UROPS Project Presentation 2

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Chpter 11 Statistics of Python for Finance

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Today's Agenda

- Statistics
 - Normality test
 - Portfolio Optimization
 - Principal Component Analysis
 - Bayesian Regression

Changes due to different Python version

We are using Python 3.6 while the version in the book is Python 2.7 So here is a list of items to change

- print x now becomes print(x)
- dict.iteritems() now becomes dict.items()
- xrange now becomes range
- lambda (k, v) : (v, k) is no longer available
- instead we can only use: lambda x : (x[1], x[0])
- x / 2 is float division, while x // 2 is integer division

Installation requirements - pandas_datareader

We are going to install pandas_datareader instead of pandas.io.data

Reason being that: ImportError: The pandas.io.data module is moved to a separate package (pandas-datareader).

Also, Anaconda does not support direct installation of this new package.

Hence, here is one line of code which you can type in Anaconda Prompt.

conda install -c https://conda.anaconda.org/anaconda pandas-datareader

Chapter 11 Statistics

We shall go through these useful methods

- Normality test
- Portfolio theory
- Principal component analysis
- Bayesian Regression

Normality test - wrapper functions for np arrays

```
def normality_tests(arr):
    ''' Tests for normality distribution of given data set.
    Parameters
    ========
    array: ndarray
    object to generate statistics on
    '''
    print("Skew of data set %14.3f" % scs.skew(arr))
    print("Skew test p-value %14.3f" % scs.skewtest(arr)[1])
    print("Kurt of data set %14.3f" % scs.kurtosis(arr))
    print("Kurt test p-value %14.3f" % scs.kurtosistest(arr)[1])
    print("Norm test p-value %14.3f" % scs.normaltest(arr)[1])
```

Portfolio Optimization

Assumptions we made are:

- Stock prices follow CAPM mostly
- Use only close price of the stock (adj close)
- Use csv.reader instead of pandas in this section

Portfolio Optimization

We are going to optimize based on these:

- higher order statistics function
- maximization of Sharpe ratio MVE
- minimization of portfolio variance MVP
- Efficient Frontier
- Capital Market Line

Read stock data from CSV files

```
def readDataFromCSV(filename, noa):
    infile = open(filename, newline = '')
    reader = csv.reader(infile)
    dates = []
    stocks = [[] for x in range(noa)];
    for row in reader:
        if row[0] != "Date":
            dates.append(row[0])
            for index in range (noa):
                stocks[index].append(float(row[index+1]))
    infile.close()
    return stocks
```

Convert stock prices to returns

There is a bug in the code provided in the book. nparray.mean() will only calculate one average for the entire 2D array

```
def calculateReturnData(dataset):
    for stock in dataset:
        stock.reverse()
    returnData = []
    returnMean = []
    for stock in dataset:
        returns = []
        for i in range(1,len(stock)):
            returns.append(stock[i] / stock[i-1] - 1)
        returnData.append(returns)
        returnMean.append(np.mean(returns))
    returnData = np.array(returnData, np.float64)
    returnMean = np.array(returnMean, np.float64)
    return returnData, returnMean
```

Generate statistics function

We can create a high order function to generate statistics function for a given set of return data

```
def generate statistics(rets, retsMean):
    def statistics (weights):
        ''' Returns portfolio statistics.
        Parameters
        weights: array-like
        weights for different securities in portfolio
        Returns
        pret : float
        expected portfolio return
        pvol : float
        expected portfolio volatility
        pret / pvol : float
        Sharpe ratio for rf=0
        weights = np.array(weights)
        pret = np.sum(retsMean * weights) * 252
        pvol = np.sqrt(np.dot(weights.T, np.dot(np.cov(rets, bias=True) * 252, weights)))
        return np.array([pret, pvol, pret / pvol])
    return statistics
returnData, returnMean = calculateReturnData(readDataFromCSV("Close Prices Data.csv"),5)
stat = generate statistics(returnData, returnMean)
```

Optimize portfolio to maximise Sharpe ratio

Make use of a new library scipy.optimize Maximsie Sharpe ratio by minimizing negative Sharpe ratio

Return value is a dictionary. $w = optimize_portfolio_max_SR(stat, 5)$ w['x'] is the optimal portfolio

Optimize to minimise portfolio variance

Portfolio variance = $w^T \Sigma w$

Return value is a dictionary. $w = optimize_portfolio_min_Var(stat, 5)$ w['x'] is the optimal portfolio

Generate Efficient Frontier

We can set certain level of return to generate points on frontier.

```
def portfolio efficient frontier(statistics, noa, tret):
    min func var = lambda weights : statistics (weights) [1]
    cons = ({\frac{1}{2}}'type': 'eq', 'fun': lambda x: statistics(x)[0] - tret},
        {'type': 'eq', 'fun': lambda x: np.sum(x) - 1})
    bnds = tuple((0, 1) for x in range(noa))
    EWP = noa * [1. / noa,]
    return sco.minimize (min func var, EWP,
                         method='SLSQP', bounds=bnds, constraints=cons)
def create efficient frontier(statistics, noa):
    targetReturns = np.linspace(0.0, 0.25, 50)
    points = []
    for targetReturn in targetReturns:
        opts = portfolio efficient frontier(statistics, noa, targetReturn)
        w = opts['x']
        points.append(statistics(w))
    return points
```

