

5.62

$$I_b = 175 \mu A \quad I_s = 4 \times 10^{-16} A, \quad \beta_F = 50, \quad \beta_R = 0.5$$

a) $V_{CE} = 3V$

$$I_e = I_s \left[\exp\left(\frac{V_{BE}}{V_T}\right) - \exp\left(\frac{V_{BC}}{V_T}\right) \right] + \frac{I_s}{\beta_R} \left(\exp\left(\frac{V_{BC}}{V_T}\right) - 1 \right)$$

V_{BC} should be negative because V_{BC} will be on the order of the p-n junction on voltage. Therefore the V_{BC} term in I_e can be neglected.

in forward active, $I_e = (1 + \beta_F) I_B$
 $= (51)(175 \mu A)$
 $I_e = 8.93 \text{ mA}$

$$8.93 \text{ mA} = I_s \left[\exp\left(\frac{V_{BE}}{0.025V}\right) \right] + \frac{I_s}{50} \left(\exp\left(\frac{V_{BE}}{0.025}\right) - 1 \right) \quad \text{w/ } I_c \text{ as above}$$

Solve for V_{BE}

$$V_{BE} = 0.768 \text{ V}$$

① $0 = i_c = I_s \left[\exp\left(\frac{V_{BE}}{V_T}\right) - \exp\left(\frac{V_{BC}}{V_T}\right) \right] - \frac{I_s}{\beta_R} \left[\exp\left(\frac{V_{BC}}{V_T}\right) - 1 \right]$

② $175 \mu A = i_b = \frac{I_s}{\beta_F} \left(\exp\left(\frac{V_{BE}}{V_T}\right) - 1 \right) - \frac{I_s}{\beta_R} \left(\exp\left(\frac{V_{BC}}{V_T}\right) - 1 \right)$

Rearrange

② to get ③ $\textcircled{3} \exp\left(\frac{V_{BC}}{V_T}\right) = \frac{\beta_R}{I_s} i_b - \frac{I_s}{\beta_F} \left(\exp\left(\frac{V_{BE}}{V_T}\right) - 1 \right) - \frac{I_s}{\beta_R}$

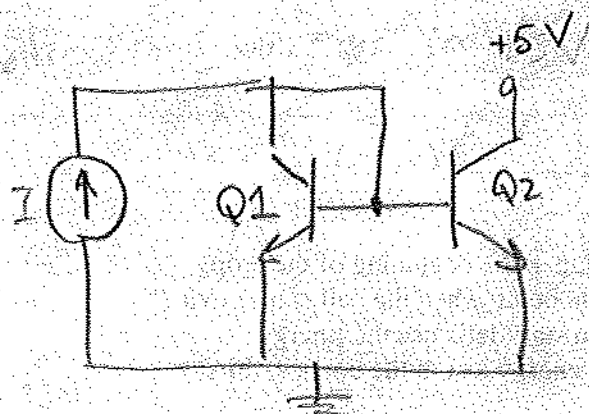
Plug ③ into ① and solve for V_{BE} , $V_{BE} = 0.680 \text{ V}$

$V_{CESat} = V_{BE} + V_{CB}$ when BJT in saturation (BJT saturation different than MOSFET saturation)

Solve ② for V_{BE} , substituting for $V_{BE} = 0.680 \text{ V}$, like MOSFET triode.

$V_{BC} = 0.652 \text{ V}, \quad V_{CE} = V_{CB} + V_{BE} = -V_{BC} + V_{BE} = -0.652 + 0.680 = 0.0275 \text{ V}$
 V_{CESat}

5.65



$$I = 25 \mu A, \beta_F = 60$$

Because $V_{CE1} = V_{BE1}$ and $V_{BE1} > 0$, $Q1$ is in forward active

Because $V_{CE2} > V_{BE2}$ and $V_{BE2} > 0$, $Q2$ is also forward active

In forward active $I_B \approx \frac{I_S}{\beta_F} \exp\left(\frac{V_{BE}}{V_T}\right)$. Therefore, Because

$Q1$ and $Q2$ are identical, and $V_{BE1} = V_{BE2}$, $I_{B1} \approx I_{B2}$

~~$$I = I_{C1} + I_{B1} + I_{B2}$$~~

Also, in forward active, $I_C = \beta_F I_B$, so $I_{C1} \approx I_{C2}$

So

$$I = I_{C1} + I_{B1} + I_{B2}$$

$$I = I_{C2} + \frac{I_{C2}}{\beta_F} + \frac{I_{C2}}{\beta_F} = I_{C2} \left(\frac{\beta_F + 2}{\beta_F} \right)$$

$$I_{C2} = I \left(\frac{\beta_F}{\beta_F + 2} \right) = 25 \mu A \left(\frac{60}{62} \right)$$

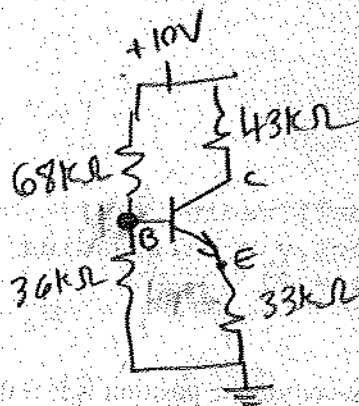
$$V_{CE2} \approx V_{CE1}$$

$$I_{C2} = 24.2 \mu A$$

5.93 part a

$$V_{BE} = 0.7V$$

$$\beta_F = 50$$



Transistor most likely in forward active.

