Parsers

Monday, September 8, 14

Agenda

- How do we define a language?
 - How do we define the set of strings that are grammatically correct
 - Context free grammars
- How do we recognize strings in the language?
 - How can we tell (easily) whether a program is a valid string in the language
 - How can we determine the structure of a program?
 - LL parsers and LR parsers

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Languages

- Key problem: programming language syntax is recursive
 - If statements can be nested inside while loops which can themselves be nested inside if statements which can be nested inside for loops which can be nested inside switch statements ...
- Nesting can be arbitrarily deep
- New formalism for specifying these kinds of recursive languages: Context-free Grammars

What is a parser

- A parser has two jobs:
 - I) Determine whether a string (program) is *valid* (think: grammatically correct)
 - 2) Determine the structure of a program (think: diagramming a sentence)

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Languages

- A language is a (possibly infinite) set of strings
- Regular expressions describe regular languages
 - Fundamental drawback: can only use finite state to recognize whether a string is in the language
 - Consider this valid piece of C code:
 - {{{int x;}}}
 - Need to make sure that there are the same number of '{' as '}'
 - How would you write a regular expression to capture that?

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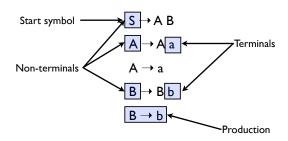
Terminology

- Grammar G = (V_t, V_n, S, P)
 - V_t is the set of terminals
 - V_n is the set of non-terminals
 - S is the start symbol
 - P is the set of productions
 - Each production takes the form: $V_n \rightarrow \lambda \mid (V_n \mid V_t) +$
 - Grammar is context-free (why?)
- A simple grammar:

 $G = (\{a,b\},\{S,A,B\},\{S \rightarrow A \ B,A \rightarrow A \ a,A \rightarrow a,B \rightarrow B \ b,B \rightarrow b\},\\ S)$

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Simple grammar



Backus Naur Form (BNF)

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Generating strings

$$S \rightarrow A B$$

 $A \rightarrow A a$

 $A \rightarrow a$

 $B \rightarrow B b$

 $B \rightarrow b$

 Given a start rule, productions tell us how to rewrite a non-terminal into a different set of symbols

Some productions may rewrite to λ.
 That just removes the non-terminal

To derive the string "a a b b b" we can do the following rewrites:

$$S \Rightarrow A B \Rightarrow A a B \Rightarrow a a B \Rightarrow a a B b \Rightarrow$$

$$a a B b b \Rightarrow a a b b b$$

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Terminology

- Strings are composed of symbols
 - AAaaBbbAais a string
 - We will use Greek letters to represent strings composed of both terminals and non-terminals
- ullet L(G) is the language produced by the grammar G
 - All strings consisting of only terminals that can be produced by G
 - In our example, L(G) = a+b+
 - The language of a context-free grammar is a context-free language
 - All regular languages are context-free, but not vice versa

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Why is this useful?

```
statement → statement; statement

statement → if_stmt;

statement → while_loop;

statement → id = lit;

statement → id = id + id;

if_stmt → if (cond_expr) then statement

while_loop → while (cond_expr) statement

cond_expr → id < lit
```

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Programming language syntax

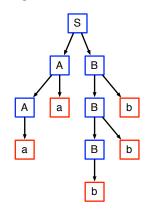
- Programming language syntax is defined with CFGs
- Constructs in language become non-terminals
 - May use auxiliary non-terminals to make it easier to define constructs

```
if_stmt \rightarrow if ( cond_expr ) then statement else_part else_part \rightarrow else statement else_part \rightarrow \lambda
```

• Tokens in language become terminals

Parse trees

- Tree which shows how a string was produced by a language
 - Interior nodes of tree: nonterminals
 - Children: the terminals and non-terminals generated by applying a production rule
 - Leaf nodes: terminals



Leftmost derivation

- Rewriting of a given string starts with the leftmost symbol
- Exercise: do a leftmost derivation of the input program

$$F(V + V)$$

using the following grammar:

E	\rightarrow	Prefix (E)
E	\rightarrow	V Tail
Prefix	→	F
Prefix	→	λ
Tail	→	+ E
Tail	→	λ

What does the parse tree look like?

