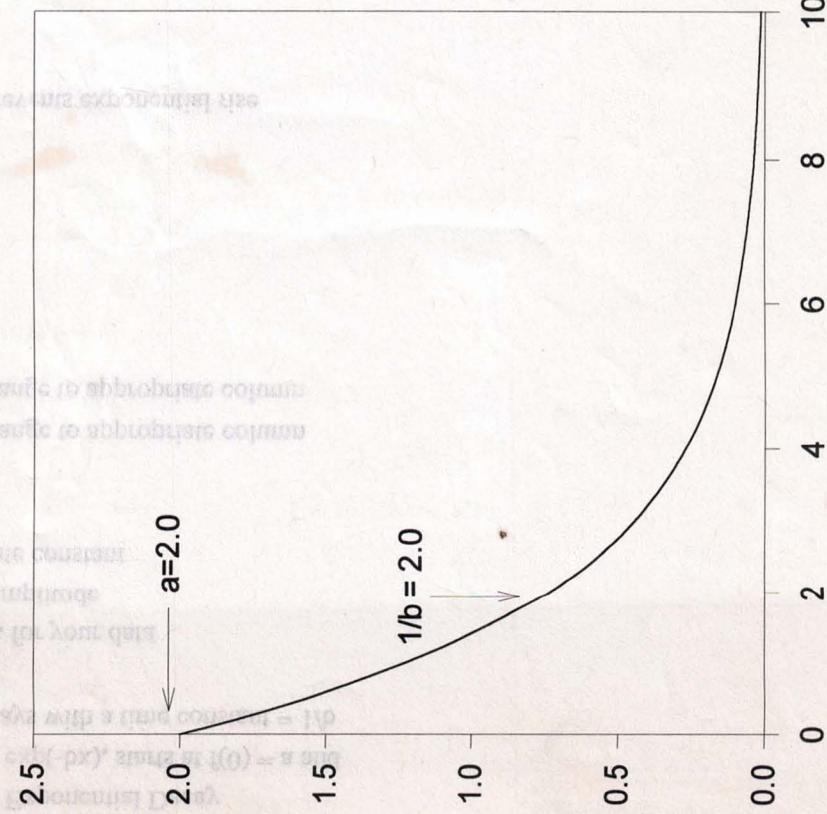


FIT

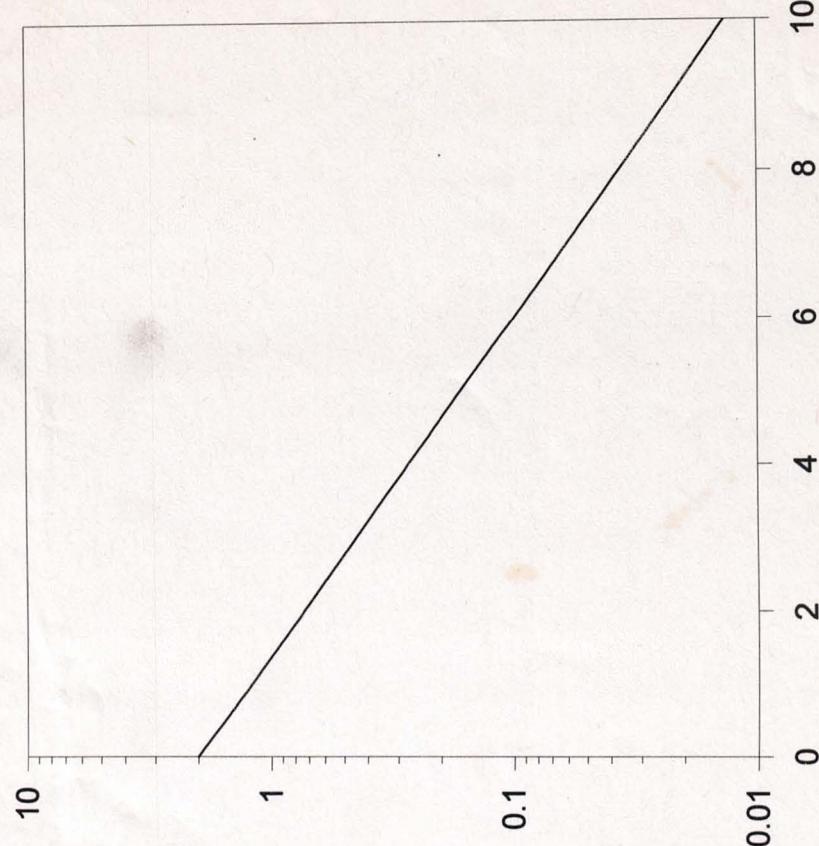
## Single Exponential Decay

$$a = 2.0, b = 0.5$$

Linear Axis Scale



Logarithmic Y Axis Scale



exp decay 1. SPW

SPW/MATH/FIT 1

[Parameters] ;Single Exponential Decay

;f=a exp(-bx), starts at f(0) = a and  
;decays with a time constant = 1/b

;Modify these values for your data

a=1 ;amplitude  
b=.1 ;rate constant

[Variables]

x=col(1) ;change to appropriate column  
y=col(2) ;change to appropriate column

[Equations]

f = a\*exp(-b\*x)  
fit f to y

[Constraints]

b > 0 ;prevents exponential rise

Exponential

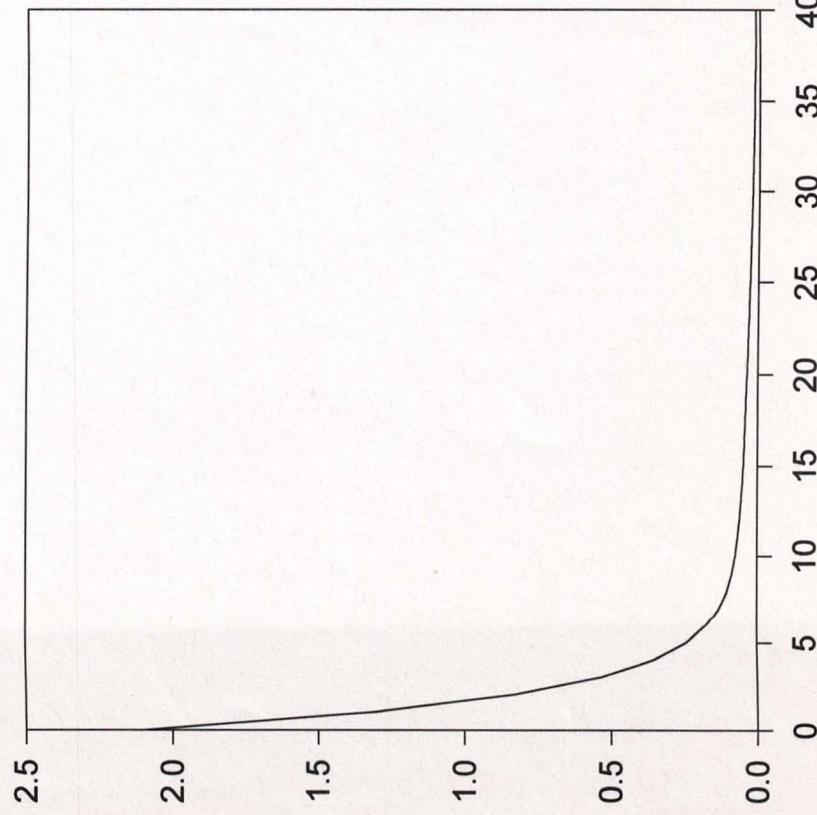
$$f = a + b \cdot \exp(cx)$$

### Double Exponential Decay

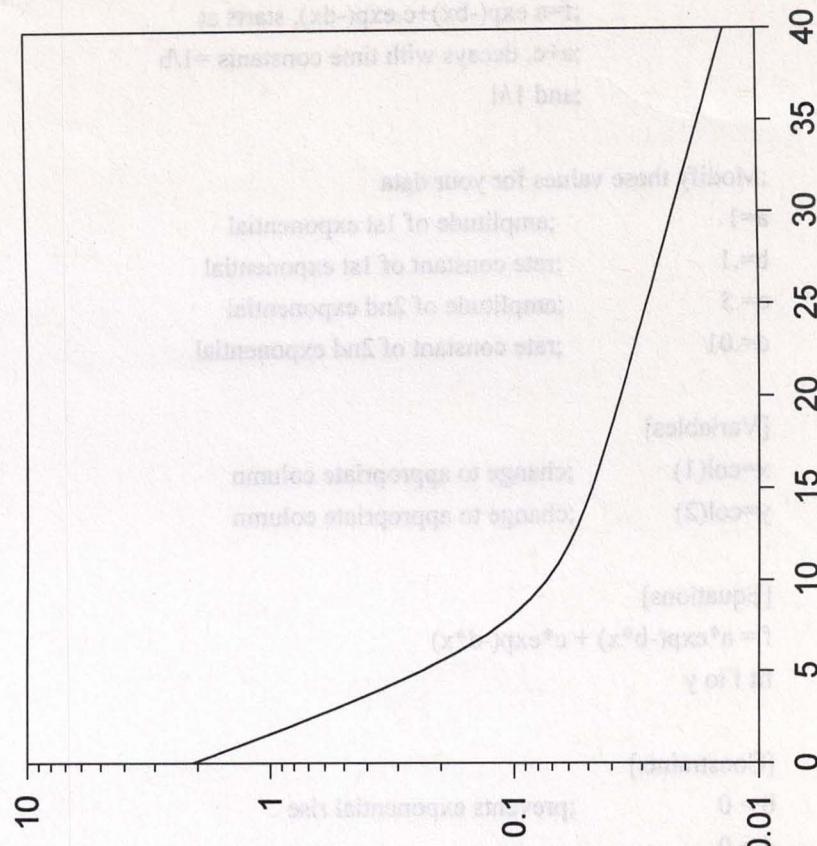
$$a = 2.0, b = 0.5$$

$$c = 0.1, d = 0.05$$

### Linear Y Axis Scale



### Logarithmic Axis Scale



[Parameters] ;Double Exponential Decay

;f=a exp(-bx)+c exp(-dx), starts at  
;a+c, decays with time constants =1/b  
;and 1/d