Capital Market Line

We can solve a system of equations to obtain this line.

$$a = r_f$$

$$a + bx = f(x)$$

$$b = f'(x)$$

```
import scipy.optimize as sco
import scipy.interpolate as sci
def f(x):
    "" Efficient frontier function (splines approximation).""
    return sci.splev(x, tck, der=0)
def df(x):
    "" First derivative of efficient frontier function.""
    return sci.splev(x, tck, der=1)
def equations(p, rf=0.01):
    eq1 = rf - p[0]
    eq2 = rf + p[1] * p[2] - f(p[2])
    eq3 = p[1] - df(p[2])
    return eal, ea2, ea3
opt = sco.fsolve(equations, [0.01, 0.01, 0.01])
```

Principal Componenet Analysis

- Obtain data using pandas (initialization)
- Determine minimum number of components
- Create PCA Index

PCA - initialization

```
1 from sklearn.decomposition import KernelPCA
 2 import pandas datareader.data as web
 3 import numpy as np
 4 import pandas as pd
 5 def initialization():
      symbols = ['ADS.DE', 'ALV.DE', 'BAS.DE', 'BAYN.DE', 'BEI.DE',
6
7
8
9
           'BMW.DE', 'CBK.DE', 'CON.DE', 'DAI.DE', 'DB1.DE',
           'DBK.DE', 'DPW.DE', 'DTE.DE', 'EOAN.DE', 'FME.DE',
           'FRE.DE', 'HEI.DE', 'HEN3.DE', 'IFX.DE', 'LHA.DE',
           'LIN.DE', 'LXS.DE', 'MRK.DE', 'MUV2.DE', 'RWE.DE',
11
12
           'SAP.DE', 'SDF.DE', 'SIE.DE', 'TKA.DE', 'VOW3.DE',
           '^GDAXI'l
13
      data = pd.DataFrame()
14
      for sym in symbols:
15
          data[sym] = web.DataReader(sym, data source='yahoo')['Close']
16
      data = data.dropna()
17
      dax = pd.DataFrame(data.pop('^GDAXI'))
```

PCA - Obtain stock data

```
In [5]: data[data.columns[:6]].head()
Out[5]:
           ADS.DE
                   ALV.DE
                           BAS.DE
                                   BAYN.DE
                                            BEI.DE
                                                    BMW.DE
Date
2010-01-04
           38.505
                    88.54 44.850
                                     56.40
                                            46.445
                                                    32.050
2010-01-05
                                            46.200
           39.720
                    88.81
                           44.170
                                     55.37
                                                    32.310
2010-01-06
           39,400
                    89.50 44.450
                                     55.02
                                            46.165
                                                    32.810
2010-01-07
           39.745
                    88.47 44.155
                                     54.30
                                            45.700
                                                    33,100
2010-01-08 39.600
                    87.99
                           44.020
                                     53.82
                                            44.380
                                                    32,655
```

PCA - Determine number of components required

```
In [10]: len(pca.lambdas )
Out[10]: 881
In [11]: pca.lambdas [:10].round()
Out[11]:
array([ 34079., 5990., 5360., 2825., 2018., 848., 756.,
         531., 309., 226.])
In [12]: get_we(pca.lambdas )[:10]
Out[12]:
array( 0.63250034, 0.11117324, 0.0994747, 0.05242408, 0.03744675,
       0.01572997, 0.01403163, 0.00985717, 0.00573016, 0.00418554])
In [13]: get we(pca.lambdas )[:5].sum()
Out[13]: 0.93301911384645353
```

More then 93.3% of the variation is explained by the first five components!

PCA - create index

```
19 def create PCA index(data, dax):
      scale function = lambda x: (x - x.mean()) / x.std() # convenience function
20
21
      get we = lambda x: x / x.sum() # convenience function
22
      pca = KernelPCA().fit(data.apply(scale function)) # multiple components
23
24
      pca = KernelPCA(n components=1).fit(data.apply(scale function)) # single component
25
      dax['PCA 1'] = pca.transform(-data)
26
27
      pca = KernelPCA(n components=5).fit(data.apply(scale function)) # five components
28
      pca components = pca.transform(-data)
29
      weights = get we(pca.lambdas )
30
      dax['PCA 5'] = np.dot(pca components, weights)
31
32
      cut date = '2011/7/1'
33
      early pca = dax[dax.index < cut date]['PCA 5']
34
      early reg = np.polyval(np.polyfit(early_pca,
35
      dax['^GDAXI'][dax.index < cut date], 1).early pca)</pre>
36
37
      late pca = dax[dax.index >= cut date]['PCA 5']
38
      late reg = np.polvval(np.polvfit(late pca.
39
      dax['^GDAXI'][dax.index >= cut date], 1),late pca)
```