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Rightmost derivation

- Rewrite using the rightmost non-terminal, instead of the left
- What is the rightmost derivation of this string?

$$F(V + V)$$

E	\rightarrow	Prefix (E)
E	\rightarrow	V Tail
Prefix	→	F
Prefix	→	λ
Tail	→	+ E
Tail	→	λ

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Simple conversions









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Top-down vs. Bottom-up parsers

- Top-down parsers expand the parse tree in pre-order
 - Identify parent nodes before the children
- Bottom-up parsers expand the parse tree in post-order
 - Identify children before the parents
- Notation:
 - LL(I):Top-down derivation with I symbol lookahead
 - LL(k):Top-down derivation with k symbols lookahead
 - LR(I): Bottom-up derivation with I symbol lookahead

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What is parsing

- Parsing is recognizing members in a language specified/ defined/generated by a grammar
- When a construct (corresponding to a production in a grammar) is recognized, a typical parser will take some action
 - In a compiler, this action generates an intermediate representation of the program construct
 - In an interpreter, this action might be to perform the action specified by the construct. Thus, if a+b is recognized, the value of a and b would be added and placed in a temporary variable

Top-down parsing

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Top-down parsing

- Idea: we know sentence has to start with initial symbol
- Build up partial derivations by predicting what rules are used to expand non-terminals
 - Often called predictive parsers
- If partial derivation has terminal characters, match them from the input stream

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A simple example

 $S \rightarrow A B c$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$

• A sentence in the grammar:

 $B \rightarrow \lambda$ x a c c \$

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A simple example

 $S \rightarrow A B c$

A→xaA

special "end of input" symbol

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$

• A sentence in the grammar:

 $B \to \lambda$

хасс\$

A simple example

 $S \rightarrow A B c$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$ • A sentence in the grammar:

 $B \rightarrow \lambda$ x a c c \$

Current derivation: S

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A simple example

 $S \rightarrow A B c$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$ • A sentence in the grammar:

 $B \rightarrow \lambda$ xacc\$

Current derivation: A B c \$

Predict rule

A simple example

 $S \rightarrow A B c$ \$

Choose based on first set of rules

 $A \rightarrow x a A$ $A \rightarrow y a A$ $A \rightarrow c$

 $B \rightarrow b$

• A sentence in the grammar:

 $B \rightarrow \lambda$

хасс\$

Current derivation: x a A B c \$

Predict rule based on next token

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A simple example

 $S \rightarrow A B c$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$ • A sentence in the grammar:

 $B \rightarrow \lambda$ xacc\$

Current derivation: x a A B c \$

Match token

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A simple example

 $S \rightarrow A B c$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$ • A sentence in the grammar:

 $B \rightarrow \lambda$ xacc\$

Current derivation: xaABc\$

Match token

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A simple example

 $S \rightarrow A B c$ \$

Choose based on first set of rules



 $B \rightarrow b$

• A sentence in the grammar:

 $B \rightarrow \lambda$

xacc\$

Current derivation: x a c B c \$

Predict rule based on next token

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A simple example

 $S \rightarrow A B c$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$ • A sentence in the grammar:

 $B \rightarrow \lambda$ хасс\$

Current derivation: x a c B c \$

Match token

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A simple example

 $S \rightarrow A B c$ \$

 $A \rightarrow x a A$

Choose based on follow set

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$ • A sentence in the grammar: $B \rightarrow \lambda$ хасс\$

Current derivation: $x = c \lambda c$

Predict rule based on next token

A simple example

 $S \rightarrow A B c$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$ • A sentence in the grammar:

