# MASTER: Market-Guided Stock Transformer for Stock Price Forecasting

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#### **Stock Price Forecasting**

- Stock price forecasting uses the historical data of stocks to predict their future trends.
  - Profitable stock investment.
  - Close price of stock u at day t: c<sub>u,t</sub>
  - Return ratio, the relative change of close price in d days:

$$\tilde{r}_u = \frac{c_{u,\tau+d} - c_{u,\tau+1}}{c_{u,\tau+1}}$$

- Stock price patterns are intricate.
  - Multiple factors: macroeconomic factors, capital flows, investor sentiments ...
  - The mixing of factors interweaves the stock market as a correlated network.

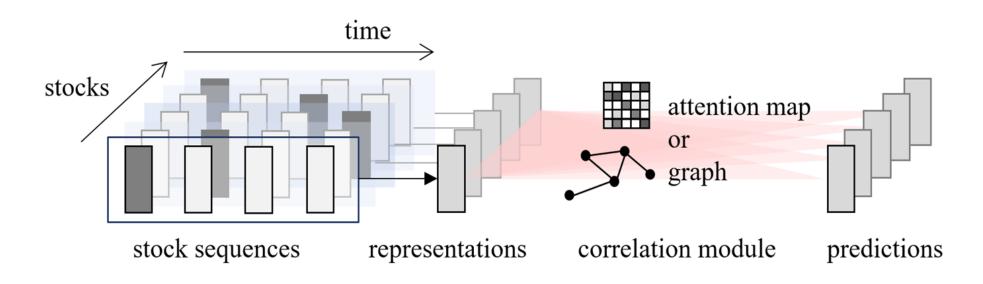


#### **Modeling Stock Correlation**

- 1. Static: Predefined concepts, relationships or rules.
  - Example:
    - Industry graph stocks in the same industry are connected to each other.
  - relationship ≠ real-time correlation
  - not generalizable when events such as company listing, delisting or change in main business happen.
- 2. Dynamic: Attention mechanism.
  - Data-driven, more flexible, and applicable to the time-varying stock sets.



## Framework of Existing Works

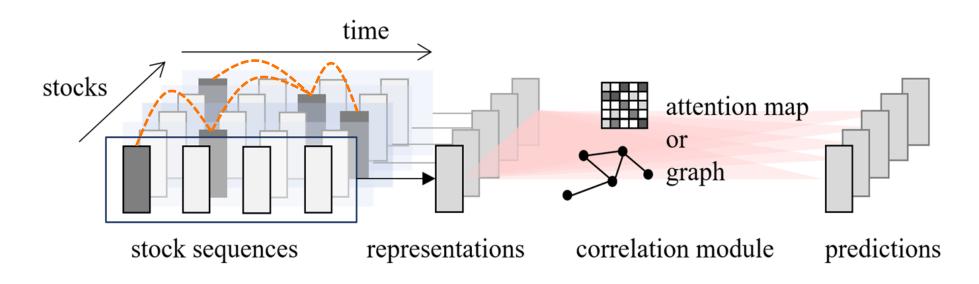


- Use sequential encoder to summarize the historical sequence of stock features and obtain stock representation.
- 2. Establish overall stock correlation and aggregate information to refine each stock representation.

Limitation: They cannot model the realistic stock correlation.



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#### **Realistic Stock Correlation**

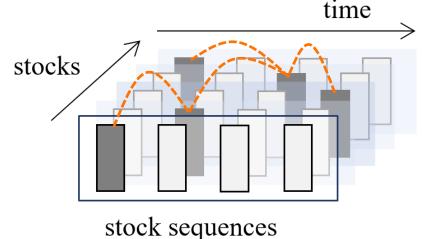
- The dominating factors of stock prices constantly change.
- Different stocks may react to the same factor with different delays.

Instead of holding true through the whole look back window, realistic stock correlation:

- 1. Momentary: highly dynamic
- 2. Cross-time: residing in misaligned time steps.

#### Example:

Upstream companies' stock prices may react faster to a shortage of raw materials than those of downstream companies.

