

11.25



$$P_{avg} = 40 \text{ kW}$$

$$\text{pf} = 0.7 \text{ lagging}$$

$$\omega = 120\pi$$

find C for $\text{pf} = 0.9$

$$Q_{old} = P \sqrt{\frac{1}{\text{pf}^2} - 1} = 40000 \sqrt{\frac{1}{0.7^2} - 1} = 40808.2 \text{ VAR}$$

$$Q_{new} = 40000 \sqrt{\frac{1}{0.9^2} - 1} = 19372.9 \text{ VAR}$$

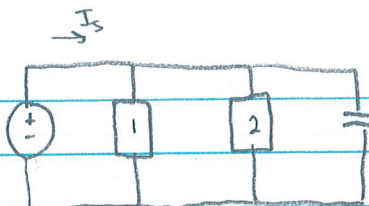
$$Q_{cap} = Q_{new} - Q_{old} = 19372.9 - 40808.2 = -21435.3 \text{ VAR}$$

$$-jQ_c = V_c I_c^* = (j\omega C V_c)^* V_c = -j\omega C |V_c|^2$$

$$Q_c = -\omega C |V_c|^2 = -120\pi C (230\text{V})^2 = -21435.3$$

$$\rightarrow C = 1.07 \text{ mF}$$

11.27



1: 360 W $\text{pf} = .9$

2: 1440 W $\text{pf} = .866$

$V_s = 120\sqrt{2} \angle 0^\circ$

$\omega = 120\pi$

find C for $|I_s| = 16 \text{ A rms}$,

$V_{\text{rms}} = 120\sqrt{2}/\sqrt{2} = 120 \text{ V rms}$

$Q_1 = 360 \sqrt{\frac{1}{.9^2} - 1} = 174.4 \text{ VAR}$

$S_1 = 360 + j174.4$

$Q_2 = 1440 \sqrt{\frac{1}{.866^2} - 1} = 831.5 \text{ VAR}$

$S_2 = 1440 + j831.5$

$\text{pf} = \frac{P_{\text{avg}}}{V_{\text{rms}} I_{\text{rms}}} = \frac{360 + 1440}{(120)(16)} = \boxed{.9375}$

$Q_{\text{old}} = 174.4 + 831.5$

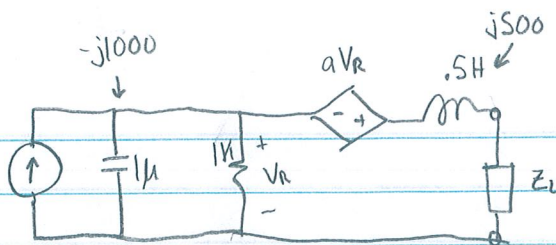
$Q_{\text{new}} = (16)(120) \sqrt{\frac{1}{.9375^2} - 1} = 712.67$

$Q_C = Q_{\text{new}} - Q_{\text{old}} = -293.23$

$Q_C = -\omega C |V_s|^2 = -120\pi C |120\sqrt{2}|^2 = -293.23$

$C = \boxed{27 \mu\text{F}}$

11.32



$$a=3$$

$$I_s = 2 \angle 0 \text{ Arms}$$

$$\omega = 1000$$

find V_{oc} : KCL @ V_R : $-2 + \frac{V_R}{-j1000} + \frac{V_R}{1000} = 0 \rightarrow V_R \left(\frac{1}{1000} + \frac{j}{1000} \right) = 2$

$$V_R = 1000 - j1000$$

$$V_{oc} = V_R + aV_R = 4V_R = \underline{4000 - j4000}$$

find i_{sc} : KCL @ V_R : $-2 + \frac{V_R}{-j1000} + \frac{V_R}{1000} + i_{sc} = 0$

$$i_{sc} = \frac{V_R + aV_R}{j500}$$

$$V_R \left(\frac{1}{-j1000} + \frac{1}{1000} + \frac{4}{j500} \right) = 2 \rightarrow V_R = 40 + j280$$

$$i_{sc} = 4V_R / j500 = 2.24 - j0.32$$

$$Z_{th} = V_{oc} / i_{sc} = 2000 - j1500 \Omega$$

$$Z_L = Z_{th}^* = 2000 + j1500 \Omega$$

$$P_{max} = \frac{V_{rms}^2}{4 R_c(Z_L)} = \frac{4000^2}{4(2000)} = \boxed{2000 \text{ W}}$$