 $B \rightarrow \lambda$ xacc\$

Current derivation: x a c c \$

Match token

A simple example

 $S \rightarrow A B c$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow c$

 $B \rightarrow b$ • A sentence in the grammar:

 $B \rightarrow \lambda$ xacc\$

Current derivation: x a c c \$

Match token

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First and follow sets

 First(α): the set of terminals (and/or λ) that begin all strings that can be derived from α

• First(A) = $\{x, y, \lambda\}$

 $S \rightarrow A B$ \$

• First(xaA) = $\{x\}$

 $A \rightarrow x a A$

• First (AB) = {x, y, b}

 $A \rightarrow y a A$ $A \rightarrow \lambda$

 Follow(A): the set of terminals (and/ or \$, but no λs) that can appear immediately after A in some partial derivation

В → Ь

derivation

Follow(A) = {b}

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First and follow sets

- First(α) = { $a \in V_t \mid \alpha \Rightarrow^* a\beta$ } \cup { $\lambda \mid \text{if } \alpha \Rightarrow^* \lambda$ }
- Follow(A) = $\{a \in V_t \mid S \Rightarrow^+ ... Aa ...\} \cup \{\$ \mid \text{if } S \Rightarrow^+ ... A \$\}$

S: start symbol

a: a terminal symbol

A: a non-terminal symbol

 α,β : a string composed of terminals and non-terminals (typically, α is the

RHS of a production

derived in 1 step

*: derived in 0 or more steps

⇒+: derived in I or more steps

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Computing first sets

- Terminal: First(a) = {a}
- Non-terminal: First(A)
 - Look at all productions for A

$$A \to X_1 X_2 ... X_k$$

- First(A) \supseteq (First(X₁) λ)
- If $\lambda \in First(X_1)$, $First(A) \supseteq (First(X_2) \lambda)$
- If λ is in First(X_i) for all i, then $\lambda \in First(A)$
- Computing First(α): similar procedure to computing First(A)

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Exercise

 What are the first sets for all the non-terminals in following grammar:

S → A B \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow \lambda$

B → b

 $B \rightarrow A$

Computing follow sets

- Follow(S) = {}
- To compute Follow(A):
 - Find productions which have A on rhs. Three rules:
 - 1. $X \rightarrow \alpha A \beta$: Follow(A) \supseteq (First(β) λ)
 - 2. $X \rightarrow \alpha A \beta$: If $\lambda \in First(\beta)$, Follow(A) \supseteq Follow(X)
 - 3. $X \rightarrow \alpha A$: Follow(A) \supseteq Follow(X)
- Note: Follow(X) never has λ in it.

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Exercise

• What are the follow sets for

 $S \rightarrow A B$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow \lambda$

 $B \rightarrow b$

 $B \rightarrow A$

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Towards parser generators

- Key problem: as we read the source program, we need to decide what productions to use
- Step I: find the tokens that can tell which production P (of the form A $\to X_1 X_2 \dots X_m$) applies

Predict(P) =

$$\left\{ \begin{array}{ll} \operatorname{First}(X_1 \dots X_m) & \text{if } \lambda \not \in \operatorname{First}(X_1 \dots X_m) \\ (\operatorname{First}(X_1 \dots X_m) - \lambda) \cup \operatorname{Follow}(A) & \text{otherwise} \end{array} \right.$$

 If next token is in Predict(P), then we should choose this production

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Parse tables

- Step 2: build a parse table
 - Given some non-terminal V_n (the non-terminal we are currently processing) and a terminal V_t (the lookahead symbol), the parse table tells us which production P to use (or that we have an error
 - More formally:

 $T:V_n \times V_t \rightarrow P \cup \{Error\}$

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Building the parse table

• Start:T[A][t] = //initialize all fields to "error"

foreach A:

foreach P with A on its lhs:

foreach t in Predict(P):

