`wannier90`: User Guide

Version 3.1

Contents

Part I

Introduction

Introduction

Getting Help

The latest release of `wannier90` and documentation can always be found at `http://www.wannier.org`.

The development version may be cloned/downloaded from the official repository of the `wannier90` code on GitHub (see `https://github.com/wannier-developers/wannier90`).

There is a `wannier90` mailing list for discussing issues in the development, theory, coding and algorithms pertinent to MLWF. You can register for this mailing list by following the links at `http://www.wannier.org/forum.html`. Alternatively, for technical issues about the `wannier90` code, check the official repository of `wannier90` on GitHub where you may raise issues or ask questions about about its functionalities.

Finally, many frequently asked questions are answered in Appendix B. An expanded FAQ session may be found on the Wiki page of the GitHub repository at `https://github.com/wannier-developers/wannier90/wiki/FAQ`.

Citation

We ask that you acknowledge the use of `wannier90` in any publications arising from the use of this code through the following reference

> [ref] G. Pizzi, V. Vitale, R. Arita, S. Blügel, F. Freimuth, G. Géranton, M. Gibertini, D. Gresch, C. Johnson, T. Koretsune, J. Ibañez-Azpiroz, H. Lee, J.M. Lihm, D. Marchand, A. Marrazzo, Y. Mokrousov, J.I. Mustafa, Y. Nohara, Y. Nomura, L. Paulatto, S. Poncé, T. Ponweiser, J. Qiao, F. Thöle, S.S. Tsirkin, M. Wierzbowska, N. Marzari, D. Vanderbilt, I. Souza, A.A. Mostofi, J.R. Yates,
> Wannier90 as a community code: new features and applications, *J. Phys. Cond. Matt.* **32**, 165902 (2020)
> `https://doi.org/10.1088/1361-648X/ab51ff`

If you are using versions 2.x of the code, cite instead:

> [ref] A. A. Mostofi, J. R. Yates, G. Pizzi, Y.-S. Lee, I. Souza, D. Vanderbilt and N. Marzari,
> An updated version of `wannier90`: A Tool for Obtaining Maximally-Localised Wannier Functions, *Comput. Phys. Commun.* **185**, 2309 (2014)
> `http://dx.doi.org/10.1016/j.cpc.2014.05.003`

It would also be appropriate to cite the original articles:

Maximally localized generalized Wannier functions for composite energy bands,
N. Marzari and D. Vanderbilt, *Phys. Rev. B* **56**, 12847 (1997)

Maximally localized Wannier functions for entangled energy bands,
I. Souza, N. Marzari and D. Vanderbilt, *Phys. Rev. B* **65**, 035109 (2001)

Credits

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Contributors to the code include: Daniel Aberg (w90pov code), Lampros Andrinopoulos (w90vdw code), Pablo Aguado Puente (gyrotropic routines), Raffaello Bianco (k-slice plotting), Marco Buongiorno Nardelli (dosqc v1.0 subroutines upon which transport.f90 is based), Stefano De Gironcoli (pw2wannier90.x interface to Quantum ESPRESSO), Pablo Garcia Fernandez (matrix elements of the position operator), Nicholas D. M. Hine (w90vdw code), Young-Su Lee (specialised Gamma point routines and transport), Antoine Levitt (preconditioning), Graham Lopez (extension of pw2wannier90 to add terms needed for orbital magnetisation), Radu Miron (constrained centres), Nicolas Poilvert (transport routines), Michel Posternak (original plotting routines), Rei Sakuma (Symmetry-adapted Wannier functions), Gabriele Sclauzero (disentanglement in spheres in k-space), Matthew Shelley (transport routines), Christian Stieger (routine to print the U matrices), David Strubbe (various bugfixes/improvements), Timo Thonhauser (extension of pw2wannier90 to add terms needed for orbital magnetisation), Junfeng Qiao (spin Hall conductivity).

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`wannier90` Version 2.x was written by: Arash A. Mostofi, Giovanni Pizzi, Ivo Souza, Jonathan R. Yates. `wannier90` Version 1.0 was written by: Arash A. Mostofi, Jonathan R. Yates, Young-Su Lee. `wannier90` is based on the Wannier Fortran 77 code written for isolated bands by Nicola Marzari and David Vanderbilt and for entangled bands by Ivo Souza, Nicola Marzari, and David Vanderbilt.

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Part II

wannier90.x

Chapter 1

Methodology

`wannier90` computes maximally-localised Wannier functions (MLWF) following the method of Marzari and Vanderbilt (MV) [1]. For entangled energy bands, the method of Souza, Marzari and Vanderbilt (SMV) [2] is used. We introduce briefly the methods and key definitions here, but full details can be found in the original papers and in Ref. [3].

First-principles codes typically solve the electronic structure of periodic materials in terms of Bloch states, $\psi_{n\mathbf{k}}$. These extended states are characterised by a band index n and crystal momentum $\mathbf{k}$. An alternative representation can be given in terms of spatially localised functions known as Wannier functions (WF). The WF centred on a lattice site $\mathbf{R}$, $w_{n\mathbf{R}}(\mathbf{r})$, is written in terms of the set of Bloch states as

$$w_{n\mathbf{R}}(\mathbf{r}) = \frac{V}{(2\pi)^3} \int_{\mathrm{BZ}} \left[\sum_m U_{mn}^{(\mathbf{k})} \psi_{m\mathbf{k}}(\mathbf{r}) \right] e^{-i\mathbf{k}.\mathbf{R}} \, \mathrm{d}\mathbf{k} \ , \tag{1.1}$$

where V is the unit cell volume, the integral is over the Brillouin zone (BZ), and $\mathbf{U}^{(\mathbf{k})}$ is a unitary matrix that mixes the Bloch states at each $\mathbf{k}$. $\mathbf{U}^{(\mathbf{k})}$ is not uniquely defined and different choices will lead to WF with varying spatial localisations. We define the spread Ω of the WF as

$$\Omega = \sum_n \left[\langle w_{n\mathbf{0}}(\mathbf{r}) | r^2 | w_{n\mathbf{0}}(\mathbf{r}) \rangle - |\langle w_{n\mathbf{0}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2 \right]. \tag{1.2}$$

The total spread can be decomposed into a gauge invariant term Ω_{I} plus a term $\tilde{\Omega}$ that is dependant on the gauge choice $\mathbf{U}^{(\mathbf{k})}$. $\tilde{\Omega}$ can be further divided into terms diagonal and off-diagonal in the WF basis, Ω_{D} and Ω_{OD},

$$\Omega = \Omega_{\mathrm{I}} + \tilde{\Omega} = \Omega_{\mathrm{I}} + \Omega_{\mathrm{D}} + \Omega_{\mathrm{OD}} \tag{1.3}$$

where

$$\Omega_{\mathrm{I}} = \sum_n \left[\langle w_{n\mathbf{0}}(\mathbf{r}) | r^2 | w_{n\mathbf{0}}(\mathbf{r}) \rangle - \sum_{\mathbf{R}m} |\langle w_{n\mathbf{R}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2 \right] \tag{1.4}$$

$$\Omega_{\mathrm{D}} = \sum_n \sum_{\mathbf{R} \neq \mathbf{0}} |\langle w_{n\mathbf{R}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2 \tag{1.5}$$

$$\Omega_{\mathrm{OD}} = \sum_{m \neq n} \sum_{\mathbf{R}} |\langle w_{m\mathbf{R}}(\mathbf{r}) | \mathbf{r} | w_{n\mathbf{0}}(\mathbf{r}) \rangle|^2 \tag{1.6}$$

The MV method minimises the gauge dependent spread $\tilde{\Omega}$ with respect the set of $\mathbf{U}^{(\mathbf{k})}$ to obtain MLWF.

`wannier90` requires two ingredients from an initial electronic structure calculation.

1. The overlaps between the cell periodic part of the Bloch states $|u_{n\mathbf{k}}\rangle$

$$M_{mn}^{(\mathbf{k},\mathbf{b})} = \langle u_{m\mathbf{k}}|u_{n\mathbf{k}+\mathbf{b}}\rangle, \tag{1.7}$$

where the vectors $\mathbf{b}$, which connect a given k-point with its neighbours, are determined by `wannier90` according to the prescription outlined in Ref. [1].

2. As a starting guess the projection of the Bloch states $|\psi_{n\mathbf{k}}\rangle$ onto trial localised orbitals $|g_n\rangle$

$$A_{mn}^{(\mathbf{k})} = \langle \psi_{m\mathbf{k}}|g_n\rangle, \tag{1.8}$$

Note that $\mathbf{M}^{(\mathbf{k},\mathbf{b})}$, $\mathbf{A}^{(\mathbf{k})}$ and $\mathbf{U}^{(\mathbf{k})}$ are all small, $N \times N$ matrices[1] that are independent of the basis set used to obtain the original Bloch states.

To date, `wannier90` has been used in combination with electronic codes based on plane-waves and pseudopotentials (norm-conserving and ultrasoft [4]) as well as mixed basis set techniques such as FLAPW [5].

1.1   Entangled Energy Bands

The above description is sufficient to obtain MLWF for an isolated set of bands, such as the valence states in an insulator. In order to obtain MLWF for entangled energy bands we use the "disentanglement" procedure introduced in Ref. [2].

We define an energy window (the "outer window"). At a given k-point $\mathbf{k}$, $N_{\mathrm{win}}^{(\mathbf{k})}$ states lie within this energy window. We obtain a set of N Bloch states by performing a unitary transformation amongst the Bloch states which fall within the energy window at each k-point:

$$|u_{n\mathbf{k}}^{\mathrm{opt}}\rangle = \sum_{m \in N_{\mathrm{win}}^{(\mathbf{k})}} U_{mn}^{\mathrm{dis}(\mathbf{k})}|u_{m\mathbf{k}}\rangle \tag{1.9}$$

where $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ is a rectangular $N_{\mathrm{win}}^{(\mathbf{k})} \times N$ matrix[2]. The set of $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ are obtained by minimising the gauge invariant spread Ω_{I} within the outer energy window. The MV procedure can then be used to minimise $\tilde{\Omega}$ and hence obtain MLWF for this optimal subspace.

It should be noted that the energy bands of this optimal subspace may not correspond to any of the original energy bands (due to mixing between states). In order to preserve exactly the properties of a system in a given energy range (e.g., around the Fermi level) we introduce a second energy window. States lying within this inner, or "frozen", energy window are included unchanged in the optimal subspace.

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[1]Technically, this is true for the case of an isolated group of N bands from which we obtain N MLWF. When using the disentanglement procedure of Ref. [2], $\mathbf{A}^{(\mathbf{k})}$, for example, is a rectangular matrix. See Section 1.1.

[2]As $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ is a rectangular matrix this is a unitary operation in the sense that $(\mathbf{U}^{\mathrm{dis}(\mathbf{k})})^{\dagger}\mathbf{U}^{\mathrm{dis}(\mathbf{k})} = \mathbf{1}_N$.

Chapter 2

Parameters

2.1   Usage

`wannier90.x` can be run in parallel using MPI libraries to reduce the computation time.

For serial execution use: `wannier90.x [-pp] [seedname]`

- `seedname`: If a seedname string is given the code will read its input from a file `seedname.win`. The default value is `wannier`. One can also equivalently provide the string `seedname.win` instead of `seedname`.

- `-pp`: This optional flag tells the code to generate a list of the required overlaps and then exit. This information is written to the file `seedname.nnkp`.

For parallel execution use: `mpirun -np NUMPROCS wannier90.x [-pp] [seedname]`

- `NUMPROCS`: substitute with the number of processors that you want to use.

Note that the `mpirun` command and command-line flags may be different in your MPI implementation: read your MPI manual or ask your computer administrator.

Note also that this requires that the `wannier90.x` executable has been compiled in its parallel version (follow the instructions in the file `README.install` in the main directory of the wannier90 distribution) and that the MPI libraries and binaries are installed and correctly configured on your machine.

2.2   `seedname.win` File

The `wannier90` input file `seedname.win` has a flexible free-form structure.

The ordering of the keywords is not significant. Case is ignored (so `num_bands` is the same as `Num_Bands`). Characters after !, or # are treated as comments. Most keywords have a default value that is used unless the keyword is given in `seedname.win`. Keywords can be set in any of the following ways

```
num_wann 4
num_wann = 4
num_wann :   4
```

A logical keyword can be set to `true` using any of the following strings: `T`, `true`, `.true.`.

For further examples see Section 10.1 and the the `wannier90` Tutorial.

2.3 Keyword List

Keyword	Type	Description
System Parameters		
NUM_WANN	I	Number of WF
NUM_BANDS	I	Number of bands passed to the code
UNIT_CELL_CART	P	Unit cell vectors in Cartesian coordinates
ATOMS_CART *	P	Positions of atoms in Cartesian coordinates
ATOMS_FRAC *	R	Positions of atoms in fractional coordinates with respect to the lattice vectors
MP_GRID	I	Dimensions of the Monkhorst-Pack grid of k-points
KPOINTS	R	List of k-points in the Monkhorst-Pack grid
GAMMA_ONLY	L	Wavefunctions from underlying ab initio calculation are manifestly real
SPINORS	L	WF are spinors
SHELL_LIST	I	Which shells to use in finite difference formula
SEARCH_SHELLS	I	The number of shells to search when determining finite difference formula
SKIP_B1_TESTS	L	Check the condition B1 of Ref. [1]
NNKPTS	I	Explicit list of nearest-neighbour k-points.
KMESH_TOL	R	The tolerance to control if two kpoint belong to the same shell

Table 2.1: `seedname.win` file keywords defining the system. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.
* ATOMS_CART and ATOMS_FRAC may not both be defined in the same input file.

Keyword	Type	Description
Job Control		
POSTPROC_SETUP	L	To output the `seedname.nnkp` file
EXCLUDE_BANDS	I	List of bands to exclude from the calculation
SELECT_PROJECTIONS	I	List of projections to use in Wannierisation
AUTO_PROJECTIONS	L	To automatically generate initial projections
RESTART	S	Restart from checkpoint file
IPRINT	I	Output verbosity level
LENGTH_UNIT	S	System of units to output lengths
WVFN_FORMATTED	L	Read the wavefunctions from a (un)formatted file
SPIN	S	Which spin channel to read
DEVEL_FLAG	S	Flag for development use
TIMING_LEVEL	I	Determines amount of timing information written to output
OPTIMISATION	I	Optimisation level
TRANSLATE_HOME_CELL	L	To translate final Wannier centres to home unit cell when writing xyz file
WRITE_XYZ	L	To write atomic positions and final centres in xyz file format
WRITE_VDW_DATA	L	To write data for futher processing by w90vdw utility
WRITE_HR_DIAG	L	To write the diagonal elements of the Hamiltonian in the Wannier basis to seedname.wout (in eV)

Table 2.2: `seedname.win` file keywords defining job control. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string. TRANSLATE_HOME_CELL only relevant if WRITE_XYZ is `.true.`

Keyword	Type	Description
Plot Parameters		
WANNIER_PLOT	L	Plot the WF
WANNIER_PLOT_LIST	I	List of WF to plot
WANNIER_PLOT_SUPERCELL	I	Size of the supercell for plotting the WF
WANNIER_PLOT_FORMAT	S	File format in which to plot the WF
WANNIER_PLOT_MODE	S	Mode in which to plot the WF, molecule or crystal
WANNIER_PLOT_RADIUS	R	Cut-off radius of WF*
WANNIER_PLOT_SCALE	R	Scaling parameter for cube files
WANNIER_PLOT_SPINOR_MODE	S	Quantity to plot for spinor WF

WANNIER_PLOT_SPINOR_PHASE	L	Include the "phase" when plotting spinor WF
BANDS_PLOT	L	Plot interpolated band structure
KPOINT_PATH	P	K-point path for the interpolated band structure
BANDS_NUM_POINTS	I	Number of points along the first section of the k-point path
BANDS_PLOT_FORMAT	S	File format in which to plot the interpolated bands
BANDS_PLOT_PROJECT	I	WF to project the band structure onto
BANDS_PLOT_MODE	S	Slater-Koster type interpolation or Hamiltonian cut-off
BANDS_PLOT_DIM	I	Dimension of the system
FERMI_SURFACE_PLOT	L	Plot the Fermi surface
FERMI_SURFACE_NUM_POINTS	I	Number of points in the Fermi surface plot
FERMI_ENERGY	P	The Fermi energy
FERMI_ENERGY_MIN	P	Lower limit of the Fermi energy range
FERMI_ENERGY_MAX	P	Upper limit of the Fermi energy range
FERMI_ENERGY_STEP	R	Step for increasing the Fermi energy in the specified range
FERMI_SURFACE_PLOT_FORMAT	S	File format for the Fermi surface plot
HR_PLOT	L	This parameter is not used anymore. Use WRITE_HR instead.
WRITE_HR	L	Write the Hamiltonian in the WF basis
WRITE_RMN	L	Write the position operator in the WF basis
WRITE_BVEC	L	Write to file the matrix elements of the bvectors and their weights
WRITE_TB	L	Write lattice vectors, Hamiltonian, and position operator in WF basis
HR_CUTOFF	P	Cut-off for the absolute value of the Hamiltonian
DIST_CUTOFF	P	Cut-off for the distance between WF
DIST_CUTOFF_MODE	S	Dimension in which the distance between WF is calculated
TRANSLATION_CENTRE_FRAC	R	Centre of the unit cell to which final WF are translated
USE_WS_DISTANCE	L	Improve interpolation using minimum distance between WFs, see Chap. 9
WS_DISTANCE_TOL	R	Absolute tolerance for the distance to equivalent positions.

WS_SEARCH_SIZE	I	Maximum extension in each direction of the super-cell of the Born-von Karmann cell to search for points inside the Wigner-Seitz cell
WRITE_U_MATRICES	L	Write $\mathbf{U}^{(\mathbf{k})}$ and $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ matrices to files

Table 2.5: `seedname.win` file keywords controlling the plotting. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string. * Only applies when WANNIER_PLOT_FORMAT is `cube`.

Keyword	Type	Description
Disentanglement Parameters		
DIS_WIN_MIN	P	Bottom of the outer energy window
DIS_WIN_MAX	P	Top of the outer energy window
DIS_FROZ_MIN	P	Bottom of the inner (frozen) energy window
DIS_FROZ_MAX	P	Top of the inner (frozen) energy window
DIS_NUM_ITER	I	Number of iterations for the minimisation of Ω_I
DIS_MIX_RATIO	R	Mixing ratio during the minimisation of Ω_I
DIS_CONV_TOL	R	The convergence tolerance for finding Ω_I
DIS_CONV_WINDOW	I	The number of iterations over which convergence of Ω_I is assessed.
DIS_SPHERES_NUM	I	Number of spheres in k-space where disentaglement is performed
DIS_SPHERES_FIRST_WANN	I	Index of the first band to be considered a Wannier function
DIS_SPHERES	R	List of centres and radii, for disentanglement only in spheres

Table 2.3: `seedname.win` file keywords controlling the disentanglement. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

Keyword	Type	Description
Wannierise Parameters		
NUM_ITER	I	Number of iterations for the minimisation of Ω
NUM_CG_STEPS	I	During the minimisation of Ω the number of Conjugate Gradient steps before resetting to Steepest Descents
CONV_WINDOW	I	The number of iterations over which convergence of Ω is assessed
CONV_TOL	P	The convergence tolerance for finding Ω
PRECOND	L	Use preconditioning
CONV_NOISE_AMP	R	The amplitude of random noise applied towards end of minimisation procedure
CONV_NOISE_NUM	I	The number of times random noise is applied
NUM_DUMP_CYCLES	I	Control frequency of check-pointing
NUM_PRINT_CYCLES	I	Control frequency of printing
WRITE_R2MN	L	Write matrix elements of r^2 between WF to file
GUIDING_CENTRES	L	Use guiding centres
NUM_GUIDE_CYCLES	I	Frequency of guiding centres
NUM_NO_GUIDE_ITER	I	The number of iterations after which guiding centres are used
TRIAL_STEP *	R	The trial step length for the parabolic line search during the minimisation of Ω
FIXED_STEP *	R	The fixed step length to take during the minimisation of Ω, instead of doing a parabolic line search
USE_BLOCH_PHASES **	L	To use phases for initial projections
SITE_SYMMETRY***	L	To construct symmetry-adapted Wannier functions
SYMMETRIZE_EPS***	R	The convergence tolerance used in the symmetry-adapted mode
SLWF_NUM	I	The number of objective WFs for selective localization
SLWF_CONSTRAIN	L	Whether to constrain the centres of the objective WFs
SLWF_LAMBDA	R	Value of the Lagrange multiplier for constraining the objective WFs
SLWF_CENTRES	P	The centres to which the objective WFs are to be constrained

Table 2.4: `seedname.win` file keywords controlling the wannierisation. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string. * FIXED_STEP and TRIAL_STEP may not both be defined in the same input file. **Cannot be used in conjunction with disentanglement. ***Cannot be used in conjunction with the inner (frozen) energy window.