;Modify these values for your data

a=1 ;amplitude of 1st exponential  
b=.1 ;rate constant of 1st exponential  
c=.5 ;amplitude of 2nd exponential  
d=.01 ;rate constant of 2nd exponential

[Variables]

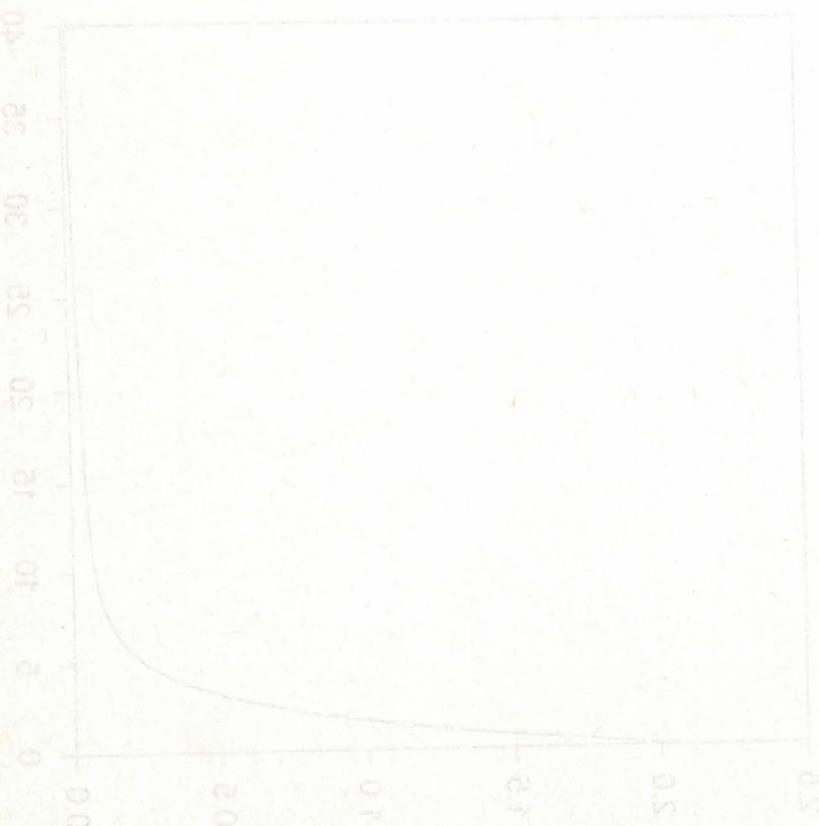
x=col(1) ;change to appropriate column  
y=col(2) ;change to appropriate column

[Equations]

f = a\*exp(-b\*x) + c\*exp(-d\*x)  
fit f to y

[Constraints]

b > 0 ;prevents exponential rise  
d > 0



Logarithmic Y axis Scale

Linear Y axis Scale

c = 0.1, d = 0.08  
b = 0.1, a = 0.9  
c = 0.5, d = 0.2  
b = 0.5, a = 0.5

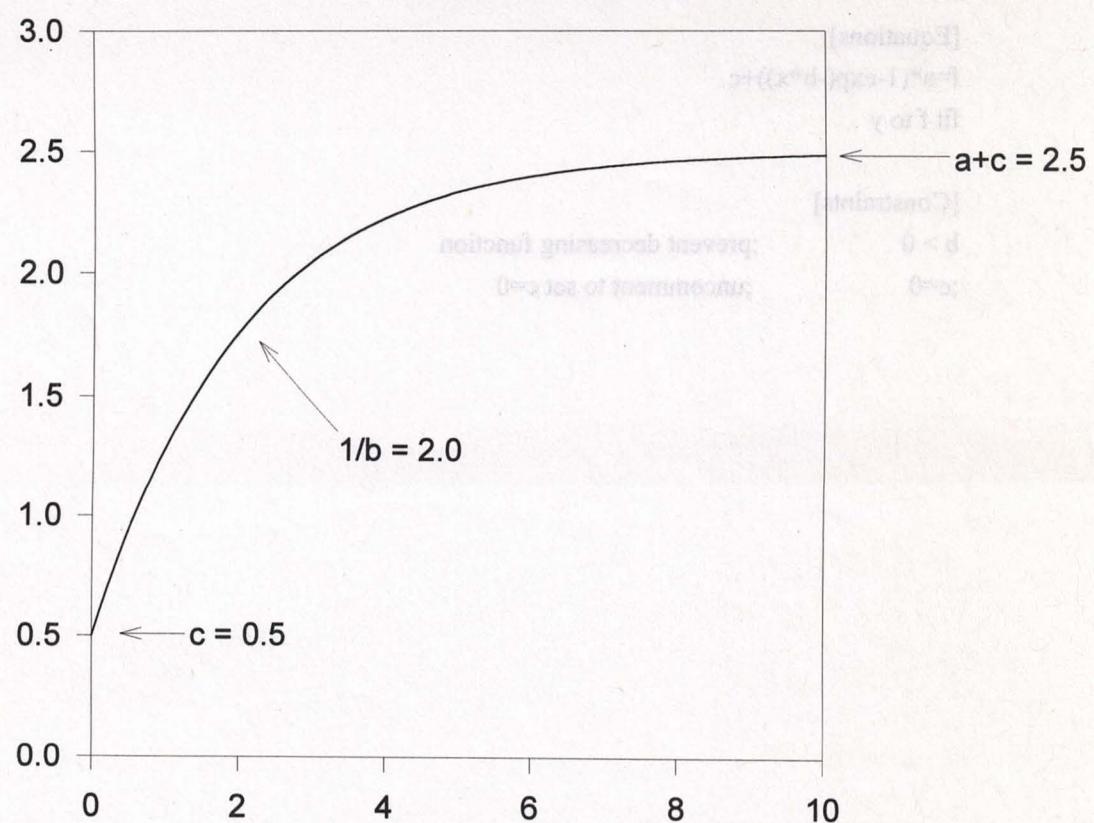
Double Exponential Decay

# Exprise - SPW

## Exponential Rise to Maximum

$$a = 2.0, b = 0.5$$

$$c = 0.5$$



[Parameters] ;Exponential Rise to Maximum

;f=a[1-exp(-bx)]+c, starts at c,  
;rises to a+c with time constant=1/b

;Modify these values for your data

a=1 ;amplitude of exponential

b=.1 ;rate constant

c=1 ;zero intercept

[Variables]

x=col(1) ;change to appropriate column

y=col(2) ;change to appropriate column

[Equations]

f=a\*(1-exp(-b\*x))+c

fit f to y

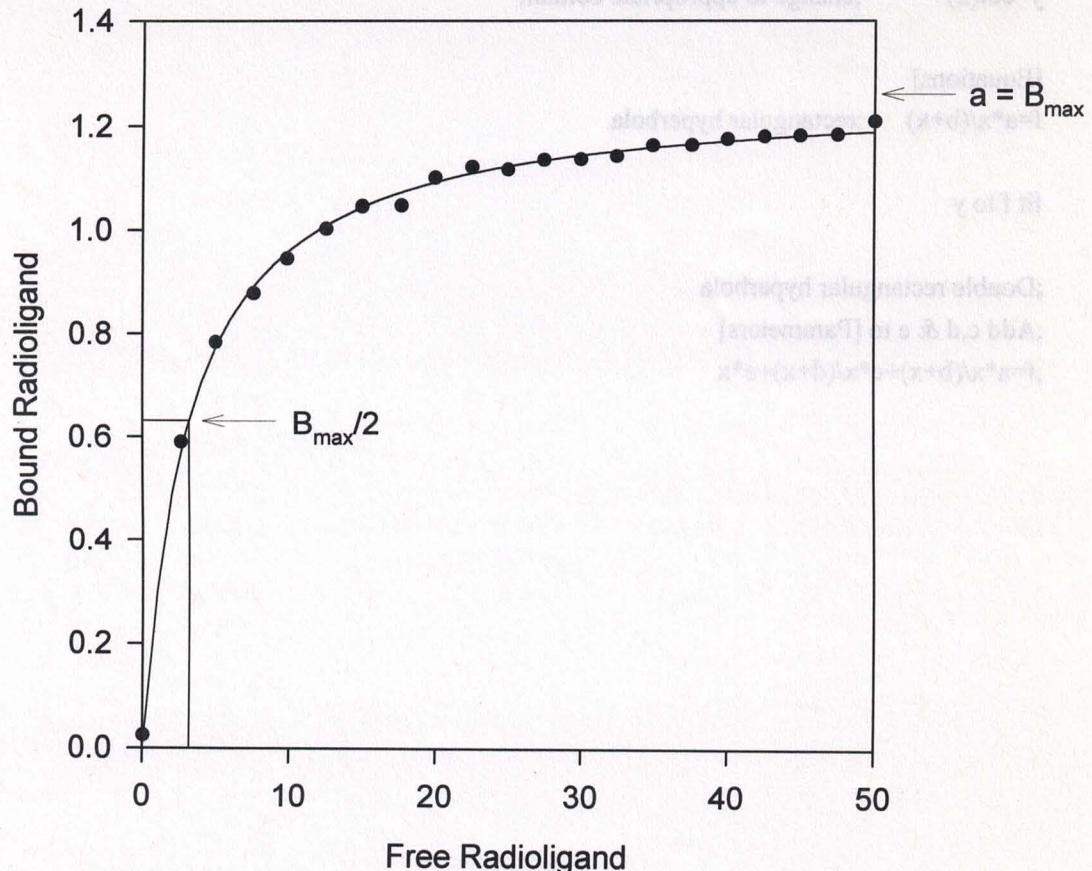
[Constraints]

b > 0 ;prevent decreasing function

;c=0 ;uncomment to set c=0

# Hyperbol · Spw

## Hyperbolic Function



Parameters] ;Hyperbolic Functions

; (Saturating Binding Curves)  
;  $f = a * x / (b + x)$ , starts at 0, rises to  
; a (Bmax) and for  $x = b$  (KD) is  $a/2$ .

