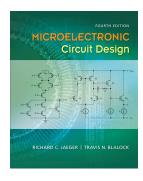
Chapter 1 Introduction to Electronics

Microelectronic Circuit Design

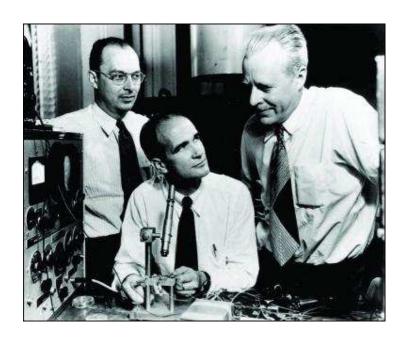
Richard C. Jaeger Travis N. Blalock



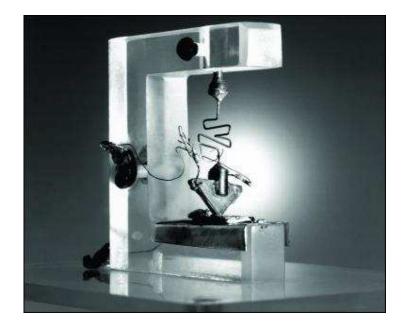
Chapter Goals

- Explore the history of electronics.
- Quantify the impact of integrated circuit technologies.
- Describe classification of electronic signals.
- Review circuit notation and theory.
- Introduce tolerance impacts and analysis.
- Describe problem solving approach

The Start of the Modern Electronics Era



Bardeen, Shockley, and Brattain at Bell Labs - Brattain and Bardeen invented the bipolar transistor in 1947.



The first germanium bipolar transistor. Roughly 50 years later, electronics account for 10% (4 trillion dollars) of the world GDP.

Electronics Milestones

1874	Braun invents the solid-state rectifier.	1958	Integrated circuits developed by Kilby and Noyce
1906	DeForest invents triode vacuum tube.	1961	First commercial IC from Fairchild Semiconductor
1907-1927 First radio circuits developed from		1963	IEEE formed from merger of IRE and AIEE
	diodes and triodes.	1968	First commercial IC opamp
1925	Lilienfeld field-effect device patent filed.	1970	One transistor DRAM cell invented by Dennard at IBM.
1947	Bardeen and Brattain at Bell Laboratories invent bipolar	1971	4004 Intel microprocessor introduced.
	transistors.	1978	First commercial 1-kilobit memory.
1952	Commercial bipolar transistor production at Texas Instruments.	1974	8080 microprocessor introduced.
		1984	Megabit memory chip introduced.
1956	Bardeen, Brattain, and Shockley receive Nobel prize.	2000	Alferov, Kilby, and Kromer share Nobel prize
		2009	Boyle and Smith share Nobel prize

Evolution of Electronic Devices

Vacuum Tubes

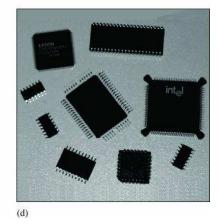


(b)

Discrete Transistors

SSI and MSI
Integrated
Circuits





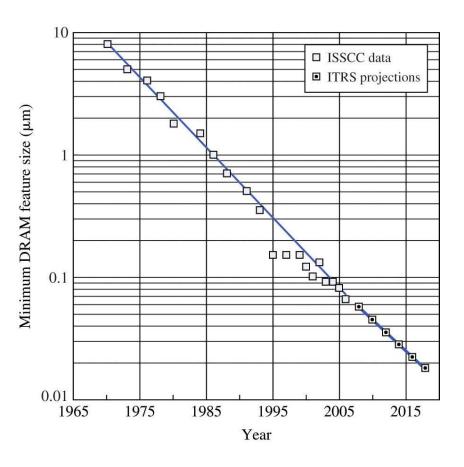
VLSI
Surface-Mount
Circuits

Microelectronics Proliferation

- The integrated circuit was invented in 1958.
- World transistor production has more than doubled every year for the past twenty years.
- Every year, more transistors are produced than in all previous years combined.
- Approximately 10¹⁸ transistors were produced in a recent year.
- Roughly 50 transistors for every ant in the world.

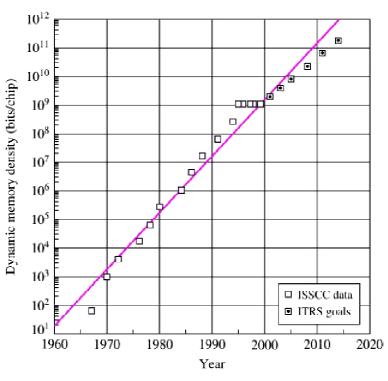
*Source: Gordon Moore's Plenary address at the 2003 International Solid-State Circuits Conference.

Device Feature Size

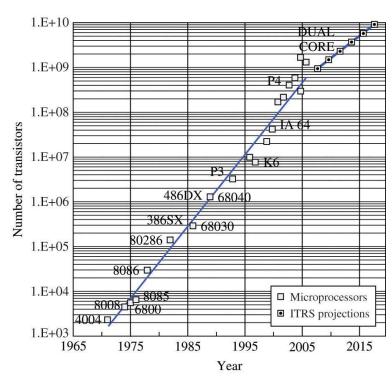


- Feature size reductions enabled by process innovations.
- Smaller features lead to more transistors per unit area and therefore higher density.