Keyword	Type	Description
Transport Parameters		
TRANSPORT	L	Calculate quantum conductance and density of states
TRANSPORT_MODE	S	Bulk or left-lead_conductor_right-lead calculation
TRAN_WIN_MIN	P	Bottom of the energy window for transport calculation
TRAN_WIN_MAX	P	Top of the energy window for transport calculation
TRAN_ENERGY_STEP	R	Sampling interval of the energy values
FERMI_ENERGY	R	The Fermi energy
TRAN_NUM_BB	I	Size of a bulk Hamiltonian
TRAN_NUM_LL	I	Size of a left-lead Hamiltonian
TRAN_NUM_RR	I	Size of a right-lead Hamiltonian
TRAN_NUM_CC	I	Size of a conductor Hamiltonian
TRAN_NUM_LC	I	Number of columns in a left-lead_conductor Hamiltonian
TRAN_NUM_CR	I	Number of rows in a conductor_right-lead Hamiltonian
TRAN_NUM_CELL_LL	I	Number of unit cells in PL of left lead
TRAN_NUM_CELL_RR	I	Number of unit cells in PL of right lead
TRAN_NUM_BANDC	I	Half-bandwidth+1 of a band-diagonal conductor Hamiltonian
TRAN_WRITE_HT	L	Write the Hamiltonian for transport calculation
TRAN_READ_HT	L	Read the Hamiltonian for transport calculation
TRAN_USE_SAME_LEAD	L	Left and right leads are the same
TRAN_GROUP_THRESHOLD	R	Distance that determines the grouping of WFs
HR_CUTOFF	P	Cut-off for the absolute value of the Hamiltonian
DIST_CUTOFF	P	Cut-off for the distance between WF
DIST_CUTOFF_MODE	S	Dimension in which the distance between WF is calculated
ONE_DIM_AXIS	S	Extended direction for a one-dimensional system
TRANSLATION_CENTRE_FRAC	R	Centre of the unit cell to which final WF are translated

Table 2.6: `seedname.win` file keywords controlling transport. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

2.4   System

2.4.1   integer :: num_wann

Number of WF to be found.

No default.

2.4.2   integer :: num_bands

Total number of bands passed to the code in the `seedname.mmn` file.

Default `num_bands`=`num_wann`

2.4.3   Cell Lattice Vectors

The cell lattice vectors should be specified in Cartesian coordinates.

`begin unit_cell_cart`
`[units]`

$$
\begin{matrix}
A_{1x} & A_{1y} & A_{1z} \\
A_{2x} & A_{2y} & A_{2z} \\
A_{3x} & A_{3y} & A_{3z}
\end{matrix}
$$

`end unit_cell_cart`

Here A_{1x} is the x-component of the first lattice vector $\mathbf{A}_1$, A_{2y} is the y-component of the second lattice vector $\mathbf{A}_2$, etc.

`[units]` specifies the units in which the lattice vectors are defined: either `Bohr` or `Ang`.

The default value is `Ang`.

2.4.4   Ionic Positions

The ionic positions may be specified in fractional coordinates relative to the lattice vectors of the unit cell, or in absolute Cartesian coordinates. Only one of `atoms_cart` and `atoms_frac` may be given in the input file.

Cartesian coordinates

`begin atoms_cart`
`[units]`

$$
\begin{matrix}
P & R_x^P & R_y^P & R_z^P \\
Q & R_x^Q & R_y^Q & R_z^Q \\
 & \vdots & &
\end{matrix}
$$

`end atoms_cart`

The first entry on a line is the atomic symbol. The next three entries are the atom's position $\mathbf{R} = (R_x, R_y, R_z)$ in Cartesian coordinates. The first line of the block, [units], specifies the units in which the coordinates are given and can be either `bohr` or `ang`. If not present, the default is `ang`.

Fractional coordinates

begin atoms_frac

$$\begin{array}{cccc} P & F_1^P & F_2^P & F_3^P \\ Q & F_1^Q & F_2^Q & F_3^Q \\ & \vdots & & \end{array}$$

end atoms_frac

The first entry on a line is the atomic symbol. The next three entries are the atom's position in fractional coordinates $\mathbf{F} = F_1\mathbf{A}_1 + F_2\mathbf{A}_2 + F_3\mathbf{A}_3$ relative to the cell lattice vectors $\mathbf{A}_i$, $i \in [1,3]$.

2.4.5 integer, dimension :: mp_grid(3)

Dimensions of the regular (Monkhorst-Pack) k-point mesh. For example, for a $2 \times 2 \times 2$ grid:

mp_grid : 2 2 2

No default.

2.4.6 K-points

Each line gives the coordinate $\mathbf{K} = K_1\mathbf{B}_1 + K_2\mathbf{B}_2 + K_3\mathbf{B}_3$ of a k-point in relative (crystallographic) units, i.e., in fractional units with respect to the primitive reciprocal lattice vectors $\mathbf{B}_i$, $i \in [1,3]$. The position of each k-point in this list assigns its numbering; the first k-point is k-point 1, the second is k-point 2, and so on.

begin kpoints

$$\begin{array}{ccc} K_1^1 & K_2^1 & K_3^1 \\ K_1^2 & K_2^2 & K_3^2 \\ & \vdots & \end{array}$$

end kpoints

There is no default.

Note: There is an utility provided with `wannier90`, called `kmesh.pl`, which helps to generate the explicit list of k points required by `wannier90`. See Sec. A.1.

2.4.7 logical :: gamma_only

If `gamma_only=true`, then `wannier90` uses a branch of algorithms for disentanglement and localisation that exploit the fact that the Bloch eigenstates obtained from the underlying ab initio calculation are manifestly real. This can be the case when only the Γ-point is used to sample the Brillouin zone. The localisation procedure that is used in the Γ-only branch is based on the method of Ref. [6].

The default value is `false`.

2.4.8 `logical :: spinors`

If `spinors=true`, then `wannier90` assumes that the WF correspond to singularly occupied spinor states and `num_elec_per_state=1`.

The default value is `false`.

2.4.9 Shells

The MV scheme requires a finite difference expression for $\nabla_{\mathbf{k}}$ defined on a uniform Monkhorst-Pack mesh of k-points. The vectors $\{\mathbf{b}\}$ connect each mesh-point $\mathbf{k}$ to its nearest neighbours. N_{sh} shells of neighbours are included in the finite-difference formula, with M_s vectors in the sth shell. For $\nabla_{\mathbf{k}}$ to be correct to linear order, we require that the following equation is satisfied (Eq. B1 of Ref. [1]):

$$\sum_s^{N_{\mathrm{sh}}} w_s \sum_i^{M_{\mathrm{s}}} b_\alpha^{i,s} b_\beta^{i,s} = \delta_{\alpha\beta} \;, \tag{2.1}$$

where $\mathbf{b}^{i,s}$, $i \in [1, M_s]$, is the ith vector belonging to the sth shell with associated weight w_s, and α and β run over the three Cartesian indices.

2.4.10 `integer :: shell_list(:)`

`shell_list` is vector listing the shells to include in the finite difference expression. If this keyword is absent, the shells are chosen automatically.

2.4.11 `integer :: search_shells`

Specifies the number of shells of neighbours over which to search in attempting to determine an automatic solution to the B1 condition Eq. 2.1. Larger values than the default may be required in special cases e.g. for very long thin unit cells.

The default value is 36.

2.4.12 `logical :: skip_B1_tests`

If set to `.true.`, does not check the B1 condition Eq. 2.1. This should *only* be used if one knows why the B1 condition should not be verified. A typical use of this flag is in conjunction with the Z2PACK code: `http://www.physics.rutgers.edu/z2pack/`.

The default value is `.false.`.

2.4.13 `integer, dimension(:, 5) :: nnkpts`

Specifies the nearest-neighbour k-points which are written to the `.nnkp` file. This can be used to explicitly specify which overlap matrices should be calculated.

```
begin nnkpts
1   2   0  0  0
.
.
end nnkpts
```

Each nearest neighbour $\mathbf{k} + \mathbf{b}$ is given by a line of 5 integers. The first specifies the k-point number `nkp` of $\mathbf{k}$. The second is the k-point number of the neighbour. The final three integers specify the reciprocal lattice vector which brings the k-point specified by the second integer to $\mathbf{k} + \mathbf{b}$.

This format is the same as in the `.nnkp` file, except that the number of neighbours per k-point is not specified. However, the number of neighbours still needs to be a multiple of the number of k-points.

This input parameter can be used only if `postproc_setup = .true.`, and is not intended to be used with a full Wannier90 run. It can be used also if the k-points do not describe a regular mesh.

2.4.14 `real(kind=dp) :: kmesh_tol`

Two kpoints belong to the same shell if the distance between them is less than `kmesh_tol`. Units are Ang.

The default value is 0.000001 Ang.

2.5   Projection

The projections block defines a set of localised functions used to generate an initial guess for the unitary transformations. This data will be written in the `seedname.nnkp` file to be used by a first-principles code.

```
begin projections
.
.
end projections
```

If `guiding_centres=true`, then the projection centres are used as the guiding centres in the Wannierisation routine.

For details see Section 3.1.

2.6   Job Control

2.6.1 `logical :: postproc_setup`

If `postproc_setup=true`, then the wannier code will write `seedname.nnkp` file and exit. If `wannier90` is called with the option `-pp`, then `postproc_setup` is set to `true`, over-riding its value in the `seedname.win` file.

The default value is `false`.

2.6.2 `integer :: iprint`

This indicates the level of verbosity of the output from 0 ("low"), the bare minimum, to 3 ("high"), which corresponds to full debugging output.

The default value is 1.

2.6.3 `integer :: optimisation`

This indicates the level of optimisation used in the code. This is a trade between speed and memory. A positive number indicates fastest execution time at the cost of more memory. Zero or negative numbers indicates a smaller memory footprint - at increased execution time.

At the moment the only values that have an effect are `optimisation<=0` (low memory) and `optimisation>0` (fast)

The default value is 3.

2.6.4 `character(len=20) :: length_unit`

The length unit to be used for writing quantities in the output file `seedname.wout`.

The valid options for this parameter are:

  – `Ang` (default)

  – `Bohr`

2.6.5 `character(len=50) :: devel_flag`

Not a regular keyword. Its purpose is to allow a developer to pass a string into the code to be used inside a new routine as it is developed.

No default.

2.6.6 `integer :: exclude_bands(:)`

A k-point independent list of states to excluded from the calculation of the overlap matrices; for example to select only valence states, or ignore semi-core states. This keyword is passed to the first-principles code via the `seedname.nnkp` file. For example, to exclude bands 2, 6, 7, 8 and 12:

`exclude_bands : 2, 6-8, 12`

2.6.7 `integer :: select_projections(:)`

A list of projections to be included in the wannierisation procedure. In the case that `num_proj` is greater than `num_wann`, this keyword allows a subset of the projections in the projection matrices to be used. For example, to select the projections given by the indices 2, 6, 7, 8 and 12:

`select_projections : 2, 6-8, 12`

2.6.8 logical :: auto_projections

If .true. and no projections block is defined, then wannier90 writes an additional block in the .nnkp file during the pre-processing step, to instruct the interface code to automatically generate the $A_{mn}^{(\mathbf{k})}$.

For additional information on the behavior and on the added block, see Sec. 5.1.9.

Note: the interface code (e.g. pw2wannier90.x) must have at least one implementation of a method to automatically generate initial projections in order for this option to be usable.

The default value of this parameter is false.

2.6.9 character(len=20) :: restart

If restart is present the code will attempt to restart the calculation from the seedname.chk file. The value of the parameter determines the position of the restart

The valid options for this parameter are:

- default. Restart from the point at which the check file seedname.chk was written

- wannierise. Restart from the beginning of the wannierise routine

- plot. Go directly to the plotting phase

- transport. Go directly to the transport routines

2.6.10 character(len=20) :: wvfn_formatted

If wvfn_formatted=true, then the wavefunctions will be read from disk as formatted (ie ASCII) files; otherwise they will be read as unformatted files. Unformatted is generally preferable as the files will take less disk space and I/O is significantly faster. However such files will not be transferable between all machine architectures and formatted files should be used if transferability is required (i.e., for test cases).

The default value of this parameter is false.

2.6.11 character(len=20) :: spin

For bands from a spin polarised calculation spin determines which set of bands to read in, either up or down.

The default value of this parameter is up.

2.6.12 integer :: timing_level

Determines the amount of timing information regarding the calculation that will be written to the output file. A value of 1 produces the least information.

The default value is 1.

2.6.13 `logical :: translate_home_cell`

Determines whether to translate the final Wannier centres to the home unit cell at the end of the calculation. Mainly useful for molecular systems in which the molecule resides entirely within the home unit cell and user wants to write an xyz file (`write_xyz=.true.`) for the WF centres to compare with the structure.

The default value is `false`.

2.6.14 `logical :: write_xyz`

Determines whether to write the atomic positions and final Wannier centres to an xyz file, `seedname_centres.xyz`, for subsequent visualisation.

The default value is `false`.

2.6.15 `logical :: write_vdw_data`

Determines whether to write `seedname.vdw` for subsequent post-processing by the `w90vdw` utility (in the `utility/w90vdw/` directory of the distribution) for calculating van der Waals energies. Brillouin zone sampling must be at the Gamma-point only.

The default value is `false`.

2.7 Disentanglement

These keywords control the disentanglement routine of Ref. [2], i.e., the iterative minimisation of Ω_I. This routine will be activated if `num_wann` < `num_bands`.

2.7.1 `real(kind=dp) :: dis_win_min`

The lower bound of the outer energy window for the disentanglement procedure. Units are eV.

The default is the lowest eigenvalue in the system.

2.7.2 `real(kind=dp) :: dis_win_max`

The upper bound of the outer energy window for the disentanglement procedure. Units are eV.

The default is the highest eigenvalue in the given states (i.e., all states are included in the disentanglement procedure).

2.7.3 `real(kind=dp) :: dis_froz_min`

The lower bound of the inner energy window for the disentanglement procedure. Units are eV.

If `dis_froz_max` is given, then the default for `dis_froz_min` is `dis_win_min`.

2.7.4 real(kind=dp) :: dis_froz_max

The upper bound of the inner (frozen) energy window for the disentanglement procedure. If `dis_froz_max` is not specified, then there are no frozen states. Units are eV.

No default.

2.7.5 integer :: dis_num_iter

In the disentanglement procedure, the number of iterations used to extract the most connected subspace.

The default value is 200.

2.7.6 real(kind=dp) :: dis_mix_ratio

In the disentanglement procedure, the mixing parameter to use for convergence (see pages 4-5 of Ref. [2]). A value of 0.5 is a 'safe' choice. Using 1.0 (i.e., no mixing) often gives faster convergence, but may cause the minimisation of Ω_I to be unstable in some cases.

Restriction: $0.0 < $ `dis_mix_ratio` ≤ 1.0

The default value is 0.5

2.7.7 real(kind=dp) :: dis_conv_tol

In the disentanglement procedure, the minimisation of Ω_I is said to be converged if the fractional change in the gauge-invariant spread between successive iterations is less than `dis_conv_tol` for `dis_conv_window` iterations. Units are Å^2.

The default value is 1.0E-10

2.7.8 integer :: dis_conv_window

In the disentanglement procedure, the minimisation is said to be converged if the fractional change in the spread between successive iterations is less than `dis_conv_tol` for `dis_conv_window` iterations.

The default value of this parameter is 3.

2.7.9 integer :: dis_spheres_num

Number of spheres in reciprocal space where the k-dependent disentanglement is performed. No disentanglement is performed for those k-points that are not included in any of the spheres.

The default is 0, which means disentangle at every k-point in the full BZ (the standard mode in Wannier90).

2.7.10   integer :: dis_spheres_first_wann

Index of the first band that has to be considered as a Wannier function. Used only if `dis_spheres_num` is greater than zero. At k-points where disentanglement is not performed the bands from `dis_spheres_first_wann` to `dis_spheres_first_wann+num_wann` are used to wannierise. The bands excluded using `exclude_bands` should not be counted.

The default is 1, the band at the lowest energy.

2.7.11   dis_spheres

Each line gives the coordinate $\mathbf{K} = K_1\mathbf{B}_1 + K_2\mathbf{B}_2 + K_3\mathbf{B}_3$ of a k-point representing the center of one of the spheres used for k-dependent disentanglement. The same crystallographic units as for `kpoints` are used here. Each k-point coordinate $\mathbf{K}^i$ must the followed by the respectice sphere radius r_i in inverse angstrom (on the same line).

The number of lines must be equal to `dis_spheres_num`.

`begin dis_spheres`

$$
\begin{array}{cccc}
K_1^1 & K_2^1 & K_3^1 & r_1 \\
K_1^2 & K_2^2 & K_3^2 & r_2 \\
& \vdots &
\end{array}
$$

`end dis_spheres`

There is no default.

2.8   Wannierise

Iterative minimisation of $\widetilde{\Omega}$, the non-gauge-invariant part of the spread functional.

2.8.1   integer :: num_iter

Total number of iterations in the minimisation procedure. Set `num_iter=0` if you wish to generate projected WFs rather than maximally-localized WFs (see Example 8 in the Tutorial).

The default value is 100

2.8.2   integer :: num_cg_steps

Number of conjugate gradient steps to take before resetting to steepest descents.

The default value is 5

2.8.3   integer :: conv_window

If `conv_window` > 1, then the minimisation is said to be converged if the change in Ω over `conv_window` successive iterations is less than `conv_tol`. Otherwise, the minimisation proceeds for num_iter iterations (default).

The default value is -1

2.8.4 `real(kind=dp) :: conv_tol`

If `conv_window > 1`, then this is the convergence tolerance on Ω, otherwise not used. Units are Å^2.

The default value is 1.0E-10

2.8.5 `logical :: precond`

Whether or not to use preconditioning to speed up the minimization of the spreads. This is based on the same idea as the classical Tetter-Payne-Allan preconditionning for DFT and dampens the high-frequency oscillations of the gradient due to contributions from large real lattice vectors. It is useful when the optimization is slow, especially on fine grids. When `optimisation<3`, this uses a slower algorithm to save memory.

The default value is `false`.

2.8.6 `real(kind=dp) :: conv_noise_amp`

If `conv_noise_amp > 0`, once convergence (as defined above) is achieved, some random noise f is added to the search direction, and the minimisation is continued until convergence is achieved once more. If the same value of Ω as before is arrived at, then the calculation is considered to be converged. If not, then random noise is added again and the procedure repeated up to a maximum of `conv_noise_num` times. `conv_noise_amp` is the amplitude of the random noise f that is added to the search direction: $0 < |f| < $ `conv_noise_amp`. This functionality requires `conv_window > 1`. If `conv_window` is not specified, it is set to the value 5 by default.

If `conv_noise_amp` ≤ 0, then no noise is added (default).

The default value is -1.0

2.8.7 `integer :: conv_noise_num`

If `conv_noise_amp > 0`, then this is the number of times in the minimisation that random noise is added.

The default value is 3

2.8.8 `integer :: num_dump_cycles`

Write sufficient information to do a restart every `num_dump_cycles` iterations.

The default is 100

2.8.9 `integer :: num_print_cycles`

Write data to the master output file `seedname.wout` every `num_print_cycles` iterations.

The default is 1

2.8.10 `logical :: write_r2mn`

If `write_r2mn = true`, then the matrix elements $\langle m|r^2|n\rangle$ (where m and n refer to WF) are written to file `seedname.r2mn` at the end of the Wannierisation procedure.

The default value of this parameter is `false`.

2.8.11 `logical :: guiding_centres`

Use guiding centres during the minimisation, in order to avoid local minima.

`wannier90` uses a logarithm definition of the spread functional. As we are taking the log of a complex argument there is a possibility that the algorithm might make inconsistent choices for the branch cut. This manifests itself as complex WF with a large spread. By using guiding centres the code will attempt to make a consistent choice of branch cut. Experience shows that with `guiding_centres` set to true this problem is avoided and doing so does not cause any problems. For this reason we recommend setting `guiding_centres` to true where possible (it is only not possible if an explicit projection block is not defined).

