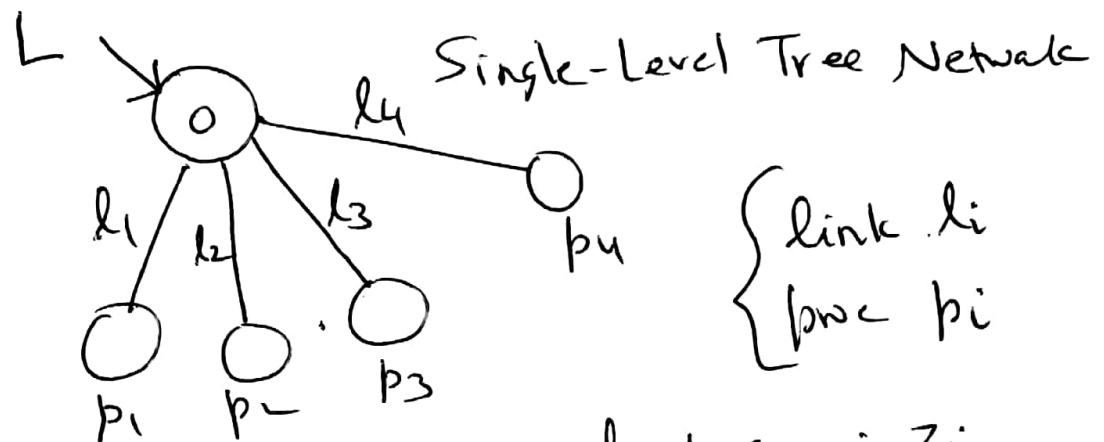


## Arbitrarily Divisible Loads Scheduling



link speed:  $z_i$   
proc. speed:  $w_i$

### Linear Model:

① can be arbitrarily divided

$d_i \longrightarrow p_i$

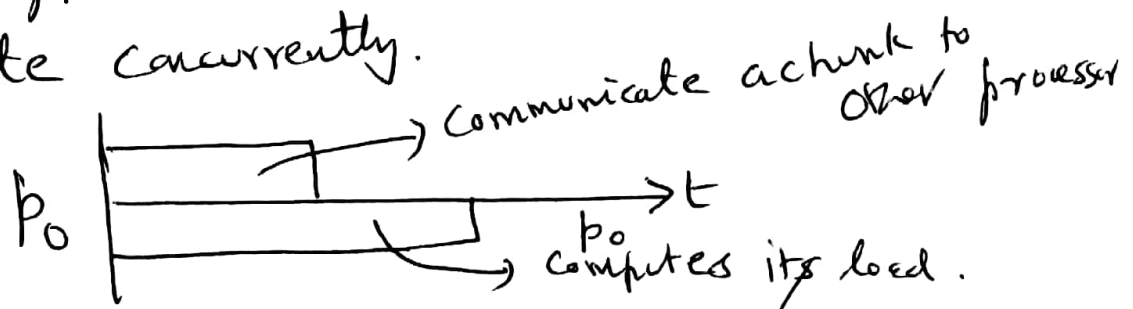
$\Rightarrow$  Communication time =  $d_i z_i$