Rapid Increase in Density of Microelectronics

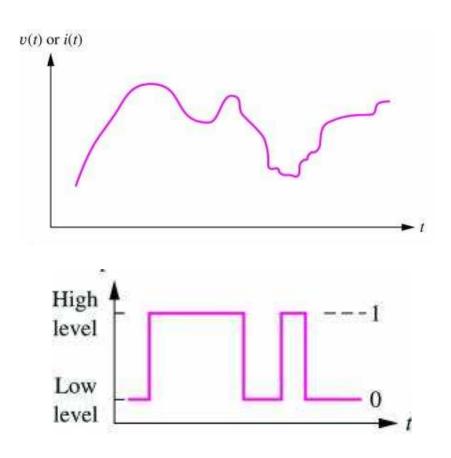


Memory chip density versus time.



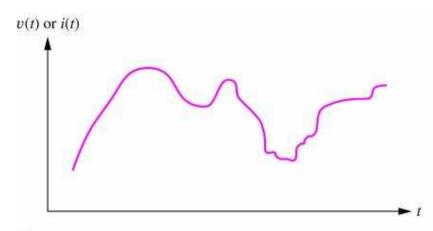
Microprocessor complexity versus time.

Signal Types

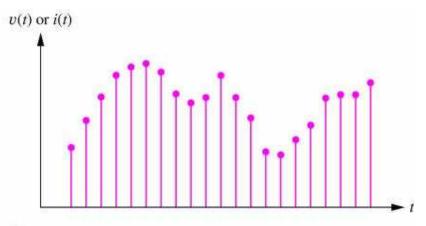


- Analog electrical signals take on continuous values
 typically current or voltage.
- Digital signals appear at discrete levels. Usually we use binary signals which utilize only two levels.
- One level is referred to as logical 1 and logical 0 is assigned to the other level.

Analog and Digital Signals

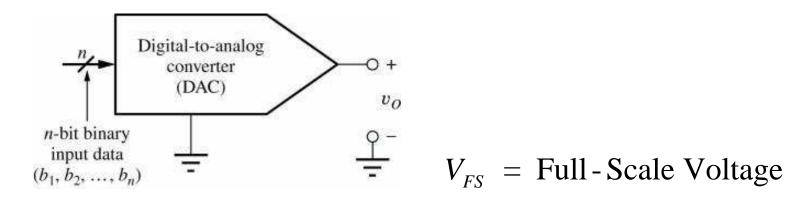


Analog electrical signals are continuous in time - most often voltage or current. (Charge can also be utilized as a signal conveyor.)



• After digitization, the continuous analog signal becomes a set of discrete values, typically separated by fixed time intervals.

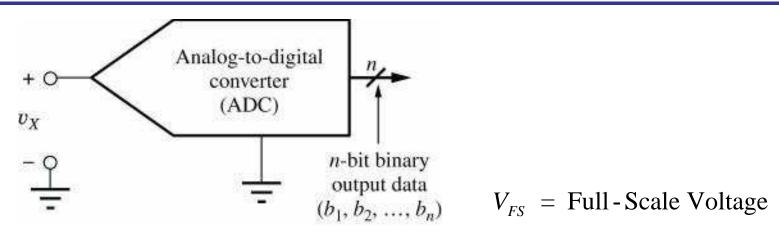
Digital-to-Analog (D/A) Conversion



- For an n-bit D/A converter, the output voltage is expressed as: $V_O = (b_1 2^{-1} + b_2 2^{-2} + ... + b_n 2^{-n})V_{FS}$
- The smallest possible voltage change is known as the least significant bit or LSB.

$$V_{LSB} = 2^{-n} V_{FS}$$

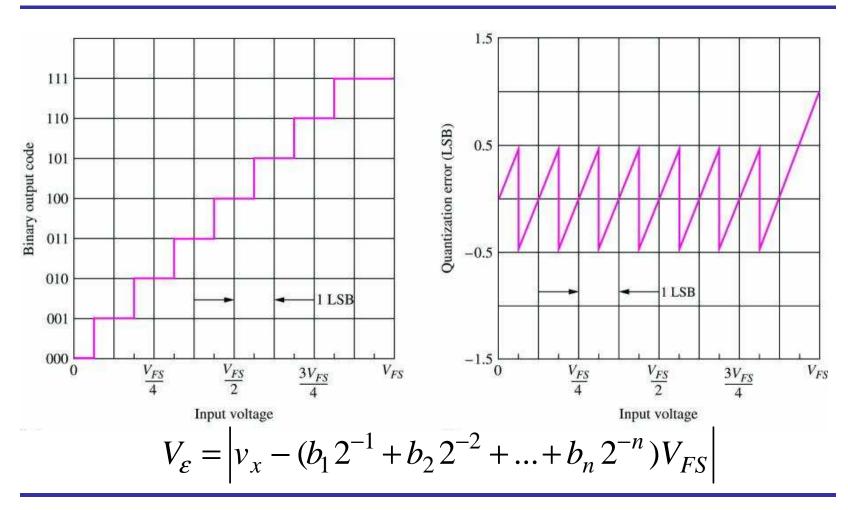
Analog-to-Digital (A/D) Conversion



- Analog input voltage v_x is converted to an n-bit number.
- For a four-bit converter, v_x ranging between 0 and V_{FS} yields a digital output code between 0000 and 1111.
- The output is an approximation of the input due to the limited resolution of the n-bit output. Error is expressed as:

$$V_{\varepsilon} = \left| v_x - (b_1 2^{-1} + b_2 2^{-2} + \dots + b_n 2^{-n}) V_{FS} \right|$$