The default value is `false`.

2.8.12 `integer :: num_guide_cycles`

If `guiding_centres` is set to true, then the guiding centres are used only every `num_guide_cycles`.

The default value is 1.

2.8.13 `integer :: num_no_guide_iter`

If `guiding_centres` is set to true, then the guiding centres are used only after `num_no_guide_iter` minimisation iterations have been completed.

The default value is 0.

2.8.14 `real(kind=dp) :: trial_step`

The value of the trial step for the parabolic fit in the line search minimisation used in the minimisation of the spread function. Cannot be used in conjunction with `fixed_step` (see below). If the minimisation procedure doesn't converge, try decreasing the value of `trial_step` to give a more accurate line search.

The default value is 2.0

2.8.15 `real(kind=dp) :: fixed_step`

If this is given a value in the input file, then a fixed step of length `fixed_step` (instead of a parabolic line search) is used at each iteration of the spread function minimisation. Cannot be used in conjunction

with `trial_step`. This can be useful in cases in which minimisation with a line search fails to converge.

There is no default value.

2.8.16   logical :: use_bloch_phases

Determines whether to use the Bloch functions as the initial guess for the projections. Can only be used if `disentanglement = false`.

The default value is `false`.

2.8.17   logical :: site_symmetry

Construct symmetry-adapted Wannier functions. For the detail of the theoretical background, see Ref. [7]. Cannot be used in conjunction with the inner (frozen) energy window.

The default value is `false`.

2.8.18   real(kind=dp) :: symmetrize_eps

Convergence threshold to check whether the symmetry condition (Eq. (19) in Ref. [7]) on the unitary matrix $\mathbf{U}^{(\mathbf{k})}$ is satisfied or not. See also Eq. (29) in Ref. [7]. Used when `site_symmetry = .true.`

The default value is 1.0E-3.

2.8.19   integer :: slwf_num

The number of objective Wannier functions for selective localisation in the selectively localised Wannier function (SLWF) method of Ref. [8]. These functions are obtained by minimising the spread functional only with respect to the degrees of freedom of a subset of `slwf_num` < `num_wann` functions. At convergence, the objective WFs will have a minimum cumulative spread, whereas the remaining `num_wann` − `slwf_num` functions are left unoptimised. The initial guesses for the objective WFs are given by the first `slwf_num` orbitals in the `projections` block. If `slwf_num` = `num_wann` no selective minimisation is performed. In this case, `wannier90` will simply generate a set of `num_wann` MLWFs.

The default is `num_wann`.

2.8.20   logical :: slwf_constrain

If `slwf_constrain=true`, then the centres of the objective Wannier functions are constrained to either the centres of the first `slwf_num` orbitals in the `projections` block or to new positions specified in the `slwf_centres` block (see Sec. 2.8.22). In this case, a modified spread functional, Ω_c, with the addition of a constraint term, as described in Ref. [8].

The default is `false`

2.8.21 `real(kind=dp) :: slwf_lambda`

The value of the Lagrange multiplier λ for the constraint term in term added to modify the spread functional: $\lambda \sum_{n=1}^{J'} (\bar{\mathbf{r}}_n - \mathbf{r}_{0n})^2$, where J' is `slwf_num`, and $\bar{\mathbf{r}}_n$ and $\mathbf{r}_{0n}$ are the centre and target centre, respectively, for the nth objective WF.

The default is `0.0`.

2.8.22 Constraints on centres

If `slwf_constrain=true`, then by default the centres to which the `slwf_num` objective Wannier function centres are constrained are given by the first `slwf_num` rows of the `projections` block.

Optionally, the `slwf_centres` block may be used to define alternative target centres for some or all of the `slwf_num` objective Wannier functions.

The block below shows an example of how to set the constraints:

```
begin slwf_centres
   2  0.0   0.0  0.0
   4  0.25  0.0  0.0
end slwf_centres
```

- The first line sets the constraint for the centre of objective WF number 2 (as defined by the order of WFs in the `projections` block) to (0.0,0.0,0.0) in fractional co-ordinates.

- The second line sets the constraint for the centre of objective WF number 4 (as defined by the order of WFs in the `projections` block) to (0.25,0.0,0.0) in fractional co-ordinates.

- The target centres of all other objective Wannier functions remain as the centres given in the corresponding rows of the `projections` block.

2.9 Post-Processing

Capabilities:

- Plot the WF

- Plot the interpolated band structure

- Plot the Fermi surface

- Output the Hamiltonian in the WF basis

- Transport calculation (quantum conductance and density of states)

2.9.1 `logical :: wannier_plot`

If `wannier_plot = true`, then the code will write out the Wannier functions in a format specified by `wannier_plot_format`

The default value of this parameter is `false`.

2.9.2 integer :: wannier_plot_list(:)

A list of WF to plot. The WF numbered as per the `seedname.wout` file after the minimisation of the spread.

The default behaviour is to plot all WF. For example, to plot WF 4, 5, 6 and 10:

`wannier_plot_list : 4-6, 10`

2.9.3 integer :: wannier_plot_supercell

The code generates the WFs on a grid corresponding to a 'super-unit-cell'. If `wannier_plot_supercell` is provided as a single integer, then the size of the super-unit-cell is `wannier_plot_supercell` times the size of the unit cell along all three linear dimensions (the 'home' unit cell is kept approximately in the middle); otherwise, if three integers are provided, the size of the super-unit-cell is `wannier_plot_supercell(i)` times the size of the unit cell along the $i-$th linear dimension.

The default value is 2.

2.9.4 character(len=20) :: wannier_plot_format

WF can be plotted in either XCrySDen (xsf) format or Gaussian cube format. The valid options for this parameter are:

– `xcrysden` (default)

– `cube`

If `wannier_plot_format=xsf`: the code outputs the WF on the entire super-unit-cell specified by `wannier_plot_supercell`.

If `wannier_plot_format=cube`: the code outputs the WF on a grid that is smaller than the super-unit-cell specified by `wannier_plot_supercell`. This grid is determined by `wannier_plot_mode`, `wannier_plot_radius` and `wannier_plot_scale`, described in detail below.

The code is able to output Gaussian cube files for systems with non-orthogonal lattice vectors. Many visualisation programs (including XCrySDen), however, are only able to handle cube files for systems with *orthogonal* lattice vectors. One visualisation program that is capable of dealing with non-orthogonal lattice vectors is VESTA (`http://jp-minerals.org/vesta/en/`).[1]

2.9.5 character(len=20) :: wannier_plot_mode

Choose the mode in which to plot the WF, either as a molecule or as a crystal.

The valid options for this parameter are:

– `crystal` (default)

---

[1]It's worth noting that another visualisation program, VMD (`http://www.ks.uiuc.edu/Research/vmd`), is able to deal with certain special cases of non-orthogonal lattice vectors; see `http://www.ks.uiuc.edu/Research/vmd/plugins/molfile/cubeplugin.html` for details.

– `molecule`

If `wannier_plot_format=cube`:

- if `wannier_plot_mode = molecule`, then wherever the WF centre sits in the supercell, the origin of the cube is shifted (for the purpose of plotting only, ie, nothing is done to the U matrices etc) to coincide with the centre of mass of the atomic positions specified by the user in the `*.win` input file. These atomic positions are also written to the cube file, so when it is visualised, the WF appears superimposed on the molecular structure.

- if `wannier_plot_mode = crystal`, then the WF is not shifted, but instead the code searches for atoms that are within a radius of `wannier_plot_scale` × `wannier_plot_radius` of the WF centre and writes the coordinates of these atoms to the cube file. In this way, when the cube file is visualised, the WF appears superimposed on the nearest atoms to the WF centre.

- `crystal` mode can be used for molecules, and `molecule` mode can be used for crystals.

2.9.6   real(kind=dp) ::   wannier_plot_radius

If `wannier_plot_format=cube`, then `wannier_plot_radius` is the radius of the sphere that must fit inside the parallelepiped in which the WF is plotted. `wannier_plot_radius` must be greater than 0. Units are Å.

The default value is 3.5.

2.9.7   real(kind=dp) ::   wannier_plot_scale

If `wannier_plot_format=cube` and `wannier_plot_mode=crystal`, then the code searches for atoms that are within a radius of `wannier_plot_scale` × `wannier_plot_radius` of the WF centre and writes the coordinates of these atoms to the cube file. In this way, when the cube file is visualised, the WF appears superimposed on the nearest atoms to the WF centre. `wannier_plot_scale` must be greater than 0. This parameter is dimensionless.

The default value is 1.0.

2.9.8   character(len=20) ::   wannier_plot_spinor_mode

If `spinors = true` then this parameter controls the quantity to plot. For a spinor WF with components $[\phi, \psi]$ the quatity plotted is

- `total` (default). $\sqrt{[|\phi|^2 + |\psi|^2}$

- `up`. $|\phi| \times sign(Re\{\phi\})$ if `wannier_plot_spinor_phase = true`, otherwise $|\phi|$

- `down`. $|\psi| \times sign(Re\{\psi\})$ if `wannier_plot_spinor_phase = true`, otherwise $|\psi|$

Note: making a visual representation of a spinor WF is not as straightforward as for a scalar WF. While a scalar WF is typically a real valued function, a spinor WF is a complex, two component spinor. `wannier90` is able to plot several different quantities derived from a spinor WF which should give you a good idea of the nature of the WF.

2.9.9 logical :: wannier_plot_spinor_phase

If `wannier_plot_spinor_phase = true` phase information will be taken into account when plotting a spinor WF.

2.9.10 logical :: bands_plot

If `bands_plot = true`, then the code will calculate the band structure, through Wannier interpolation, along the path in k-space defined by `bands_kpath` using `bands_num_points` along the first section of the path and write out an output file in a format specified by `bands_plot_format`.

The default value is `false`.

2.9.11 kpoint_path

Defines the path in k-space along which to calculate the bandstructure. Each line gives the start and end point (with labels) for a section of the path. Values are in fractional coordinates with respect to the primitive reciprocal lattice vectors.

`begin kpoint_path`

$$
\begin{array}{cccccccc}
G & 0.0 & 0.0 & 0.0 & L & 0.0 & 0.0 & 1.0 \\
L & 0.0 & 0.0 & 1.0 & N & 0.0 & 1.0 & 1.0 \\
& \vdots & & & & & &
\end{array}
$$

`end kpoint_path`

There is no default

2.9.12 integer :: bands_num_points

If `bands_plot = true`, then the number of points along the first section of the bandstructure plot given by `kpoint_path`. Other sections will have the same density of k-points.

The default value for `bands_num_points` is 100.

2.9.13 character(len=20) :: bands_plot_format

Format in which to plot the interpolated band structure. The valid options for this parameter are:

- `gnuplot` (default)

- `xmgrace`

Note: it is possible to request output in both formats eg `bands_format = gnuplot xmgrace`

2.9.14 integer :: bands_plot_project(:)

If present `wannier90` will compute the contribution of this set of WF to the states at each point of the interpolated band structure. The WF are numbered according to the seedname.wout file. The result is

written in the `seedname_band.dat` file, and a corresponding gnuplot script to `seedname_band_proj.dat`
.

For example, to project on to WFs 2, 6, 7, 8 and 12:

`bands_plot_project : 2, 6-8, 12`

2.9.15 character(len=20) :: bands_plot_mode

To interpolate the band structure along the k-point path, either use the Slater-Koster interpolation
scheme or truncate the Hamiltonian matrix in the WF basis. Truncation criteria are provided by
`hr_cutoff` and `dist_cutoff`.

The valid options for this parameter are:

- `s-k` (default)

- `cut`

2.9.16 integer :: bands_plot_dim

Dimension of the system. If `bands_plot_dim` < 3 and `bands_plot_mode` $=$ `cut`, lattice vector $\mathbf{R} = N_1\mathbf{A}_1 + N_2\mathbf{A}_2 + N_3\mathbf{A}_3$, where $N_i = 0$ if $\mathbf{A}_i$ is parallel to any of the confined directions specified by
`one_dim_axis`, are exclusively used in the band structure interpolation.

The valid options for this parameter are:

- 3 (default)

- 2

- 1

2.9.17 logical :: fermi_surface_plot

If `fermi_surface_plot` $=$ `true`, then the code will calculate, through Wannier interpolation, the
eigenvalues on a regular grid with `fermi_surface_num_points` in each direction. The code will write
a file in bxsf format which can be read by XCrySDen in order to plot the Fermi surface.

The default value is `false`.

2.9.18 integer :: fermi_surface_num_points

If `fermi_surface_plot` $=$ `true`, then the number of divisions in the regular k-point grid used to
calculate the Fermi surface.

The default value for `fermi_surface_num_points` is 50.

2.9.19 `real(kind=dp) :: fermi_energy`

The Fermi energy in eV. This parameter is written into the bxsf file. If `fermi_energy` is specified, `fermi_energy_min`, `fermi_energy_max`, and `fermi_energy_step` should not be specified, and vice-versa.

The default value is 0.0

2.9.20 `real(kind=dp) :: fermi_energy_min`

Instead of specifyfing a single Fermi energy, it is possible to scan the Fermi level over a range of values, and recompute certain quantities for each ε_F.[2] This is the minimum value in the range (in eV).

There is no default value.

2.9.21 `real(kind=dp) :: fermi_energy_max`

The maximum value in the range of Fermi energies. Units are eV.

The default value is `fermi_energy_min`+1.0.

2.9.22 `real(kind=dp) :: fermi_energy_step`

Difference between consecutive values of the Fermi energy when scanning from `fermi_energy_min` to `fermi_energy_max`. Units are eV.

The default value is 0.01.

2.9.23 `character(len=20) :: fermi_surface_plot_format`

Format in which to plot the Fermi surface. The valid options for this parameter are:

- `xcrysden` (default)

2.9.24 `logical :: write_hr`

If `write_hr = true`, then the Hamiltonian matrix in the WF basis will be written to a file `seedname_hr.dat`.

The default value is `false`.

2.9.25 `logical :: write_rmn`

If `write_rmn = true`, then the position operator in the WF basis will be written to a file `seedname_r.dat`.

The default value is `false`.

---

[2]Scanning the Fermi level is currently supported only by the `postw90` module `berry`, for `berry_task=ahc,morb`. For all other functionalities that require a knowledge of ε_F, use `fermi_energy` instead.

2.9.26 logical :: write_bvec

If `write_bvec = true`, then the the matrix elements of bvector and their weights will be written to a file `seedname.bvec`.

The default value is `false`.

2.9.27 logical :: write_tb

If `write_tb = true`, then the lattice vectors, together with the Hamiltonian and position-operator matrices in the WF basis, will be written to a file `seedname_tb.dat`, in units of Angstrom and eV.

The default value is `false`.

2.9.28 logical :: transport

If `transport = true`, then the code will calculate quantum conductance and density of states of a one-dimensional system. The results will be written to files `seedname_qc.dat` and `seedname_dos.dat`, respectively. Since both quantities are a function of energy, they will be evaluated from `tran_win_min` to `tran_win_max` with an interval of `tran_energy_step`.

The default value of this parameter is `false`.

2.9.29 character(len=20) :: transport_mode

If `transport_mode = bulk`, quantum conductance and density of states are calculated for a perfectly-periodic one-dimensional system. In this case, the transport part can either use the Hamiltonian matrix in the WF basis generated by `wannier90` or a Hamiltonian matrix provided by the external file `seedname_htB.dat`.

If `transport_mode = lcr`, quantum conductance and density of states are calculated for a system where semi-infinite, left and right leads are connected through a central conductor region. In this case, the transport part will work independently from the disentanglement and wannierise procedure. Details of the method is described in Ref. [9].

If `tran_read_ht = true` then the Hamiltonian matrices must be provided by the five external files: `seedname_htL.dat, seedname_htLC.dat, seedname_htC.dat, seedname_htCR.dat, seedname_htR.dat`. If `tran_read_ht = false` then the Hamiltonian matrices are found automatically provided the super-cell adheres to conditions outlined in Section 7.3.

The valid options for this parameter are:

- `bulk` (default)

- `lcr`

2.9.30 real(kind=dp) :: tran_win_min

The lower bound of the energy window for the transport calculation. Units are eV.

The default value is -3.0.

2.9.31 real(kind=dp) :: tran_win_max

The upper bound of the energy window for the transport calculation. Units are eV.

The default value is 3.0.

2.9.32 real(kind=dp) :: tran_energy_step

Sampling interval of the energy values from `tran_win_min` to `tran_win_max`. Units are eV.

The default value is 0.01.

2.9.33 real(kind=dp) :: fermi_energy

The Fermi energy in eV. The energy axis of the quantum conductance and density of states data will be shifted rigidly by this amount.

The default value is 0.0

2.9.34 integer :: tran_num_bb

Size of a bulk Hamiltonian matrix. This number is equal to the number of WFs in one principal layer.

A one-dimensional system can be viewed as an array of principal layers which are defined in a way that localized basis functions inside a certain principal layer only interact with those in the nearest neighbor principal layer. In `wannier90` a principal layer will be an integer multiple of a unit cell, and the size is determined by `hr_cutoff` and/or `dist_cutoff`. The criterion is rather arbitrary when WFs are adopted as a localized basis set, and it is up to a user's choice.

The default value is 0.

2.9.35 integer :: tran_num_ll

Size of a left-lead Hamiltonian matrix. If `transport_mode = lcr` and `tran_read_ht = false` then `tran_num_ll` is the number of Wannier functions in a principal layer.

The default value is 0.

2.9.36 integer :: tran_num_rr

Size of a right-lead Hamiltonian matrix.

The default value is 0.

2.9.37 integer :: tran_num_cc

Size of a conductor Hamiltonian matrix.

The default value is 0.

2.9.38 integer :: tran_num_lc

Number of columns in a left-lead_conductor Hamiltonian matrix. Number of rows must be equal to `tran_num_ll`.

The default value is 0.

2.9.39 integer :: tran_num_cr

Number of rows in a conductor_right-lead Hamiltonian matrix. Number of columns must be equal to `tran_num_rr`.

The default value is 0.

2.9.40 integer :: tran_num_cell_ll

Number of unit cells in one principal layer of left lead. Used if `transport_mode = lcr` and `tran_read_ht = false`.

The default value is 0.

2.9.41 integer :: tran_num_cell_rr

Number of unit cells in one principal layer of right lead. Not used at present.

The default value is 0.

2.9.42 integer :: tran_num_bandc

Half-bandwidth+1 of a band-diagonal conductor Hamiltonian matrix.

The Hamiltonian matrix of a central conductor part, which is read from `seedname_htC.dat`, will be diagonally dominant when `tran_num_cc` is very large. `tran_num_bandc` is used to construct a compact matrix which contains the non-zero band-diagonal part of a full conductor Hamiltonian matrix. Setting this parameter is only meaningful when `tran_num_bandc` is greater than `tran_num_lc` and `tran_num_cr`.

The default value is 0.

2.9.43 logical :: tran_write_ht

If `tran_write_ht = true`, then the Hamiltonian matrix formatted for the transport calculation will be written to a file `seedname_htB.dat`.

The default value is `false`.

2.9.44 logical :: tran_read_ht

If `tran_write_ht = true`, then the Hamiltonian matrix formatted for the transport calculation will be read from a set of files described in the parameter `transport_mode`. Set `tran_write_ht = false` to perform automated lcr calculations (see Section 7.3).

The default value is `false`.

2.9.45 logical :: tran_use_same_lead

If `tran_use_same_lead = true`, then the left and the right leads are the same. In this case, `seedname_htR.dat` is not required.

The default value is `true`.

2.9.46 real(kind=dp) :: tran_group_threshold

Used to group and sort Wannier functions according to the positions of their centres. Wannier functions in a group are within `tran_group_threshold` from one another in `x,y` and `z` directions. Units are Å

The default is 0.15

2.9.47 real(kind=dp) :: translation_centre_frac(3)

Centre of the unit cell to which the final Wannier centres are translated. Numbers are in fractional coordinates with respect to the lattice vectors.

The default value is (0.0,0.0,0.0).

2.9.48 logical :: use_ws_distance

Improves the interpolation of the k-space Hamiltonian, by applying a translation to each WF by a basis vector of the super-lattice that minimises the distance between their centres. The translation is dependent on both WF and on the unit cell vector to which they belong, i.e., translate function $W_j(\mathbf{r} - \mathbf{R})$ inside the Wigner-Seitz cell centred on WF $W_i(\mathbf{r})$.

For a longer explanation, see Chapter 9.

If `false` the code puts all the WF in the home cell, only possible choice until wannier90 v2.0.1.