 $1.S \rightarrow AB \$$ $2.A \rightarrow x aA$

T[A][t] = P

3. A → y a A

• Exercise: build parse table for our toy grammar

4. A → λ

5.B → b

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Stack-based parser for LL(I)

- Given the parse table, a stack-based algorithm is much simpler to generate than a recursive descent parser
- Basic algorithm:
 - 1. Push the RHS of a production onto the stack
 - 2. Pop a symbol, if it is a terminal, match it
 - 3. If it is a non-terminal, take its production according to the parse table and go to $\mbox{\it I}$
- Note: always start with start state

An example

1. $S \rightarrow A B \$$ 2. $A \rightarrow x a A$ 3. $A \rightarrow y a A$

• How would a stack-based parser parse:

xayab

4. A → λ5. B → b

Parse stack	Remaining input	Parser action
S	xayab\$	predict I
AB\$	xayab\$	predict 2
xaAB\$	xayab\$	match(x)
a A B \$	ayab\$	match(a)
AB\$	y a b \$	predict 3
y a A B \$	y a b \$	match(y)
a A B \$	a b \$	match(a)
AB\$	b \$	predict 4
В\$	b \$	predict 5
b \$	b \$	match(b)
\$	\$	Done!

Dealing with semantic actions

- When a construct (corresponding to a production in a grammar) is recognized, a typical parser will invoke a semantic action
 - In a compiler, this action generates an intermediate representation of the program construct
 - In an interpreter, this action might be to perform the action specified by the construct. Thus, if a+b is recognized, the value of a and b would be added and placed in a temporary variable

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Dealing with semantic actions

- We can annotate a grammar with action symbols
 - Tell the parser to invoke a semantic action routine
- Can simply push action symbols onto stack as well
- When popped, the semantic action routine is called
 - Routine manipulates semantic records on a stack
 - Can generate new records (e.g., to store variable info)
 - Can generate code using existing records
- Example: semantic actions for x = a + 3

statement ::= ID = expr #assign expr ::= term + term #addop term ::= ID | LITERAL

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Non-LL(I) grammars

- Not all grammars are LL(I)!
- Consider

<stmt> → if <expr> then <stmt list> endif

<stmt> → if <expr> then <stmt list> else <stmt list> endif

- This is not LL(I) (why?)
- We can turn this in to

<stmt $> \rightarrow$ if <expr> then <stmt list> <if suffix>

<if suffix> → endif

<if suffix> → else <stmt list> endif

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Left recursion

- Left recursion is a problem for LL(I) parsers
 - LHS is also the first symbol of the RHS
- Consider:

 $E \rightarrow E + T$

• What would happen with the stack-based algorithm?

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Removing left recursion



LL(k) parsers

- Can look ahead more than one symbol at a time
 - k-symbol lookahead requires extending first and follow sets
 - 2-symbol lookahead can distinguish between more rules:

 $A \rightarrow ax \mid ay$

- More lookahead leads to more powerful parsers
- What are the downsides?

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Are all grammars LL(k)?

• No! Consider the following grammar:

 $S \rightarrow E$ $E \rightarrow (E + E)$ $E \rightarrow (E - E)$ $E \rightarrow x$

- When parsing E, how do we know whether to use rule 2 or 3?
 - Potentially unbounded number of characters before the distinguishing '+' or '-' is found
 - No amount of lookahead will help!

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In real languages?

- Consider the if-then-else problem
- if x then y else z
- Problem: else is optional
- if a then if b then c else d
 - Which if does the else belong to?
- This is analogous to a "bracket language": $[i]^j$ ($i \ge j$)

$$\begin{array}{lll} S & \rightarrow [S C \\ S & \rightarrow \lambda & & [[] can be parsed: SS\C or SSC\Lambda \\ C & \rightarrow] & & (it's ambiguous!) \\ C & \rightarrow \lambda & & & \end{array}$$

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Solving the if-then-else problem

- The ambiguity exists at the language level. To fix, we need to define the semantics properly
 - "] matches nearest unmatched ["
 - This is the rule C uses for if-then-else
 - What if we try this?

