neural network

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1 CS498DL Assignment 2

The autoreload extension is already loaded. To reload it, use: %reload_ext autoreload

1.1 Loading CIFAR-10

Now that you have implemented a neural network that passes gradient checks and works on toy data, you will test your network on the CIFAR-10 dataset.

```
[139]: # You can change these numbers for experimentation
    # For submission be sure they are set to the default values
    TRAIN_IMAGES = 49000
    VAL_IMAGES = 10000

    TEST_IMAGES = 10000

data = get_CIFAR10_data(TRAIN_IMAGES, VAL_IMAGES, TEST_IMAGES)
    X_train, y_train = data['X_train'], data['y_train']
    X_val, y_val = data['X_val'], data['y_val']
    X_test, y_test = data['X_test'], data['y_test']
```

1.2 Train using SGD

To train our network we will use SGD. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

You can try different numbers of layers and other hyperparameters on the CIFAR-10 dataset below.

```
[170]: # Hyperparameters
       input size = 32 * 32 * 3
       num_layers = 3
       hidden_size = 120
       hidden_sizes = [hidden_size] * (num_layers - 1)
       num_classes = 10
       epochs = 40
       batch_size = 200
       learning_rate = 0.05
       learning_rate_decay = 0.85
       regularization = 0.0004
       # Initialize a new neural network model
       net = NeuralNetwork(input_size, hidden_sizes, num_classes, num_layers)
       # Variables to store performance for each epoch
       train loss = np.zeros(epochs)
       train_accuracy = np.zeros(epochs)
       val_accuracy = np.zeros(epochs)
       test_accuracy = np.zeros(epochs)
       learning_rates = np.zeros(epochs)
       # For each epoch...
       for epoch in range(epochs):
           # Shuffle the dataset
           indicies = np.random.permutation(len(X train))
           # Training
           # For each mini-batch...
           for batch in range(TRAIN_IMAGES // batch_size):
               i = batch*batch_size
               # Create a mini-batch of training data and labels
               X_batch = X_train[indicies[i:i+batch_size], : ]
               y_batch = y_train[indicies[i:i+batch_size], ]
               # Run the forward pass of the model to get a prediction and compute the
        \rightarrowaccuracy
```

```
scores = net.forward(X_batch)
       pred = np.argmax(scores, axis=1)
       train_accuracy[epoch] += (pred == y_batch).sum()
       # Run the backward pass of the model to compute the loss, and update_
\rightarrow the weights
       train_loss[epoch] += net.backward(y_batch, regularization)
       net.update(learning_rate, 0.5)
   train_accuracy /= len(X_train)
   # Va.1. i.d.a.t.i.on.
   # No need to run the backward pass here, just run the forward pass to_{\sqcup}
\rightarrow compute accuracy
   scores_val = net.forward(X_val)
   pred_val = np.argmax(scores_val, axis=1)
   val_accuracy[epoch] += (pred_val == y_val).mean()
   scores_test = net.forward(X_test)
   pred_test = np.argmax(scores_test, axis=1)
   test_accuracy[epoch] += (pred_test == y_test).mean()
   learning_rate *= learning_rate_decay
   learning_rates[epoch] = learning_rate
```

1.3 Check accuracy by numbers

```
[171]: print(val_accuracy) print(test_accuracy)
```

```
[0.448 0.47 0.491 0.486 0.492 0.509 0.509 0.526 0.529 0.519 0.527 0.528 0.525 0.529 0.538 0.529 0.525 0.527 0.541 0.539 0.535 0.533 0.533 0.535 0.534 0.535 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.534 0.535 0.535 0.534 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.536 0.536 0.536 0.536 0.535 0.534 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.536 0.536 0.536 0.535 0.534 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535 0.535
```