Bayesian Regression

- Trouble shooting for package Pymc3
- Building of model
- Gaussian random walk
- Uniform model
- Optimization

If this ValueError happens, go to the file font_manager.py

```
path = _getfullpathname(path)
ValueError: _getfullpathname: embedded null character
```

and add in one line of code in the function win32InstalledFonts

```
try:
                for i in range(winreg.OuervInfoKev(local)[1]):
224
                    try:
226
                        key, direc, any = winreg.EnumValue( local, j)
                        if not is string like(direc):
                            continue
                        if not os.path.dirname(direc):
230
                            direc = os.path.join(directory, direc)
231
                        direc = direc.split('\0', 1)[0]
                        direc = os.path.abspath(direc).lower()
                        if os.path.splitext(direc)[1][1:] in fontext:
234
                            items[direc] = 1
235
                    except EnvironmentError:
236
                        continue
                    except WindowsError:
                        continue
239
                    except MemoryError:
240
                        continue
241
                return list(six.iterkeys(items))
242
           finally:
243
                winreg.CloseKey(local)
```

Building model

If you can run this without having AttributeError,

```
3 import pymc as pm
 4 import numpy as np
 5 np.random.seed(1000)
 7x = np.linspace(0, 10, 500)
 8v = 4 + 2 * x + np.random.standard normal(len(x)) * 2
10 reg = np.polyfit(x, y, 1)
12 with pm.Model() as model:
     # model specifications in PvMC3
14
     # are wrapped in a with statement
     # define priors
      alpha = pm.Normal('alpha', mu=0, sd=20)
      beta = pm.Normal('beta', mu=0, sd=20)
      sigma = pm.Uniform('sigma', lower=0, upper=10)
      # define linear regression
      y est = alpha + beta * x
      # define likelihood
      likelihood = pm.Normal('v', mu=v est, sd=sigma, observed=v)
      # inference
24
      start = pm.find MAP()
      # find starting value by optimization
      step = pm.NUTS(state=start)
      # instantiate MCMC sampling algorithm
      trace = pm.sample(100, step, start=start, progressbar=False)
      # draw 100 posterior samples using NUTS sampling
```

If this AttributeError (__exit__) happens,

```
with pm.Model() as model:
AttributeError: __exit__
```

that means you are using a version of Pymc3 in which with statement is not incorporated yet. You should go to Anaconda prompt and type: conda install -c conda-forge pymc3

If this AttributeError (TransformedVar) happens,

```
model_randomwalk.TransformedVar('sigma_alpha',
AttributeError: 'Model' object has no attribute 'TransformedVar'
```

when you are running the model below

the reason is that the attribute TransformedVar is removed from Pymc3.

If the AttributeError (TransformVar) happens, one fix is to use Exponential attribute of the package itself.

```
4 model_randomwalk = pm.Model()
5 with model_randomwalk:
6  # std of random walk best sampled in log space
7  sigma = pm.Exponential('sigma', 1./.02, testval = .1)
```

Trouble shooting for package Zipline

This package seems to be conflicting with python 3.5.0 and above

```
with pm.Model() as model:
AttributeError: __exit__
```

so it is not feasible for us to use zipline, instead we can use pandas just like in the previous section

Gaussian walk using pandas data

This is an example of gaussian walk model using pandas library data

```
1 import pandas datareader.data as web
 2 import pandas as pd
 3 import numpy as no
 4 import pymc3 as pm
 6 symbols = ['GLD', 'GDX']
 7 data = pd.DataFrame()
 8 for sym in symbols:
      data[sym] = web.DataReader(sym, data source='yahoo')['Close']
10 data = data.dropna()
12 #from pymc3.distributions.timeseries import GaussianRandomWalk
13 # to make the model simpler, we will apply the same coefficients
14 # to 50 data points at a time
15 subsample alpha = 50
16 subsample beta = 50
17 model randomwalk = pm.Model()
18 with model randomwalk:
      # std of random walk best sampled in log space
      sigma alpha = pm.Exponential('sigma alpha', 1./.02, testval = .1)
      sigma beta = pm.Exponential('sigma beta', 1./.02, testval = .1)
23 with model randomwalk:
      alpha = pm.GaussianRandomWalk('alpha', sigma alpha**-2,
                                     shape= len(data) // subsample alpha)
      beta = pm.GaussianRandomWalk('beta', sigma beta**-2,
                                    shape= len(data) // subsample beta)
      # make coefficients have the same length as prices
      alpha r = np.repeat(alpha, subsample alpha)
      beta r = np.repeat(beta, subsample beta)
```

Add pm. in front of GaussianRandomWalk

Uniform model - errorneous

There is error occurred when we try to multiply two vectors with different lengths.

This error has not been solved.

Bayesian regression - optimization

```
import scipy.optimize as sco
with model_randomwalk:
    # first optimize random walk
    start = pm.find_MAP(vars=[alpha, beta], fmin=sco.fmin_l_bfgs_b)
    # sampling
    step = pm.NUTS(scaling=start)
    trace_rw = pm.sample(100, step, start=start, progressbar=False)
```

Thank You

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