 $S \rightarrow [S \\ S \rightarrow SI \\ SI \rightarrow [SI]$

This grammar is still not LL(I) (or LL(k) for any k!)

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Two possible fixes

- If there is an ambiguity, prioritize one production over another
 - e.g., if C is on the stack, always match "]" before matching "\"

$$S \rightarrow [SC]$$

 $S \rightarrow \lambda$
 $C \rightarrow J$
 $C \rightarrow \lambda$

- Another option: change the language!
 - e.g., all if-statements need to be closed with an endif

 $S \rightarrow \text{if } S E$ $S \rightarrow \text{other}$ $E \rightarrow \text{else } S \text{ endif}$ $E \rightarrow \text{endif}$

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Parsing if-then-else

- What if we don't want to change the language?
 - C does not require { } to delimit single-statement blocks
- To parse if-then-else, we need to be able to look ahead at the entire rhs of a production before deciding which production to use
 - In other words, we need to determine how many "]" to match before we start matching "["s
- LR parsers can do this!

LR Parsers

- Parser which does a Left-to-right, Right-most derivation
 - Rather than parse top-down, like LL parsers do, parse bottom-up, starting from leaves
- Basic idea: put tokens on a stack until an entire production is found
- Issues:
- Recognizing the endpoint of a production
- Finding the length of a production (RHS)
- Finding the corresponding nonterminal (the LHS of the production)

LR Parsers

- Basic idea:
 - **shift** tokens onto the stack.At any step, keep the set of productions that could generate the read-in tokens
 - reduce the RHS of recognized productions to the corresponding non-terminal on the LHS of the production. Replace the RHS tokens on the stack with the LHS non-terminal.

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Data structures

- At each state, given the next token,
 - A goto table defines the successor state
 - An action table defines whether to
 - shift put the next state and token on the stack
 - reduce an RHS is found; process the production
 - terminate parsing is complete

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Simple example

- I. $P \rightarrow S$
- 2. $S \rightarrow x; S$
- 3. $S \rightarrow e$

		Symbol					
		х	;	e	Р	S	Action
	0	_		3		5	Shift
			2				Shift
State	2	- 1		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

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Parsing using an LR(0) parser

- Basic idea: parser keeps track, simultaneously, of all possible productions that could be matched given what it's seen so far.
 When it sees a full production, match it.
- Maintain a parse stack that tells you what state you're in
 - Start in state 0
- In each state, look up in action table whether to:
 - shift: consume a token off the input; look for next state in goto table; push next state onto stack
 - reduce: match a production; pop off as many symbols from state stack as seen in production; look up where to go according to non-terminal we just matched; push next state onto stack
 - accept: terminate parse

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Example

Parse "x;x;e"

Step	Parse Stack	Remaining Input	Parser Action
1	0	x;x;e	Shift I
2	0 1	; x ; e	Shift 2
3	0 2	x ; e	Shift I
4	0 2	; e	Shift 2
5	0 2 2	e	Shift 3
6	0 2 2 3		Reduce 3 (goto 4)
7	0 2 2 4		Reduce 2 (goto 4)
8	0124		Reduce 2 (goto 5)
9	0.5		Accept

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LR(k) parsers

- LR(0) parsers
 - No lookahead
 - Predict which action to take by looking only at the symbols currently on the stack
- LR(k) parsers
 - Can look ahead k symbols
 - Most powerful class of deterministic bottom-up parsers
 - LR(I) and variants are the most common parsers

Terminology for LR parsers

• Configuration: a production augmented with a "•"

 $A \rightarrow X_1 \dots X_i \cdot X_{i+1} \dots X_i$

- The "•" marks the point to which the production has been recognized. In this case, we have recognized $X_1 \dots X_i$
- Configuration set: all the configurations that can apply at a given point during the parse:

