{\delta}(q, w) = \{r_1, r_2, \dots, r_m\}$

# The language of NFA

*Definition* The language of an NFA  $A$  is denoted  $L(A)$ , and defined by

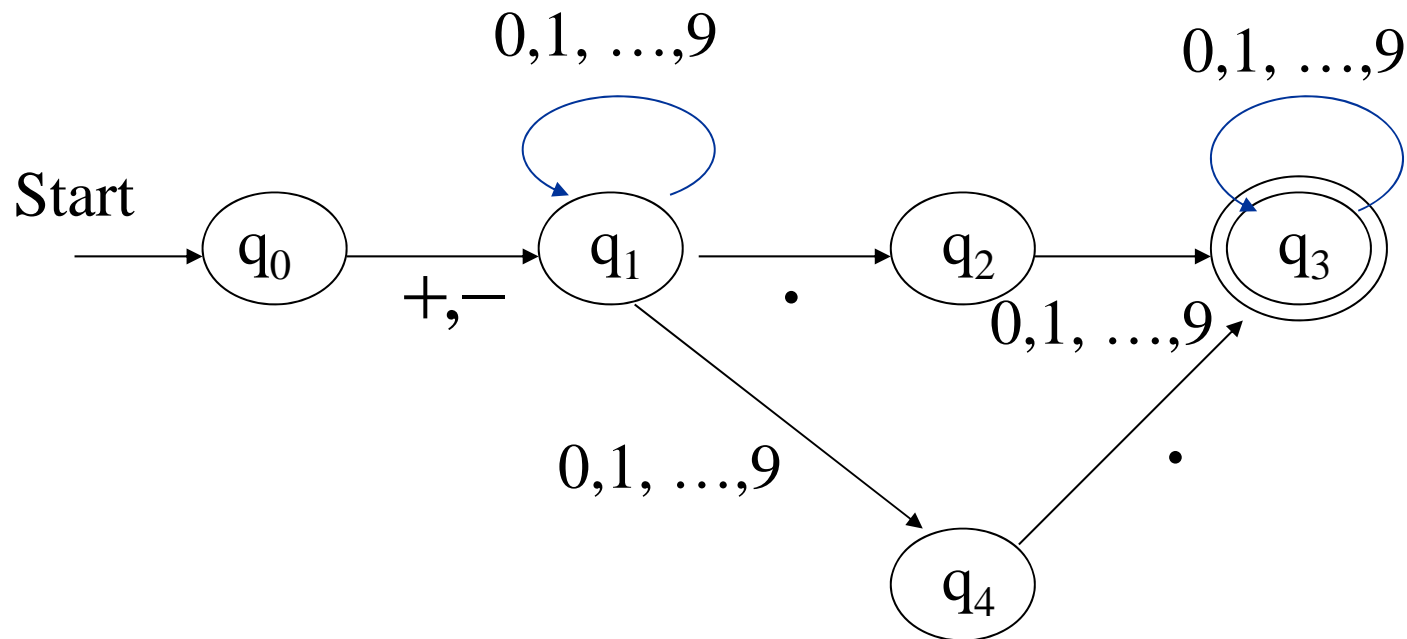
$$L(A) = \{w \mid \hat{\delta}(q_0, w) \cap F \neq \emptyset\}$$



*There is at least a path, labeled with  $w$ , from start state to final state.*

## An Exercise

Describe the language accepted by this NFA :



What about the NFA just accept the float numbers ?

Good good study  
day day up!