; Modify these values for your data

a=1 ;maximum value (Bmax)  
b=.5 ;dissociation constant (KD)

[Variables]

x=col(1) ;change to appropriate column  
y=col(2) ;change to appropriate column

[Equations]

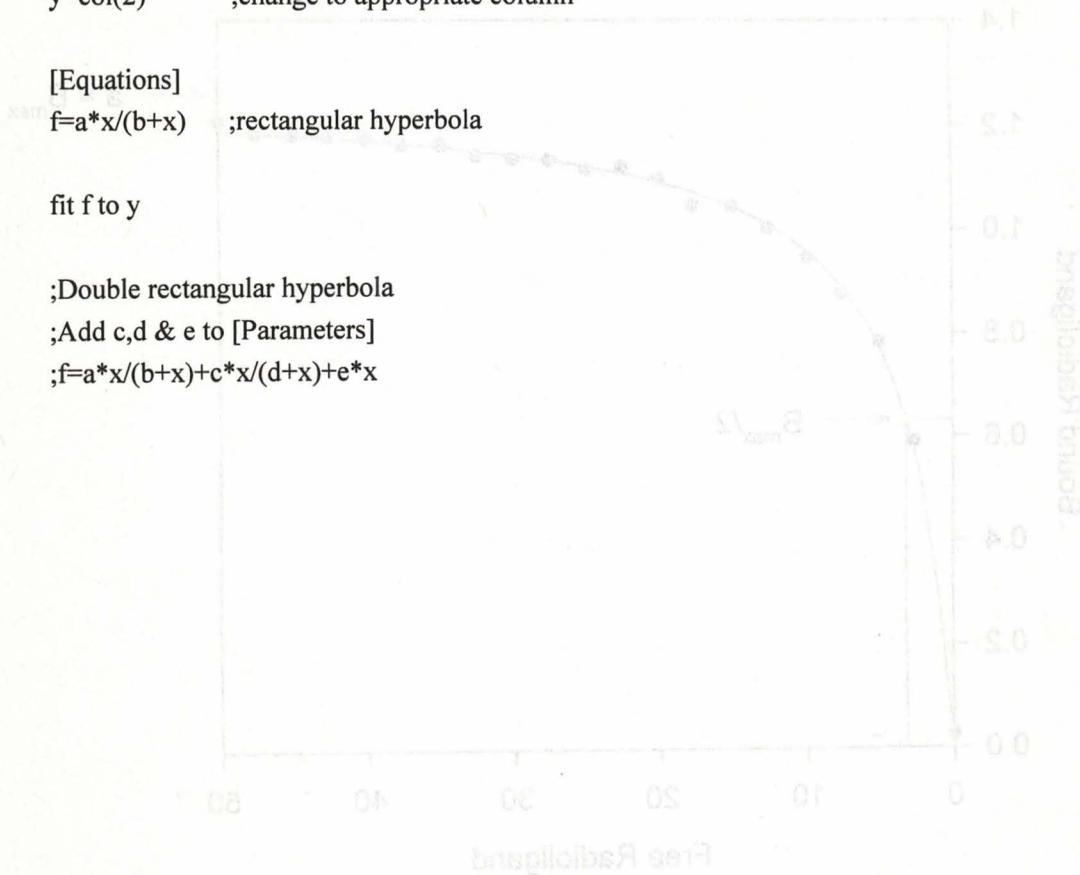
$f = a * x / (b + x)$  ;rectangular hyperbola

fit f to y

; Double rectangular hyperbola

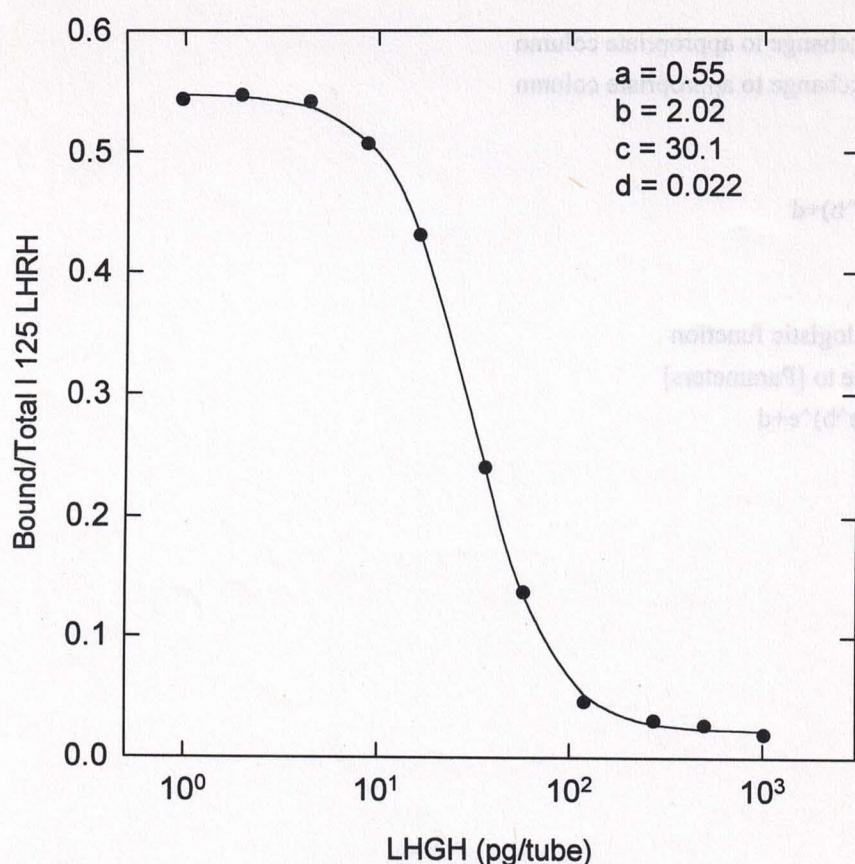
; Add c,d & e to [Parameters]

$f = a * x / (b + x) + c * x / (d + x) + e * x$



fit  
logistic-spw

## Logistic Function



[Parameters] ;4 Parameter Logistic Function

;f=(a-d)/[1+(x/c)^b]+d, if b>0 it  
;starts at a and falls to d. If b<0  
;it starts at d and rises to a.

;Modify these values for your data

a=.5 ;asymptotic maximum  
b=1.5 ;slope parameter, b>0 gives slope<0  
c=45 ;value at inflexion point  
d=.01 ;asymptotic minimum

[Variables]

x=col(1) ;change to appropriate column  
y=col(2) ;change to appropriate column

[Equations]

