#### CS1010S Tutorial 5

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# Today's Agenda

- Recap
- Question One
  - Discussion
  - Standard solution
- Question 2
  - Discussion
  - Standard solutions
- Question 3
  - Discussion
  - Standard solutions
- Question 4
  - Discussion
  - Standard solutions
- Question 5
  - Discussion
  - Standard solutions
- Extra stuff: your midterm question

March 5, 2017

#### Recap - Tuple

Why do you use tuple?

- Allow for multiple storage
- Immutable
- Allow for nested tuple

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#### Recap - List

#### Why do you use list?

- Mutable
- list1 + list2
- list.append(element) → also touch on list comprehension
- list.extend(element)
- del a[index]
- len, min, max, in, \* scalar (sequence operations)
- list.copy() → shallow copy, often tested in finals
- list.insert(position, element)
- list.pop(position)
- list.remove(element)
- list.clear()
- list.reverse()

### Recap - Box and pointer diagram

- Most important when you are using lists than tuples
- Below is a screenshot of your lecture notes
- Why is it so? Explain using box and pointer diagram

```
lst = [1, 2, 3]
1st2 = 1st
1st == 1st2
                     →True
                     →True
lst is lst2
1st += [4, 5, 6]
lst
                      \rightarrow[1, 2, 3, 4, 5, 6]
                      \rightarrow[1, 2, 3, 4, 5, 6]
1st2
1st == 1st2
                      \rightarrowTrue
                     \rightarrowTrue
lst is lst2
```

# Recap - Searching

- Linear search
  - Time: O(n)
- Binary search
  - only when array is sorted
  - Time:  $O(\log n)$

#### Recap - Sorting

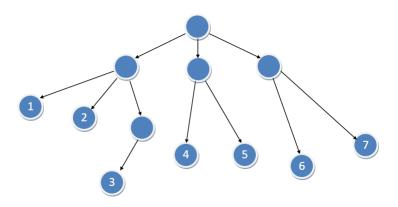
- Selection sort
  - Time:  $O(n^2)$
  - Stable
- Merge sort
  - Time:  $O(n \log n)$
  - Space: O(n)
  - Stable
- list.sort(key = lambda x: f(x), reverse = True)
  - Sort based on the value of f(x)
  - Sort to be in reverse order
- Other sorting methods and many more ...
  - Bubble sort
  - Quick sort
  - Shell sort
  - Bucket sort
  - Heap sort

#### Question 1

Draw box-and-pointer diagrams for the values of the following tuples.

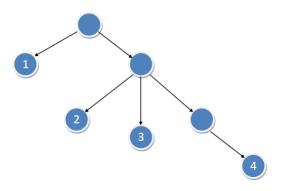
#### Question 1 Discussion

- How important is your box-and-pointer diagram?
- You will never be asked to draw them.
- But, you will need to draw them for solving other problems.
- Especially some problems of Question 1 of Final Exam
- There is no fixed form that you need to follow
- As long as you understand what you draw

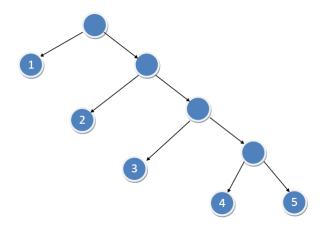


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(1, (2, 3, (4,)))



(1, (2, (3, (4, 5))))



#### Question 2

Write expressions using index notation that will return the value 1 when the identifier tup is bound to the following values: (7, (6, 5, 4), 3, (2, 1)) ((7), (6, 5, 4), (3, 2), 1) (7, (6,), (5, (4,)), (3, (2, (1,)))) (7, ((6, 5), (4,), 3, 2), ((1,),))

#### Question 2 Discussion

#### Your task now is to:

- Draw the box-and-pointer diagram in your head
- And identify which element you are going to visit
- Count the index of the element and put it down

Denote the element which you are going to visit by bolding it

- (7, (6, 5, 4), 3, (2, **1**))
- (7, (6, 5, 4), 3, **(2, 1)**)
- **o** (7, (6, 5, 4), 3, (2, 1))

If we go backwards, the indices we are going to record down are: 3 and 1 Hence the answer is  $\sup[3][1]$ 

Denote the element which you are going to visit by bolding it

- ((7), (6, 5, 4), (3, 2), **1**)
- **o** ((7), (6, 5, 4), (3, 2), 1)
- Problem now is: what is (7)?
- Is this really a problem?

If we go backwards, the indices we are going to record down is: 3 Hence the answer is tup[3]

Denote the element which you are going to visit by bolding it

- (7, (6,), (5, (4,)), (3, (2, (1,))))
- (7, (6,), (5, (4,)), (3, (2, **(1,)**)))
- (7, (6,), (5, (4,)), (3, **(2, (1,))**))
- (7, (6,), (5, (4,)), (3, (2, (1,))))
- (7, (6,), (5, (4,)), (3, (2, (1,))))

If we go backwards, the indices we are going to record down are: 3, 1, 1, 0 Hence the answer is  $\sup[3][1][1][0]$ 

Denote the element which you are going to visit by bolding it

- (7, ((6, 5), (4,), 3, 2), ((1,),))
- (7, ((6, 5), (4,), 3, 2), (**(1,)**,))
- (7, ((6, 5), (4,), 3, 2), **((1,),)**)
- (7, ((6, 5), (4,), 3, 2), ((1,),))

If we go backwards, the indices we are going to record down are: 2, 0, 0 Hence the answer is  $\sup[2][0][0]$ 

```
tup = (7, (6, 5, 4), 3, (2, 1))
print(tup[3][1])
tup = ((7), (6, 5, 4), (3, 2), 1)
print(tup[3])
tup = (7, (6,), (5, (4,)), (3, (2, (1,))))
print(tup[3][1][1][0])
tup = (7, ((6, 5), (4,), 3, 2), ((1,),))
print(tup[2][0][0])
```

- Order of growth for time complexity is?
- Order of growth for space complexity is?