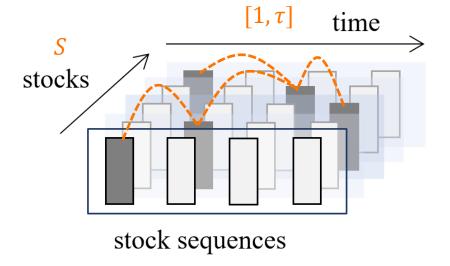




## Difficulties: Complex Attention Field

To simulate the correlation, calculate pair-wise attention among all  $\tau \times S$  feature vectors.

- 1. Large and complex attention field vs. stock data hunger
  - Limited observation: around 250 trading days per year
  - Clustering approaches are sensitive to initialization, unsuitable in stock domain.
  - Our solution: aggregate information from different time steps and other stocks alternatively.





#### **Difficulties: Market Variation**

- 2. The stock correlation is different under varying market status.
  - Example: in a bull market, the correlation are more significant due to investors' optimism.
  - With market variation, the features come into effect and expire.
  - Traditional investors repeatedly conduct statistical examination to select features.
  - Our solution: incorporate the market information to perform automatic feature selection.



#### **Preliminaries**

#### Input:

- Stock feature sequences  $\{x_{u,t}\}_{u \in S, t \in [1,\tau]}$ , where  $x_{\{u,t\}} \in \mathbf{R}^F$
- Market status vector  $m_{\tau} \in {\it I\!\!R}^{F'}$ 
  - Market index price (historical and current)
  - Market index trading volume (historical and current)

#### **Output:**

- Normalized Return Ratios  $\{r_u\}_{u\in S}$  ,  $r_u=\operatorname{Norm}_S(\tilde{r}_u)$ 
  - Encode the labels with ranking information.



## **MASTER:** Overview

**→** *y*<sub>1,1</sub>

Feature Layer

4. Temporal Aggregation 1. Market-Guided Gating  $z_{1,\tau}$  $z_{1,1}$  $Z_{1,2}$ Gate  $m_{ au}$ 3. Inter-Stock Aggregation 5. Prediction  $h_{u,1}$  $h_{u,\tau}$  $h_{1,1}$  $x_{1,1}$ 2. Intra-Stock Aggregation  $\tilde{x}_{1,1}$ 

 $y_{1,2}$ 

 $y_{1, au}$ 

time

stocks



## **MASTER:** Market-Guided Gating

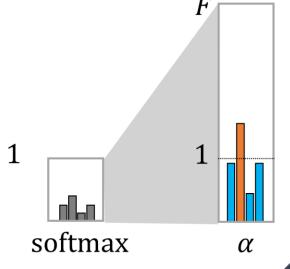
Input:  $m_{ au}$ 

**Output:**  $\alpha$ ,  $|\alpha| = F$ , one scaling coefficient for each feature.

$$\alpha(m_{\tau}) = F \cdot \operatorname{softmax}_{\beta}(W_{\alpha}m_{\tau} + b_{\alpha})$$

- Softmax compels a competition among features to distinguish effective ones.
- $\beta$ : temperature parameters.
- F: adjust the coefficient range to be [0, F]
  - the coefficient can either enlarge or shrink the magnitude.

$$\tilde{x}_{u,t} = \alpha(m_{\tau}) \circ x_{u,t}$$





#### **MASTER: Intra-Stock Aggregation**

We perform intra-stock aggregation first.

- Smaller attention field.
- The feature of a single stock is distributed simpler.
- (1) For each stock u, we gather its feature sequence, and encode each feature with

$$Y_u = ||_{t \in [1,\tau]} \text{LayerNorm}(f(\tilde{x}_{u,t}) + p_t).$$
  $p$ : positional codes.

- (2) Transform  $Y_u$  into  $Q_u^1$ ,  $K_u^1$ ,  $V_u^1$ .
- (3) Compute multi-head attention and send to feed forward layers.

$$H_u^1 = ||_{t \in [1,\tau]} h_{u,t} = FFN^1(MHA^1(Q_u^1, K_u^1, V_u^1) + Y_u)$$