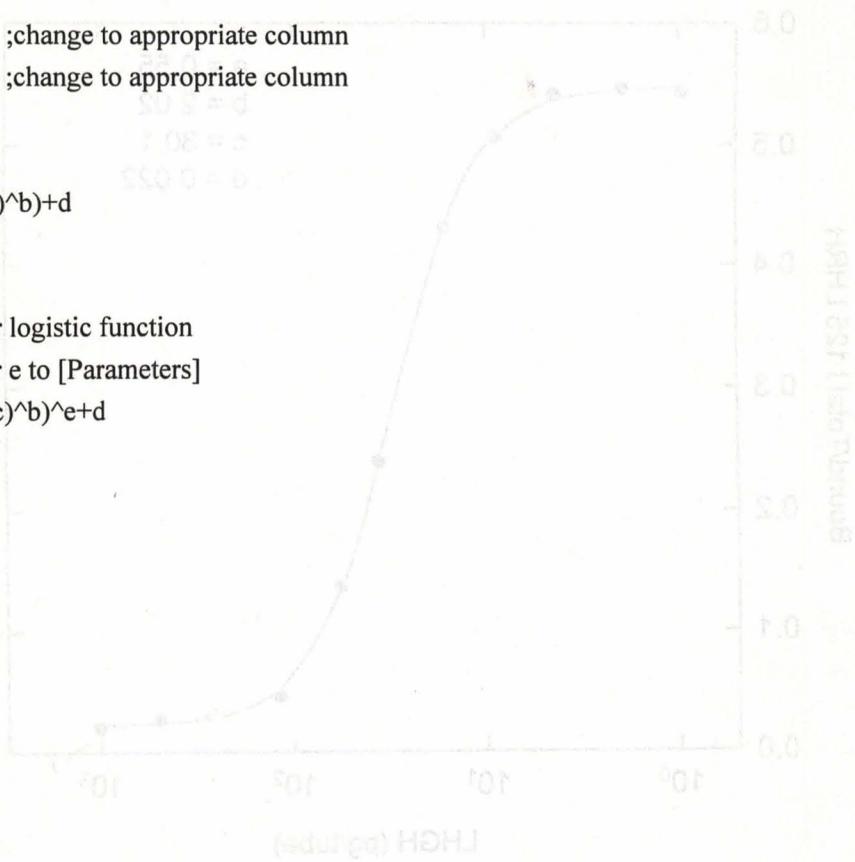
f=(a-d)/(1+(x/c)^b)+d

fit f to y

;Five parameter logistic function

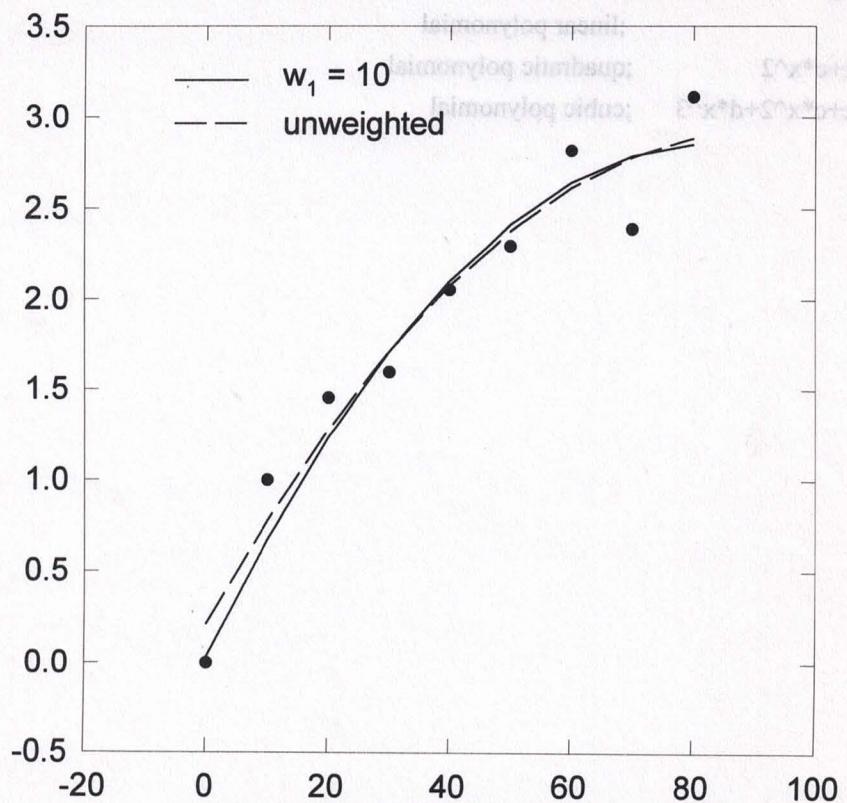
;Add parameter e to [Parameters]

;f=(a-d)/(1+(x/c)^b)^e+d



Poly. SPW

### Quadratic Polynomial Fit of signals; Forced Through Zero Using Weighting



### [Parameters] ;Polynomial Curve Fits

;These fits may also be obtained  
;using the Regression feature

a=1 ;zero intercept  
b=2 ;slope  
;c=1 ;used for alternate models below  
;d=2 ;ditto

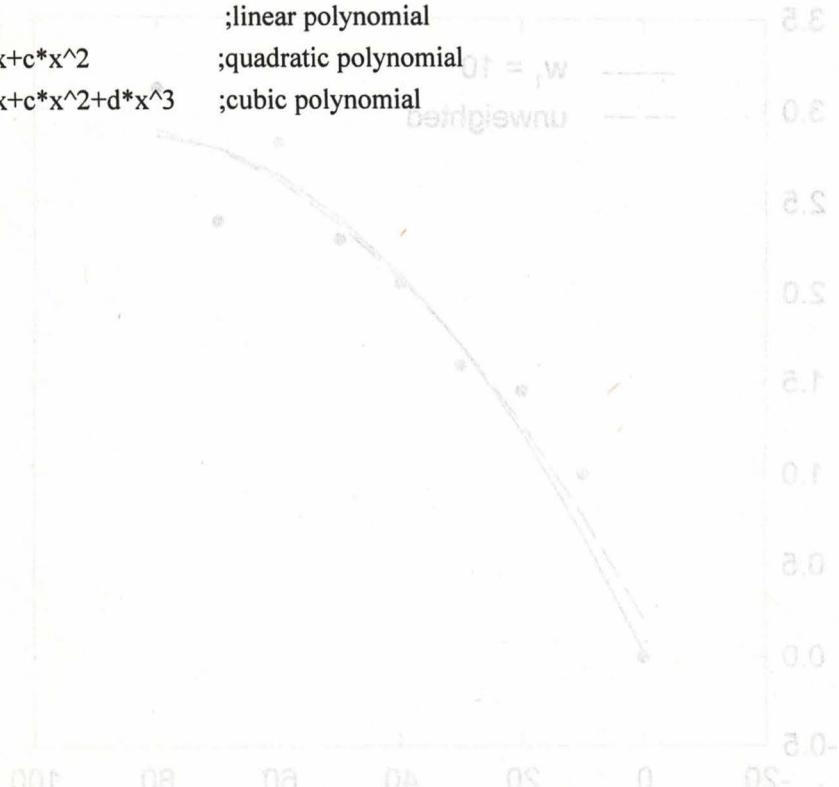
### [Variables]

x=col(1) ;change to appropriate column  
y=col(2) ;change to appropriate column

### [Equations]

f = a+b\*x ;linear polynomial  
;f = a+b\*x+c\*x^2 ;quadratic polynomial  
;f = a+b\*x+c\*x^2+d\*x^3 ;cubic polynomial

fit f to y



spw\math\

[residuals]

A: moments Cumulative distribution of points

S: sample size Estimated values for t-distribution

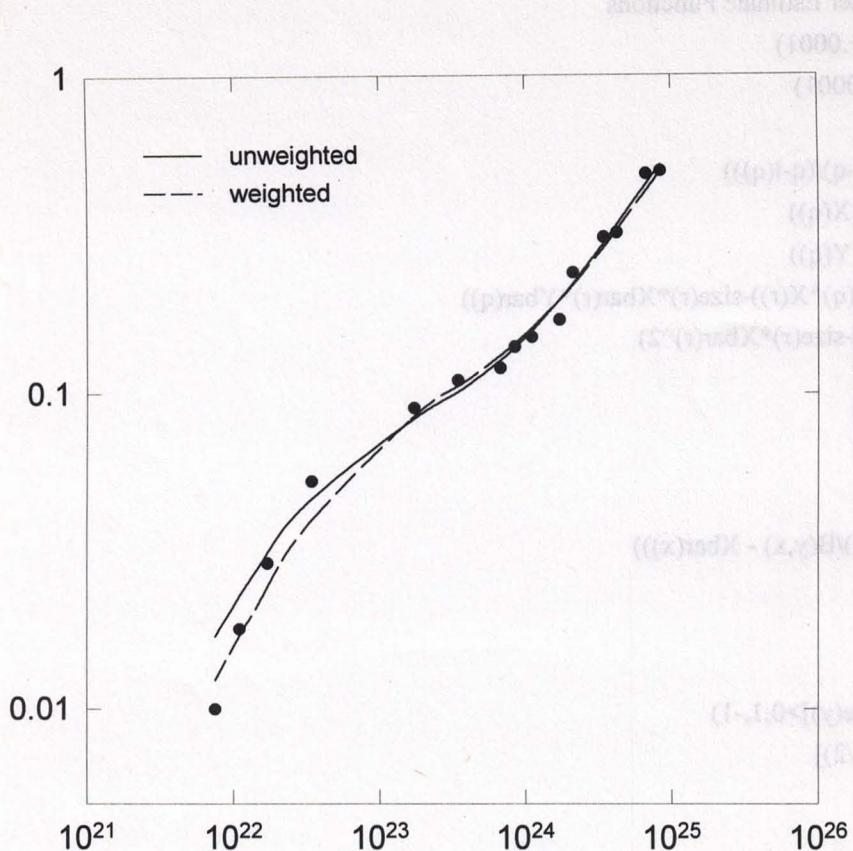
T: standard deviation

residuals in V.

(I) log=2

(C) log=7

## Advanced - SPW



$$A = 0.1$$

$$CD = -1$$

$$db = -1$$

$$\begin{aligned} X &= \text{col}(1) + 1e-24 \\ Y &= \text{col}(2) \\ W &= 1/\text{col}(2)^2 \end{aligned} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \text{Variables}$$

$$f = 1 - \exp(-X * (db + CD * X) / (X + A))$$

fit f to y with weight w

### [Variables]

```
;Automatic Computation of Initial  
;Parameter Estimates for 4 Parameter  
;Logistic Function
```

### ;Variables

```
x=col(1)  
y=col(2)
```

### ;Initial Parameter Estimate Functions

```
u(q)=(max(q)+.0001)  
l(q)=(min(q)-.0001)  
X(q)=log(q)  
Y(q)=log((u(q)-q)/(q-l(q)))  
Xbar(q)=mean(X(q))  
Ybar(q)=mean(Y(q))  
B(q,r)=(total(Y(q)*X(r))-size(r)*Xbar(r)*Ybar(q))  
/(total(X(r)^2)-size(r)*Xbar(r)^2)
```