 $A \rightarrow B \cdot CD$

 $A \rightarrow B \cdot GH$

 $T \rightarrow B \cdot Z$

 Idea: every configuration in a configuration set is a production that we could be in the process of matching

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Configuration closure set

- Include all the configurations necessary to recognize the next symbol after the •
- For each configuration in set:
 - If next symbol is terminal, no new configuration added
 - If next symbol is non-terminal X, for each production of the form $X \to \alpha$, add configuration $X \to {}^\bullet\alpha$





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Successor configuration set

• Starting with the initial configuration set

 $s0 = closure0(\{S \rightarrow \bullet \alpha \$\})$

an LR(0) parser will find the successor given the next symbol \boldsymbol{X}

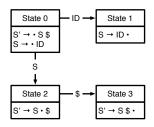
- X can be either a terminal (the next token from the scanner) or a non-terminal (the result of applying a reduction)
- Determining the successor s' = go to0(s, X):
 - For each configuration in s of the form A \rightarrow B X γ add A \rightarrow B X γ to t
 - s' = closure0(t)

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CFSM

- CFSM = Characteristic Finite State Machine
- Nodes are configuration sets (starting from s0)
- Arcs are go_to relationships





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Building the goto table

• We can just read this off from the CFSM

		Symbol			
		D	\$	S	
State	0	- 1		2	
	- 1				
	2		3		
	3				

Building the action table

- Given the configuration set s:
 - We shift if the next token matches a terminal after the in some configuration

• We reduce production P if the • is at the end of a production

 $B \to \alpha \cdot \in s$ where production P is $B \to \alpha$

- Extra actions:
 - shift if goto table transitions between states on a nonterminal
 - accept if we have matched the goal production

Action table

State -	0	Shift			
	ı	Reduce 2			
	2	Shift			
	3	Accept			

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Shift/reduce conflict

Consider the following grammar:

$$S \rightarrow Ay$$

$$A \rightarrow x \mid xx$$

 This leads to the following configuration set (after shifting one "x":

$$A \rightarrow x \cdot x$$

$$\mathsf{A} \to \mathsf{x} \bullet$$

• Can shift or reduce here

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Shift/reduce example (2)

Conflicts in action table

For LR(0) grammars, the action table entries are unique:

Reduce/reduce conflicts: multiple reductions possible

Shift/reduce conflicts: we can either shift or reduce from

from each state, can only shift or reduce But other grammars may have conflicts

from the given configuration

the given configuration

• Consider the following grammar:

$$S \rightarrow Ay$$

$$A \rightarrow \lambda \mid x$$

• This leads to the following initial configuration set:

$$S \rightarrow \bullet A y$$

$$A \rightarrow \cdot x$$

$$A \rightarrow \lambda$$

• Can shift or reduce here

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Lookahead

- Can resolve reduce/reduce conflicts and shift/reduce conflicts by employing lookahead
 - Looking ahead one (or more) tokens allows us to determine whether to shift or reduce
 - (cf how we resolved ambiguity in LL(1) parsers by looking ahead one token)

Semantic actions

- Recall: in LL parsers, we could integrate the semantic actions with the parser
 - Why? Because the parser was predictive
- Why doesn't that work for LR parsers?
 - Don't know which production is matched until parser reduces
- For LR parsers, we put semantic actions at the end of productions
 - May have to rewrite grammar to support all necessary semantic actions

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Parsers with lookahead

- Adding lookahead creates an LR(1) parser
 - Built using similar techniques as LR(0) parsers, but uses lookahead to distinguish states
 - LR(1) machines can be much larger than LR(0) machines, but resolve many shift/reduce and reduce/ reduce conflicts
 - Other types of LR parsers are SLR(I) and LALR(I)
 - Differ in how they resolve ambiguities
 - yacc and bison produce LALR(I) parsers

