

## Equations

$$\vec{B} = \frac{\mu_o}{4\pi} \frac{q\vec{v} \times \hat{r}}{|\vec{r}|^2}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_o} \frac{q}{|\vec{r}|^2} \hat{r}$$

$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$

$$\Delta V = \frac{\Delta U_{el}}{q}$$

$$q\Delta V = \Delta U_{el}$$

$$\Delta V = - \int_i^f \vec{E} \bullet d\vec{l}$$

$$\Delta V \approx - \sum (E_x \Delta x + E_y \Delta y + E_z \Delta z)$$

$$\oint \vec{E} \bullet \hat{n} dA = \frac{\sum q_{inside}}{\epsilon_o}$$

$$\oint \vec{B} \bullet \hat{n} dA = 0$$

$$\oint \vec{B} \bullet d\vec{l} = \mu_o \left[ \sum I_{inside path} + \epsilon_o \frac{d}{dt} \int \vec{E} \bullet \hat{n} dA \right] \quad |\text{emf}| = \left| \frac{d\Phi_{mag}}{dt} \right|, \quad \Phi_{mag} = \int \vec{B} \bullet \hat{n} dA$$

## Specific Results

Electric field due to uniformly charged spherical shell: outside like point charge; inside zero.

$$|\vec{E}_{rod}| = \frac{1}{4\pi\epsilon_o} \frac{Q}{r\sqrt{r^2 + (L/2)^2}} \quad (r \text{ perpendicular from center})$$

$$|\vec{E}_{rod}| \approx \frac{1}{4\pi\epsilon_o} \frac{2Q/L}{r} \quad (\text{if } r \ll L)$$

$$|\vec{E}_{ring}| = \frac{1}{4\pi\epsilon_o} \frac{qz}{(z^2 + R^2)^{3/2}} \quad (z \text{ along axis})$$

$$|\vec{E}_{disk}| = \frac{Q/A}{2\epsilon_o} \left[ 1 - \frac{z}{(z^2 + R^2)^{1/2}} \right] \quad (z \text{ along axis}); \quad |\vec{E}_{disk}| \approx \frac{Q/A}{2\epsilon_o} \left[ 1 - \frac{z}{R} \right] \approx \frac{Q/A}{2\epsilon_o} \quad (\text{if } z \ll R)$$

$$|\vec{E}_{capacitor}| \approx \frac{Q/A}{\epsilon_o} \quad (+Q \text{ or } -Q \text{ disks}) \quad |\vec{E}_{fringe}| \approx \frac{Q/A}{\epsilon_o} \left( \frac{s}{2R} \right) \text{ just outside capacitor}$$

$$|\vec{E}_{dipole,axis}| \approx \frac{1}{4\pi\epsilon_o} \frac{2qs}{r^3} \quad (\text{along dipole axis, where } r \gg s)$$

$$|\vec{E}_{dipole,perp}| \approx \frac{1}{4\pi\epsilon_o} \frac{qs}{r^3} \quad (\text{along axis perpendicular to dipole axis, where } r \gg s)$$

$$i = nA\bar{v}; \quad I = |q| nA\bar{v}; \quad \bar{v} = uE$$

$$\Delta V = \frac{q}{4\pi\epsilon_o} \left[ \frac{1}{r_f} - \frac{1}{r_i} \right]$$

$$E_{dielectric} = \frac{E_{applied}}{K}$$

$$\text{kinetic energy} \approx \frac{1}{2}mv^2 \text{ if } v \ll c$$

$$\Delta \vec{B} = \frac{\mu_o}{4\pi} \frac{I \Delta \vec{l} \times \vec{r}}{r^2} \quad (\text{short wire})$$

$$\Delta \vec{F} = I \Delta \vec{l} \times \vec{B}$$

$$|\vec{B}_{wire}| = \frac{\mu_o}{4\pi} \frac{LI}{r\sqrt{r^2 + (L/2)^2}} \approx \frac{\mu_o}{4\pi} \frac{2I}{r} \quad (r \ll L)$$

$$|\vec{B}_{loop}| = \frac{\mu_o}{4\pi} \frac{2I\pi R^2}{(z^2 + R^2)^{3/2}} \approx \frac{\mu_o}{4\pi} \frac{2I\pi R^2}{z^3} \quad (\text{on axis, } z \gg R); \quad \mu = IA = I\pi R^2$$