#### **MASTER:** Inter-Stock Aggregation

(1) For each time step t, we gather the embedding of all stocks

$$H_t^2 = ||_{u \in S} h_{u,t}$$

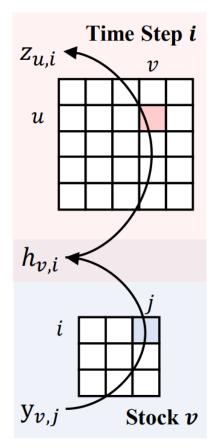
- (2) Transform  $H_t^2$  into  $Q_t^2$ ,  $K_t^2$ ,  $V_t^2$ .
- (3) Compute multi-head attention and send to feed forward layers.

$$Z_{t} = ||_{u \in S} z_{u,t} = FFN^{2}(MHA^{2}(Q_{t}^{2}, K_{t}^{2}, V_{t}^{2}) + H_{t}^{2})$$

#### Correlation from (v, j) to (u, i):

- 1. The local details of  $y_{v,j}$  is conveyed to  $h_{v,i}$  by the intra-stock aggregation of stock v.
- 2. Transmit  $h_{v,i}$  to  $z_{u,i}$  by inter-stock aggregation at time step i.

#### cross-time correlation





#### > MASTER: Temporal Aggregation & Prediction

- For each stock u, MASTER produces a series of temporal embedding  $z_{u,t}$ ,  $t \in [1, \tau]$ .
- We use the latest temporal embedding to query from others, and summarize them into the comprehensive stock embedding:

$$e_{u} = \sum_{t \in [1,\tau]} \lambda_{u,t} z_{u,t}, \qquad \lambda_{u,t} = \frac{\exp(z_{u,t}^{T} W_{\lambda} z_{u,\tau})}{\sum_{i \in [1,\tau]} \exp(z_{u,i}^{T} W_{\lambda} z_{u,\tau})}$$

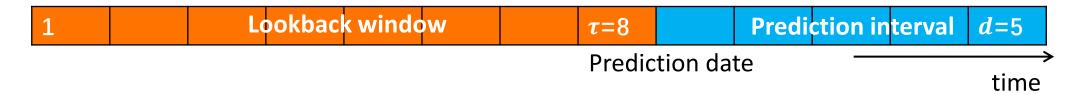
• Regression:  $\hat{r}_{u} = g(e_{u})$ 

• Optimization:  $L = \sum_{u \in S} MSE(r_u, \hat{r}_u)$ 



#### **Experiments: Settings**

- Chinese market, Stock sets: CSI300, CSI800
- Dataset Split:
  - Training 2008 Q1~2020 Q1, Validation 2020 Q2, Test 2020 Q3, 2022 Q4
- Prediction Setting



- Baselines: XGBoost, LSTM, GRU, TCN, Transformer, GAT, DTML
- Evaluation metrics:

Ranking-based - IC, ICIR, RankIC, RankICIR, Portfolio-based - AR, IR.



## **Experiments: Overall Performance**

Table 1: Overall performance comparison. The best results are in bold and the second-best results are underlined. And \* denotes statistically significant improvement (measured by t-test with p-value < 0.01) over all baselines.

