Chapter 0 Exercises

Hui

1 Exercise 0.1

- a) The set of all odd natural numbers.
- b) The set of all integers that are multiples of 2.
- c) The set of all natural numbers divisible by 2.
- d) The set of all natural numbers divisible by 2 and 3.
- e) The set of all strings of 0s and 1s that are palindromic.
- f) An empty set.

2 Exercise 0.2

```
a) \{n|n=10^m \text{ for some } m \in \mathbb{N}\}
b) \{n \in \mathbb{Z}|n>5\}
c) \{n \in \mathbb{N}|n<5\}
d) \{aba\}
e) \{\epsilon\}
f) \emptyset
```

3 Exercise 0.3

```
a) A is not a subset of B.
b) B is a subset of A.
c) A \cup B = \{x, y, z\}
d) A \cap B = \{x, y\}
e) A \times B = \{(x, x), (x, y), (y, x), (y, y), (z, x), (z, y)\}
f) \mathcal{P}(B) = \{\emptyset, \{x\}, \{y\}, B\}
```

4 Exercise 0.4

The Cartesian product of n sets is the set of all n-tuples where the first element is an element of the first operand, the second element is an element of the second operand, and so on. In the case of $A \times B$, the first element of each 2-tuple is an element of A, and the second element of each 2-tuple is an element of B. So, if A has a elements and B has b elements, to make every possible pair, you would

need a elements b times, or a*b pairs. Similarly, if A has a elements, B has b elements, and C has c elements, $A \times B \times C$ has a*b*c elements.

5 Exercise 0.5

Each element of $\mathcal{P}(C)$ is a subset of C, meaning each element of $\mathcal{P}(C)$ is a permutation where each element of C is either present or not present (2 possibilities per element). Thus, if C is a set with c elements, there are 2^c elements in $\mathcal{P}(C)$.

6 Exercise 0.6

- a) f(2) = 7
- b) $f:[1,5] \to \{6,7\}$
- c) g(2,10) = 6
- d) $g: [1,5] \times [6,10] \rightarrow [6,10]$
- e) g(4, f(4)) = g(4,7) = 8

7 Exercise 0.7

- a)
- b)
- c)

8 Exercise 0.8

9 Exercise 0.9