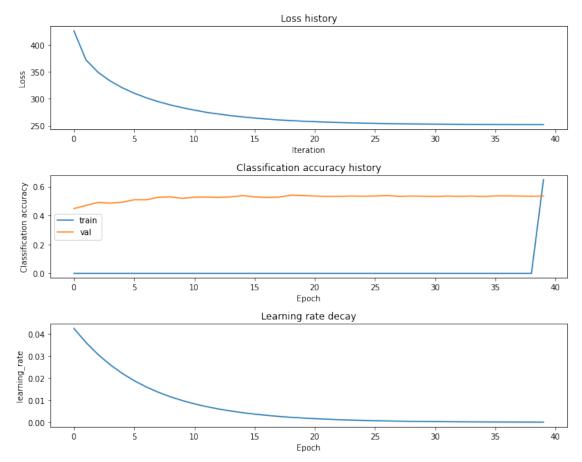
1.4 plot the results

```
[172]: # Plot the loss function and train / validation accuracies
plt.subplot(3, 1, 1)
plt.plot(train_loss)
plt.title('Loss history')
plt.xlabel('Iteration')
plt.ylabel('Loss')
```

```
plt.subplot(3, 1, 2)
plt.plot(train_accuracy, label='train')
plt.plot(val_accuracy, label='val')
plt.title('Classification accuracy history')
plt.xlabel('Epoch')
plt.ylabel('Classification accuracy')
plt.legend()

plt.subplot(3, 1, 3)
plt.plot(learning_rates)
plt.title('Learning rate decay')
plt.xlabel('Epoch')
plt.ylabel('learning_rate')

plt.tight_layout()
plt.show()
```



1.5 Train using Adam

Next we will train the same model using the Adam optimizer. You should take the above code for SGD and modify it to use Adam instead. For implementation details, see the lecture slides. The original paper that introduced Adam is also a good reference, and contains suggestions for default values: https://arxiv.org/pdf/1412.6980.pdf

```
[201]: # TODO: implement me
       # Hyperparameters
       input_size = 32 * 32 * 3
       num_layers = 3
       hidden_size = 120
       hidden_sizes = [hidden_size] * (num_layers - 1)
       num classes = 10
       epochs = 40
       batch size = 200
       learning_rate = 0.0003
       learning_rate_decay = 0.85
       regularization = 0.00001
       b1 = 0.7
       b2 = 0.79
       eps = 1e-8
       opt = "Adam"
       # Initialize a new neural network model
       net = NeuralNetwork(input_size, hidden_sizes, num_classes, num_layers)
       # Variables to store performance for each epoch
       adam_train_loss = np.zeros(epochs)
       adam_train_accuracy = np.zeros(epochs)
       adam_val_accuracy = np.zeros(epochs)
       adam_test_accuracy = np.zeros(epochs)
       learning_rates = np.zeros(epochs)
       # For each epoch...
       for epoch in range(epochs):
           # Shuffle the dataset
           indicies = np.random.permutation(len(X_train))
           # Training
           # For each mini-batch...
           i = 0
           for batch in range(TRAIN_IMAGES // batch_size):
               i = batch*batch_size
               # Create a mini-batch of training data and labels
               X_batch = X_train[indicies[i:i+batch_size], : ]
               y_batch = y_train[indicies[i:i+batch_size], ]
```

```
# Run the forward pass of the model to get a prediction and compute the
\rightarrowaccuracy
       scores = net.forward(X batch)
       pred = np.argmax(scores, axis=1)
       adam train accuracy[epoch] += (pred == y batch).sum()
       # Run the backward pass of the model to compute the loss, and update_
\rightarrow the weights
       adam_train_loss[epoch] += net.backward(y_batch, regularization)
       net.update(learning_rate, b1, b2, eps, opt, epoch+1)
   adam_train_accuracy /= len(X_train)
   # Validation
   # No need to run the backward pass here, just run the forward pass to \Box
\rightarrow compute accuracy
   scores_val = net.forward(X_val)
   pred_val = np.argmax(scores_val, axis=1)
   adam_val_accuracy[epoch] += (pred_val == y_val).mean()
   adam_scores_test = net.forward(X_test)
   pred test = np.argmax(adam scores test, axis=1)
   adam_test_accuracy[epoch] += (pred_test == y_test).mean()
   learning_rate *= learning_rate_decay
   learning_rates[epoch] = learning_rate
```