A/D Converter Transfer Characteristic and Quantization Error



Notational Conventions

• Total signal = DC bias + time varying signal

$$v_T = V_{DC} + v_{sig}$$

$$i_T = I_{DC} + i_{sig}$$

Resistance and conductance - R and G with same subscripts will denote reciprocal quantities. The most convenient form will be used within expressions.

$$G_x = \frac{1}{R_x}$$
 and $g_\pi = \frac{1}{r_\pi}$

Problem-Solving Approach

- Make a clear problem statement.
- List known information and given data.
- Define the **unknowns** required to solve the problem.
- List **assumptions**.
- Develop an **approach** to the solution.
- Perform the analysis based on the approach.
- Check the results and the assumptions.
 - Has the problem been solved? Have all the unknowns been found?
 - Is the math correct? Have the assumptions been satisfied?
- Evaluate the solution.
 - Do the results satisfy reasonableness constraints?
 - Are the values realizable?
- Use **computer-aided analysis** to verify hand analysis

What are Reasonable Numbers?

- If the power suppy is ± 10 V, a calculated DC bias value of 15 V (not within the range of the power supply voltages) is unreasonable.
- Generally, our bias current levels will be between 1 microamp and a few hundred milliamps.
- A calculated bias current of 3.2 amps is probably unreasonable and should be reexamined.
- Peak-to-peak ac voltages should be within the power supply voltage range.
- A calculated component value that is unrealistic should be rechecked. For example, a resistance equal to 0.013 ohms or 10¹² ohms
- Given the inherent variations in most electronic components, three significant digits are adequate for representation of results. Three significant digits are used throughout the text.

Circuit Theory Review: Voltage **Division**

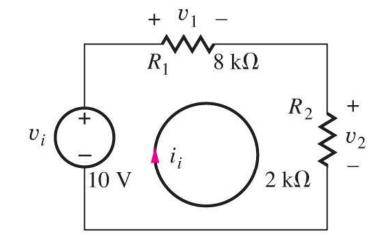
$$v_1 = i_i R_1$$

$$v_1 = i_i R_1 \quad \text{and} \quad v_2 = i_i R_2$$

Applying KVL to the loop,

$$v_i = v_1 + v_2 = i_i (R_1 + R_2)$$

and $i_i = \frac{v_i}{R_1 + R_2}$



Combining these yields the basic voltage division formula:

$$v_1 = v_i \frac{R_1}{R_1 + R_2}$$
 $v_2 = v_i \frac{R_2}{R_1 + R_2}$

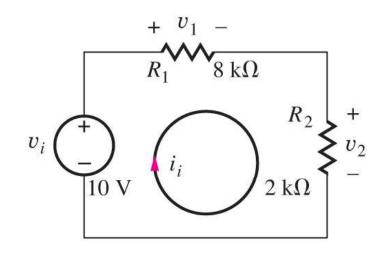
$$v_2 = v_i \frac{R_2}{R_1 + R_2}$$

Circuit Theory Review: Voltage Division (cont.)

Using the derived equations with the indicated values,

$$v_1 = 10 \text{ V} \frac{8 \text{ k}\Omega}{8 \text{ k}\Omega + 2 \text{ k}\Omega} = 8.00 \text{ V}$$

$$v_2 = 10 \text{ V} \frac{2 \text{ k}\Omega}{8 \text{ k}\Omega + 2 \text{ k}\Omega} = 2.00 \text{ V}$$



Design Note: Voltage division only applies when both resistors are carrying the same current.

Circuit Theory Review: Current Division

$$i_{i} = i_{1} + i_{2} \text{ where } i_{1} = \frac{v_{i}}{R_{1}} \text{ and } i_{2} = \frac{v_{i}}{R_{2}}$$
Combining and solving for v_{i} ,
$$v_{i} = i_{i} \frac{1}{R_{1}} + \frac{1}{R_{2}} = i_{i} \frac{R_{1}R_{2}}{R_{1} + R_{2}} = i_{i} \left(R_{1} \parallel R_{2}\right)$$

$$\sum_{i=1}^{l_{1}} \frac{1}{R_{1}} + \frac{1}{R_{2}} = i_{i} \frac{R_{1}R_{2}}{R_{1} + R_{2}} = i_{i} \left(R_{1} \parallel R_{2}\right)$$

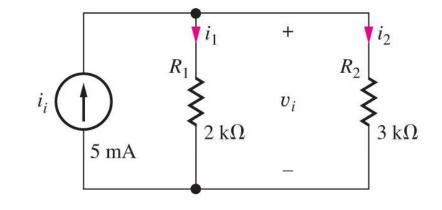
Combining these yields the basic current division formula:

$$i_1 = i_i \frac{R_2}{R_1 + R_2}$$
 $i_2 = i_i \frac{R_1}{R_1 + R_2}$

Circuit Theory Review: Current Division (cont.)