To find base current, use loop 1

$$① V_B = V_{BE} + I_C(33k\Omega) = V_{BE} + (\beta + 1)I_B(33k\Omega)$$

$$\frac{10V - V_B}{68k\Omega} = \frac{V_B - V_{BE}}{36k\Omega} + I_B \quad (\text{Node equation at Base})$$

$$② I_B = \frac{10V}{68k} - \frac{V_B}{68k} - \frac{V_B}{36k} = \frac{10V}{68k} - V_B \left(\frac{1}{68k} + \frac{1}{36k} \right)$$

Substitute ② into ①, solve for V_B

$$\boxed{V_B = 3.43V} \quad \text{Substitute in ②, calculate } \boxed{I_B = 1.41\mu A}$$

$$V_E = V_B - V_{BE} = 3.43V - 0.7V = \boxed{2.73V = V_E}$$

$$I_C = \beta I_B = 50(1.41\mu A) = \boxed{70.4\mu A = I_C}$$

$$I_E = (\beta + 1)I_B = 51(1.41\mu A) = \boxed{71.8\mu A = I_E}$$

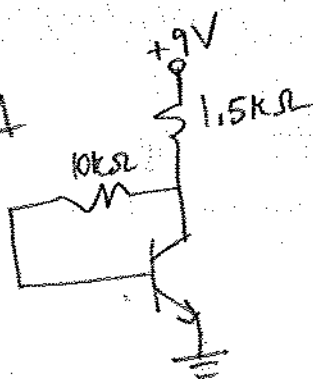
$$V_C = 10V - I_C(43k\Omega) = \boxed{6.97V = V_C}$$

$V_C - V_E > 0$, so forward active is verified.

5.96 part (a)

$$\beta_F = 40$$

use $I_S = 10^{-10} \text{ A}$
from front



$$9\text{V} + (I_C + I_B)1.5\text{k}\Omega + I_B(10\text{k}\Omega) + V_{BE} = 0$$

$$\textcircled{1} \quad 9\text{V} + (1 + \beta)I_B(1.5\text{k}\Omega) + I_B(10\text{k}\Omega) + V_{BE} = 0$$

In forward active $\textcircled{2} \quad I_B \approx \frac{I_S}{\beta} \exp\left(\frac{V_{BE}}{V_T}\right)$ use $V_T = 0.025\text{V}$ for room temp ($\sim 290\text{K}$)

plug $\textcircled{2}$ into $\textcircled{1}$ solve for I_B

$$I_B = 115\mu\text{A}$$

plug I_B into $\textcircled{1}$, solve for V_{BE} ,

$$V_{BE} = 0.786\text{V}$$

$$I_C = \beta I_B = (40)(115\mu\text{A}) = 4.59\text{mA} = I_C$$

$$I_E = (\beta + 1)I_B = (41)(115\mu\text{A}) = 4.71\text{mA} = I_E$$

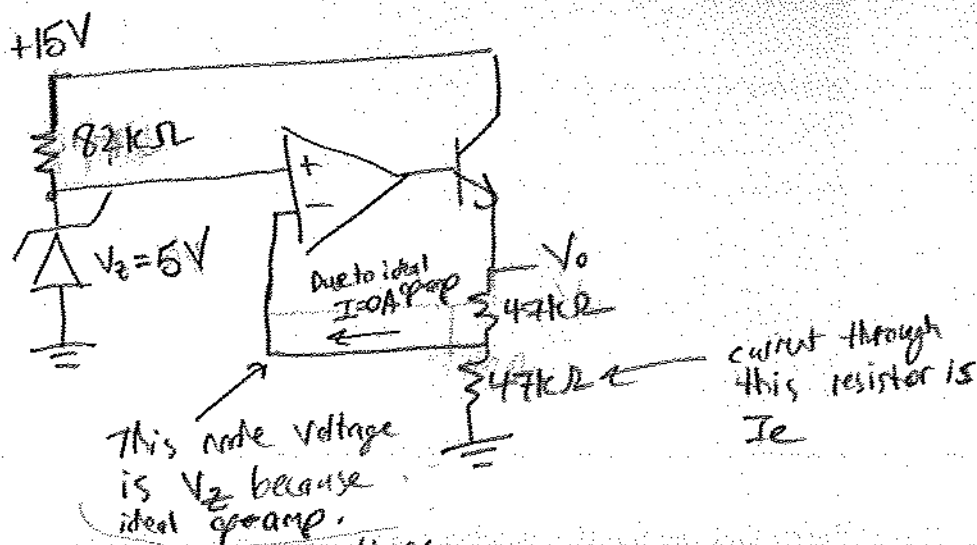
$$V_C = 0\text{V}$$

$$V_B = V_{BE} = 0.786\text{V}$$

$$V_C = V_{CE} = 9\text{V} - (I_B + I_C)(1.5\text{k}\Omega) = 9\text{V} - (\beta + 1)I_B(1.5\text{k}\Omega) \\ = 9\text{V} - I_E(1.5\text{k}\Omega)$$

$$V_C = V_{CE} = 1.94\text{V}$$

5.105



Ideal op-amp assumptions:

- No current flows in or out of the op-amp inputs
- The voltage between the input terminals of the op-amp is zero.

The emitter current is

$$I_e = \frac{V_z}{47k\Omega} = \frac{5V}{47k\Omega} = \boxed{106\mu A = I_e}$$

$$V_o = I_e(47k\Omega + 47k\Omega) = 2V_z = \boxed{10V = V_o}$$

Power Supply current

$$I_{supply} = I_e + \frac{15V - 5V}{82k\Omega} = 106\mu A + 122\mu A = \boxed{228\mu A = I_{supply}}$$