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LR(I) parsing

 Configurations in LR(I) look similar to LR(0), but they are extended to include a lookahead symbol

$$A \rightarrow X_1 \dots X_i \cdot X_{i+1} \dots X_j$$
, I (where $I \in V_t \cup \lambda$)

 If two configurations differ only in their lookahead component, we combine them

$$A \rightarrow X_1 \dots X_i \cdot X_{i+1} \dots X_j, \{I_1 \dots I_m\}$$

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Building configuration sets

• To close a configuration

$$B \rightarrow \alpha \cdot A \beta, I$$

- Add all configurations of the form A → γ, u where u ∈ First(βI)
- Intuition: the lookahead symbol for any configuration is the terminal we expect to see after the configuration has been matched
 - The parse could apply the production for A, and the lookahead after we apply the production should match the next token that would be produced by B

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Example



closure I ($\{S \rightarrow \bullet E \$, \{\lambda\}\}\) =$				
	S → • E \$, {λ}			
	E → • E + T, {\$}			
	E → • T, {\$}			
	T → • ID, {\$}			
	T → • (E), {\$}			
	E → • E + T, {+}			
	E → • T, {+}			
	T → • ID, {+}			
	T → • (E), {+}			

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Building goto and action tables

- The function gotol (configuration-set, symbol) is analogous to goto0(configuration-set, symbol) for LR(0)
 - Build goto table in the same way as for LR(0)
- Key difference: the action table.

action[s][x] =

• reduce when • is at end of configuration and x ∈ lookahead set of configuration

$$A \, \rightarrow \, \alpha \, \bullet, \{... \, x \, ...\} \in s$$

• shift when • is before x

$$A \to \beta \bullet x \ \gamma \in s$$

Example

• Consider the simple grammar:

oprogram> → begin <stmts> end \$

<stmts> → SimpleStmt; <stmts>

<stmts> → begin <stmts> end ; <stmts>

<stmts> →

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Action and goto tables

	begin	end	;	SimpleStmt	\$	<pre><pre><pre><pre><pre><pre><pre><pre></pre></pre></pre></pre></pre></pre></pre></pre>	<stmts></stmts>
0	S / I						
1	S / 4	R4		S / 5			S / 2
2		\$/3					
3					Α		
4	S / 4	R4		S / 5			S / 7
5			S / 6				
6	S / 4	R4		S / 5			S / 10
7		S / 8					
8			S / 9				
9	\$ / 4	R4		\$ / 6	·		\$/11
10		R2					
П		R3					

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• Parse: begin SimpleStmt; SimpleStmt; end \$

Step	Parse Stack	Remaining Input	Parser Action
I	0	begin S;S;end \$	Shift I
2	0 1	S;S;end\$	Shift 5
3	0 5	; S ; end \$	Shift 6
4	0 5 6	S ; end \$	Shift 5
5	0 5 6 5	; end \$	Shift 6
6	015656	end \$	Reduce 4 (goto 10)
7	0 5 6 5 6 0	end \$	Reduce 2 (goto 10)
8	0 5 6 10	end \$	Reduce 2 (goto 2)
9	0 2	end \$	Shift 3
10	0 2 3	\$	Accept

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Problems with LR(I) parsers

- LR(I) parsers are very powerful ...
 - But the table size is much larger than LR(0) — as much as a factor of $|V_t|$ (why?)
 - Example: Algol 60 (a simple language) includes several thousand states!
- Storage efficient representations of tables are an important issue

Solutions to the size problem

- Different parser schemes
- SLR (simple LR): build an CFSM for a language, then add lookahead wherever necessary (i.e., add lookahead to resolve shift/reduce conflicts)
 - What should the lookahead symbol be?
 - To decide whether to reduce using production $A \rightarrow \alpha$, use Follow(A)
- LALR: merge LR states when they only differ by lookahead symbols

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