$$|\vec{B}_{dipole,axis}| \approx \frac{\mu_o}{4\pi} \frac{2\mu}{r^3} \quad (\text{along dipole axis, where } r \gg s)$$

$$|\vec{B}_{dipole,perp}| \approx \frac{\mu_o}{4\pi} \frac{\mu}{r^3} \quad (\text{along axis perpendicular to dipole axis, where } r \gg s)$$

$$\vec{E}_{rad} = \frac{1}{4\pi\epsilon_o} \frac{-q\vec{a}_\perp}{c^2 r}; \quad \hat{v} = \hat{E}_{rad} \times \hat{B}_{rad}; \quad |\vec{B}_{rad}| = \frac{|\vec{E}_{rad}|}{c}$$

$$\sigma = |q|nu; \quad J = \frac{I}{A} = \sigma E; \quad R = \frac{L}{\sigma A}$$

$$I = \frac{|\Delta V|}{R} \text{ for an ohmic resistor } (R \text{ independent of } \Delta V); \quad \text{power} = I\Delta V$$

$$Q = C|\Delta V| \qquad \text{circular motion: } \left| \frac{d\vec{p}}{dt} \right|_{\perp} = \frac{|\vec{v}|}{R} |\vec{p}| \approx \frac{mv^2}{R}$$

$$f = \frac{1}{T}$$

$$\omega = \frac{2\pi}{T}$$

$$v = f\lambda$$

Constant	Symbol	Approximate Value
Speed of light	$c$	$3 \times 10^8 \text{ m/s}$
Gravitational constant	$G$	$6.7 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$
Approx. grav field near Earth's surface	$g$	$9.8 \text{ N/kg}$
Electron mass	$m_e$	$9 \times 10^{-31} \text{ kg}$
Proton mass	$m_p$	$1.7 \times 10^{-27} \text{ kg}$
Neutron mass	$m_n$	$1.7 \times 10^{-27} \text{ kg}$
Electric constant	$\frac{1}{4\pi\epsilon_0}$	$9 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$
Electric constant	$\epsilon_0$	$8.85 \times 10^{-12} \text{ N} \cdot \text{m}^2/\text{C}^2$
Magnetic constant	$\frac{\mu_0}{4\pi}$	$1 \times 10^{-7} \text{ T} \cdot \text{m/A}$
Magnetic constant	$\mu_0$	$4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$
Proton charge	$e$	$1.6 \times 10^{-19} \text{ C}$
Electron volt	$1 \text{ eV}$	$1.6 \times 10^{-19} \text{ J}$
Avogadro's number	$N_A$	$6.02 \times 10^{23} \text{ molecules/mole}$
Atomic radius	$R_a$	$1 \times 10^{-10} \text{ m}$
Proton radius	$R_p$	$\approx 1 \times 10^{-15} \text{ m}$
E to ionize air	$E_{\text{ionize}}$	$\approx 3 \times 10^6 \text{ V/m}$
$B_{\text{Earth}}$	$B_{\text{Earth}}$	$\approx 2 \times 10^{-5} \text{ T}$

### Maxwell Equations - Integral Form

$$\oint \vec{B} \cdot \hat{n} dA = 0$$

$$\oint \vec{B} \cdot d\vec{l} = \mu_o \left[ \sum I_{\text{enclosed}} + \epsilon_o \frac{d}{dt} \int \vec{E} \cdot \hat{n} dA \right]$$

$$\oint \vec{E} \cdot \hat{n} dA = \frac{1}{\epsilon_o} \sum Q_{\text{enclosed}}$$

$$\oint \vec{E} \cdot d\vec{l} = -\frac{d}{dt} \int \vec{B} \cdot \hat{n} dA$$

### Maxwell Equations - Differential Form

$$\vec{\nabla} \times \vec{B} = \mu_o \left( \vec{J} + \epsilon_o \frac{\partial \vec{E}}{\partial t} \right)$$

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\vec{\nabla} \cdot \vec{B} = 0$$

$$\vec{\nabla} \cdot \vec{E} = \frac{1}{\epsilon_o} \rho$$