Using the derived equations with the indicated values,

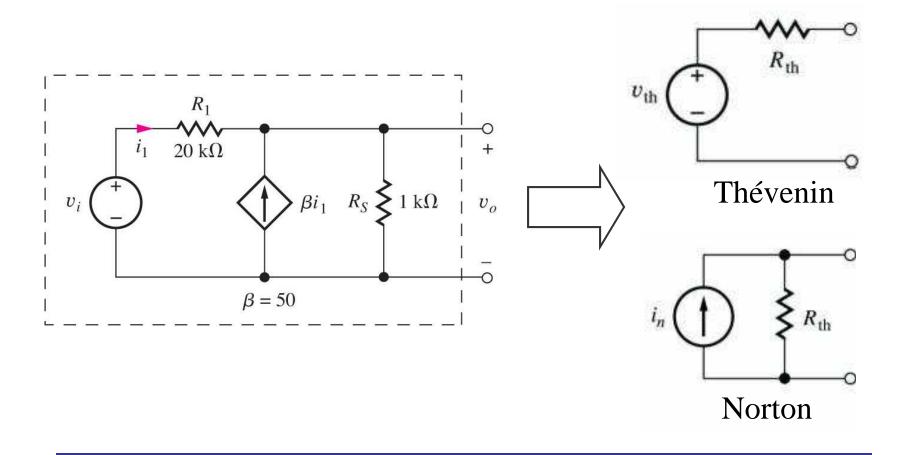
$$i_1 = 5 \text{ ma} \frac{3 \text{ k}\Omega}{2 \text{ k}\Omega + 3 \text{ k}\Omega} = 3.00 \text{ mA}$$



$$i_2 = 5 \text{ ma} \frac{2 \text{ k}\Omega}{2 \text{ k}\Omega + 3 \text{ k}\Omega} = 2.00 \text{ mA}$$

Design Note: Current division only applies when the same voltage appears across both resistors.

Circuit Theory Review: Thévenin and Norton Equivalent Circuits

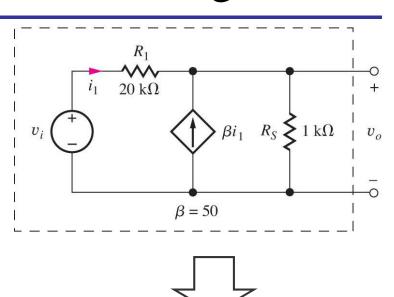


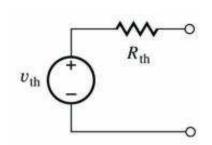
Circuit Theory Review: Find the Thévenin Equivalent Voltage

Problem: Find the Thévenin equivalent voltage at the output.

Solution:

- Known Information and Given
 Data: Circuit topology and values in figure.
- Unknowns: Thévenin equivalent voltage v_{th} .
- **Approach:** Voltage source v_{th} is defined as the output voltage with no load (open-circuit voltage).
- **Assumptions:** None.
- Analysis: Next slide...





Circuit Theory Review: Find the Thévenin Equivalent Voltage

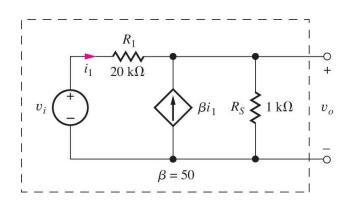
Applying KCL at the output node,

$$\beta i_1 = \frac{v_o - v_i}{R_1} + \frac{v_o}{R_S} = G_1(v_o - v_i) + G_S v_o$$

Current i_1 can be written as: $i_1 = G_1(v_o - v_i)$

Combining the previous equations

$$G_1(\beta+1)v_i = [G_1(\beta+1)+G_S]v_o$$



$$v_{o} = \frac{G_{1}(\beta+1)}{G_{1}(\beta+1)+G_{S}}v_{i} \times \frac{R_{1}R_{S}}{R_{1}R_{S}} = \frac{(\beta+1)R_{S}}{(\beta+1)R_{S}+R_{1}}v_{i}$$

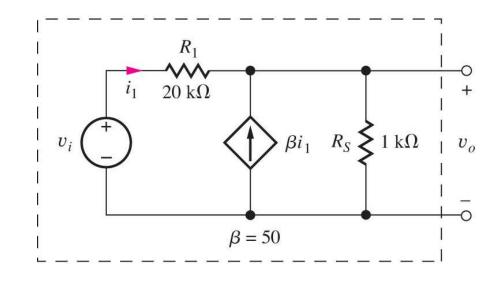
Circuit Theory Review: Find the Thévenin Equivalent Voltage (cont.)

Using the given component values:

$$v_o = \frac{(\beta + 1)R_S}{(\beta + 1)R_S + R_1} v_i = \frac{(50 + 1)1 \text{ k}\Omega}{(50 + 1)1 \text{ k}\Omega + 1 \text{ k}\Omega} v_i = 0.718 v_i$$

and

$$v_{\rm th} = 0.718 v_i$$

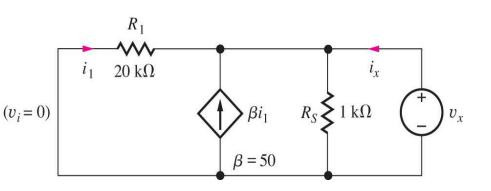


Circuit Theory Review: Find the Thévenin Equivalent Resistance

Problem: Find the Thévenin equivalent resistance.

Solution:

- Known Information and Given Data: Circuit topology and values in figure.
- **Unknowns**: Thévenin equivalent Resistance R_{th} .
- **Approach**: Find R_{th} as the output equivalent resistance with independent sources set to zero.
- **Assumptions**: None.
- **Analysis**: Next slide...



Test voltage v_x has been added to the previous circuit. Applying v_x and solving for i_x allows us to find the Thévenin resistance as v_x/i_x .