The default value is `true` (default changed since v.3.0). Introduced in v2.1.

2.9.49 real(kind=dp) :: ws_distance_tol

Tolerance when determining whether two values $\|\mathbf{d}_{ij\mathbf{R}} + \tilde{\mathbf{R}}_{nml}\|$ and $\|\mathbf{d}_{ij\mathbf{R}} + \tilde{\mathbf{R}}_{n'm'l'}\|$ (as defined in chapter 9) for the shortest distance between two Wannier functions are equivalent. If the difference in distance (in Angstrom) is less than `ws_distance_tol`, they are taken to be equivalent.

The default value is 10^{-5}.

2.9.50 :: ws_search_size

Maximum absolute value for the integers n, m, l that identify the super-lattice vectors $\tilde{\mathbf{R}}_{nml}$ (see chapter 9) when searching for points inside the Wigner-Seitz cell. If `ws_search_size` is provided as a single integer, then the number of repetitions of the Born-von Karman cell is the same along all three linear dimensions; otherwise, if three integers are provided, the number of repetitions along the i−th linear dimension is `ws_search_size(i)`. The variable is used both in `hamiltonian.F90` and in `ws_distance.F90`. In the latter case, its value is incremented by one in order to account for WFs whose centre wanders away from the original reference unit cell.
The default value is generally sufficient, but might need to be increased in case of elongated cells.

The default value is 2.

2.9.51 logical :: write_u_matrices

Write the $\mathbf{U}^{(\mathbf{k})}$ and $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$ matrices obtained at the end of wannierization to files `seedname_u.mat` and `seedname_u_dis.mat`, respectively.

The default value is `false`.

2.9.52 real(kind=dp) :: hr_cutoff

The absolute value of the smallest matrix element of the Hamiltonian in the WF basis. If $h_{mn}(\mathbf{R}) >$ `hr_cutoff`, then the matrix element $h_{mn}(\mathbf{R})$ is retained and used in the band structure interpolation (when `bands_plot_mode = cut`) or in the transport calculation. Otherwise it is deemed to be insignificant and is discarded. Units are eV.

The default value is 0.0.

2.9.53 real(kind=dp) :: dist_cutoff

The largest distance between two WFs for which the Hamiltonian matrix element is retained and used in the band interpolation (when `bands_plot_mode = cut`) or in the transport calculation. Units are Å.

The default value is 1000.0.

2.9.54 character(len=20) :: dist_cutoff_mode

Dimension in which the distance between two WFs is calculated. The vector connecting two WFs may be projected to a line (`one_dim`) or a plane (`two_dim`). The size of the projected vector is calculated, and `dist_cutoff` is applied. When `one_dim` or `two_dim` is used, `one_dim_axis` must be given to specify extended or confined direction.

The valid options for this parameter are:

  − `three_dim` (default)

  − `two_dim`

  − `one_dim`

2.9.55 character(len=20) :: one_dim_axis

Extended direction for a one-dimensional system or confined direction for a two-dimensional system. This direction must be parallel to one of the Cartesian axes.

The valid options for this parameter are:

  − `x`

  − `y`

  − `z`

No default.

Chapter 3

Projections

3.1 Specification of projections in `seedname.win`

Here we describe the projection functions used to construct the initial guess $A_{mn}^{(\mathbf{k})}$ for the unitary transformations.

Each projection is associated with a site and an angular momentum state defining the projection function. Optionally, one may define, for each projection, the spatial orientation, the radial part, the diffusivity, and the volume over which real-space overlaps A_{mn} are calculated.

The code is able to

1. project onto s,p,d and f angular momentum states, plus the hybrids sp, sp^2, sp^3, sp^3d, sp^3d^2.

2. control the radial part of the projection functions to allow higher angular momentum states, e.g., both 3s and 4s in silicon.

The atomic orbitals of the hydrogen atom provide a good basis to use for constructing the projection functions: analytical mathematical forms exist in terms of the good quantum numbers n, l and m; hybrid orbitals (sp, sp^2, sp^3, sp^3d etc.) can be constructed by simple linear combination $|\phi\rangle = \sum_{nlm} C_{nlm}|nlm\rangle$ for some coefficients C_{nlm}.

The angular functions that use as a basis for the projections are not the canonical spherical harmonics Y_{lm} of the hydrogenic Schrödinger equation but rather the *real* (in the sense of non-imaginary) states $\Theta_{lm_{\mathrm{r}}}$, obtained by a unitary transformation. For example, the canonical eigenstates associated with $l = 1$, $m = \{-1, 0, 1\}$ are not the real p_x, p_y and p_z that we want. See Section 3.4 for our mathematical conventions regarding projection orbitals for different n, l and m_{r}.

We use the following format to specify projections in `<seedname>.win`:

```
Begin Projections
[units]
site:ang_mtm:zaxis:xaxis:radial:zona
    ⋮
End Projections
```

Notes:

`units`:
Optional. Either `Ang` or `Bohr` to specify whether the projection centres specified in this block (if given in Cartesian co-ordinates) are in units of Angstrom or Bohr, respectively. The default value is `Ang`.

`site`:
`C`, `Al`, etc. applies to all atoms of that type
`f=0,0.50,0` – centre on (0.0,0.5,0.0) in **f**ractional coordinates (crystallographic units) relative to the direct lattice vectors
`c=0.0,0.805,0.0` – centre on (0.0,0.805,0.0) in **C**artesian coordinates in units specified by the optional string `units` in the first line of the projections block (see above).

`ang_mtm`:
Angular momentum states may be specified by `l` and `mr`, or by the appropriate character string. See Tables 3.1 and 3.2. Examples:
`l=2,mr=1`   or   `dz2` – a single projection with $l = 2$, $m_r = 1$ (i.e., d_{z^2})
`l=2,mr=1,4`   or   `dz2,dx2-y2` – two functions: d_{z^2} and d_{xz}
`l=-3`   or   `sp3` – four sp^3 hybrids
Specific hybrid orbitals may be specified as follows:
`l=-3,mr=1,3`   or   `sp3-1,sp3-3` – two specific sp^3 hybrids
Multiple states may be specified by separating with ';', e.g.,
`sp3;l=0`   or   `l=-3;l=0` – four sp^3 hybrids and one s orbital

`zaxis` (optional):
`z=1,1,1` – set the z-axis to be in the (1,1,1) direction. Default is `z=0,0,1`

`xaxis` (optional):
`x=1,1,1` – set the x-axis to be in the (1,1,1) direction. Default is `x=1,0,0`

`radial` (optional):
`r=2` – use a radial function with one node (ie second highest pseudostate with that angular momentum). Default is `r=1`. Radial functions associated with different values of `r` should be orthogonal to each other.

`zona` (optional):
`zona=2.0` – the value of $\frac{Z}{a}$ for the radial part of the atomic orbital (controls the diffusivity of the radial function). Units always in reciprocal Angstrom. Default is `zona=1.0`.

Examples

1. CuO, s,p and d on all Cu; sp^3 hybrids on O:

`Cu:l=0;l=1;l=2`

`O:l=-3`   or   `O:sp3`

2. A single projection onto a p_z orbital orientated in the (1,1,1) direction:

`c=0,0,0:l=1,mr=1:z=1,1,1`   or   `c=0,0,0:pz:z=1,1,1`

3. Project onto s, p and d (with no radial nodes), and s and p (with one radial node) in silicon:

`Si:l=0;l=1;l=2`

`Si:l=0;l=1:r=2`

3.2 Spinor Projections

When `spinors=.true.` it is possible to select a set of localised functions to project onto 'up' states and a set to project onto 'down' states where, for complete flexibility, it is also possible to set the local spin quantisation axis.

Note, however, that this feature requires a recent version of the interface between the ab-initio code and Wannier90 (i.e., written after the release of the 2.0 version, in October 2013) supporting spinor projections.

```
Begin Projections
[units]
site:ang_mtm:zaxis:xaxis:radial:zona(spin)[quant_dir]
    ⋮
End Projections
```

`spin` (optional):
Choose projection onto 'up' or 'down' states
`u` – project onto 'up' states.
`d` – project onto 'down' states.
Default is `u,d`

`quant_dir` (optional):
`1,0,0` – set the spin quantisation axis to be in the (1,0,0) direction. Default is `0,0,1`

Examples

- 18 projections on an iron site

  `Fe:sp3d2;dxy;dxx;dyz`

- same as above

  `Fe:sp3d2;dxy;dxx;dyz(u,d)`

- same as above

  `Fe:sp3d2;dxy;dxz;dyz(u,d)[0,0,1]`

- same as above but quantisation axis is now x

  `Fe:sp3d2;dxy;dxz;dyz(u,d)[1,0,0]`

- now only 9 projections onto up states

  `Fe:sp3d2;dxy;dxz;dyz(u)`

- 9 projections onto up-states and 3 on down

  `Fe:sp3d2;dxy;dxz;dyz(u)`
  `Fe:dxy;dxz;dyz(d)`

- projections onto alternate spin states for two lattice sites (Cr1, Cr2)

  `Cr1:d(u)`
  `Cr2:d(d)`

3.3 Short-Cuts

3.3.1 Random projections

It is possible to specify the projections, for example, as follows:

```
Begin Projections
random
C:sp3
End Projections
```

in which case `wannier90` uses four sp^3 orbitals centred on each C atom and then chooses the appropriate number of randomly-centred s-type Gaussian functions for the remaining projection functions. If the block only consists of the string `random` and no specific projection centres are given, then all of the projection centres are chosen randomly.

3.3.2 Bloch phases

Setting `use_bloch_phases = true` in the input file absolves the user of the need to specify explicit projections. In this case, the Bloch wave-functions are used as the projection orbitals, namely $A_{mn}^{(\mathbf{k})} = \langle \psi_{m\mathbf{k}} | \psi_{n\mathbf{k}} \rangle = \delta_{mn}$.

3.4 Orbital Definitions

The angular functions $\Theta_{lm_{\rm r}}(\theta, \varphi)$ associated with particular values of l and $m_{\rm r}$ are given in Tables 3.1 and 3.2.

The radial functions $R_{\rm r}(r)$ associated with different values of r should be orthogonal. One choice would be to take the set of solutions to the radial part of the hydrogenic Schrödinger equation for $l = 0$, i.e., the radial parts of the 1s, 2s, 3s... orbitals, which are given in Table 3.3.

l	m_{r}	Name	$\Theta_{lm_{\mathrm{r}}}(\theta, \varphi)$
0	1	s	$\frac{1}{\sqrt{4\pi}}$
1	1	pz	$\sqrt{\frac{3}{4\pi}} \cos\theta$
1	2	px	$\sqrt{\frac{3}{4\pi}} \sin\theta \cos\varphi$
1	3	py	$\sqrt{\frac{3}{4\pi}} \sin\theta \sin\varphi$
2	1	dz2	$\sqrt{\frac{5}{16\pi}}(3\cos^2\theta - 1)$
2	2	dxz	$\sqrt{\frac{15}{4\pi}} \sin\theta \cos\theta \cos\varphi$
2	3	dyz	$\sqrt{\frac{15}{4\pi}} \sin\theta \cos\theta \sin\varphi$
2	4	dx2-y2	$\sqrt{\frac{15}{16\pi}} \sin^2\theta \cos 2\varphi$
2	5	dxy	$\sqrt{\frac{15}{16\pi}} \sin^2\theta \sin 2\varphi$
3	1	fz3	$\frac{\sqrt{7}}{4\sqrt{\pi}}(5\cos^3\theta - 3\cos\theta)$
3	2	fxz2	$\frac{\sqrt{21}}{4\sqrt{2\pi}}(5\cos^2\theta - 1)\sin\theta \cos\varphi$
3	3	fyz2	$\frac{\sqrt{21}}{4\sqrt{2\pi}}(5\cos^2\theta - 1)\sin\theta \sin\varphi$
3	4	fz(x2-y2)	$\frac{\sqrt{105}}{4\sqrt{\pi}} \sin^2\theta \cos\theta \cos 2\varphi$
3	5	fxyz	$\frac{\sqrt{105}}{4\sqrt{\pi}} \sin^2\theta \cos\theta \sin 2\varphi$
3	6	fx(x2-3y2)	$\frac{\sqrt{35}}{4\sqrt{2\pi}} \sin^3\theta(\cos^2\varphi - 3\sin^2\varphi)\cos\varphi$
3	7	fy(3x2-y2)	$\frac{\sqrt{35}}{4\sqrt{2\pi}} \sin^3\theta(3\cos^2\varphi - \sin^2\varphi)\sin\varphi$

Table 3.1: Angular functions $\Theta_{lm_{\mathrm{r}}}(\theta, \varphi)$ associated with particular values of l and m_{r} for $l \geq 0$.

l	m_{r}	Name	$\Theta_{lm_{\mathrm{r}}}(\theta, \varphi)$
-1	1	sp-1	$\frac{1}{\sqrt{2}}\mathrm{s} + \frac{1}{\sqrt{2}}\mathrm{px}$
-1	2	sp-2	$\frac{1}{\sqrt{2}}\mathrm{s} - \frac{1}{\sqrt{2}}\mathrm{px}$
-2	1	sp2-1	$\frac{1}{\sqrt{3}}\mathrm{s} - \frac{1}{\sqrt{6}}\mathrm{px} + \frac{1}{\sqrt{2}}\mathrm{py}$
-2	2	sp2-2	$\frac{1}{\sqrt{3}}\mathrm{s} - \frac{1}{\sqrt{6}}\mathrm{px} - \frac{1}{\sqrt{2}}\mathrm{py}$
-2	3	sp2-3	$\frac{1}{\sqrt{3}}\mathrm{s} + \frac{2}{\sqrt{6}}\mathrm{px}$
-3	1	sp3-1	$\frac{1}{2}(\mathrm{s} + \mathrm{px} + \mathrm{py} + \mathrm{pz})$
-3	2	sp3-2	$\frac{1}{2}(\mathrm{s} + \mathrm{px} - \mathrm{py} - \mathrm{pz})$
-3	3	sp3-3	$\frac{1}{2}(\mathrm{s} - \mathrm{px} + \mathrm{py} - \mathrm{pz})$
-3	4	sp3-4	$\frac{1}{2}(\mathrm{s} - \mathrm{px} - \mathrm{py} + \mathrm{pz})$
-4	1	sp3d-1	$\frac{1}{\sqrt{3}}\mathrm{s} - \frac{1}{\sqrt{6}}\mathrm{px} + \frac{1}{\sqrt{2}}\mathrm{py}$
-4	2	sp3d-2	$\frac{1}{\sqrt{3}}\mathrm{s} - \frac{1}{\sqrt{6}}\mathrm{px} - \frac{1}{\sqrt{2}}\mathrm{py}$
-4	3	sp3d-3	$\frac{1}{\sqrt{3}}\mathrm{s} + \frac{2}{\sqrt{6}}\mathrm{px}$
-4	4	sp3d-4	$\frac{1}{\sqrt{2}}\mathrm{pz} + \frac{1}{\sqrt{2}}\mathrm{dz2}$
-4	5	sp3d-5	$-\frac{1}{\sqrt{2}}\mathrm{pz} + \frac{1}{\sqrt{2}}\mathrm{dz2}$
-5	1	sp3d2-1	$\frac{1}{\sqrt{6}}\mathrm{s} - \frac{1}{\sqrt{2}}\mathrm{px} - \frac{1}{\sqrt{12}}\mathrm{dz2} + \frac{1}{2}\mathrm{dx2\text{-}y2}$
-5	2	sp3d2-2	$\frac{1}{\sqrt{6}}\mathrm{s} + \frac{1}{\sqrt{2}}\mathrm{px} - \frac{1}{\sqrt{12}}\mathrm{dz2} + \frac{1}{2}\mathrm{dx2\text{-}y2}$
-5	3	sp3d2-3	$\frac{1}{\sqrt{6}}\mathrm{s} - \frac{1}{\sqrt{2}}\mathrm{py} - \frac{1}{\sqrt{12}}\mathrm{dz2} - \frac{1}{2}\mathrm{dx2\text{-}y2}$
-5	4	sp3d2-4	$\frac{1}{\sqrt{6}}\mathrm{s} + \frac{1}{\sqrt{2}}\mathrm{py} - \frac{1}{\sqrt{12}}\mathrm{dz2} - \frac{1}{2}\mathrm{dx2\text{-}y2}$
-5	5	sp3d2-5	$\frac{1}{\sqrt{6}}\mathrm{s} - \frac{1}{\sqrt{2}}\mathrm{pz} + \frac{1}{\sqrt{3}}\mathrm{dz2}$
-5	6	sp3d2-6	$\frac{1}{\sqrt{6}}\mathrm{s} + \frac{1}{\sqrt{2}}\mathrm{pz} + \frac{1}{\sqrt{3}}\mathrm{dz2}$

Table 3.2: Angular functions $\Theta_{lm_{\mathrm{r}}}(\theta, \varphi)$ associated with particular values of l and m_{r} for $l < 0$, in terms of the orbitals defined in Table 3.1.

r	$R_{\mathrm{r}}(r)$
1	$2\alpha^{3/2}\exp(-\alpha r)$
2	$\frac{1}{2\sqrt{2}}\alpha^{3/2}(2-\alpha r)\exp(-\alpha r/2)$
3	$\sqrt{\frac{4}{27}}\alpha^{3/2}(1-2\alpha r/3+2\alpha^2 r^2/27)\exp(-\alpha r/3)$

Table 3.3: One possible choice for the radial functions $R_{\mathrm{r}}(r)$ associated with different values of r: the set of solutions to the radial part of the hydrogenic Schrödinger equation for $l = 0$, i.e., the radial parts of the 1s, 2s, 3s... orbitals, where $\alpha = Z/a = $ `zona`.

3.5   Projections via the SCDM-k method in pw2wannier90

For many systems, such as aperiodic systems, crystals with defects, or novel materials with complex band structure, it may be extremely hard to identify *a-priori* a good initial guess for the projection functions used to generate the $A_{mn}^{(\mathbf{k})}$ matrices. In these cases, one can use a different approach, known as the SCDM-**k** method[10], based on a QR factorization with column pivoting (QRCP) of the density matrix from the self-consistent field calculation, which allows one to avoid the tedious step of specifying a projection block altogether, hence to avoid . This method is robust in generating well localised function with the correct spatial orientations and in general in finding the global minimum of the spread functional Ω. Any electronic-structure code should in principle be able to implement the SCDM-**k** method within their interface with Wannier90, however at the moment (develop branch on the GitHub repository July 2019) only the Quantum ESPRESSO package has this capability implemented in the `pw2wannier90` interface program. Moreover, the `pw2wannier90` interface program supports also the SCDM-**k** method for spin-noncollinear systems. The SCDM-**k** can operate in two modes:

1. In isolation, i.e., without performing a subsequent Wannier90 optimisation (not recommended). This can be achieved by setting `num_iter=0` and `dis_num_iter=0` in the `<seedname>.win` input file. The rationale behind this is that in general the projection functions obtained with the SCDM-**k** are already well localised with the correct spatial orientations. However, the spreads of the resulting functions are usually larger than the MLWFs ones.

2. In combination with the Marzari-Vanderbilt (recommended option). In this case, the SCDM-**k** is only used to generate the initial $A_{mn}^{(\mathbf{k})}$ matrices as a replacement scheme for the projection block.