Dataset	Model	IC	ICIR	RankIC	RankICIR	AR	IR
CSI300	XGBoost	$0.051 \pm 0.001$	$0.37 \pm 0.01$	$0.050 \pm 0.001$	$0.36 \pm 0.01$	$0.23 \pm 0.03$	$1.9 \pm 0.3$
	LSTM	$0.049 \pm 0.001$	$0.41 \pm 0.01$	$0.051 \pm 0.002$	$0.41 \pm 0.03$	$0.20 \pm 0.04$	$2.0 \pm 0.4$
	GRU	$0.052 \pm 0.004$	$\overline{0.35 \pm 0.04}$	$0.052 \pm 0.005$	$0.34 \pm 0.04$	$0.19 \pm 0.04$	$1.5 \pm 0.3$
	TCN	$0.050 \pm 0.002$	$0.33 \pm 0.04$	$0.049 \pm 0.002$	$0.31 \pm 0.04$	$0.18 \pm 0.05$	$1.4 \pm 0.5$
	Transformer	$0.047 \pm 0.007$	$0.39 \pm 0.04$	$0.051 \pm 0.002$	$0.42 \pm 0.04$	$0.22 \pm 0.06$	$2.0 \pm 0.4$
	GAT	$0.054 \pm 0.002$	$0.36 \pm 0.02$	$0.041 \pm 0.002$	$0.25 \pm 0.02$	$0.19 \pm 0.03$	$1.3 \pm 0.3$
	DTML	$0.049 \pm 0.006$	$0.33 \pm 0.04$	$0.052 \pm 0.005$	$0.33 \pm 0.04$	$0.21 \pm 0.03$	$1.7 \pm 0.3$
	MASTER	$0.064^* \pm 0.006$	$\boldsymbol{0.42 \pm 0.04}$	$0.076^* \pm 0.005$	$\boldsymbol{0.49 \pm 0.04}$	$0.27 \pm 0.05$	$\boldsymbol{2.4 \pm 0.4}$
CSI800	XGBoost	$0.040 \pm 0.000$	$0.37 \pm 0.01$	$0.047 \pm 0.000$	$0.42 \pm 0.01$	$0.08 \pm 0.02$	$0.6 \pm 0.2$
	LSTM	$0.028 \pm 0.002$	$0.32 \pm 0.02$	$0.039 \pm 0.002$	$0.41 \pm 0.03$	$0.09 \pm 0.02$	$0.9 \pm 0.2$
	GRU	$0.039 \pm 0.002$	$0.36 \pm 0.05$	$0.044 \pm 0.003$	$0.39 \pm 0.07$	$0.07 \pm 0.04$	$0.6 \pm 0.3$
	TCN	$0.038 \pm 0.002$	$0.33 \pm 0.04$	$0.045 \pm 0.002$	$0.38 \pm 0.05$	$0.05 \pm 0.04$	$0.4 \pm 0.3$
	Transformer	$0.040 \pm 0.003$	$0.43 \pm 0.03$	$0.048 \pm 0.003$	$0.51 \pm 0.05$	$0.13 \pm 0.04$	$1.1 \pm 0.3$
	GAT	$0.043 \pm 0.002$	$0.39 \pm 0.02$	$0.042 \pm 0.002$	$0.35 \pm 0.02$	$0.10 \pm 0.04$	$0.7 \pm 0.3$
	DTML	$0.039 \pm 0.004$	$0.29 \pm 0.03$	$0.053 \pm 0.008$	$0.37 \pm 0.06$	$0.16 \pm 0.03$	$1.3 \pm 0.2$
	MASTER	$0.052^* \pm 0.006$	$0.40 \pm 0.06$	$0.066\pm0.007$	$0.48 \pm 0.06$	$0.28^* \pm 0.02$	$2.3^* \pm 0.3$



## **Experiments: Stock Transformer Architecture**

Table 2: Experiments on CSI300 to validate the effectiveness of proposed stock transformer architecture. The best results are in bold and the second-best results are underlined.

Model	IC	ICIR	RankIC	RankICIR	AR	IR
(MA)STER	$0.064 \pm 0.003$	$\boldsymbol{0.43 \pm 0.02}$	$0.074 \pm 0.004$	$\boldsymbol{0.48 \pm 0.04}$	$0.25 \pm 0.03$	$2.1 \pm 0.3$
(MA)STER-Bi	$0.058 \pm 0.005$	$0.38 \pm 0.04$	$0.066 \pm 0.008$	$0.41 \pm 0.05$	$0.19 \pm 0.03$	$1.6 \pm 0.2$
Naive	$0.041 \pm 0.008$	$\overline{0.30 \pm 0.05}$	$0.046 \pm 0.007$	$0.32 \pm 0.04$	$\overline{0.18\pm0.05}$	$1.6 \pm 0.6$
Clustering	$0.044 \pm 0.003$	$0.36 \pm 0.02$	$0.049 \pm 0.005$	$0.39 \pm 0.04$	$0.18 \pm 0.04$	$1.7 \pm 0.3$

(MA)STER: An ablation of MASTER without the Market-Guided Gating.

(MA)STER-Bi: Substitute the transformer layer with Bi-LSTM.

Naïve: Directly compute pair-wise attention among  $\tau \times S$  feature vectors.

Clustering: Apply Local Sensitive Hashing to break down the attention field.