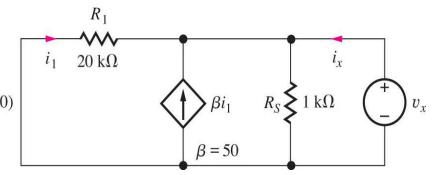
Circuit Theory Review: Find the Thévenin Equivalent Resistance (cont.)

Applying KCL,

$$i_{x} = -i_{1} - \beta i_{1} + G_{S} v_{x}$$

$$= G_{1} v_{x} + \beta G_{1} v_{x} + G_{S} v_{x}$$

$$= [G_{1}(\beta + 1) + G_{S}] v_{x}$$



$$R_{th} = \frac{v_x}{i_x} = \frac{1}{G_1(\beta+1)+G_S} = R_S \left\| \frac{R_1}{\beta+1} \right\|$$

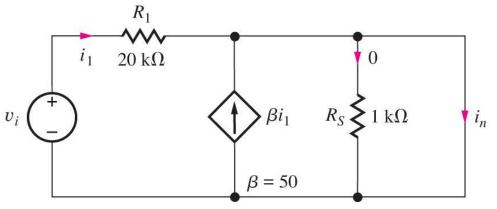
$$R_{th} = R_S \left\| \frac{R_1}{\beta + 1} = 1 \text{ k}\Omega \right\| \frac{20 \text{ k}\Omega}{50 + 1} = 1 \text{ k}\Omega \| 392 \Omega = 282 \Omega$$

Circuit Theory Review: Find the Norton Equivalent Circuit

Problem: Find the Norton equivalent circuit.

Solution:

- Known Information and Given Data: Circuit topology and values in figure.
- **Unknowns**: Norton equivalent short circuit current i_n .
- **Approach**: Evaluate current through output short circuit.
- **Assumptions**: None.
- Analysis: Next slide...



A short circuit has been applied across the output. The Norton current is the current flowing through the short circuit at the output.

Circuit Theory Review: Find the Norton Equivalent Circuit (cont.)

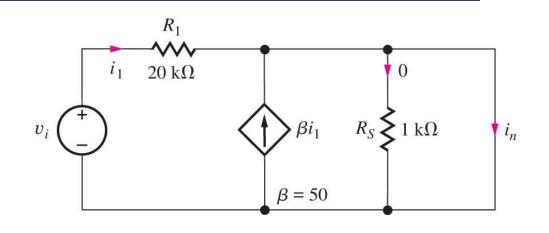
Applying KCL,

$$i_n = i_1 + \beta i_1$$

$$= G_1 v_i + \beta G_1 v_i$$

$$= G_1 (\beta + 1) v_i$$

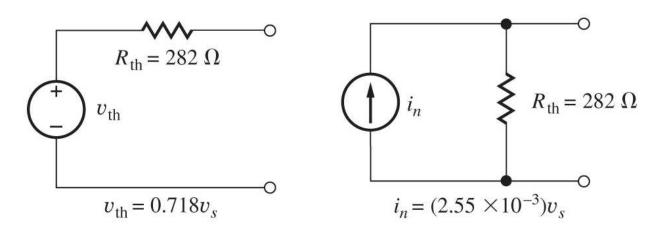
$$= \frac{v_i (\beta + 1)}{R_1}$$



Short circuit at the output causes zero current to flow through R_S . R_{th} is equal to R_{th} found earlier.

$$i_n = \frac{50+1}{20 \text{ k}\Omega} v_i = \frac{v_i}{392 \Omega} = (2.55 \text{ mS}) v_i$$

Final Thévenin and Norton Circuits



Check of Results: Note that $v_{\text{th}} = i_{\text{n}}R_{\text{th}}$ and this can be used to check the calculations: $i_{\text{n}}R_{\text{th}} = (2.55 \text{ mS})v_{\text{i}}(282 \Omega) = 0.719v_{\text{i}}$, accurate within round-off error.

While the two circuits are identical in terms of voltages and currents at the output terminals, there is one difference between the two circuits. With no load connected, the Norton circuit still dissipates power!

Frequency Spectrum of Electronic Signals

- Non repetitive signals have continuous spectra often occupying a broad range of frequencies
- Fourier theory tells us that repetitive signals are composed of a set of sinusoidal signals with distinct amplitude, frequency, and phase.
- The set of sinusoidal signals is known as a **Fourier series**.
- The frequency spectrum of a signal represents the amplitude and phase components of the signal versus frequency.

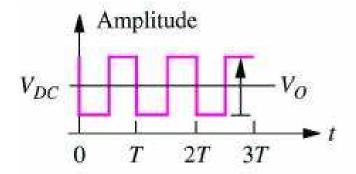
Frequencies of Some Common Signals

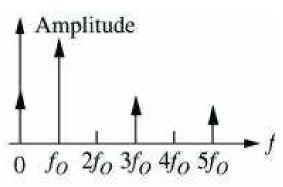
 Audible sounds 	20 Hz - 20 KHz
 Baseband TV 	0 - 4.5 MHz
 FM Radio 	88 - 108 MHz
 Television (Channels 2-6) 	54 - 88 MHz
 Television (Channels 7-13) 	174 - 216 MHz
 Maritime and Govt. Comm. 	216 - 450 MHz
 Cell phones and other wireless 	0.8 - 3 GHz
 Satellite TV 	3.7 - 4.2 GHz
 Wireless Devices 	5.0 - 5.5 GHz

Fourier Series

- A periodic signal contains spectral components only at discrete frequencies related to the period of the original signal.
- A square wave is represented by the following Fourier series:

$$v(t) = V_{DC} + \frac{2V_O}{\pi} \left(\sin \omega_0 t + \frac{1}{3} \sin 3\omega_0 t + \frac{1}{5} \sin 5\omega_0 t + \dots \right)$$





 $\omega_0 = 2\pi/T$ (rad/s) is the fundamental radian frequency, and $f_0 = 1/T$ (Hz) is the fundamental frequency of the signal. $2f_0$, $3f_0$, and $4f_0$ are known as the second, third, and fourth harmonic frequencies.