1.6 Check accuracy by numbers

```
[202]: print(adam_val_accuracy)
print(adam_test_accuracy)

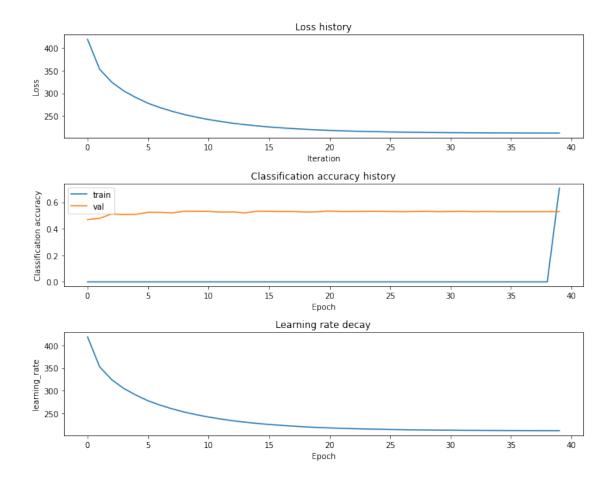
[0.452 0.502 0.506 0.497 0.501 0.506 0.518 0.521 0.522 0.53 0.528 0.519 0.529 0.526 0.532 0.531 0.53 0.524 0.533 0.531 0.524 0.53 0.527 0.527 0.524 0.525 0.526 0.527 0.525 0.526 0.525 0.526 0.525 0.525 0.525 0.526 0.526 0.526 [0.434 0.4941 0.5103 0.5092 0.5249 0.523 0.5238 0.526 0.5267 0.5323
```

0.5275 0.5292 0.5306 0.5315 0.5337 0.5313 0.5342 0.5325 0.5309 0.5305 0.5328 0.5324 0.5322 0.5311 0.5322 0.531 0.5314 0.532 0.5318 0.532 0.533 0.5326 0.5324 0.5326 0.5323 0.5323 0.532 0.5317 0.5326 0.5323 0.5322]

1.7 Graph loss and train/val accuracies

Examining the loss graph along with the train and val accuracy graphs should help you gain some intuition for the hyperparameters you should try in the hyperparameter tuning below. It should also help with debugging any issues you might have with your network.

```
[198]: # Plot the loss function and train / validation accuracies
      plt.subplot(3, 1, 1)
       plt.plot(adam_train_loss)
       plt.title('Loss history')
       plt.xlabel('Iteration')
      plt.ylabel('Loss')
       plt.subplot(3, 1, 2)
      plt.plot(adam_train_accuracy, label='train')
       plt.plot(adam_val_accuracy, label='val')
       plt.title('Classification accuracy history')
       plt.xlabel('Epoch')
       plt.ylabel('Classification accuracy')
       plt.legend()
      plt.subplot(3, 1, 3)
       plt.plot(adam_train_loss)
       plt.title('Learning rate decay')
       plt.xlabel('Epoch')
      plt.ylabel('learning_rate')
       plt.tight_layout()
       plt.show()
```



1.8 Hyperparameter tuning

Once you have successfully trained a network you can tune your hyparameters to increase your accuracy.

Based on the graphs of the loss function above you should be able to develop some intuition about what hyperparameter adjustments may be necessary. A very noisy loss implies that the learning rate might be too high, while a linearly decreasing loss would suggest that the learning rate may be too low. A large gap between training and validation accuracy would suggest overfitting due to a large model without much regularization. No gap between training and validation accuracy would indicate low model capacity.

You will compare networks of two and three layers using the different optimization methods you implemented.

The different hyperparameters you can experiment with are: - Batch size: We recommend you leave this at 200 initially which is the batch size we used. - Number of iterations: You can gain an intuition for how many iterations to run by checking when the validation accuracy plateaus in your train/val accuracy graph. - Initialization Weight initialization is very important for neural networks. We used the initialization W = np.random.randn(n) / sqrt(n) where n is the input dimension for layer corresponding to W. We recommend you stick with the given initializations, but

you may explore modifying these. Typical initialization practices: http://cs231n.github.io/neural-networks-2/#init - Learning rate: Generally from around 1e-4 to 1e-1 is a good range to explore according to our implementation. - Learning rate decay: We recommend a 0.95 decay to start. - Hidden layer size: You should explore up to around 120 units per layer. For three-layer network, we fixed the two hidden layers to be the same size when obtaining the target numbers. However, you may experiment with having different size hidden layers. - Regularization coefficient: We recommend trying values in the range 0 to 0.1.

Hints: - After getting a sense of the parameters by trying a few values yourself, you will likely want to write a few for-loops to traverse over a set of hyperparameters. - If you find that your train loss is decreasing, but your train and val accuracy start to decrease rather than increase, your model likely started minimizing the regularization term. To prevent this you will need to decrease the regularization coefficient.