The following keywords need to be specified in the `pw2wannier90.x` input file `<seedname>.pw2wan`: `scdm_proj scdm_entanglement scdm_mu scdm_sigma`

Chapter 4

Code Overview

`wannier90` can operate in two modes:

1. *Post-processing mode:* read in the overlaps and projections from file as computed inside a first-principles code. We expect this to be the most common route to using `wannier90`, and is described in Ch. 5;

2. *Library mode:* as a set of library routines to be called from within a first-principles code that passes the overlaps and projections to the `wannier90` library routines and in return gets the unitary transformation corresponding to MLWF. This route should be used if the MLWF are needed within the first-principles code, for example in post-LDA methods such as LDA+U or SIC, and is described in Ch. 6.
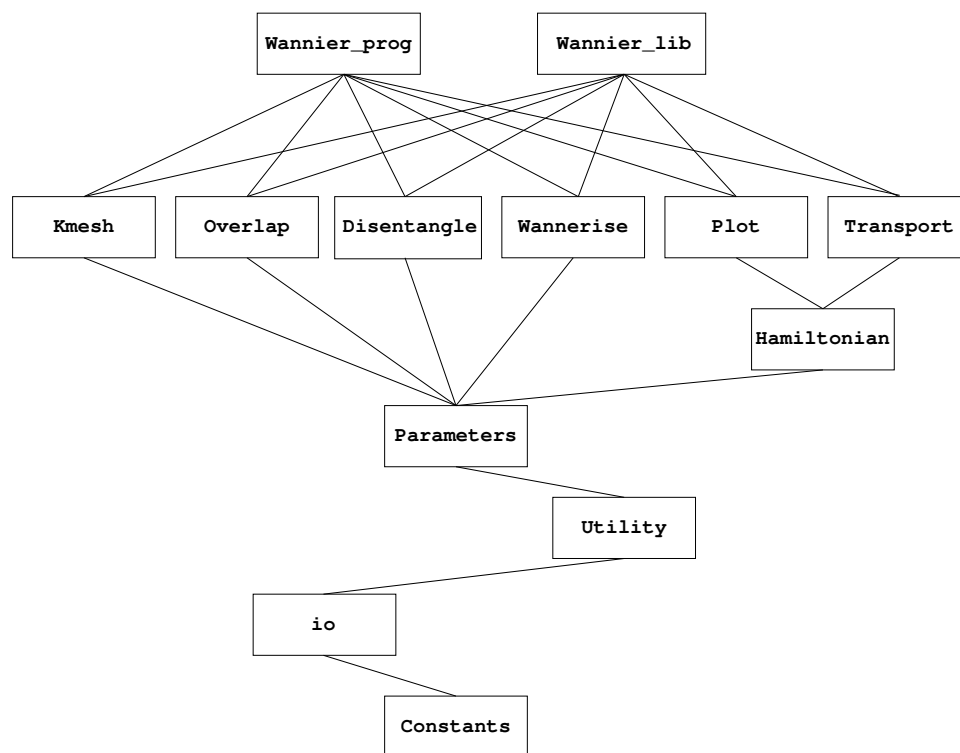
Figure 4.1: Schematic overview of the module structure of `wannier90`. Modules may only use data and subroutines from lower modules.

Chapter 5

`wannier90` as a post-processing tool

This is a description of how to use `wannier90` as a post-processing tool.

The code must be run twice. On the first pass either the logical keyword `postproc_setup` must be set to `.true.` in the input file `seedname.win` or the code must be run with the command line option `-pp`. Running the code then generates the file `seedname.nnkp` which provides the information required to construct the $M_{mn}^{(\mathbf{k},\mathbf{b})}$ overlaps (Ref. [1], Eq. (25)) and $A_{mn}^{(\mathbf{k})}$ (Ref. [1], Eq. (62); Ref. [2], Eq. (22)).

Once the overlaps and projection have been computed and written to files `seedname.mmn` and `seedname.amn`, respectively, set `postproc_setup` to `.false.` and run the code. Output is written to the file `seedname.wout`.

5.1 seedname.nnkp file

OUTPUT, if `postproc_setup` = `.true.`

The file `seedname.nnkp` provides the information needed to determine the required overlap elements $M_{mn}^{(\mathbf{k},\mathbf{b})}$ and projections $A_{mn}^{(\mathbf{k})}$. It is written automatically when the code is invoked with the `-pp` command-line option (or when `postproc_setup=.true.` in `seedname.win`. There should be no need for the user to edit this file.

Much of the information in `seedname.nnkp` is arranged in blocks delimited by the strings `begin block_name` ...`end block_name`, as described below.

5.1.1 Keywords

The first line of the file is a user comment, e.g., the date and time:

`File written on 12Feb2006 at 15:13:12`

The only logical keyword is `calc_only_A`, eg,

`calc_only_A  :  F`

5.1.2 Real_lattice block

`begin real_lattice`

```
 2.250000     0.000000     0.000000
 0.000000     2.250000     0.000000
 0.000000     0.000000     2.250000
end real_lattice
```

The real lattice vectors in units of Angstrom.

5.1.3 Recip_lattice **block**

```
begin recip_lattice
 2.792527     0.000000     0.000000
 0.000000     2.792527     0.000000
 0.000000     0.000000     2.792527
end recip_lattice
```

The reciprocal lattice vectors in units of inverse Angstrom.

5.1.4 Kpoints **block**

```
begin kpoints
  8
  0.00000     0.00000     0.00000
  0.00000     0.50000     0.00000
   .
   .
   .
  0.50000     0.50000     0.50000
end kpoints
```

The first line in the block is the total number of k-points `num_kpts`. The subsequent `num_kpts` lines specify the k-points in crystallographic co-ordinates relative to the reciprocal lattice vectors.

5.1.5 Projections **block**

```
begin projections
   n_proj
   centre   l  mr  r
     z-axis   x-axis    zona
   centre   l  mr  r
     z-axis   x-axis    zona
   .
   .
end projections
```

Notes:

`n_proj`: integer; the number of projection centres, equal to the number of MLWF `num_wann`.

`centre`: three real numbers; projection function centre in crystallographic co-ordinates relative to the direct lattice vectors.

`l mr r`: three integers; l and m_r specify the angular part $\Theta_{lm_r}(\theta, \varphi)$, and r specifies the radial part $R_r(r)$ of the projection function (see Tables 3.1, 3.2 and 3.3).

`z-axis`: three real numbers; default is `0.0 0.0 1.0`; defines the axis from which the polar angle θ in spherical polar coordinates is measured.

`x-axis`: three real numbers; must be orthogonal to `z-axis`; default is `1.0 0.0 0.0` or a vector perpendicular to `z-axis` if `z-axis` is given; defines the axis from with the azimuthal angle φ in spherical polar coordinates is measured.

`zona`: real number; the value of $\frac{Z}{a}$ associated with the radial part of the atomic orbital. Units are in reciprocal Angstrom.

5.1.6 `spinor_projections` block

```
begin spinor_projections
   n_proj
   centre   l  mr  r
    z-axis   x-axis   zona
     spin spn_quant
   centre   l  mr  r
    z-axis   x-axis   zona
     spin spn_quant
   .
   .
end spinor_projections
```

Notes: Only one of projections and spinor_projections should be defined. Variables are the same as the projections block with the addition of `spin` and `spn_quant`.

`spin`: integer. '1' or '-1' to denote projection onto up or down states.

`spn_quant`: three real numbers. Defines the spin quantisation axis in Cartesian coordinates.

5.1.7 `nnkpts` block

```
begin nnkpts
  10
  1   2   0  0  0
  .
  .
end nnkpts
```

First line: `nntot`, the number of nearest neighbours belonging to each k-point of the Monkhorst-Pack mesh

Subsequent lines: `nntot`×`num_kpts` lines, ie, `nntot` lines of data for each k-point of the mesh.

Each line of consists of 5 integers. The first is the k-point number `nkp`. The second to the fifth specify it's nearest neighbours $\mathbf{k} + \mathbf{b}$: the second integer points to the k-point that is the periodic image of the $\mathbf{k} + \mathbf{b}$ that we want; the last three integers give the G-vector, in reciprocal lattice units, that brings the k-point specified by the second integer (which is in the first BZ) to the actual $\mathbf{k} + \mathbf{b}$ that we need.

5.1.8 `exclude_bands` block

```
begin exclude_bands
   8
   1
   2
   .
   .
end exclude_bands
```

To exclude bands (independent of k-point) from the calculation of the overlap and projection matrices, for example to ignore shallow-core states. The first line is the number of states to exclude, the following lines give the states for be excluded.

5.1.9 `auto_projections` block

```
begin auto_projections
    8
    0
end auto_projections
```

This block is only printed if `auto_projections=true` in the input. The choice of an additional block has been made in order to maintain back-compatibility with codes that interface with `wannier90`, e.g. `pw2wannier90`. The first entry in the block (in the example above, 8) is the total number of target projections and it is equal to the number of sought Wannier functions.

The second entry is a reserved flag with the value of zero. The implementations of the interface codes MUST check for this value to be zero and stop otherwise. In the future, one possible extension that we plan is to combine the automatic generation of initial projections with the selection of projections via a projections block. This will allow the user to specify only a subset of initial projections in the projections block and leave the interface code to automatically generate the remaining ones. In that case the constraint on the second entry will be lifted, so that it can take on the meaning of the number of projections that need to be generated automatically.

The selected columns of the density matrix (SCDM) method [10] is one way of generating the initial $A_{mn}^{(\mathbf{k})}$ in an automatic way. This has been implemented in the `pw2wannier90` interface code (you need v6.3 with the files provided in the `pwscf` folder of Wannier90, or v6.4), see for instance Example 27 in the `wannier90` tutorial that shows how to use it.

Moreover, also the automatic generation of initial projections with spinor WFs is implemented in the `pw2wannier90` interface. See Example 31 in the `wannier90` tutorial that shows how to use it.

5.1.10   An example of projections

As a concrete example: one wishes to have a set of four sp^3 projection orbitals on, say, a carbon atom at (0.5,0.5,0.5) in fractional co-ordinates relative to the direct lattice vectors. In this case `seedname.win` will contain the following lines:

```
begin projections
 C:l=-1
end projections
```

and `seedname.nnkp`, generated on the first pass of `wannier90` (with `postproc_setup=T`), will contain:

```
begin projections
   4
   0.50000     0.50000     0.50000     -1  1  1
      0.000  0.000  1.000    1.000  0.000  0.000     2.00
   0.50000     0.50000     0.50000     -1  2  1
      0.000  0.000  1.000    1.000  0.000  0.000     2.00
   0.50000     0.50000     0.50000     -1  3  1
      0.000  0.000  1.000    1.000  0.000  0.000     2.00
   0.50000     0.50000     0.50000     -1  4  1
      0.000  0.000  1.000    1.000  0.000  0.000     2.00
end projections
```

where the first line tells us that in total four projections are specified, and the subsequent lines provide the projection centre, the angular and radial parts of the orbital (see Section 3.4 for definitions), the z and x axes, and the diffusivity and cut-off radius for the projection orbital.

PWSCF, or any other *ab initio* electronic structure code, then reads `seedname.nnkp` file, calculates the projections and writes them to `seedname.amn`.

5.2   `seedname.mmn` file

INPUT.

The file `seedname.mmn` contains the overlaps $M_{mn}^{(\mathbf{k},\mathbf{b})}$.

First line: a user comment, e.g., the date and time

Second line: 3 integers: `num_bands`, `num_kpts`, `nntot`

Then: `num_kpts` × `nntot` blocks of data:

First line of each block: 5 integers. The first specifies the $\mathbf{k}$ (i.e., gives the ordinal corresponding to its position in the list of k-points in `seedname.win`). The 2nd to 5th integers specify $\mathbf{k} + \mathbf{b}$. The 2nd integer, in particular, points to the k-point on the list that is a periodic image of $\mathbf{k} + \mathbf{b}$, and in particular is the image that is actually mentioned in the list. The last three integers specify the $\mathbf{G}$ vector, in reciprocal lattice units, that brings the k-point specified by the second integer, and that thus lives inside the first BZ zone, to the actual $\mathbf{k} + \mathbf{b}$ that we need.

Subsequent `num_bands` × `num_bands` lines of each block: two real numbers per line. These are the real and imaginary parts, respectively, of the actual scalar product $M_{mn}^{(\mathbf{k},\mathbf{b})}$ for $m, n \in [1, \mathtt{num\_bands}]$. The order of these elements is such that the first index m is fastest.

5.3 `seedname.amn` file

INPUT.

The file `seedname.amn` contains the projection $A_{mn}^{(\mathbf{k})}$.

First line: a user comment, e.g., the date and time

Second line: 3 integers: `num_bands`, `num_kpts`, `num_wann`

Subsequently `num_bands` × `num_wann` × `num_kpts` lines: 3 integers and 2 real numbers on each line. The first two integers are the band index m and the projection index n, respectively. The third integer specifies the $\mathbf{k}$ by giving the ordinal corresponding to its position in the list of k-points in `seedname.win`. The real numbers are the real and imaginary parts, respectively, of the actual $A_{mn}^{(\mathbf{k})}$.

5.4 `seedname.dmn` file

INPUT.

The file `seedname.dmn` contains the data needed to construct symmetry-adapted Wannier functions [7]. Required if `site_symmetry = .true.`

First line: a user comment, e.g., the date and time

Second line: 4 integers: `num_bands`, `nsymmetry`, `nkptirr`, `num_kpts`.
        `nsymmetry`: the number of symmetry operations
        `nkptirr`: the number of irreducible k-points

Blank line

`num_kpts` integers: Mapping between full k- and irreducible k-points. Each k-point is related to some k-point in the irreducible BZ. The information of this mapping is written. Each entry corresponds to a k-point in the full BZ, in the order in which they appear in the k-point list in `seedname.win` file. The (integer) value of each entry is the k-point index in the IBZ to which the k-point maps. The number of unique values is equal to the number of k-points in the IBZ. The data is written 10 values per line.

Blank line

`nkptirr` integers: List of irreducible k-points. Each entry corresponds to a k-point of the IBZ. The (integer) value of each entry is the k-point index corresponding to the k-point list in `seedname.win` file. The values should be between 1 and `num_kpts`. The data is written 10 values per line.

Blank line

`nkptirr` blocks of `nsymmetry` integer data (each block separated by a blank line): List of k-points obtained by acting the symmetry operations on the irreducible k-points. The data is written 10 values per line.

Blank line

`nsymmetry` × `nkptirr` blocks of data:
The information of D matrix in Eq. (15) of Ref. [7]. Each block contains `num_wann` × `num_wann` lines and is separated by a blank line. The data are stored in `d_matrix_wann(m,n,isym,ikirr)` with $\mathtt{m,n} \in [1, \mathtt{num\_wann}]$, $\mathtt{isym} \in [1, \mathtt{nsymmetry}]$, and $\mathtt{ikirr} \in [1, \mathtt{nkptirr}]$. The order of the elements is such that left indices run faster than right indices (`m`: fastest, `ikirr`: slowest).

Blank line

`nsymmetry` × `nkptirr` blocks of data:
The information of $\tilde{d}$ matrix in Eq. (17) of Ref. [7]. Each block contains `num_bands` × `num_bands` lines and is separated by a blank line. The data are stored in `d_matrix_band(m,n,isym,ikirr)` with $\mathtt{m,n} \in [1, \mathtt{num\_bands}]$, $\mathtt{isym} \in [1, \mathtt{nsymmetry}]$, and $\mathtt{ikirr} \in [1, \mathtt{nkptirr}]$. The order of the elements is such that left indices run faster than right indices (`m`: fastest, `ikirr`: slowest).

5.5 `seedname.eig` file

INPUT.

Required if any of `disentanglement`, `plot_bands`, `plot_fermi_surface` or `write_hr` are `.true.`

The file `seedname.eig` contains the Kohn-Sham eigenvalues $\varepsilon_{n\mathbf{k}}$ (in eV) at each point in the Monkhorst-Pack mesh.

Each line consist of two integers and a real number. The first integer is the band index, the second integer gives the ordinal corresponding to the k-point in the list of k-points in `seedname.win`, and the real number is the eigenvalue.

E.g.,

```
1           1   -6.43858831271328
2           1   19.3977795287297
3           1   19.3977795287297
4           1   19.3977795287298
```

5.6 Interface with PWSCF

Interfaces between `wannier90` and many ab-initio codes such as PWSCF, ABINIT (http://www.abinit.org), SIESTA (http://www.icmab.es/siesta/), FLEUR, VASP and WIEN2K (http://www.wien2k.at) are available. Here we describe the seamless interface between `wannier90` and PWSCF, a plane-wave DFT code that comes as part of the QUANTUM ESPRESSO package (see http://www.quantum-espresso.org). You will need to download and compile PWSCF (i.e., the `pw.x` code) and the post-processing interface `pw2wannier90.x`. Please refer to the documentation that comes with the QUANTUM ESPRESSO distribution for instructions.

1. Run 'scf'/'nscf' calculation(s) with `pw`

2. Run `wannier90` with `postproc_setup = .true.` to generate `seedname.nnkp`

3. Run `pw2wannier90`. First it reads an input file, e.g., `seedname.pw2wan`, which defines `prefix` and `outdir` for the underlying 'scf' calculation, as well as the name of the file `seedname.nnkp`, and

does a consistency check between the direct and reciprocal lattice vectors read from `seedname.nnkp` and those defined in the files specified by `prefix`. pw2wannier90 generates `seedname.mmn`, `seedname.amn` and `seedname.eig`. `seedname.dmn` and `seedname.sym` files are additionally created when `write_dmn = .true.` (see below).

4. Run `wannier90` with `postproc_setup = .false.` to disentangle bands (if required), localise MLWF, and use MLWF for plotting, bandstructures, Fermi surfaces etc.

Examples of how the interface with PWSCF works are given in the `wannier90` Tutorial.

5.6.1   `seedname.pw2wan`

A number of keywords may be specified in the `pw2wannier90` input file:

- `outdir` – Location to write output files. Default is '`./`'

- `prefix` – Prefix for the PWSCF calculation. Default is ' '

- `seedname` – Seedname for the `wannier90` calculation. Default is '`wannier`'

- `spin_component` – Spin component. Takes values '`up`', '`down`' or '`none`' (default).

- `wan_mode` – Either '`standalone`' (default) or '`library`'

- `write_unk` – Set to `.true.` to write the periodic part of the Bloch functions for plotting in `wannier90`. Default is `.false.`

- `reduce_unk` – Set to `.true.` to reduce file-size (and resolution) of Bloch functions by a factor of 8. Default is `.false.` (only relevant if `write_unk=.true.`)[1]

- `wvfn_formatted` – Set to `.true.` to write formatted wavefunctions. Default is `.false.` (only relevant if `write_unk=.true.`)

- `write_amn` – Set to `.false.` if $A_{mn}^{(\mathbf{k})}$ not required. Default is `.true.`

- `write_mmn` – Set to `.false.` if $M_{mn}^{(\mathbf{k},\mathbf{b})}$ not required. Default is `.true.`

- `write_spn` – Set to `.true.` to write out the matrix elements of S between Bloch states (non-collinear spin calculation only). Default is `.false.`

- `spn_formatted` – Set to `.true.` to write spn data as a formatted file. Default is `.false.` (only relevant if `write_spn=.true.`)

- `write_uHu` – Set to `.true.` to write out the matrix elements

$$\langle u_{n\mathbf{k}+\mathbf{b}_1}|H_{\mathbf{k}}|u_{m\mathbf{k}+\mathbf{b}_2}\rangle.$$

  Default is `.false.`

- `uHu_formatted` – Set to `.true.` to write uHu data as a formatted file. Default is `.false.` (only relevant if `write_uHu=.true.`)

---

[1] Note that there is a small bug with this feature in v3.2 (and subsequent patches) of quantum-espresso. Please use a later version (if available) or the CVS version of `pw2wannier90.f90`, which has been fixed.

- `write_uIu` – Set to `.true.` to write out the matrix elements of

$$\langle u_{n\mathbf{k}+\mathbf{b}_1} | u_{m\mathbf{k}+\mathbf{b}_2} \rangle.$$

  Default is `.false.`

- `uIu_formatted` – Set to `.true.` to write uIu data as a formatted file. Default is `.false.` (only relevant if `write_uIu=.true.`)

- `write_unkg` – Set to `.true.` to write the first few Fourier components of the periodic parts of the Bloch functions.

- `write_dmn` – Set to `.true.` to construct symmetry-adapted Wannier functions. Default is `.false.`

- `read_sym` – Set to `.true.` to customize symmetry operations to be used in symmetry-adapted mode. When `read_sym = .true.`, an additional input `seedname.sym` is required. Default is `.false.` (only relevant if `write_dmn=.true.`).

For examples of use, refer to the `wannier90` Tutorial.

5.6.2   `seedname.sym`

If `read_sym = .true.`, then this additional input file is required for `pw2wannier90.x`
if `read_sym = .false.`, then this file is written by `pw2wannier90.x` (only for reference – it is not used in subsequent calculations)

The file `seedname.sym` contains the information of symmetry operations used to create symmetry-adapted Wannier functions. If `read_sym = .false.` (default), `pw2wannier90.x` uses the full symmetry recognized by `pw.x`. If `read_sym = .true.`, you can specify symmetry operations to be used in symmetry-adapted mode.

First line: an integer: `nsymmetry` (number of symmetry operations)

Second line: blank

Then: `nsymmetry` blocks of data. Each block (separated by a blank line) consists of four lines. The order of the data in each block is as follows:

```
R(1,1)   R(2,1)   R(3,1)
R(1,2)   R(2,2)   R(3,2)
R(1,3)   R(2,3)   R(3,3)
 t(1)     t(2)     t(3)
```

Here, R is the rotational part of symmetry operations (3×3 matrix), and $\mathbf{t}$ is the fractional translation in the unit of "`alat`" (refer the definition of "`alat`" to the manual of PWSCF). Both data are given in Cartesian coordinates. The symmetry operations act on a point $\mathbf{r}$ as $\mathbf{r}R - \mathbf{t}$.