Amplifier Basics

- Analog signals are typically manipulated with linear amplifiers.
- Although signals may be comprised of several different components, linearity permits us to use the **superposition principle**.
- Superposition allows us to calculate the effect of each of the different components of a signal individually and then add the individual contributions to create the total resulting signal.

Amplifier Linearity

Given an input sinusoid:

$$v_i = V_i \sin(\omega_i t + \phi)$$

For a linear amplifier, the output is at the same frequency, but different amplitude and phase.

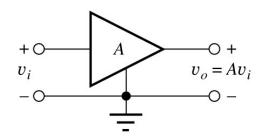
$$v_o = V_o \sin(\omega_i t + \phi + \theta)$$

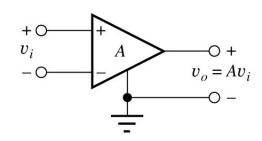
In phasor notation:

$$\mathbf{v}_i = V_i \angle \phi \qquad \mathbf{v}_o = V_o \angle (\phi + \theta)$$

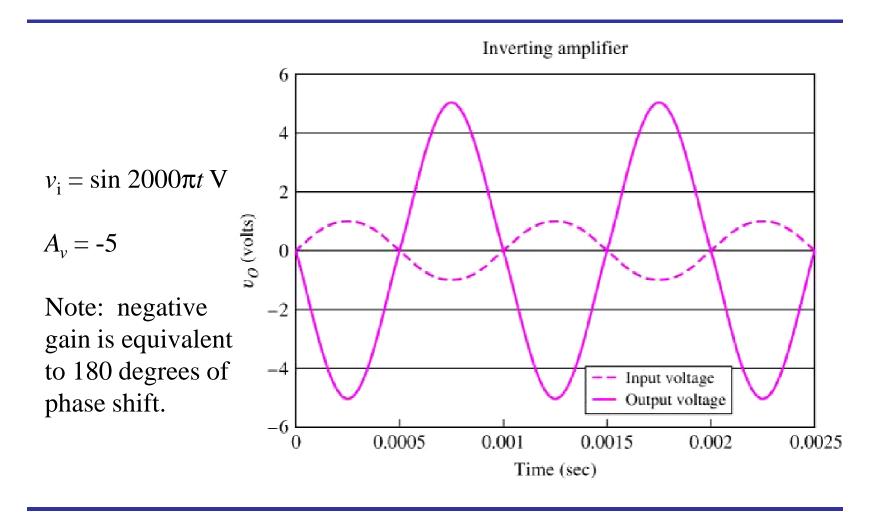
Amplifier gain is:

$$A = \frac{\mathbf{v_o}}{\mathbf{v_i}} = \frac{V_o \angle (\phi + \theta)}{V_i \angle \phi} = \frac{V_o}{V_i} \angle \theta$$





Amplifier Input/Output Response



Ideal Operational Amplifier (Op Amp)

Ideal op amps are assumed to have infinite voltage gain, and infinite input resistance.

These conditions lead to two assumptions useful in analyzing ideal op-amp circuits:

- 1. The voltage difference across the input terminals is zero.
- 2. The input currents are zero.

Ideal Op Amp Example

Find the voltage gain of an op amp with resistive feedback

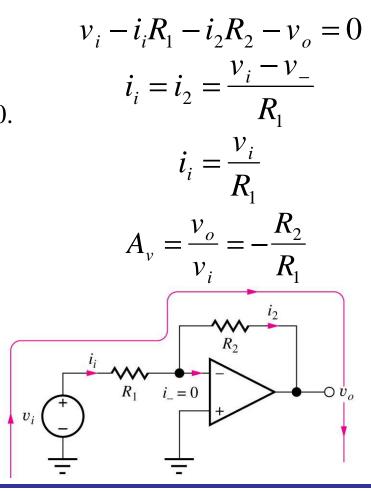
Writing a loop equation:

From assumption 2, we know that $i_{\underline{\ }}=0$.

Assumption 1 requires $v_{-} = v_{+} = 0$.

Combining these equations yields:

Assumption 1 requiring $v_{-} = v_{+} = 0$ creates what is known as a **virtual ground** at the inverting input of the amplifier.