Computation time =  $d_i w_i$

Root processor  $p_0$

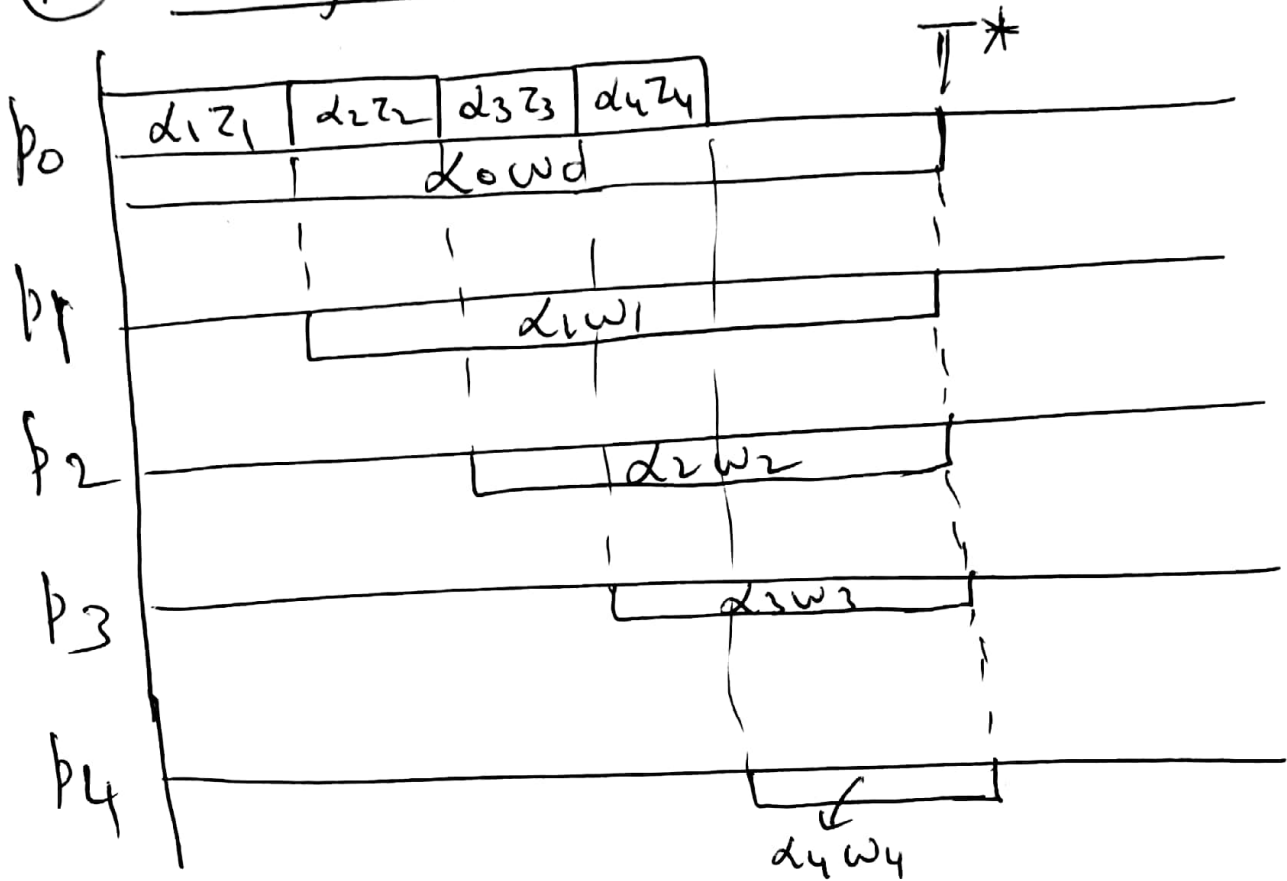
with front-end (FE)  
without front-end

If  $p_0$  is equipped with a FE, then it can compute & communicate concurrently.



②

(A) With front-end



$$\left. \begin{aligned} d_3w_3 &= d_4(w_4 + z_4) \\ d_2w_2 &= d_3(w_3 + z_3) \\ d_1w_1 &= d_2(w_2 + z_2) \\ d_0w_0 &= d_1(w_1 + z_1) \end{aligned} \right\} \textcircled{+} \sum_{i=0}^4 d_i = L$$

$$\Rightarrow d_3 = d_4 \left( \frac{w_4 + z_4}{w_3} \right) = d_4 \sigma_4, \quad \text{where } \sigma_n = \frac{w_n + z_n}{w_3}$$

$$d_2 = d_3 \sigma_3 = d_4 \sigma_4 \cdot \sigma_3$$

$$d_1 = d_2 \cdot \sigma_2 = d_4 \sigma_4 \cdot \sigma_3 \cdot \sigma_2$$

$$d_0 = d_1 \sigma_1 = d_4 \sigma_4 \cdot \sigma_3 \cdot \sigma_2 \cdot \sigma_1$$

using  $\sum d_i = L$ , we obtain,

(3)

$$d_u = \left( \frac{L}{1 + \sum_{i=0}^4 \prod_{j=i+1}^4 \sigma_j} \right)$$

in general,

$$d_m = \left( \frac{L}{1 + \sum_{i=0}^m \prod_{j=i+1}^m \sigma_j} \right)$$

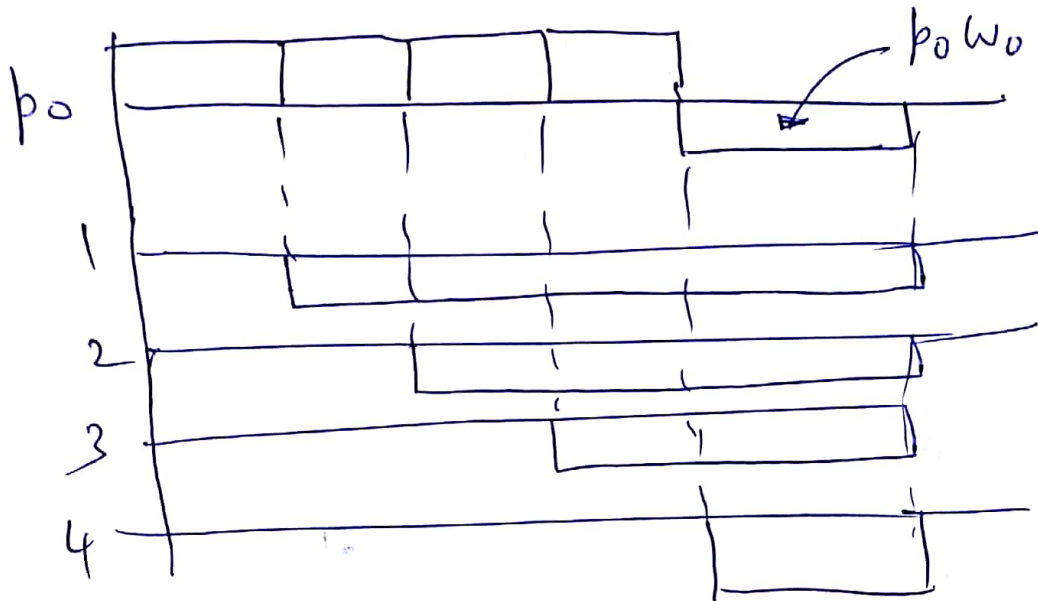
& Hence,  $T^* = d_0 w_0$

$$\Rightarrow T^* = \frac{\left( \prod_{k=1}^m \sigma_k \right) \cdot w_0 \cdot L}{1 + \sum_{i=0}^m \prod_{j=i+1}^m \sigma_j}$$

Optimal proc. time.

(B) Solve for without (FE) case and  
no participants.

④ For (B); the timing diagram would be similar to case (A) except:



Solve using the above method (A).

⑤ Solve (A) & (B) using the following affine model:

$$\text{Comm. time} = d_i z_i + O_{cm}$$

$$\text{Comp. time} = d_i w_i + O_{cp}$$

⑥ Derive closed-form soln for  $m=5$ .