Paley Constructions of Hadamard Matrixes

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Abstract

This document presents examples of constructing Hadamard matrixes using two methods attributed to Raymond Paley. In particular the illustrations include quadratic residue calculations from a Galois field for both the p^1 and p^k cases, polynomial division with remainder, and construction of the prerequisite Jacobsthal matrix for both cases.

The construction methods are implemented in Java at https://github.com/wannamak/hadamard/.

1 Choosing a construction

	Table	1:	Palev	Constructions
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		0 0 01 01 0		
Hadamard order	p^k	Paley type		
4	3	I		
8	7	I		
12	11	I		
16				
20	19	I		
24	23	I		
28	13	II		
32	31	I		
36	17	II		
40		44	43	Ι