Ideal Op Amp Example (Alternative Approach)

From Assumption 2, $i_2 = i_i$:

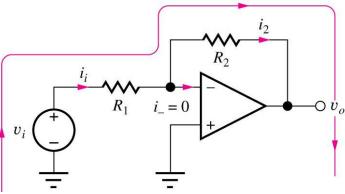
$$i_i = \frac{v_i}{R_1}$$
 and $i_2 = \frac{v_- - v_o}{R_2} = \frac{-v_o}{R_2}$

$$i_2 = i_i$$
 gives $\frac{v_i}{R_1} = \frac{-v_o}{R_2}$

Yielding:

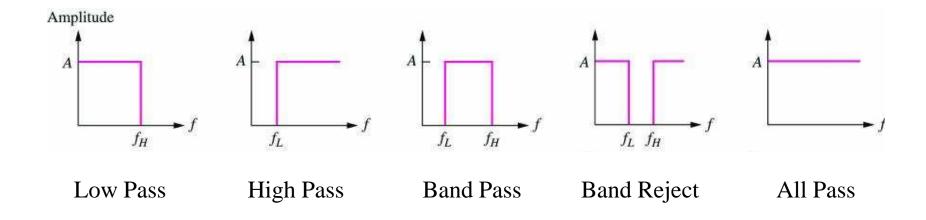
$$A_{v} = \frac{v_{o}}{v_{i}} = -\frac{R_{2}}{R_{1}}$$

Design Note: The virtual ground is *not* an actual ground. Do not short the inverting input to ground to simplify analysis.



Amplifier Frequency Response

Amplifiers can be designed to selectively amplify specific ranges of frequencies. Such an amplifier is known as a filter. Several filter types are shown below:



Circuit Element Variations

- All electronic components have manufacturing tolerances.
 - Resistors can be purchased with \pm 10%, \pm 5%, and \pm 1% tolerance. (IC resistors are often \pm 10%.)
 - Capacitors can have asymmetrical tolerances such as +20%/-50%.
 - Power supply voltages typically vary from 1% to 10%.
- Device parameters will also vary with temperature and age.
- Circuits must be designed to accommodate these variations.
- We will use worst-case and Monte Carlo (statistical) analysis to examine the effects of component parameter variations.

Tolerance Modeling

For symmetrical parameter variations

$$P_{\text{nom}}(1 - \varepsilon) \le P \le P_{\text{nom}}(1 + \varepsilon)$$

• For example, a 10 k Ω resistor with ±5% percent tolerance could take on the following range of values:

$$10k\Omega(1 - 0.05) \le R \le 10k\Omega(1 + 0.05)$$

 $9500 \Omega \le R \le 10500 \Omega$

Circuit Analysis with Tolerances

Worst-case analysis

- Parameters are manipulated to produce the worst-case min and max values of desired quantities.
- This can lead to over design since the worst-case combination of parameters is rare.
- It may be less expensive to discard a rare failure than to design for 100% yield.

Monte-Carlo analysis

- Parameters are randomly varied to generate a set of statistics for desired outputs.
- The design can be optimized so that failures due to parameter variation are less frequent than failures due to other mechanisms.
- In this way, the design difficulty is better managed than a worstcase approach.

Worst Case Analysis Example

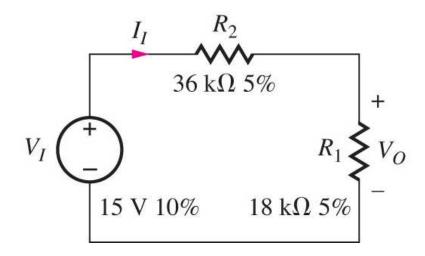
Problem: Find the nominal and worst-case values for output voltage and source current.

Solution:

- Known Information and Given Data: Circuit topology and values in figure.
- Unknowns:

$$V_O^{nom}$$
, V_O^{\min} , V_O^{\max} , I_I^{nom} , I_I^{\min} , I_I^{\max}

- **Approach**: Find nominal values and then select R₁, R₂, and V_I values to generate extreme cases of the unknowns.
- **Assumptions**: None.
- Analysis: Next slides...



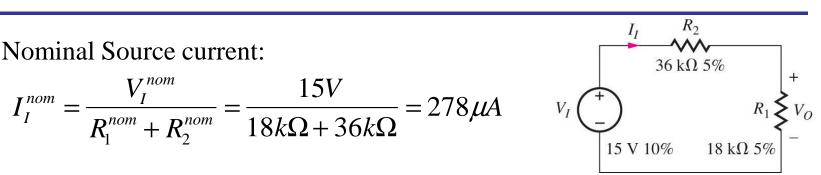
Nominal voltage solution:

$$V_O^{nom} = V_I^{nom} \frac{R_1^{nom}}{R_1^{nom} + R_2^{nom}}$$
$$= 15V \frac{18k\Omega}{18k\Omega + 36k\Omega} = 5V$$

Worst-Case Analysis Example (cont.)

Nominal Source current:

$$I_I^{nom} = \frac{V_I^{nom}}{R_1^{nom} + R_2^{nom}} = \frac{15V}{18k\Omega + 36k\Omega} = 278\mu A$$



Rewrite V_0 to help us determine how to find the worst-case values.

$$V_O = V_I \frac{R_1}{R_1 + R_2} = \frac{V_I}{1 + \frac{R_2}{R_1}} \quad \text{V}_O \text{ is maximized for max V}_I, R_1 \text{ and min R}_2.$$

$$V_O \text{ is minimized for min V}_I, R_1, \text{ and max R}_2.$$

$$V_O^{\text{max}} = \frac{15V(1.1)}{1 + \frac{36K(0.95)}{18K(1.05)}} = 5.87V \qquad V_O^{\text{min}} = \frac{15V(0.95)}{1 + \frac{36K(1.05)}{18K(0.95)}} = 4.20V$$

Worst-Case Analysis Example (cont.)