Chapter 6

`wannier90` as a library

This is a description of the interface between any external program and the wannier code. There are two subroutines: `wannier_setup` and `wannier_run`. Calling `wannier_setup` will return information required to construct the $M_{mn}^{(\mathbf{k},\mathbf{b})}$ overlaps (Ref. [1], Eq. (25)) and $A_{mn}^{(\mathbf{k})} = \langle \psi_{m\mathbf{k}} | g_n \rangle$ projections (Ref. [1], Eq. (62); Ref. [2], Eq. (22)). Once the overlaps and projection have been computed, calling `wannier_run` activates the minimisation and plotting routines in `wannier90`.

IMPORTANT NOTE: the library mode ONLY works in serial. Please call it from a serial code, or if compiled in parallel, make sure to run it from a single MPI process.

You can find a minimal example of how the library mode can be used among the tests, in the file `test-suite/library-mode-test/test_library.F90` in the Wannier90 git repository.

6.1 Subroutines

6.1.1 `wannier_setup`

```
wannier_setup(seed_name,mp_grid,num_kpts,real_lattice,recip_lattice,
              kpt_latt,num_bands_tot,num_atoms,atom_symbols,atoms_cart,
              gamma_only,spinors,nntot,nnlist,nncell,num_bands,num_wann,proj_site,
              proj_l,proj_m,proj_radial,proj_z,proj_x,proj_zona,
              exclude_bands,proj_s,proj_s_qaxis)
```

- `character(len=*), intent(in) :: seed_name`
  The seedname of the current calculation.

- `integer, dimension(3), intent(in) :: mp_grid`
  The dimensions of the Monkhorst-Pack k-point grid.

- `integer, intent(in) :: num_kpts`
  The number of k-points on the Monkhorst-Pack grid.

- `real(kind=dp), dimension(3,3), intent(in) :: real_lattice`
  The lattice vectors in Cartesian co-ordinates in units of Angstrom.

- `real(kind=dp), dimension(3,3), intent(in) :: recip_lattice`
  The reciprocal lattice vectors in Cartesian co-ordinates in units of reciprocal Angstrom.

- `real(kind=dp), dimension(3,num_kpts), intent(in) :: kpt_latt`
  The positions of the k-points in fractional co-ordinates relative to the reciprocal lattice vectors.

- `integer, intent(in) :: num_bands_tot`
  The total number of bands in the first-principles calculation (note: including semi-core states).

- `integer, intent(in) :: num_atoms`
  The total number of atoms in the system.

- `character(len=20), dimension(num_atoms), intent(in) :: atom_symbols`
  The elemental symbols of the atoms.

- `real(kind=dp), dimension(3,num_atoms), intent(in) :: atoms_cart`
  The positions of the atoms in Cartesian co-ordinates in Angstrom.

- `logical, intent(in) :: gamma_only`
  Set to `.true.` if the underlying electronic structure calculation has been performed with only Γ-point sampling and, hence, if the Bloch eigenstates that are used to construct $A_{mn}^{(\mathbf{k})}$ and $M_{mn}^{(\mathbf{k},\mathbf{b})}$ are real.

- `logical, intent(in) :: spinors`
  Set to `.true.` if underlying electronic structure calculation has been performed with spinor wavefunctions.

- `integer, intent(out) :: nntot`
  The total number of nearest neighbours for each k-point.

- `integer, dimension(num_kpts,num_nnmax), intent(out) :: nnlist`
  The list of nearest neighbours for each k-point.

- `integer,dimension(3,num_kpts,num_nnmax), intent(out) :: nncell`
  The vector, in fractional reciprocal lattice co-ordinates, that brings the `nn`[th] nearest neighbour of k-point `nkp` to its periodic image that is needed for computing the overlap $M_{mn}^{(\mathbf{k},\mathbf{b})}$.

- `integer, intent(out) :: num_bands`
  The number of bands in the first-principles calculation used to form the overlap matricies (note: excluding eg. semi-core states).

- `integer, intent(out) :: num_wann`
  The number of MLWF to be extracted.

- `real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_site`
  Projection function centre in crystallographic co-ordinates relative to the direct lattice vectors.

- `integer, dimension(num_bands_tot), intent(out) :: proj_l`
  l specifies the angular part $\Theta_{lm_{\mathrm{r}}}(\theta,\varphi)$ of the projection function (see Tables 3.1, 3.2 and 3.3).

- `integer, dimension(num_bands_tot), intent(out) :: proj_m`
  m_{r} specifies the angular part $\Theta_{lm_{\mathrm{r}}}(\theta,\varphi)$, of the projection function (see Tables 3.1, 3.2 and 3.3).

- `integer, dimension(num_bands_tot), intent(out) :: proj_radial`
  r specifies the radial part $R_{\mathrm{r}}(r)$ of the projection function (see Tables 3.1, 3.2 and 3.3).

- `real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_z`
  Defines the axis from which the polar angle θ in spherical polar coordinates is measured. Default is `0.0 0.0 1.0`.

- `real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_x`
  Must be orthogonal to `z-axis`; default is `1.0 0.0 0.0` or a vector perpendicular to `proj_z` if `proj_z` is given; defines the axis from with the azimuthal angle φ in spherical polar coordinates is measured.

- `real(kind=dp), dimension(num_bands_tot), intent(out) :: proj_zona`
  The value of $\frac{Z}{a}$ associated with the radial part of the atomic orbital. Units are in reciprocal Angstrom.

- `integer, dimension(num_bands_tot), intent(out) :: exclude_bands`
  Kpoints independant list of bands to exclude from the calculation of the MLWF (e.g., semi-core states).

- `integer, dimension(num_bands_tot), optional,intent(out) :: proj_s`
  '1' or '-1' to denote projection onto up or down spin states

- `real(kind=dp), dimension(3,num_bands_tot), intent(out) :: proj_s_qaxisx`
  Defines the spin quantisation axis in Cartesian coordinates.

Conditions:

- ⋆ `num_kpts` = `mp_grid(1)` $\times$ `mp_grid(2)` $\times$ `mp_grid(3)`.

- ⋆ `num_nnmax` = 12

This subroutine returns the information required to determine the required overlap elements $M_{mn}^{(\mathbf{k},\mathbf{b})}$ and projections $A_{mn}^{(\mathbf{k})}$, i.e., `M_matrix` and `A_matrix`, described in Section 6.1.2.

For the avoidance of doubt, `real_lattice(1,2)` is the $y-$component of the first lattice vector $\mathbf{A}_1$, etc.

The list of nearest neighbours of a particular k-point `nkp` is given by `nnlist(nkp,1:nntot)`.

Additionally, the parameter `shell_list` may be specified in the `wannier90` input file.

6.1.2   wannier_run

```
wannier_run(seed_name,mp_grid,num_kpts,real_lattice,recip_lattice,
            kpt_latt,num_bands,num_wann,nntot,num_atoms,atom_symbols,
            atoms_cart,gamma_only,M_matrix_orig,A_matrix,eigenvalues,
            U_matrix,U_matrix_opt,lwindow,wann_centres,wann_spreads,
            spread)
```

- `character(len=*), intent(in) :: seed_name`
  The seedname of the current calculation.

- `integer, dimension(3), intent(in) :: mp_grid`
  The dimensions of the Monkhorst-Pack k-point grid.

- `integer, intent(in) :: num_kpts`
  The number of k-points on the Monkhorst-Pack grid.

- `real(kind=dp), dimension(3,3), intent(in) :: real_lattice`
  The lattice vectors in Cartesian co-ordinates in units of Angstrom.

- `real(kind=dp), dimension(3,3), intent(in) :: recip_lattice`
  The reciprical lattice vectors in Cartesian co-ordinates in units of inverse Angstrom.

- `real(kind=dp), dimension(3,num_kpts), intent(in) :: kpt_latt`
  The positions of the k-points in fractional co-ordinates relative to the reciprocal lattice vectors.

- `integer, intent(in) :: num_bands`
  The total number of bands to be processed.

- `integer, intent(in) :: num_wann`
  The number of MLWF to be extracted.

- `integer, intent(in) :: nntot`
  The number of nearest neighbours for each k-point.

- `integer, intent(in) :: num_atoms`
  The total number of atoms in the system.

- `character(len=20), dimension(num_atoms), intent(in) :: atom_symbols`
  The elemental symbols of the atoms.

- `real(kind=dp), dimension(3,num_atoms), intent(in) :: atoms_cart`
  The positions of the atoms in Cartesian co-ordinates in Angstrom.

- `logical, intent(in) :: gamma_only`
  Set to `.true.` if the underlying electronic structure calculation has been performed with only Γ-point sampling and, hence, if the Bloch eigenstates that are used to construct $A_{mn}^{(\mathbf{k})}$ and $M_{mn}^{(\mathbf{k},\mathbf{b})}$ are real.

- `complex(kind=dp), dimension(num_bands,num_bands,nntot,num_kpts),`
  `                  intent(in) :: M_matrix`
  The matrices of overlaps between neighbouring periodic parts of the Bloch eigenstates at each k-point, $M_{mn}^{((\mathbf{k},\mathbf{b}))}$ (Ref. [1], Eq. (25)).

- `complex(kind=dp), dimension(num_bands,num_wann,num_kpts),`
  `                  intent(in) :: A_matrix`
  The matrices describing the projection of `num_wann` trial orbitals on `num_bands` Bloch states at each k-point, $A_{mn}^{(\mathbf{k})}$ (Ref. [1], Eq. (62); Ref. [2], Eq. (22)).

- `real(kind=dp), dimension(num_bands,num_kpts), intent(in) :: eigenvalues`
  The eigenvalues $\varepsilon_{n\mathbf{k}}$ corresponding to the eigenstates, in eV.

- `complex(kind=dp), dimension(num_wann,num_wann,num_kpts),`
  `                  intent(out) :: U_matrix`
  The unitary matrices at each k-point (Ref. [1], Eq. (59))

- `complex(kind=dp), dimension(num_bands,num_wann,num_kpts),`
  `                optional, intent(out) :: U_matrix_opt`
  The unitary matrices that describe the optimal sub-space at each k-point (see Ref. [2], Section IIIA). The array is packed (see below)

- `logical, dimension(num_bands,num_kpts), optional, intent(out) :: lwindow`
  The element `lwindow(nband,nkpt)` is `.true.` if the band `nband` lies within the outer energy window at kpoint `nkpt`.

- `real(kind=dp), dimension(3,num_wann), optional, intent(out) :: wann_centres`
  The centres of the MLWF in Cartesian co-ordinates in Angstrom.

- `real(kind=dp), dimension(num_wann), optional, intent(out) :: wann_spreads`
  The spread of each MLWF in Å^2.

- `real(kind=dp), dimension(3), optional, intent(out) :: spread`
  The values of Ω, Ω_I and $\tilde{\Omega}$ (Ref. [1], Eq. (13)).

Conditions:

- ⋆ `num_wann` $\leq$ `num_bands`

- ⋆ `num_kpts` $=$ `mp_grid(1)` $\times$ `mp_grid(2)` $\times$ `mp_grid(3)`.

If `num_bands` $=$ `num_wann` then `U_matrix_opt` is the identity matrix and `lwindow=.true.`

For the avoidance of doubt, `real_lattice(1,2)` is the $y-$component of the first lattice vector $\mathbf{A}_1$, etc.

$$
\begin{aligned}
\texttt{M\_matrix(m,n,nn,nkp)} &= \langle u_{m\mathbf{k}}|u_{n\mathbf{k}+\mathbf{b}}\rangle \\
\texttt{A\_matrix(m,n,nkp)} &= \langle \psi_{m\mathbf{k}}|g_n\rangle \\
\texttt{eigenvalues(n,nkp)} &= \varepsilon_{n\mathbf{k}}
\end{aligned}
$$

where

$$
\begin{aligned}
\mathbf{k} &= \texttt{kpt\_latt(1:3,nkp)} \\
\mathbf{k}+\mathbf{b} &= \texttt{kpt\_latt(1:3,nnlist(nkp,nn))} + \texttt{nncell(1:3,nkp,nn)}
\end{aligned}
$$

and $\{|g_n\rangle\}$ are a set of initial trial orbitals. These are typically atom or bond-centred Gaussians that are modulated by appropriate spherical harmonics.

Additional parameters should be specified in the `wannier90` input file.

Chapter 7

Transport Calculations with `wannier90`

By setting `transport = TRUE`, `wannier90` will calculate the quantum conductance and density of states of a one-dimensional system. The results will be written to files `seedname_qc.dat` and `seedname_dos.dat`, respectively.

The system for which transport properties are calculated is determined by the keyword `transport_mode`.

7.1   `transport_mode = bulk`

Quantum conductance and density of states are calculated for a perfectly periodic one-dimensional conductor. If `tran_read_ht = FALSE` the transport properties are calculated using the Hamiltonian in the Wannier function basis of the system found by `wannier90`. Setting `tran_read_ht = TRUE` allows the user to provide an external Hamiltonian matrix file `seedname_htB.dat`, from which the properties are found. See Section 2.9 for more details of the keywords required for such calculations.

7.2   `transport_mode = lcr`

Quantum conductance and density of states are calculated for a system where semi-infinite, left and right leads are connected through a central conductor region. This is known as the *lcr* system. Details of the method is described in Ref. [9].

In `wannier90` two options exist for performing such calculations:

- If `tran_read_ht = TRUE` the external Hamiltonian files `seedname_htL.dat, seedname_htLC.dat, seedname_htC.dat, seedname_htCR.dat, seedname_htR.dat` are read and used to compute the transport properties.

- If `tran_read_ht = FALSE`, then the transport calculation is performed automatically using the Wannier functions as a basis and the 2c2 geometry described in Section 7.3.

7.3   Automated lcr Transport Calculations: The 2c2 Geometry

Calculations using the 2c2 geometry provide a method to calculate the transport properties of an lcr system from a single wannier90 calculation. The Hamiltonian matrices which the five external files provide in the tran_read_ht = TRUE case are instead built from the Wannier function basis directly. As such, strict rules apply to the system geometry, which is shown in Figure 7.1. These rules are as follows:

- Left and right leads must be identical and periodic.

- Supercell must contain two principal layers (PLs) of lead on the left, a central conductor region and two principal layers of lead on the right.

- The conductor region must contain enough lead such that the disorder does not affect the principal layers of lead either side.

- A single **k**-point (Gamma) must be used.
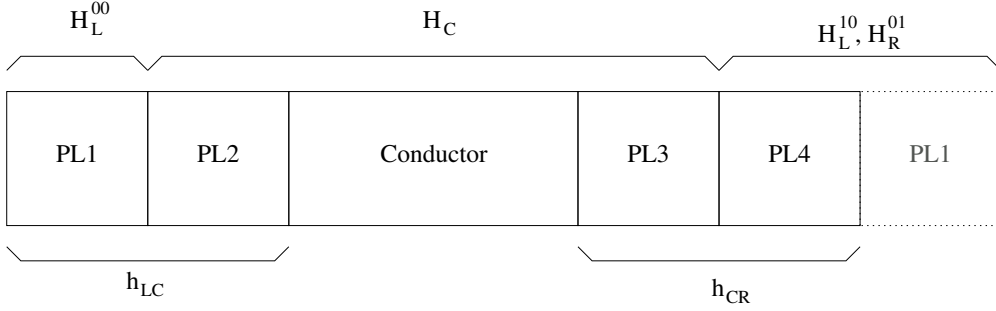
Figure 7.1: Schematic illustration of the supercell required for 2c2 lcr calculations, showing where each of the Hamiltonian matrices are derived from. Four principal layers (PLs) are required plus the conductor region.

In order to build the Hamiltonians, Wannier functions are first sorted according to position and then type if a number of Wannier functions exist with a similar centre (eg. *d*-orbital type Wannier functions centred on a Cu atom). Next, consistent parities of Wannier function are enforced. To distingiush between different types of Wannier function and assertain relative parities, a signature of each Wannier function is computed. The signature is formed of 20 integrals which have different spatial dependence. They are given by:

$$I = \frac{1}{V} \int_V g(\mathbf{r}) w(\mathbf{r}) d\mathbf{r} \tag{7.1}$$

where V is the volume of the cell, $w(\mathbf{r})$ is the Wannier function and $g(\mathbf{r})$ are the set of functions:

$$g(\mathbf{r}) = \left\{ 1, \sin\left(\frac{2\pi(x-x_c)}{L_x}\right), \sin\left(\frac{2\pi(y-y_c)}{L_y}\right), \sin\left(\frac{2\pi(z-z_c)}{L_z}\right), \sin\left(\frac{2\pi(x-x_c)}{L_x}\right)\sin\left(\frac{2\pi(y-y_c)}{L_y}\right), \right.$$
$$\left. \sin\left(\frac{2\pi(x-x_c)}{L_x}\right)\sin\left(\frac{2\pi(z-z_c)}{L_z}\right), ... \right\} \tag{7.2}$$

upto third order in powers of sines. Here, the supercell has dimension (L_x, L_y, L_z) and the Wannier function has centre $\mathbf{r}_c = (x_c, y_c, z_c)$. Each of these integrals may be written as linear combinations of the following sums:

$$S_n(\mathbf{G}) = e^{i\mathbf{G}.\mathbf{r}_c} \sum_m U_{mn} \tilde{u}^*_{m\Gamma}(\mathbf{G}) \tag{7.3}$$

where n and m are the Wannier function and band indexes, $\mathbf{G}$ is a G-vector, U_{mn} is the unitary matrix that transforms from the Bloch reopresentation of the system to the maximally-localised Wannier function basis and $\tilde{u}^*_{m\Gamma}(\mathbf{G})$ are the conjugates of the Fourier transforms of the periodic parts of the Bloch states at the Γ-point. The complete set of $\tilde{u}_{m\mathbf{k}}(\mathbf{G})$ are often outputted by plane-wave DFT codes. However, to calculate the 20 signature integrals, only 32 specific $\tilde{u}_{m\mathbf{k}}(\mathbf{G})$ are required. These are found in an additional file (`seedname.unkg`) that should be provided by the interface between the DFT code and `wannier90` . A detailed description of this file may be found in Section 8.32.

Additionally, the following keywords are also required in the input file:

- `tran_num_ll` : The number of Wannier functions in a principal layer.

- `tran_num_cell_ll` : The number of unit cells in one principal layer of lead

A further parameter related to these calculations is `tran_group_threshold`.

Examples of how 2c2 calculations are preformed can be found in the `wannier90` Tutorial.

Chapter 8

Files

8.1 `seedname.win`

INPUT. The master input file; contains the specification of the system and any parameters for the run. For a description of input parameters, see Chapter 2; for examples, see Section 10.1 and the `wannier90` Tutorial.

8.1.1 Units

The following are the dimensional quantities that are specified in the master input file:

- Direct lattice vectors

- Positions (of atomic or projection) centres in real space

- Energy windows

- Positions of k-points in reciprocal space

- Convergence thresholds for the minimisation of Ω

- `zona` (see Section 3.1)

- `wannier_plot_cube`: cut-off radius for plotting WF in Gaussian cube format

Notes:

- The units (either `ang` (default) or `bohr`) in which the lattice vectors, atomic positions or projection centres are given can be set in the first line of the blocks `unit_cell_cart`, `atoms_cart` and `projections`, respectively, in `seedname.win`.

- Energy is always in eV.

- Convergence thresholds are always in Å^2

- Positions of k-points are always in crystallographic coordinates relative to the reciprocal lattice vectors.

- `zona` is always in reciprocal Angstrom ($Å^{-1}$)

- The keyword `length_unit` may be set to `ang` (default) or `bohr`, in order to set the units in which the quantities in the output file `seedname.wout` are written.

- `wannier_plot_radius` is in Angstrom

The reciprocal lattice vectors $\{\mathbf{B}_1, \mathbf{B}_2, \mathbf{B}_3\}$ are defined in terms of the direct lattice vectors $\{\mathbf{A}_1, \mathbf{A}_2, \mathbf{A}_3\}$ by the equation

$$\mathbf{B}_1 = \frac{2\pi}{\Omega} \mathbf{A}_2 \times \mathbf{A}_3 \quad \text{etc.,} \tag{8.1}$$

where the cell volume is $V = \mathbf{A}_1 \cdot (\mathbf{A}_2 \times \mathbf{A}_3)$.