### [Parameters]

```
a=u(y)  
b=B(y,x)  
c=10^(-(Ybar(y)/B(y,x) - Xbar(x)))  
d=l(y)
```

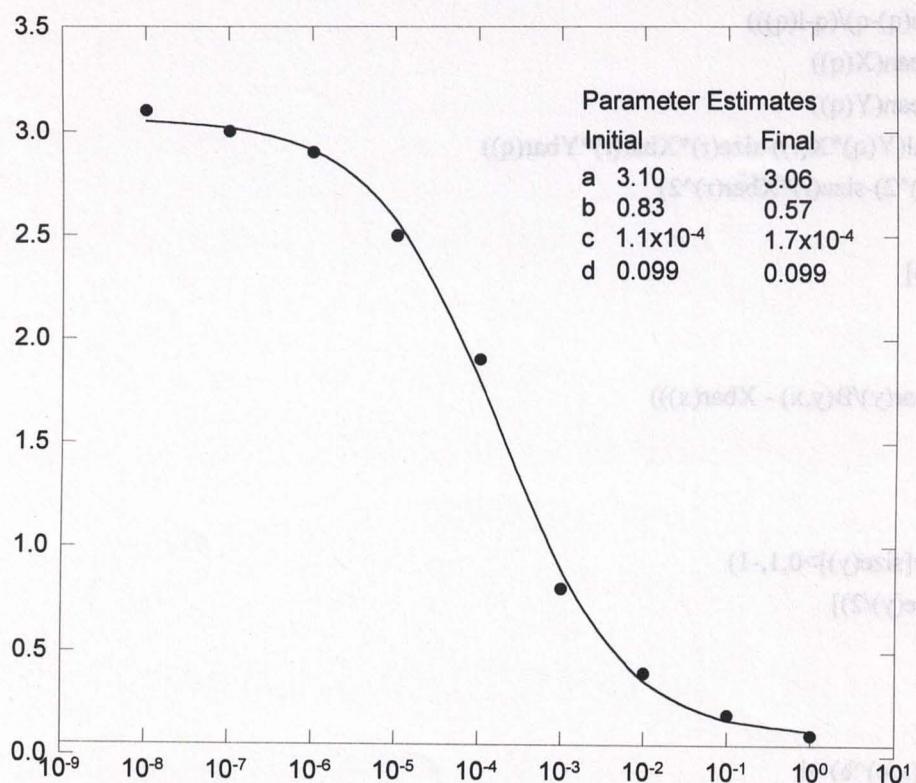
```
;a=max(y)  
;b;if(y[1]-y[size(y)]>0,1,-1)  
;c=x[int(size(y)/2)]  
;d=min(y)
```

### [Equations]

```
f=(a-d)/(1+(x/c)^b)+d  
fit f to y
```

automat-spw

### Logistic Function Fit Using Automatic Initial Parameter Estimates



[Variables]

;Automatic Computation of Initial  
;Parameter Estimates for 4 Parameter  
;Logistic Function

;Variables

x=col(1)  
y=col(2)

;Initial Parameter Estimate Functions

u(q)=(max(q)+.0001)  
l(q)=(min(q)-.0001)  
X(q)=log(q)  
Y(q)=log((u(q)-q)/(q-l(q)))  
Xbar(q)=mean(X(q))  
Ybar(q)=mean(Y(q))  
B(q,r)=(total(Y(q)\*X(r))-size(r)\*Xbar(r)\*Ybar(q))  
/(total(X(r)^2)-size(r)\*Xbar(r)^2)

[Parameters]

a=u(y)  
b=B(y,x)  
c=10^(-(Ybar(y)/B(y,x) - Xbar(x)))  
d=l(y)

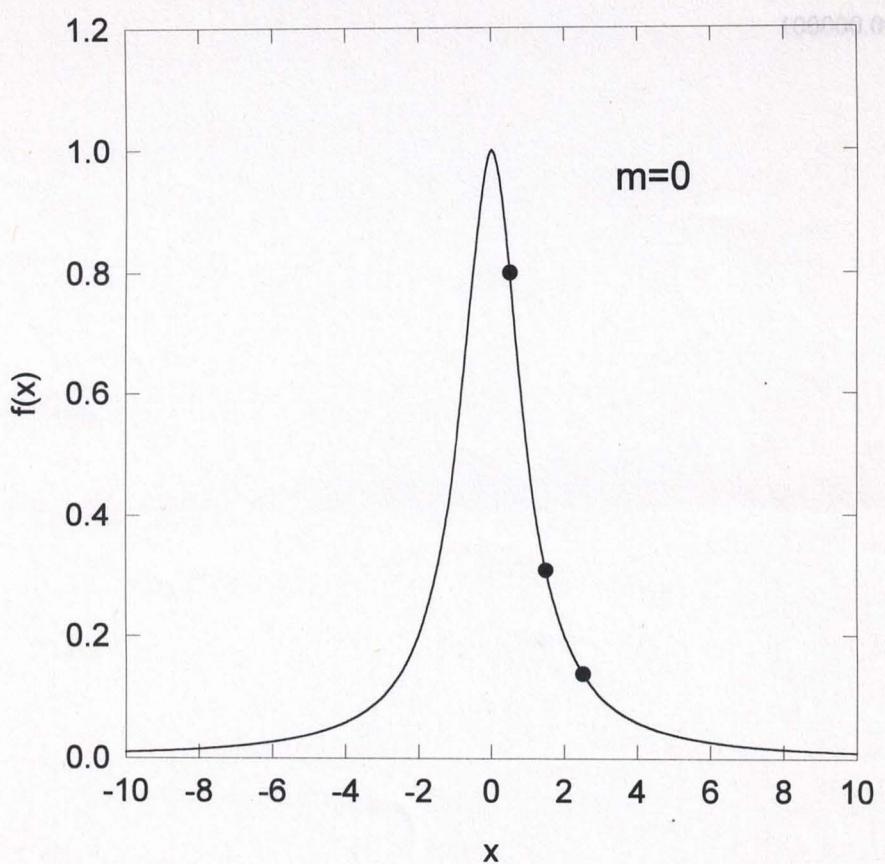
;a=max(y)  
;b;if(y[1]-y[size(y)]>0,1,-1)  
;c=x[int(size(y)/2)]  
;d=min(y)

[Equations]

f=(a-d)/(1+(x/c)^b)+d  
fit f to y

```
{GaussianFit  
000:=a;  
[x]:=xV  
(.)ico=x  
(.)eo=(  
X-eo)(  
[Equation]  
( $\Sigma$ ^n (1+(x-a)^2))  
( $\Sigma$ ^n (1+(x-a)^2))  
[Conversion]
```

fit-exp1-spw



[Parameters]

m=1000

[Variables]

x=col(1)

y=col(2)

[Equations]

f=1/(1+(x-m)^2)

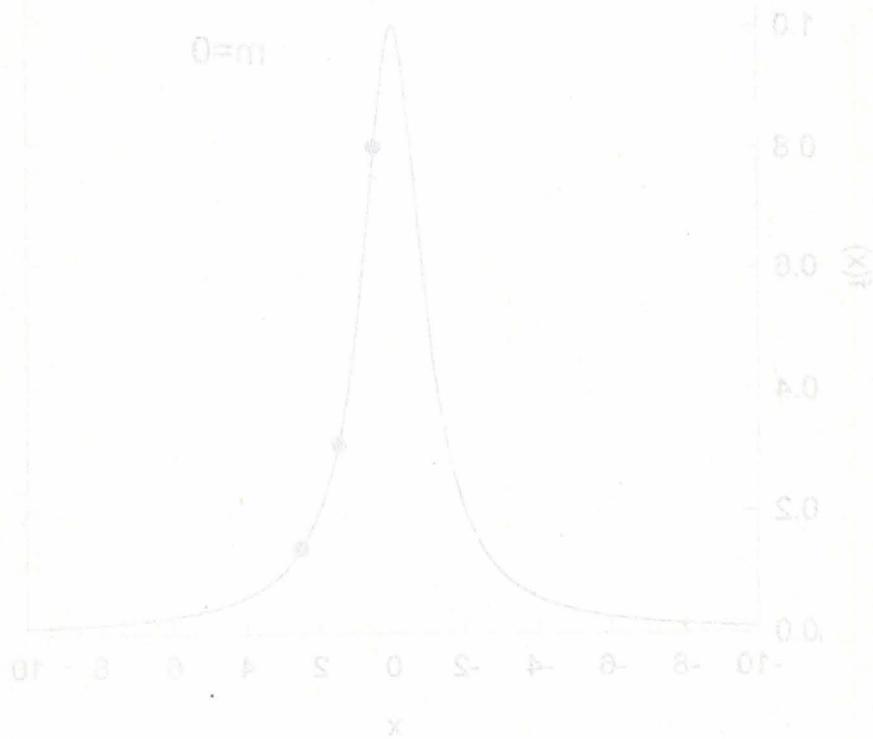
fit f to y

[Constraints]

[Options]