1.9 Run on the test set

When you are done experimenting, you should evaluate your final trained networks on the test set.

```
[203]: # best_2layer_sgd_prediction = np.argmax(scores_test, axis=1)
# best_3layer_sgd_prediction = np.argmax(scores_test, axis=1)
# best_2layer_adam_prediction = np.argmax(adam_scores_test, axis=1)
best_3layer_adam_prediction = np.argmax(adam_scores_test, axis=1)
```

1.10 Kaggle output

Once you are satisfied with your solution and test accuracy, output a file to submit your test set predictions to the Kaggle for Assignment 2 Neural Network. Use the following code to do so:

```
[204]: # output_submission_csv('./nn_2layer_sgd_submission.csv', \( \)
\( \to best_2layer_sgd_prediction \)
# output_submission_csv('./nn_3layer_sgd_submission.csv', \( \)
\( \to best_3layer_sgd_prediction \)
# output_submission_csv('./nn_2layer_adam_submission.csv', \( \)
\( \to best_2layer_adam_prediction \)

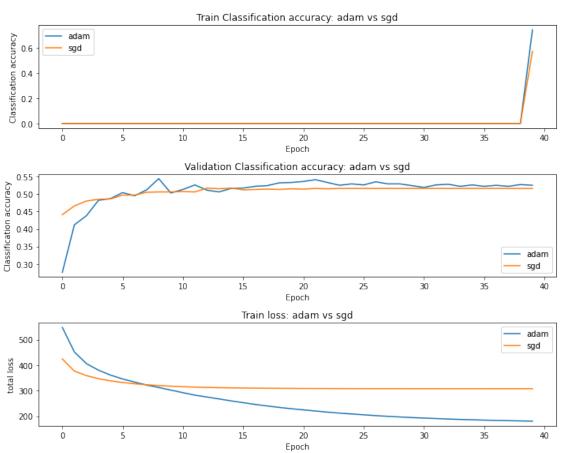
output_submission_csv('./nn_3layer_adam_submission.csv', \( \)
\( \to best_3layer_adam_prediction \)
\( \to best_3layer_adam_prediction \)
```

1.11 Compare 2 layer SGD and Adam

Create graphs to compare training loss and validation accuracy between SGD and Adam. The code is similar to the above code, but instead of comparing train and validation, we are comparing SGD and Adam.

```
[166]: # TODO: implement me
    plt.subplot(3,1,1)
    plt.plot(adam_train_accuracy, label='adam')
    plt.plot(train_accuracy, label='sgd')
    plt.title('Train Classification accuracy: adam vs sgd')
    plt.xlabel('Epoch')
```

```
plt.ylabel('Classification accuracy')
plt.legend()
plt.subplot(3,1,2)
plt.plot(adam_val_accuracy, label='adam')
plt.plot(val_accuracy, label='sgd')
plt.title('Validation Classification accuracy: adam vs sgd')
plt.xlabel('Epoch')
plt.ylabel('Classification accuracy')
plt.legend()
plt.subplot(3,1,3)
plt.plot(adam_train_loss, label='adam')
plt.plot(train_loss, label='sgd')
plt.title('Train loss: adam vs sgd')
plt.xlabel('Epoch')
plt.ylabel('total loss')
plt.legend()
plt.tight_layout()
plt.show()
```



1.12 Compare 3 layer SGD and Adam

Compare SGD and Adam using same hyperparameters

```
[154]: # TODO: implement me
      plt.subplot(3,1,1)
       plt.plot(adam_train_accuracy, label='adam')
       plt.plot(train_accuracy, label='sgd')
       plt.title('Train Classification accuracy: adam vs sgd')
       plt.xlabel('Epoch')
       plt.ylabel('Classification accuracy')
       plt.legend()
       plt.subplot(3,1,2)
       plt.plot(adam_val_accuracy, label='adam')
       plt.plot(val_accuracy, label='sgd')
       plt.title('Validation Classification accuracy: adam vs sgd')
       plt.xlabel('Epoch')
       plt.ylabel('Classification accuracy')
       plt.legend()
       plt.subplot(3,1,3)
       plt.plot(adam_train_loss, label='adam')
       plt.plot(train_loss, label='sgd')
       plt.title('Train loss: adam vs sgd')
       plt.xlabel('Epoch')
       plt.ylabel('total loss')
       plt.legend()
       plt.tight_layout()
       plt.show()
```