8.2   `seedname.mmn`

INPUT. Written by the underlying electronic structure code. See Chapter 5 for details.

8.3   `seedname.amn`

INPUT. Written by the underlying electronic structure code. See Chapter 5 for details.

8.4   `seedname.dmn`

INPUT. Read if `site_symmetry = .true.` (symmetry-adapted mode). Written by the underlying electronic structure code. See Chapter 5 for details.

8.5   `seedname.eig`

INPUT. Written by the underlying electronic structure code. See Chapter 5 for details.

8.6   `seedname.nnkp`

OUTPUT. Written by `wannier90` when `postproc_setup=.TRUE.` (or, alternatively, when `wannier90` is run with the `-pp` command-line option). See Chapter 5 for details.

8.7   `seedname.wout`

OUTPUT. The master output file. Here we give a description of the main features of the output. The verbosity of the output is controlled by the input parameter `iprint`. The higher the value, the more detail is given in the output file. The default value is 1, which prints minimal information.

8.7.1 Header

The header provides some basic information about `wannier90`, the authors, the code version and release, and the execution time of the current run. The header looks like the following different (the string might slightly change across different versions):

```
+---------------------------------------------------+
|                                                   |
|                    WANNIER90                      |
|                                                   |
+---------------------------------------------------+
|                                                   |
|        Welcome to the Maximally-Localized         |
|        Generalized Wannier Functions code         |
|             http://www.wannier.org                |
|                                                   |
|  Wannier90 Developer Group:                       |
|     Giovanni Pizzi      (EPFL)                    |
|     Valerio Vitale      (Cambridge)               |
|     David Vanderbilt    (Rutgers University)      |
|     Nicola Marzari      (EPFL)                    |
|     Ivo Souza           (Universidad del Pais Vasco) |
|     Arash A. Mostofi    (Imperial College London) |
|     Jonathan R. Yates   (University of Oxford)    |
|                                                   |
|  For the full list of Wannier90 3.x authors,      |
|  please check the code documentation and the      |
|  README on the GitHub page of the code            |
|                                                   |
|                                                   |
|  Please cite                                      |
                        .
                        .
|                                                   |
+---------------------------------------------------+
|    Execution started on 18Dec2018 at 18:39:42     |
+---------------------------------------------------+
```

8.7.2 System information

This part of the output file presents information that `wannier90` has read or inferred from the master input file `seedname.win`. This includes real and reciprocal lattice vectors, atomic positions, k-points, parameters for job control, disentanglement, localisation and plotting.

```
------
SYSTEM
```

```
                                ------

                         Lattice Vectors (Ang)
               a_1     3.938486    0.000000    0.000000
               a_2     0.000000    3.938486    0.000000
               a_3     0.000000    0.000000    3.938486

              Unit Cell Volume:       61.09251   (Ang^3)

                    Reciprocal-Space Vectors (Ang^-1)
               b_1     1.595330    0.000000    0.000000
               b_2     0.000000    1.595330    0.000000
               b_3     0.000000    0.000000    1.595330


 *----------------------------------------------------------------------------*
 |   Site       Fractional Coordinate          Cartesian Coordinate (Ang)    |
 +----------------------------------------------------------------------------+
 | Ba   1   0.00000    0.00000    0.00000   |    0.00000    0.00000    0.00000   |
 | Ti   1   0.50000    0.50000    0.50000   |    1.96924    1.96924    1.96924   |
                                          .
                                          .
 *----------------------------------------------------------------------------*


                           ------------
                           K-POINT GRID
                           ------------

            Grid size =  4 x  4 x  4     Total points =   64


 *------------------------------- MAIN ------------------------------------*
 |   Number of Wannier Functions              :               9            |
 |   Number of input Bloch states             :               9            |
 |   Output verbosity (1=low, 5=high)         :               1            |
 |   Length Unit                              :             Ang            |
 |   Post-processing setup (write *.nnkp)     :               F            |
                                          .
                                          .
 *------------------------------------------------------------------------*
```

8.7.3   Nearest-neighbour k-points

This part of the output files provides information on the b-vectors and weights chosen to satisfy the condition of Eq. 2.1.

```
 *------------------------------- K-MESH ----------------------------------*
 +------------------------------------------------------------------------+
 |               Distance to Nearest-Neighbour Shells                     |
 |               ------------------------------------                     |
 |        Shell              Distance (Ang^-1)          Multiplicity      |
```

```
|           -----             -----------------        ------------         |
|            1                    0.398833                  6               |
|            2                    0.564034                  12              |
                                      .
                                      .
  +-------------------------------------------------------------------------+
  | The b-vectors are chosen automatically                                  |
  | The following shells are used:   1                                      |
  +-------------------------------------------------------------------------+
  |                    Shell   # Nearest-Neighbours                         |
  |                    -----   -------------------                          |
  |                      1             6                                    |
  +-------------------------------------------------------------------------+
  | Completeness relation is fully satisfied [Eq. (B1), PRB 56, 12847 (1997)]  |
  +-------------------------------------------------------------------------+
```

8.7.4   Disentanglement

Then (if required) comes the part where Ω_I is minimised to disentangle the optimally-connected subspace of states for the localisation procedure in the next step.

First, a summary of the energy windows that are being used is given:

```
  *---------------------------- DISENTANGLE ------------------------------*
  +-------------------------------------------------------------------------+
  |                          Energy  Windows                                |
  |                          ---------------                                |
  |             Outer:   2.81739  to   38.00000  (eV)                       |
  |             Inner:   2.81739  to   13.00000  (eV)                       |
  +-------------------------------------------------------------------------+
```

Then, each step of the iterative minimisation of Ω_I is reported.

```
              Extraction of optimally-connected subspace
              -------------------------------------------
  +------------------------------------------------------------------+<-- DIS
  | Iter     Omega_I(i-1)      Omega_I(i)      Delta (frac.)    Time  |<-- DIS
  +------------------------------------------------------------------+<-- DIS
      1       3.82493590       3.66268867       4.430E-02       0.36   <-- DIS
      2       3.66268867       3.66268867       6.911E-15       0.37   <-- DIS
                                    .
                                    .

          <<<      Delta < 1.000E-10  over  3 iterations     >>>
          <<< Disentanglement convergence criteria satisfied >>>

      Final Omega_I     3.66268867 (Ang^2)


  +-------------------------------------------------------------------------+
```

The first column gives the iteration number. For a description of the minimisation procedure and expressions for $\Omega_\text{I}^{(i)}$, see the original paper [2]. The procedure is considered to be converged when the fractional difference between $\Omega_\text{I}^{(i)}$ and $\Omega_\text{I}^{(i-1)}$ is less than `dis_conv_tol` over `dis_conv_window` iterations. The final column gives a running account of the wall time (in seconds) so far. Note that at the end of each line of output, there are the characters "<- DIS". This enables fast searching of the output using, for example, the Unix command `grep`:

```
my_shell> grep DIS wannier.wout | less
```

8.7.5 Wannierisation

The next part of the output file provides information on the minimisation of $\widetilde{\Omega}$. At each iteration, the centre and spread of each WF is reported.

```
*---------------------------- WANNIERISE ------------------------------*
 +--------------------------------------------------------------------+<-- CONV
 | Iter  Delta Spread     RMS Gradient      Spread (Ang^2)      Time  |<-- CONV
 +--------------------------------------------------------------------+<-- CONV


 --------------------------------------------------------------------------
 Initial State
  WF centre and spread    1 (  0.000000,  1.969243,  1.969243 )     1.52435832
  WF centre and spread    2 (  0.000000,  1.969243,  1.969243 )     1.16120620
                                            .
                                            .

      0     0.126E+02     0.0000000000       12.6297685260       0.29  <-- CONV
        O_D=       0.0000000 O_OD=      0.1491718 O_TOT=      12.6297685 <-- SPRD
 --------------------------------------------------------------------------
 Cycle:      1
  WF centre and spread    1 (  0.000000,  1.969243,  1.969243 )     1.52414024
  WF centre and spread    2 (  0.000000,  1.969243,  1.969243 )     1.16059775
                                            .
                                            .
  Sum of centres and spreads ( 11.815458, 11.815458, 11.815458 )    12.62663472

      1    -0.313E-02     0.0697660962       12.6266347170       0.34  <-- CONV
        O_D=       0.0000000 O_OD=      0.1460380 O_TOT=      12.6266347 <-- SPRD
 Delta: O_D= -0.4530841E-18 O_OD= -0.3133809E-02 O_TOT= -0.3133809E-02 <-- DLTA
 --------------------------------------------------------------------------
 Cycle:      2
  WF centre and spread    1 (  0.000000,  1.969243,  1.969243 )     1.52414866
  WF centre and spread    2 (  0.000000,  1.969243,  1.969243 )     1.16052405
                                            .
                                            .
  Sum of centres and spreads ( 11.815458, 11.815458, 11.815458 )    12.62646411

      2    -0.171E-03     0.0188848262       12.6264641055       0.38  <-- CONV
        O_D=       0.0000000 O_OD=      0.1458674 O_TOT=      12.6264641 <-- SPRD
 Delta: O_D= -0.2847260E-18 O_OD= -0.1706115E-03 O_TOT= -0.1706115E-03 <-- DLTA
```

```
    -------------------------------------------------------------------------------
                                        .
                                        .
    -------------------------------------------------------------------------------
    Final State
     WF centre and spread    1  (  0.000000,  1.969243,  1.969243 )      1.52416618
     WF centre and spread    2  (  0.000000,  1.969243,  1.969243 )      1.16048545
                                        .
                                        .
     Sum of centres and spreads ( 11.815458, 11.815458, 11.815458 )    12.62645344

              Spreads (Ang^2)        Omega I      =     12.480596753
              ===============        Omega D      =      0.000000000
                                     Omega OD     =      0.145856689
         Final Spread (Ang^2)        Omega Total  =     12.626453441
    -------------------------------------------------------------------------------
```

It looks quite complicated, but things look more simple if one uses `grep`:

`my_shell> grep CONV wannier.wout`

gives

```
    +----------------------------------------------------------------+<-- CONV
    | Iter  Delta Spread     RMS Gradient      Spread (Ang^2)    Time |<-- CONV
    +----------------------------------------------------------------+<-- CONV
        0    0.126E+02      0.0000000000      12.6297685260     0.29  <-- CONV
        1   -0.313E-02      0.0697660962      12.6266347170     0.34  <-- CONV
                                        .
                                        .
       50    0.000E+00      0.0000000694      12.6264534413     2.14  <-- CONV
```

The first column is the iteration number, the second is the change in Ω from the previous iteration, the third is the root-mean-squared gradient of Ω with respect to variations in the unitary matrices $\mathbf{U}^{(\mathbf{k})}$, and the last is the time taken (in seconds). Depending on the input parameters used, the procedure either runs for `num_iter` iterations, or a convergence criterion is applied on Ω. See Section 2.8 for details.

Similarly, the command

`my_shell> grep SPRD wannier.wout`

gives

```
        O_D=      0.0000000 O_OD=       0.1491718 O_TOT=      12.6297685 <-- SPRD
        O_D=      0.0000000 O_OD=       0.1460380 O_TOT=      12.6266347 <-- SPRD
                                        .
                                        .
        O_D=      0.0000000 O_OD=       0.1458567 O_TOT=      12.6264534 <-- SPRD
```

which, for each iteration, reports the value of the diagonal and off-diagonal parts of the non-gauge-invariant spread, as well as the total spread, respectively. Recall from Section 1 that $\Omega = \Omega_{\mathrm{I}} + \Omega_{\mathrm{D}} + \Omega_{\mathrm{OD}}$.

Wannierisation with selective localization and constrained centres

For full details of the selectively localised Wannier function (SLWF) method, the reader is referred to Ref. [8]. When using the SLWF method, only a few things change in the output file and in general the same principles described above will apply. In particular, when minimising the spread with respect to the degrees of freedom of only a subset of functions, it is not possible to cast the total spread functional Ω as a sum of a gauge-invariant part and a gauge-dependent part. Instead, one has $\Omega^{'} = \Omega_{\mathrm{IOD}} + \Omega_{\mathrm{D}}$, where

$$\Omega^{'} = \sum_{n=1}^{J^{'} < J} \left[\langle r^2 \rangle_n - \bar{\mathbf{r}}_n^2 \right]$$

and

$$\Omega_{\mathrm{IOD}} = \sum_{n=1}^{J^{'} < J} \left[\langle r_n^2 \rangle - \sum_{\mathbf{R}} |\langle \mathbf{R}n|\mathbf{r}|n\mathbf{R}\rangle|^2 \right].$$

The total number of Wannier functions is J, whereas J' is the number functions to be selectively localized (so-called *objective WFs*). The information on the number of functions which are going to be selectively localized (`Number of Objective Wannier Functions`) is given in the `MAIN` section of the output file:

```
*---------------------------- MAIN ----------------------------------*
|   Number of Wannier Functions             :            4          |
|   Number of Objective Wannier Functions   :            1          |
|   Number of input Bloch states            :            4          |
```

Whether or not the selective localization procedure has been switched on is reported in the `WANNIERISE` section as

```
|  Perform selective localization           :            T          |
```

The next part of the output file provides information on the minimisation of the modified spread functional:

```
*--------------------------- WANNIERISE ---------------------------*
+-----------------------------------------------------------------+<-- CONV
| Iter  Delta Spread     RMS Gradient      Spread (Ang^2)    Time  |<-- CONV
+-----------------------------------------------------------------+<-- CONV


-------------------------------------------------------------------
Initial State
 WF centre and spread    1 ( -0.857524,  0.857524,  0.857524 )     1.80463310
 WF centre and spread    2 (  0.857524, -0.857524,  0.857524 )     1.80463311
 WF centre and spread    3 (  0.857524,  0.857524, -0.857524 )     1.80463311
 WF centre and spread    4 ( -0.857524, -0.857524, -0.857524 )     1.80463311
 Sum of centres and spreads ( -0.000000, -0.000000,  0.000000 )    7.21853243

     0    -0.317E+01    0.0000000000         -3.1653368719      0.00  <-- CONV
        O_D=      0.0000000 O_IOD=     -3.1653369 O_TOT=    -3.1653369 <-- SPRD
-------------------------------------------------------------------
```

```
 Cycle:        1
  WF centre and spread     1 ( -0.853260,  0.853260,  0.853260 )     1.70201498
  WF centre and spread     2 (  0.857352, -0.857352,  0.862454 )     1.84658331
  WF centre and spread     3 (  0.857352,  0.862454, -0.857352 )     1.84658331
  WF centre and spread     4 ( -0.862454, -0.857352, -0.857352 )     1.84658331
  Sum of centres and spreads ( -0.001010,  0.001010,  0.001010 )     7.24176492

       1    -0.884E-01     0.2093698260       -3.2536918930        0.00  <-- CONV
        O_IOD=       -3.2536919 O_D=       0.0000000 O_TOT=      -3.2536919 <-- SPRD
Delta: O_IOD= -0.1245020E+00 O_D=  0.0000000E+00 O_TOT= -0.8835502E-01 <-- DLTA
 -------------------------------------------------------------------------------
                                   .
                                   .
 -------------------------------------------------------------------------------
 Final State
  WF centre and spread     1 ( -0.890189,  0.890189,  0.890189 )     1.42375495
  WF centre and spread     2 (  0.895973, -0.895973,  0.917426 )     2.14313664
  WF centre and spread     3 (  0.895973,  0.917426, -0.895973 )     2.14313664
  WF centre and spread     4 ( -0.917426, -0.895973, -0.895973 )     2.14313664
  Sum of centres and spreads ( -0.015669,  0.015669,  0.015669 )     7.85316486

          Spreads (Ang^2)       Omega IOD    =     1.423371553
          ================       Omega D      =     0.000383395
                                 Omega Rest   =     9.276919811
     Final Spread (Ang^2)        Omega Total  =     1.423754947
 -------------------------------------------------------------------------------
```

When comparing the output from an SLWF calculation with a standard wannierisation (see Sec. 8.7.5), the only differences are in the definition of the spread functional. Hence, during the minimization O_OD is replaced by O_IOD and O_TOT now reflects the fact that the new total spread functional is Ω'. The part on the final state has one more item of information: the value of the difference between the global spread functional and the new spread functional given by Omega Rest

$$\Omega_R = \sum_{n=1}^{J-J'} \left[\langle r^2 \rangle_n - \bar{\mathbf{r}}_n^2 \right]$$

If adding centre-constraints to the SLWFs, you will find the information about the centres of the original projections and the desired centres in the SYSTEM section

```
 *-----------------------------------------------------------------------------*
 | Wannier#        Original Centres            Constrained centres             |
 +-----------------------------------------------------------------------------+
 |    1    0.25000   0.25000   0.25000  |    0.00000   0.00000   0.00000       |
 *-----------------------------------------------------------------------------*
```

As before one can check that the selective localization with constraints is being used by looking at the WANNIERISE section:

```
|   Perform selective localization             :                     T              |
|   Use constrains in selective localization   :                     T              |
|   Value of the Lagrange multiplier           :            0.100E+01               |
*----------------------------------------------------------------------------------*
```

which also gives the selected value for the Lagrange multiplier. The output file for the minimisation section is modified as follows: both `O_IOD` and `O_TOT` now take into account the factors coming from the new term in the functional due to the constraints, which are implemented by adding the following penalty functional to the spread functional,

$$\lambda_c \sum_{n=1}^{J'} \left(\bar{\mathbf{r}}_n - \mathbf{r}_{0n} \right)^2 ,$$

where $\mathbf{r}_{0n}$ is the desired centre for the nth Wannier function, see Ref. [8] for details. The layout of the output file at each iteration is unchanged.

```
     1     -0.884E-01       0.2093698260        -3.2536918930        0.00  <-- CONV
```

As regarding the final state, the only addition is the information on the value of the penalty functional associated with the constraints (`Penalty func`), which should be zero if the final centres of the Wannier functions are at the target centres:

```
Final State
 WF centre and spread    1  ( -1.412902,  1.412902,  1.412902 )     1.63408756
 WF centre and spread    2  (  1.239678, -1.239678,  1.074012 )     2.74801593
 WF centre and spread    3  (  1.239678,  1.074012, -1.239678 )     2.74801592
 WF centre and spread    4  ( -1.074012, -1.239678, -1.239678 )     2.74801592
 Sum of centres and spreads ( -0.007559,  0.007559,  0.007559 )     9.87813534

         Spreads (Ang^2)      Omega IOD_C   =     -4.261222001
         ===============      Omega D       =      0.000000000
                              Omega Rest    =      5.616913337
                              Penalty func  =      0.000000000
   Final Spread (Ang^2)       Omega Total_C =     -4.261222001
 ----------------------------------------------------------------------
```

8.7.6 Plotting

After WF have been localised, `wannier90` enters its plotting routines (if required). For example, if you have specified an interpolated bandstucture:

```
    *----------------------------------------------------------------------------*
    |                                PLOTTING                                     |
    *----------------------------------------------------------------------------*

Calculating interpolated band-structure
```

8.7.7 Summary timings

At the very end of the run, a summary of the time taken for various parts of the calculation is given. The level of detail is controlled by the `timing_level` input parameter (set to 1 by default).

```
*=======================================================================*
|                          TIMING INFORMATION                           |
*=======================================================================*
|   Tag                                            Ncalls      Time (s)|
|-----------------------------------------------------------------------|
|kmesh: get                                   :        1         0.212|
|overlap: read                                :        1         0.060|
|wann: main                                   :        1         1.860|
|plot: main                                   :        1         0.168|
*-----------------------------------------------------------------------*

 All done: wannier90 exiting
```

8.8 `seedname.chk`

INPUT/OUTPUT. Information required to restart the calculation or enter the plotting phase. If we have used disentanglement this file also contains the rectangular matrices $\mathbf{U}^{\text{dis}(\mathbf{k})}$.

8.9 `seedname.r2mn`

OUTPUT. Written if `write_r2mn = true`. The matrix elements $\langle m|r^2|n\rangle$ (where m and n refer to MLWF)

8.10 `seedname_band.dat`

OUTPUT. Written if `bands_plot=.TRUE.`; The raw data for the interpolated band structure.

8.11 `seedname_band.gnu`

OUTPUT. Written if `bands_plot=.TRUE.` and `bands_plot_format=gnuplot`; A `gnuplot` script to plot the interpolated band structure.

8.12 `seedname_band.agr`

OUTPUT. Written if `bands_plot=.TRUE.` and `bands_plot_format=xmgrace`; A `grace` file to plot the interpolated band structure.