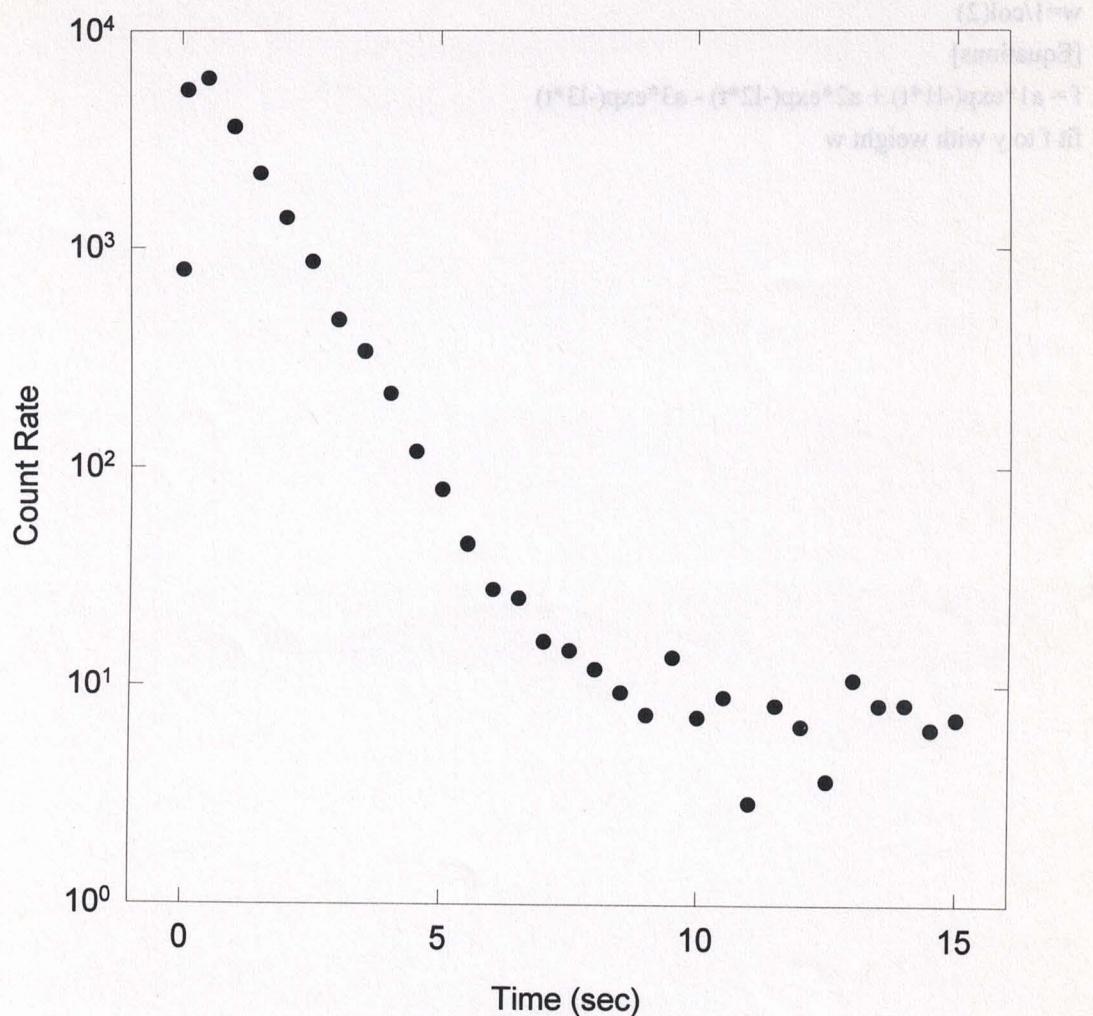
:stepsize=0.000001

:tolerance=0.000001



[fitter] = f  
[fitter] = f<sub>a</sub>  
[fitter] = f<sub>b</sub>  
[fitter] = f<sub>c</sub>  
[fitter] = f<sub>d</sub>  
[fitter] = f<sub>e</sub>  
[fitter] = f<sub>f</sub>  
[fitter] = f<sub>g</sub>  
[fitter] = f<sub>h</sub>  
[fitter] = f<sub>i</sub>  
[fitter] = f<sub>j</sub>  
[fitter] = f<sub>k</sub>  
[fitter] = f<sub>l</sub>  
[fitter] = f<sub>m</sub>  
[fitter] = f<sub>n</sub>  
[fitter] = f<sub>o</sub>  
[fitter] = f<sub>p</sub>

fit-exp2.spw



[Parameters]

a1=10000

a2=10

a3=10010

l1=1

l2=.01

l3=10

[Variables]

t=col(1)

y=col(2)

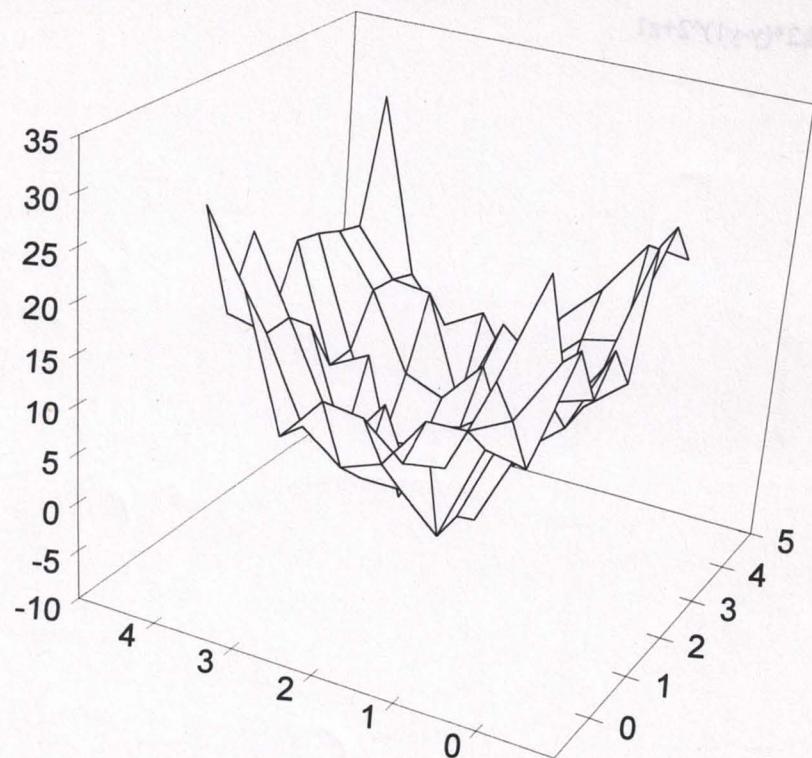
w=1/col(2)

[Equations]

f = a1\*exp(-l1\*t) + a2\*exp(-l2\*t) - a3\*exp(-l3\*t)

fit f to y with weight w

(cos) emit



[Parameters]

k1=2

k2=4

x1=2

y1=2

z1=1

[Variables]

x=col(1)

y=col(2)

z=col(3)

[Equations]

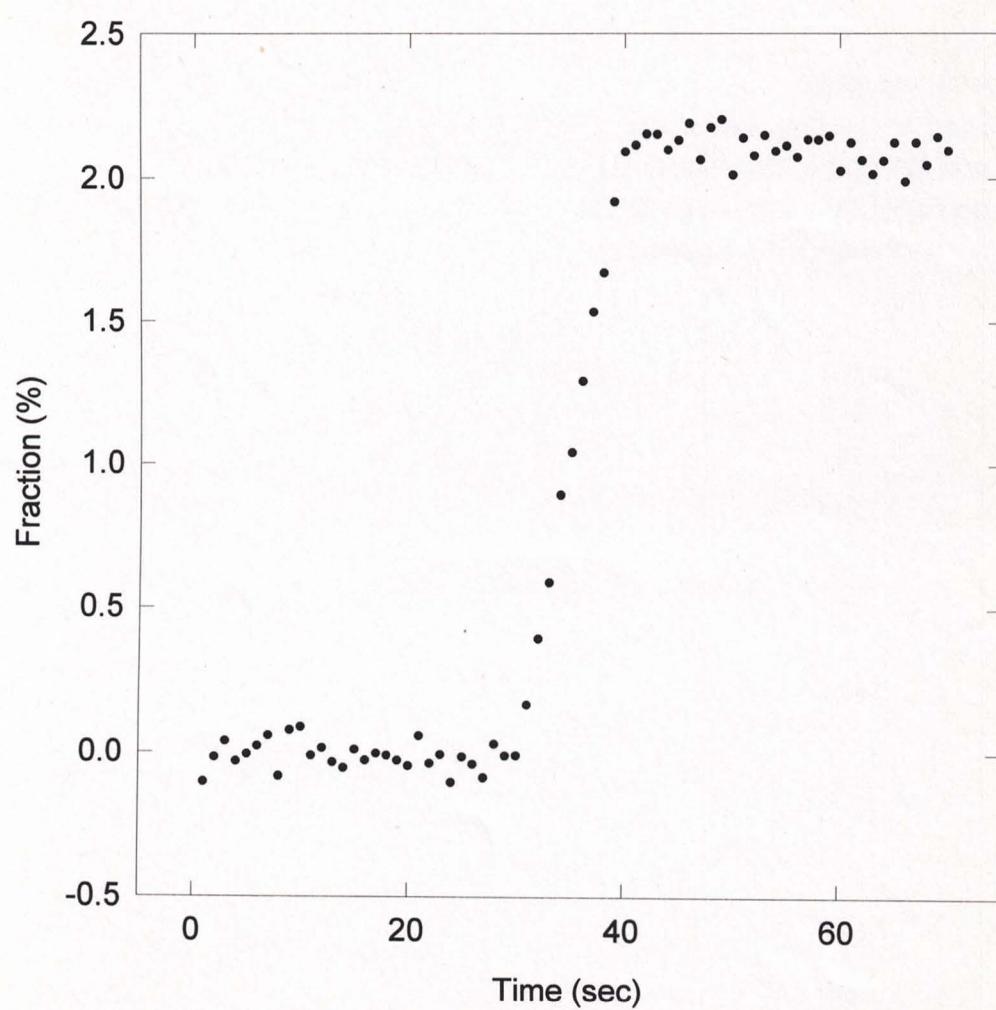
f=k1\*(x-x1)^2+k2\*(y-y1)^2+z1

fit f to z

[Constraints]

[Options]

fit-exp4.spw



[Parameters]

x1 = 0.0

x2 = 0.0

x3 = 2.1

x4 = 2.1

T1 = 30

T2 = 40

[Variables]

y=col(2)

t=col(1)

[Equations]

t1 = 1

t4 = 70

f = if(t <= T1, region1(t),

    if(t <= T2, region2(t), region3(t)))

