

Name: Zanning Wang

zID: z5224151

1.

(a) the basic pseudo-code show below:

```
1 new_list = []
2 for i in A:
3     for j in A(not include i):
4         new_list.append(pow(i,2)+j)
5 sort(new_list)
6 checksame(new_list)
```

From line2-4, we calculate all possible x^2+y , and save them in a dict, for this step, the time complexity is $O(n*(n-1)) = O(n^2)$

From line5, we sort the list in order to help the next step we check if there exist two same numbers, because the length of current list is $O(n*(n-1)) = O(n^2)$, therefore the complexity of time for sorting this array is $O(n^2*\log(n^2)) = O(n^2*\log n)$

From the line5, we only need to traverse the array once to see if there are adjacent and identical numbers.

Therefore, the total time complexity is the most time-consuming step, which is step5, $O(n^2*\log n)$

(b)

```
1 new_dict = {}
2 for i in A:
3     for j in A(not include i):
4         temp = (pow(i,2)+j)
5         if temp not in new_dict:
6             new_dict[temp] = 1
7         else:
8             return
```

In order to decrease the time complexity, we may use the dictionary instead of the list, when we try to search one certain value, it only take $O(n)$ time complexity.

From line2-4, it was same as the question (a), which take $O(n^2)$

From line 5-8, every time we calculate the x^2+y , we check if it exists in dictionary. If so, break the loop and return the result, else keep going, for this step, check element in dict only take $O(n)$ time.

Therefore, the total time complexity is $O(n^2)$.