#### **Experiments: Market-Guided Gating**

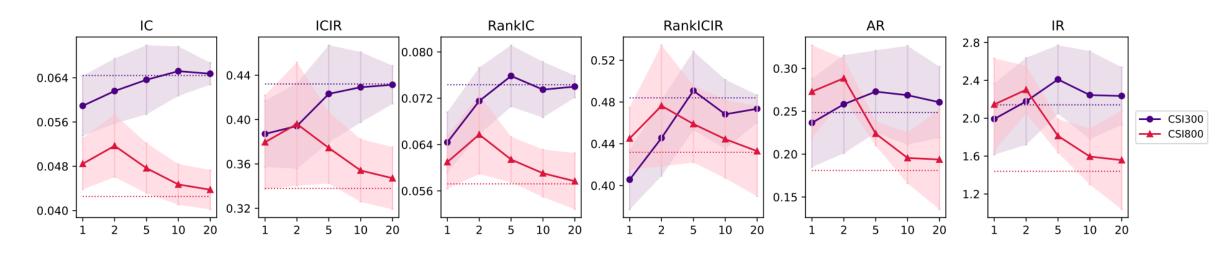


Figure 4: MASTER performance with varying  $\beta$ . The horizontal dash lines are performance without market-guided gating.

#### Gate temperature:

a smaller  $\beta$  forces a stronger feature selection while a larger  $\beta$  turns off the gating effect.



#### **Experiments: Visualization of Attention Maps**

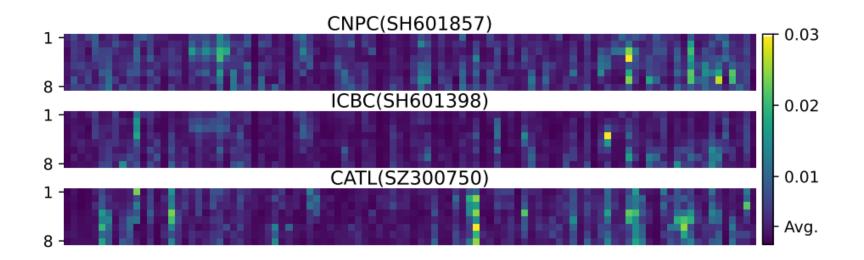


Figure 5: The correlation towards three target stocks on Aug 19th, 2022. The y-axis is time steps in the lookback window and the x-axis is source stocks. *Avg.* denotes the evenly distributed value.



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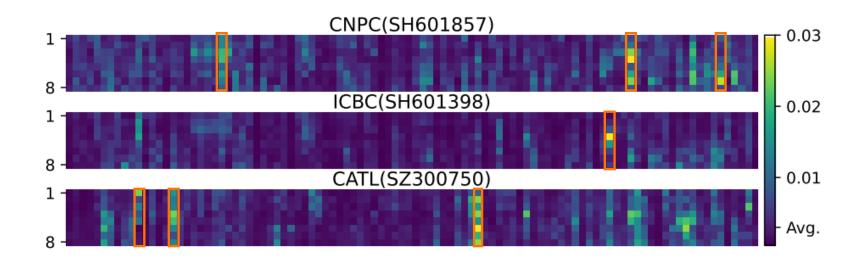


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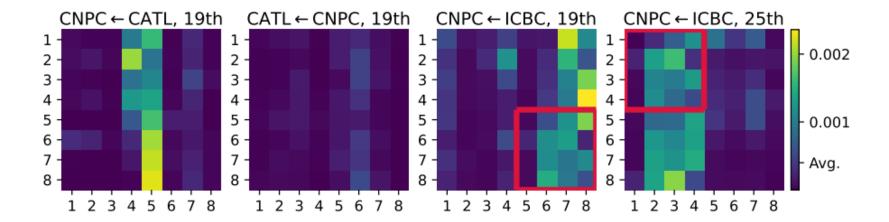


Figure 6: Cross-time correlation of stock pairs on Aug 19th and 25th, 2022. The x-axis is the source time steps and the y-axis is the target time steps.



- ➤ We introduce a novel method MASTER for stock price forecasting, which models the realistic stock correlation and guide feature selection with market information.
- Future work can explore to mine stock correlations of higher quality and study other uses of market information.
- > \tak Data & Code: <a href="mailto:github.com/SJTU-Quant/MASTER">github.com/SJTU-Quant/MASTER</a>
- ➤ Imail: 2017lt@sjtu.edu.cn

## Thank you!