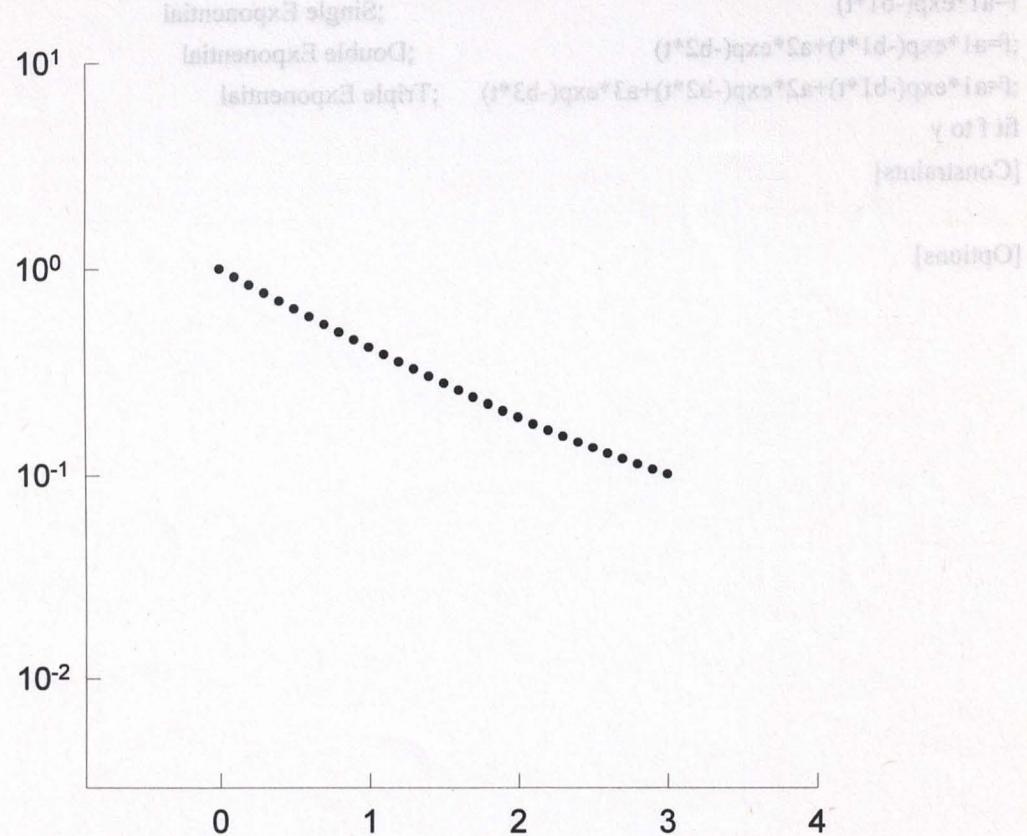
region1(t) = (x1\*(T1-t) + x2\*(t-t1))/(T1-t1)

region2(t) = (x2\*(T2-t) + x3\*(t-T1))/(T2-T1)

region3(t) = (x3\*(t4-t) + x4\*(t-T2))/(t4-T2)

fit f to y

fit-exp<sup>t</sup>.spw



[Parameters]

a1=1  
b1=1  
;a2=.1  
;b2=.1  
;a3=.01  
;b3=.01

[Variables]

t=col(1)  
y=col(2)  
;t=col(3)  
;y=col(4)

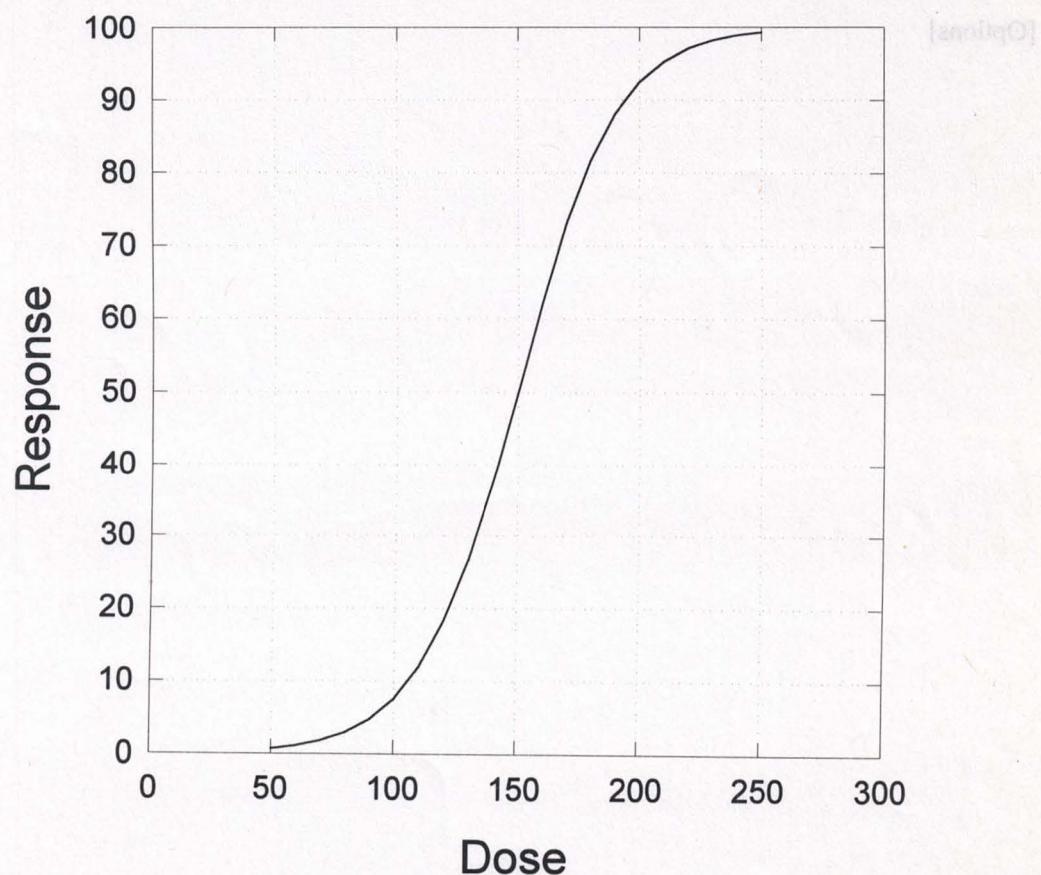
[Equations]

f=a1\*exp(-b1\*t) ;Single Exponential  
;f=a1\*exp(-b1\*t)+a2\*exp(-b2\*t) ;Double Exponential  
;f=a1\*exp(-b1\*t)+a2\*exp(-b2\*t)+a3\*exp(-b3\*t) ;Triple Exponential

fit f to y

[Constraints]

[Options]



[Parameters]

x=150

[Variables]

y=0

[Equations]