Worst-case source currents:

$$I_I^{\text{max}} = \frac{V_I^{\text{max}}}{R_1^{\text{min}} + R_2^{\text{min}}} = \frac{15V(1.1)}{18k\Omega(0.95) + 36k\Omega(0.95)} = 322\mu A$$

$$I_I^{\min} = \frac{V_I^{\min}}{R_I^{\max} + R_2^{\max}} = \frac{15V(0.9)}{18k\Omega(1.05) + 36k\Omega(1.05)} = 238\mu A$$

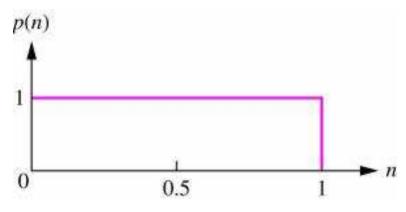
Check of Results: The worst-case values range from 14-17 percent above and below the nominal values. The sum of the three element tolerances is 20 percent, so our calculated values appear to be reasonable.

Monte Carlo Analysis

- Parameters are varied randomly and output statistics are gathered.
- We use programs like MATLAB, Mathcad, SPICE, or a spreadsheet to complete a statistically significant set of calculations.
- For example, with Excel®, a resistor with a nominal value R_{nom} and tolerance ϵ can be expressed as:

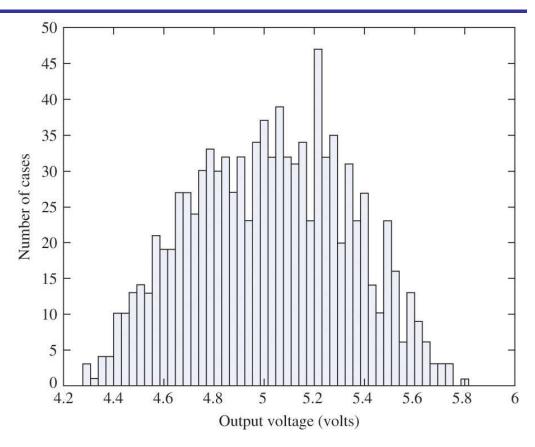
$$R = R_{nom}(1 + 2\varepsilon(RAND() - 0.5))$$

The RAND() function returns random numbers uniformly distributed between 0 and 1.



Monte Carlo Analysis Results

V _O (V)						
Average	4.96					
Nominal	5.00					
Standard Deviation	0.30					
Maximum	5.70					
W/C Maximum	5.87					
Minimum	4.37					
W/C Minimum	4.20					



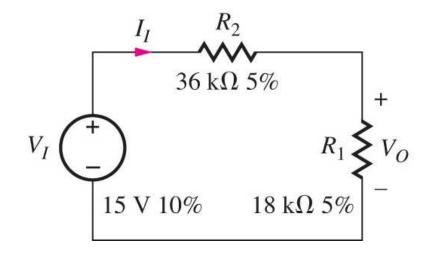
Histogram of output voltage from 1000 case Monte Carlo simulation.

Monte Carlo Analysis Example

Problem: Perform a Monte Carlo analysis and find the mean, standard deviation, min, and max for V_O, I_I, and power delivered from the source.

Solution:

- Known Information and Given Data: Circuit topology and values in figure.
- **Unknowns**: The mean, standard deviation, min, and max for V_O , I_I , and P_I .
- **Approach**: Use a spreadsheet to evaluate the circuit equations with random parameters.
- **Assumptions**: None.
- **Analysis**: Next slides...



Monte Carlo parameter definitions:

$$V_I = 15(1 + 0.2(RAND() - 0.5))$$

$$R_1 = 18,000(1+0.1(RAND()-0.5))$$

$$R_2 = 36,000(1+0.1(RAND()-0.5))$$

Monte Carlo Analysis Example (cont.)

Monte Carlo parameter definitions:

$$V_I = 15(1+0.2(RAND()-0.5))$$

$$R_1 = 18,000(1+0.1(RAND()-0.5))$$

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Circuit equations based on Monte Carlo parameters:

$$V_{O} = V_{I} \frac{R_{1}}{R_{1} + R_{2}}$$
 $I_{I} = \frac{V_{I}}{R_{1} + R_{2}}$ $P_{I} = V_{I} I_{I}$

Results:

	Avg	Nom.	Stdev	Max	WC-max	Min	WC-Min
$V_{o}(V)$	4.96	5.00	0.30	5.70	5.87	4.37	4.20
$I_{I}(mA)$	0.276	0.278	0.0173	0.310	0.322	0.242	0.238
P(mW)	4.12	4.17	0.490	5.04		3.29	

Temperature Coefficients

• Most circuit parameters are temperature sensitive.

$$P = P_{nom}(1 + \alpha_1 \Delta T + \alpha_2 \Delta T^2) \text{ where } \Delta T = T - T_{nom}$$

$$P_{nom} \text{ is defined at } T_{nom}$$

- Most versions of SPICE allow for the specification of TNOM, T, $TC1(\alpha_1)$, $TC2(\alpha_2)$.
- SPICE temperature model for resistor:
 R(T) = R(TNOM)*[1+TC1*(T-TNOM)+TC2*(T-TNOM)²]
- Many other components have similar models.

Numeric Precision

- Most circuit parameters vary from less than \pm 1 % to greater than \pm 50%.
- As a consequence, more than three significant digits is meaningless.
- Results in the text will be represented with three significant digits: 2.03 mA, 5.72 V, 0.0436 μ A, and so on.
- However, extra guard digits are normally retained during calculations.

End of Chapter 1