### Question 3

Write a Python function called  $even\_rank$  that takes in a tuple as its only argument and returns a tuple containing all the elements of even rank (i.e. every second element from the left) from the input tuple.

Test input: even\_rank(('a', 'x', 'b', 'y', 'c', 'x', 'd', 'p', 'q'))
Test output: ('x', 'y', 'x', 'p')

## Question 3 Discussion

- Iteration
  - Relatively more intuitive to do
  - Do you need to deal with the last element?
- Iteration
  - In fact easier to do
  - Transform the corner case that tup has len smaller than 2 into the base case!

```
def even_rank(tup):
    l = len(tup)
    newTup = tuple()
    for i in range(1 // 2):
        newTup = newTup + (tup[i*2+1],)
    return newTup

def even_rank(tup):
    if len(tup) < 2:
        return ()
    else:
        return (tup[1],) + even rank(tup[2:])</pre>
```

- Order of growth for time complexity is ?
- Order of growth for space complexity is ?

### Question 4

Write a function called *odd\_even\_sums* that takes in a tuple of numbers as its only argument and returns a tuple of two elements: the first is the sum of all oddranked numbers in the input tuple, whereas the second element is the sum of all even-ranked elements in the input.

```
Test input: odd_even_sums((1, 3, 2, 4, 5))
Test output: (8, 7)
```

Test input:  $odd_even_sums((1,))$ 

Test output: (1, 0)

Test input: odd\_even\_sums(())

Test output: (0, 0)

### Question 4 Discussion

- Iteration
  - Relatively more intuitive to implement?
  - This time we will have to deal with the last element
- Recursion
  - Easier to implement?
  - The base case is never so simple
  - Adding numbers to elements of the resultant tuple can be troublesome!

#### Question 4 Zexin's iterative solution

```
def odd_even_sums(tup):
    1 = len(tup)
    oddSum = 0
    evenSum = 0
    for i in range(1 // 2):
        oddSum += tup[i*2]
        evenSum += tup[i*2+1]
    if 1 % 2:
        oddSum += tup[-1]
    return (oddSum, evenSum)
```

- Order of growth for time complexity is ?
- Order of growth for space complexity is ?

#### Question 4 Zexin's recursive solution

```
def odd_even_sums(tup):
    if len(tup) == 0:
        return (0, 0)
    elif len(tup) == 1:
        return (tup[0], 0)
    else:
        result = odd_even_sums(tup[2:])
        return (result[0]+tup[0], result[1]+tup[1])
```

- Order of growth for time complexity is ?
- Order of growth for space complexity is ?

#### Question 5

Write a function called **hanoi** that takes in 4 parameters:

- number of disks
- source pole
- destination pole
- auxiliary pole

```
Test input: hanoi(1, 1, 2, 3)
Test output: ((1, 2),)
Test input: hanoi(1, 1, 3, 2)
Test output: ((1, 3),)
Test input: hanoi(3, 1, 2, 3)
```

Test output: ((1, 2), (1, 3), (2, 3), (1, 2), (3, 1), (3, 2), (1, 2))

#### Question 5 Discussion

#### Iteration

- Please do not use iteration to implement hanoi.
- There is a way called backtracking if you are **really** bored.

#### Recursion

- Easier to implement? Of course
- The base case is very simple
- If there is only one disk, just move it from source to destination
- The recurrence relation is as follows:
- If there are more than one disks,
- move the most upper (n-1) disks from source to auxiliary
- move the most lower one from source to destination
- move the most upper (n-1) disks from auxiliary to destination

- Order of growth for time complexity is ?
- Order of growth for space complexity is ?

If time permits, we will go through this.

- This is the first problem of your midterm question 3.
- We think this is quite hard.
- Going through this is more for the benefits of those going for remidterm.

More details about the grill\_on\_flame here

```
def grill_on_flame(kebab, flame, at):
    if flame == "":
        return kebab
    else:
        kebab = grill_piece(kebab, at, int(flame[0]))
        return grill_on_flame(kebab, flame[1:], at + 1)
```

If you are wondering where is the definition for grill\_piece, do we really need the definition of that?

- Difficulty lies in the fact that we have to start from the middle.
- The pieces to grill and the times for grilling all depend on flame only.
- Now we need to define something to extract those information out.

- tail gives you the ability to repeat certain function n times on the same object.
- So the function we define should be grilling the piece at index at + n.
- And the function should be grilling that piece with time flame[n-1].

So here is what we should put in the <PRE> part.

```
def grill_piece_at(n, kebab):
    return grill_piece(kebab, at + n - 1, int(flame[n-1]))
```

So here are the answers: The <PRE> part is

```
def grill piece at(n, kebab):
```

- The <T1> part is: grill\_piece\_at
- The <T2> part is: *kebab*
- The <T3> part is: len(flame)

return grill piece (kebab, at + n - 1, int(flame[n-1]))

#### Feedback & more

• Slides + relevant material available at:

https://github.com/wangzexin/Teaching

• After the tutorial, if you have further questions:

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# Thank You

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