p1=100.96

p2=-.05010

p3=148.96

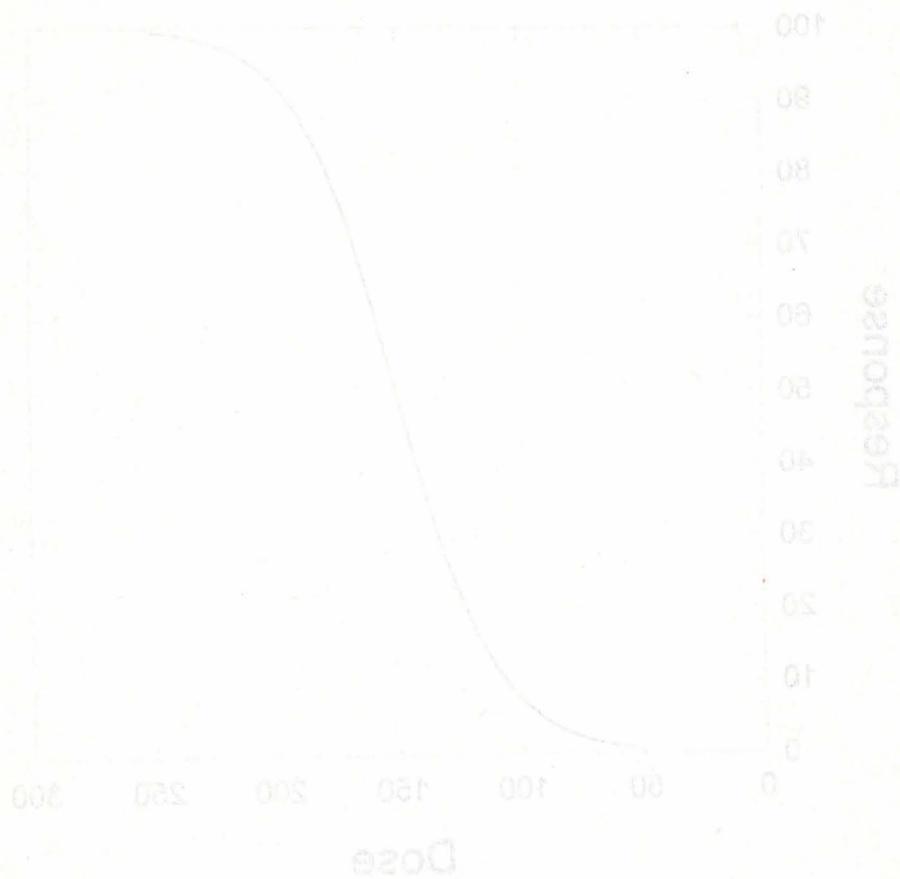
p4=-1.2080

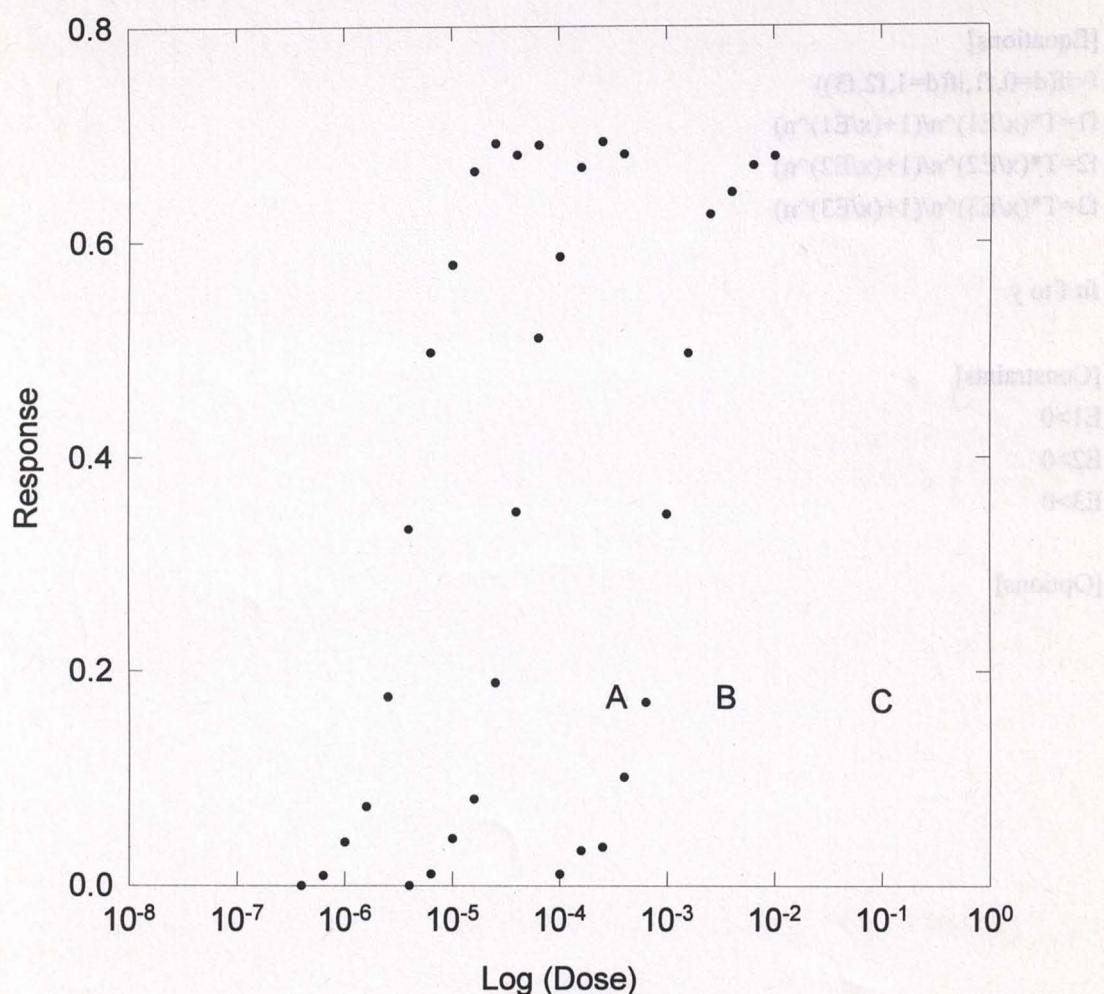
f=p1/(1+exp(p2\*(x-p3)))+p4-50

fit f to y

[Constraints]

[Options]





[Parameters]

T=1  
n=2  
E1=1e-6  
E2=1e-5  
E3=1e-4

[Variables]

x=col(7) ;concatonated x data  
y=col(8) ;concatonated y data  
d=col(9) ;function identifier

[Equations]

f=if(d=0,f1,if(d=1,f2,f3))  
f1=T\*(x/E1)^n/(1+(x/E1)^n)  
f2=T\*(x/E2)^n/(1+(x/E2)^n)  
f3=T\*(x/E3)^n/(1+(x/E3)^n)

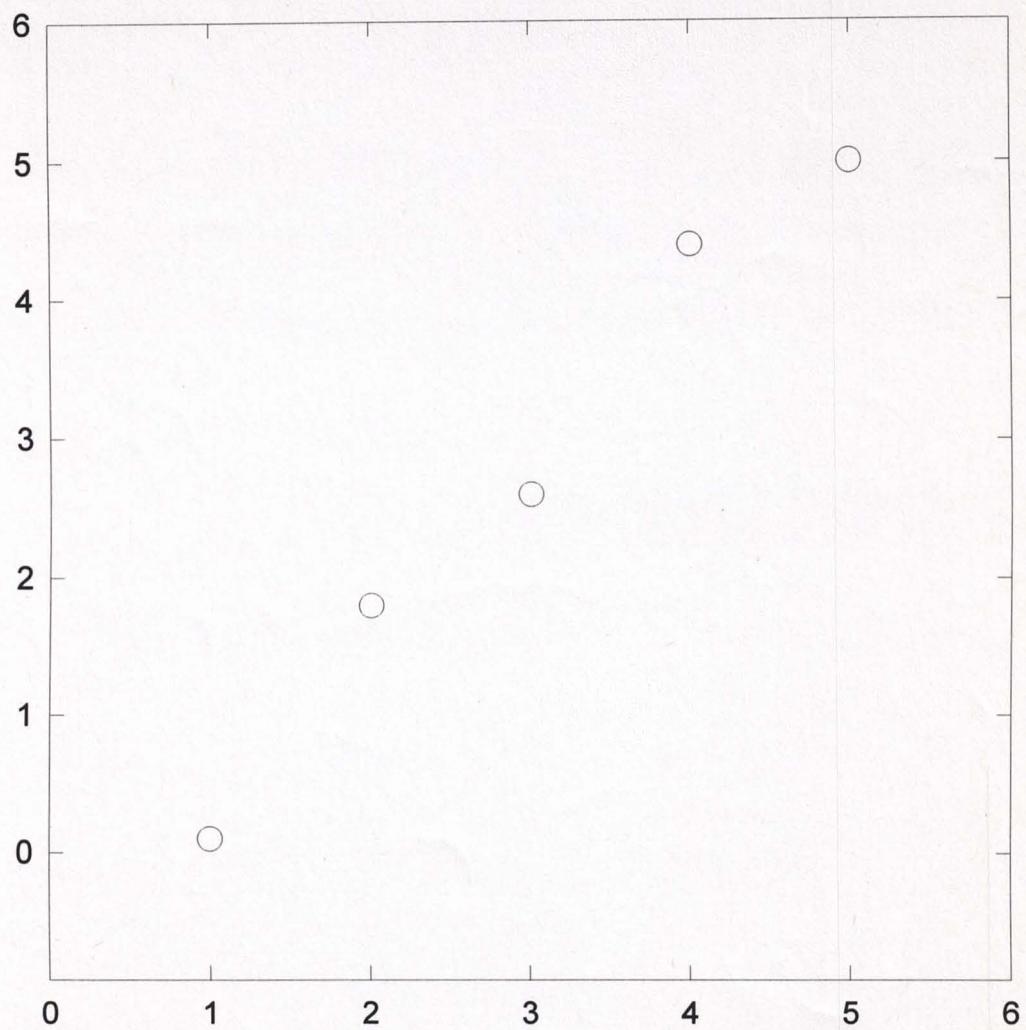
fit f to y

[Constraints]

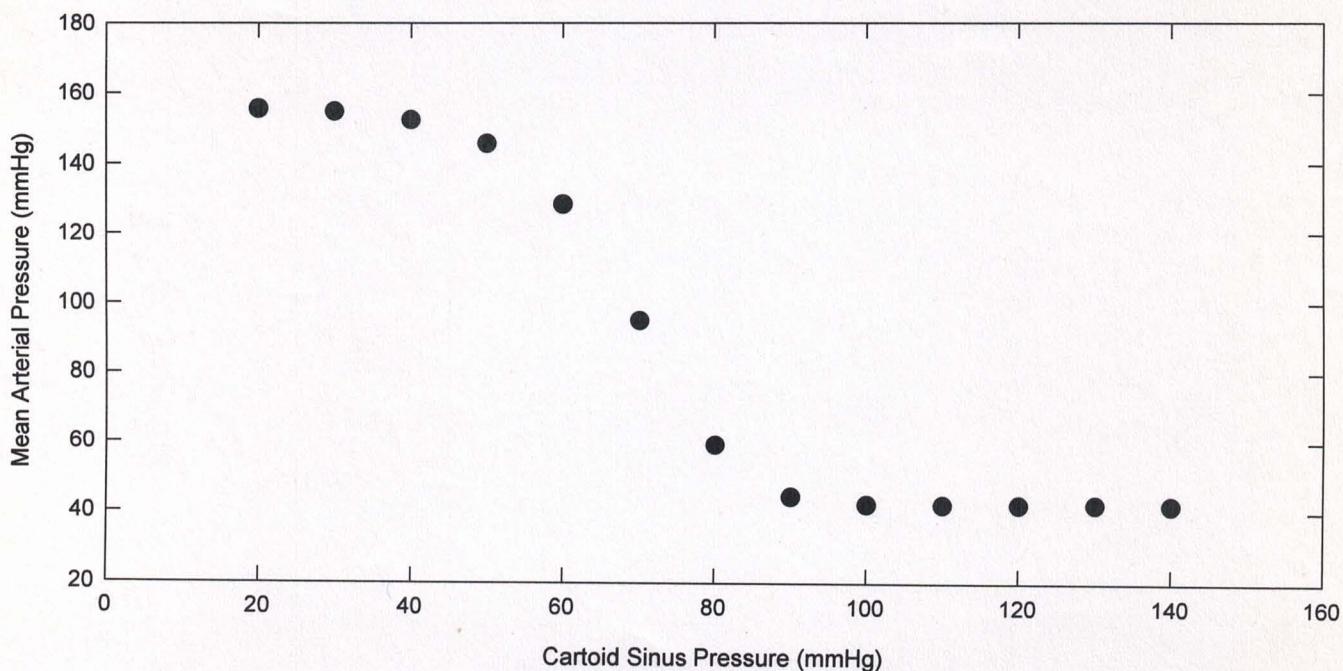
E1>0  
E2>0  
E3>0

[Options]

fit\_tut1.spw



## Cartoid Sinus Reflex Response



[Parameters]

a=120 ;range for mean arterial pressure  
b=0.1 ;slope coefficient  
c=90 ;sinus pressure at maximum rate of change  
d=40 ;minimum mean arterial pressure  
;e=2

[Variables]

x=col(1) y=col(2)

[Equations]

f=a/(1+exp(b\*(x-c)))+d ;^e+d

fit f to y ;fit statement

[Constraints]

;e>0

[Options]

;iterations=5