8.13   `seedname_band.kpt`

OUTPUT. Written if `bands_plot=.TRUE.`; The k-points used for the interpolated band structure, in units of the reciprocal lattice vectors. This file can be used to generate a comparison band structure from a first-principles code.

8.14   `seedname.bxsf`

OUTPUT. Written if `fermi_surface_plot=.TRUE.`; A Fermi surface plot file suitable for plotting with XCrySDen.

8.15   `seedname_w.xsf`

OUTPUT. Written if `wannier_plot=.TRUE.` and `wannier_plot_format=xcrysden`. Contains the wth WF in real space in a format suitable for plotting with XCrySDen or VMD, for example.

8.16   `seedname_w.cube`

OUTPUT. Written if `wannier_plot=.TRUE.` and `wannier_plot_format=cube`. Contains the wth WF in real space in Gaussian cube format, suitable for plotting in XCrySDen, VMD, gopenmol etc.

8.17   `UNKp.s`

INPUT. Read if `wannier_plot=.TRUE.` and used to plot the MLWF. Read if `transport_mode=lcr` and `tran_read_ht=.FALSE.` for use in automated lcr transport calculations.

The periodic part of the Bloch states represented on a regular real space grid, indexed by k-point `p` (from 1 to `num_kpts`) and spin `s` ('1' for 'up', '2' for 'down').

The name of the wavefunction file is assumed to have the form:

```
    write(wfnname,200) p,spin
200 format ('UNK',i5.5,'.',i1)
```

The first line of each file should contain 5 integers: the number of grid points in each direction (`ngx`, `ngy` and `ngz`), the k-point number `ik` and the total number of bands `num_band` in the file. The full file will be read by `wannier90` as:

```
read(file_unit) ngx,ngy,ngz,ik,nbnd
do loop_b=1,num_bands
  read(file_unit) (r_wvfn(nx,loop_b),nx=1,ngx*ngy*ngz)
end do
```

If `spinors=true` then `s`='NC', and the name of the wavefunction file is assumed to have the form:

```
   write(wfnname,200) p
200 format ('UNK',i5.5,'.NC')
```

and the file will be read by `wannier90` as:

```
read(file_unit) ngx,ngy,ngz,ik,nbnd
do loop_b=1,num_bands
   read(file_unit) (r_wvfn_nc(nx,loop_b,1),nx=1,ngx*ngy*ngz) ! up-spinor
   read(file_unit) (r_wvfn_nc(nx,loop_b,2),nx=1,ngx*ngy*ngz) ! down-spinor
end do
```

All UNK files can be in formatted or unformatted style, this is controlled by the logical keyword `wvfn_formatted`.

8.18   `seedname_centres.xyz`

OUTPUT. Written if `write_xyz=.TRUE.`; xyz format atomic structure file suitable for viewing with your favourite visualiser (`jmol`, `gopenmol`, `vmd`, etc.).

8.19   `seedname_hr.dat`

OUTPUT. Written if `write_hr=.TRUE.`. The first line gives the date and time at which the file was created. The second line states the number of Wannier functions `num_wann`. The third line gives the number of Wigner-Seitz grid-points `nrpts`. The next block of `nrpts` integers gives the degeneracy of each Wigner-Seitz grid point, with 15 entries per line. Finally, the remaining $\text{num\_wann}^2 \times \text{nrpts}$ lines each contain, respectively, the components of the vector $\mathbf{R}$ in terms of the lattice vectors $\{\mathbf{A}_i\}$, the indices m and n, and the real and imaginary parts of the Hamiltonian matrix element $H_{mn}^{(\mathbf{R})}$ in the WF basis, e.g.,

```
 Created on 24May2007 at 23:32:09
      20
      17
   4   1   2   1   4   1   1   2   1   4   6   1   1   1   2
   1   2
   0   0  -2   1   1   -0.001013    0.000000
   0   0  -2   2   1    0.000270    0.000000
   0   0  -2   3   1   -0.000055    0.000000
   0   0  -2   4   1    0.000093    0.000000
   0   0  -2   5   1   -0.000055    0.000000
   .
   .
   .
```

8.20   `seedname_r.dat`

OUTPUT. Written if `write_rmn = true`. The matrix elements $\langle m\mathbf{0}|\mathbf{r}|n\mathbf{R}\rangle$ (where $n\mathbf{R}$ refers to MLWF n in unit cell $\mathbf{R}$). The first line gives the date and time at which the file was created. The second line states the number of Wannier functions `num_wann`. The third line states the number of $\mathbf{R}$ vectors `nrpts`. Similar to the case of the Hamiltonian matrix above, the remaining `num_wann`$^2\times$ `nrpts` lines each contain, respectively, the components of the vector $\mathbf{R}$ in terms of the lattice vectors $\{\mathbf{A}_i\}$, the indices m and n, and the real and imaginary parts of the position matrix element in the WF basis.

8.21   `seedname_tb.dat`

OUTPUT. Written if `write_tb=.TRUE.`. This file is essentially a combination of `seedname_hr.dat` and `seedname_r.dat`, plus lattice vectors. The first line gives the date and time at which the file was created. The second to fourth lines are the lattice vectors in Angstrom unit.

```
written on 27Jan2020 at 18:08:42
 -1.8050234585004898        0.0000000000000000      1.8050234585004898
  0.0000000000000000        1.8050234585004898      1.8050234585004898
 -1.8050234585004898        1.8050234585004898      0.0000000000000000
```

The next part is the same as `seedname_hr.dat`. The fifth line states the number of Wannier functions `num_wann`. The sixth line gives the number of Wigner-Seitz grid-points `nrpts`. The next block of `nrpts` integers gives the degeneracy of each Wigner-Seitz grid point, with 15 entries per line. Then, the next `num_wann`$^2\times$ `nrpts` lines each contain, respectively, the components of the vector $\mathbf{R}$ in terms of the lattice vectors $\{\mathbf{A}_i\}$, the indices m and n, and the real and imaginary parts of the Hamiltonian matrix element $H_{mn}^{(\mathbf{R})}$ in the WF basis, e.g.,

```
          7
         93
    4   6   2   2   2   1   2   2   1   1   2   6   2   2   2
    6   2   2   4   1   1   1   4   1   1   1   1   2   1   1
    1   2   2   1   1   2   4   2   1   2   1   1   1   1   2
    1   1   1   2   1   1   1   1   2   1   2   4   2   1   1
    2   2   1   1   1   2   1   1   1   1   4   1   1   1   4
    2   2   6   2   2   2   6   2   1   1   2   2   1   2   2
    2   6   4

   -3   1   1
    1   1    0.42351556E-02 -0.95722060E-07
    2   1    0.69481480E-07 -0.20318638E-06
    3   1    0.10966508E-06 -0.13983284E-06
    .
    .
    .
```

Finally, the last part is the same as `seedname_r.dat`. The `num_wann`$^2\times$ `nrpts` lines each contain, respectively, the components of the vector $\mathbf{R}$ in terms of the lattice vectors $\{\mathbf{A}_i\}$, the indices m and n,

and the real and imaginary parts of the position matrix element in the WF basis (the float numbers in columns 3 and 4 are the real and imaginary parts for $\langle m\mathbf{0}|\mathbf{r}_x|n\mathbf{R}\rangle$, columns 5 and 6 for $\langle m\mathbf{0}|\mathbf{r}_y|n\mathbf{R}\rangle$, and columns 7 and 8 for $\langle m\mathbf{0}|\mathbf{r}_z|n\mathbf{R}\rangle$), e.g.

```
   -3    1    1
    1    1     0.32277552E-09   0.21174901E-08  -0.85436987E-09   0.26851510E-08   ...
    2    1    -0.18881883E-08   0.21786973E-08   0.31123076E-03   0.39228431E-08   ...
    3    1     0.31123242E-03  -0.35322230E-09   0.70867281E-09   0.10433480E-09   ...
    .
    .
    .
```

8.22   `seedname.bvec`

OUTPUT. Written if `write_bvec = true`. This file contains the matrix elements of bvector and their weights. The first line gives the date and time at which the file was created. The second line states the number of k-points and the total number of neighbours for each k-point `nntot`. Then all the other lines contain the b-vector (x,y,z) coordinate and weigths for each k-points and each of its neighbours.

8.23   `seedname_wsvec.dat`

OUTPUT. Written if `write_hr = true` or `write_rmn = true` or `write_tb = true`. The first line gives the date and time at which the file was created and the value of `use_ws_distance`. For each pair of Wannier functions (identified by the components of the vector $\mathbf{R}$ separating their unit cells and their indices) it gives: (i) the number of lattice vectors of the periodic supercell $\mathbf{T}$ that bring the Wannier function in $\mathbf{R}$ back in the Wigner-Seitz cell centred on the other Wannier function and (ii) the set of superlattice vectors $\mathbf{T}$ to make this transformation. These superlattice vectors $\mathbf{T}$ should be added to the $\mathbf{R}$ vector to obtain the correct centre of the Wannier function that underlies a given matrix element (e.g. the Hamiltonian matrix elements in `seedname_hr.dat`) in order to correctly interpolate in reciprocal space.

```
## written on 20Sep2016 at 18:12:37  with use_ws_distance=.true.
    0    0    0    1    1
    1
    0    0    0
    0    0    0    1    2
    1
    0    0    0
    0    0    0    1    3
    1
    0    0    0
    0    0    0    1    4
    1
    0    0    0
    0    0    0    1    5
    1
```

```
   0    0    0
   0    0    0    1    6
   2
   0   -1   -1
   1   -1   -1
   .
   .
   .
```

8.24   `seedname_qc.dat`

OUTPUT. Written if `transport = .TRUE.`. The first line gives the date and time at which the file was created. In the subsequent lines, the energy value in units of eV is written in the left column, and the quantum conductance in units of $\frac{2e^2}{h}$ ($\frac{e^2}{h}$ for a spin-polarized system) is written in the right column.

```
## written on 14Dec2007 at 11:30:17
   -3.000000        8.999999
   -2.990000        8.999999
   -2.980000        8.999999
   -2.970000        8.999999
    .
    .
    .
```

8.25   `seedname_dos.dat`

OUTPUT. Written if `transport = .TRUE.`. The first line gives the date and time at which the file was created. In the subsequent lines, the energy value in units of eV is written in the left column, and the density of states in an arbitrary unit is written in the right column.

```
## written on 14Dec2007 at 11:30:17
   -3.000000        6.801199
   -2.990000        6.717692
   -2.980000        6.640828
   -2.970000        6.569910
    .
    .
    .
```

8.26   `seedname_htB.dat`

INPUT/OUTPUT. Read if `transport_mode = bulk` and `tran_read_ht = .TRUE.`. Written if `tran_write_ht = .TRUE.`. The first line gives the date and time at which the file was created. The second line gives `tran_num_bb`. The subsequent lines contain `tran_num_bb`×`tran_num_bb` H_{mn} matrix, where the indices m and n span all `tran_num_bb` WFs located at 0th principal layer. Then `tran_num_bb` is recorded

again in the new line followed by H_{mn}, where m^{th} WF is at 0th principal layer and n^{th} at 1st principal layer. The H_{mn} matrix is written in such a way that m is the fastest varying index.

```
written on 14Dec2007 at 11:30:17
  150
  -1.737841   -2.941054    0.052673   -0.032926    0.010738   -0.009515
   0.011737   -0.016325    0.051863   -0.170897   -2.170467    0.202254
   .
   .
   .
  -0.057064   -0.571967   -0.691431    0.015155   -0.007859    0.000474
  -0.000107   -0.001141   -0.002126    0.019188   -0.686423  -10.379876
  150
   0.000000    0.000000    0.000000    0.000000    0.000000    0.000000
   0.000000    0.000000    0.000000    0.000000    0.000000    0.000000
   .
   .
   .
   0.000000    0.000000    0.000000    0.000000    0.000000   -0.001576
   0.000255   -0.000143   -0.001264    0.002278    0.000000    0.000000
```

8.27   seedname_htL.dat

INPUT. Read if `transport_mode = lcr` and `tran_read_ht = .TRUE.`. The file must be written in the same way as in `seedname_htB.dat`. The first line can be any comment you want. The second line gives `tran_num_ll`. `tran_num_ll` in `seedname_htL.dat` must be equal to that in `seedname.win`. The code will stop otherwise.

```
Created by a WANNIER user
  105
   0.316879    0.000000   -2.762434    0.048956    0.000000   -0.016639
   0.000000    0.000000    0.000000    0.000000    0.000000   -2.809405
   .
   .
   .
   0.000000    0.078188    0.000000    0.000000   -2.086453   -0.001535
   0.007878   -0.545485  -10.525435
  105
   0.000000    0.000000    0.000315   -0.000294    0.000000    0.000085
   0.000000    0.000000    0.000000    0.000000    0.000000    0.000021
   .
   .
   .
   0.000000    0.000000    0.000000    0.000000    0.000000    0.000000
   0.000000    0.000000    0.000000
```

8.28   seedname_htR.dat

INPUT. Read if `transport_mode = lcr` and `tran_read_ht = .TRUE.` and `tran_use_same_lead = .FALSE..` The file must be written in the same way as in `seedname_htL.dat`. `tran_num_rr` in `seedname_htR.dat` must be equal to that in `seedname.win`.

8.29   seedname_htC.dat

INPUT. Read if `transport_mode = lcr` and `tran_read_ht = .TRUE.`. The first line can be any comment you want. The second line gives `tran_num_cc`. The subsequent lines contain `tran_num_cc`×`tran_num_cc` H_{mn} matrix, where the indices m and n span all `tran_num_cc` WFs inside the central conductor region. `tran_num_cc` in `seedname_htC.dat` must be equal to that in `seedname.win`.

```
Created by a WANNIER user
   99
 -10.499455    -0.541232     0.007684    -0.001624    -2.067078    -0.412188
   0.003217     0.076965     0.000522    -0.000414     0.000419    -2.122184
   .
   .
   .
  -0.003438     0.078545     0.024426     0.757343    -2.004899    -0.001632
   0.007807    -0.542983   -10.516896
```

8.30   seedname_htLC.dat

INPUT. Read if `transport_mode = lcr` and `tran_read_ht = .TRUE.`. The first line can be any comment you want. The second line gives `tran_num_ll` and `tran_num_lc` in the given order. The subsequent lines contain `tran_num_ll`×`tran_num_lc` H_{mn} matrix. The index m spans `tran_num_ll` WFs in the surface principal layer of semi-infinite left lead which is in contact with the conductor region. The index n spans `tran_num_lc` WFs in the conductor region which have a non-negligible interaction with the WFs in the semi-infinite left lead. Note that `tran_num_lc` can be different from `tran_num_cc`.

```
Created by a WANNIER user
  105      99
   0.000000     0.000000     0.000000     0.000000     0.000000     0.000000
   0.000000     0.000000     0.000000     0.000000     0.000000     0.000000
   .
   .
   .
  -0.000003     0.000009     0.000290     0.000001    -0.000007    -0.000008
   0.000053    -0.000077    -0.000069
```

8.31   `seedname_htCR.dat`

INPUT. Read if `transport_mode = lcr` and `tran_read_ht = .TRUE.`. The first line can be any comment you want. The second line gives `tran_num_cr` and `tran_num_rr` in the given order. The subsequent lines contain `tran_num_cr`×`tran_num_rr` H_{mn} matrix. The index m spans `tran_num_cr` WFs in the conductor region which have a non-negligible interaction with the WFs in the semi-infinite right lead. The index n spans `tran_num_rr` WFs in the surface principal layer of semi-infinite right lead which is in contact with the conductor region. Note that `tran_num_cr` can be different from `tran_num_cc`.

```
Created by a WANNIER user
   99    105
  -0.000180     0.000023     0.000133    -0.000001     0.000194     0.000008
  -0.000879    -0.000028     0.000672    -0.000257    -0.000102    -0.000029
    .
    .
    .
   0.000000     0.000000     0.000000     0.000000     0.000000     0.000000
   0.000000     0.000000     0.000000
```

8.32   `seedname.unkg`

INPUT. Read if `transport_mode = lcr` and `tran_read_ht = .FALSE.`. The first line is the number of G-vectors at which the $\tilde{u}_{m\mathbf{k}}(\mathbf{G})$ are subsequently printed. This number should always be 32 since 32 specific $\tilde{u}_{m\mathbf{k}}$ are required. The following lines contain the following in this order: The band index m, a counter on the number of G-vectors, the integer co-efficient of the G-vector components a, b, c (where $\mathbf{G} = a\mathbf{b}_1 + b\mathbf{b}_2 + c\mathbf{b}_3$), then the real and imaginary parts of the corresponding $\tilde{u}_{m\mathbf{k}}(\mathbf{G})$ at the Γ-point. We note that the ordering in which the G-vectors and $\tilde{u}_{m\mathbf{k}}(\mathbf{G})$ are printed is not important, but the specific G-vectors are critical. The following example displays for a single band, the complete set of $\tilde{u}_{m\mathbf{k}}(\mathbf{G})$ that are required. Note the G-vectors (a, b, c) needed.

```
    32
   1    1    0    0    0    0.4023306    0.0000000
   1    2    0    0    1   -0.0000325    0.0000000
   1    3    0    1    0   -0.3043665    0.0000000
   1    4    1    0    0   -0.3043665    0.0000000
   1    5    2    0    0    0.1447143    0.0000000
   1    6    1   -1    0    0.2345179    0.0000000
   1    7    1    1    0    0.2345179    0.0000000
   1    8    1    0   -1    0.0000246    0.0000000
   1    9    1    0    1    0.0000246    0.0000000
   1   10    0    2    0    0.1447143    0.0000000
   1   11    0    1   -1    0.0000246    0.0000000
   1   12    0    1    1    0.0000246    0.0000000
   1   13    0    0    2    0.0000338    0.0000000
   1   14    3    0    0   -0.0482918    0.0000000
   1   15    2   -1    0   -0.1152414    0.0000000
```

```
1   16   2   1    0   -0.1152414   0.0000000
1   17   2   0   -1   -0.0000117   0.0000000
1   18   2   0    1   -0.0000117   0.0000000
1   19   1  -2    0   -0.1152414   0.0000000
1   20   1   2    0   -0.1152414   0.0000000
1   21   1  -1   -1   -0.0000190   0.0000000
1   22   1  -1    1   -0.0000190   0.0000000
1   23   1   1   -1   -0.0000190   0.0000000
1   24   1   1    1   -0.0000190   0.0000000
1   25   1   0   -2   -0.0000257   0.0000000
1   26   1   0    2   -0.0000257   0.0000000
1   27   0   3    0   -0.0482918   0.0000000
1   28   0   2   -1   -0.0000117   0.0000000
1   29   0   2    1   -0.0000117   0.0000000
1   30   0   1   -2   -0.0000257   0.0000000
1   31   0   1    2   -0.0000257   0.0000000
1   32   0   0    3    0.0000187   0.0000000
2    1   0   0    0   -0.0000461   0.0000000
.
.
.
```

8.33   `seedname_u.mat`

OUTPUT. Written if `write_u_matrices` = .TRUE.. The first line gives the date and time at which the file was created. The second line states the number of kpoints `num_kpts` and the number of wannier functions `num_wann` twice. The third line is empty. Then there are `num_kpts` blocks of data, each of which starts with a line containing the kpoint (in fractional coordinates of the reciprocal lattice vectors) followed by `num_wann * num_wann` lines containing the matrix elements (real and imaginary parts) of $\mathbf{U^{(k)}}$. The matrix elements are in column-major order (ie, cycling over rows first and then columns). There is an empty line between each block of data.

```
written on 15Sep2016 at 16:33:46
         64              8              8

  0.0000000000  +0.0000000000  +0.0000000000
  0.4468355787  +0.1394579978
 -0.0966033667  +0.4003934902
 -0.0007748974  +0.0011788678
 -0.0041177339  +0.0093821027
  .
  .
  .


  0.1250000000   0.0000000000  +0.0000000000
  0.4694005589  +0.0364941808
 +0.2287801742  -0.1135511138
 -0.4776782452  -0.0511719121
```

```
+0.0142081014   +0.0006203139
   .
   .
   .
```

8.34   seedname_u_dis.mat

OUTPUT. Written if `write_u_matrices` = `.TRUE.` and disentanglement is enabled. The first line gives the date and time at which the file was created. The second line states the number of kpoints `num_kpts`, the number of wannier functions `num_bands` and the number of `num_bands`. The third line is empty. Then there are `num_kpts` blocks of data, each of which starts with a line containing the kpoint (in fractional coordinates of the reciprocal lattice vectors) followed by `num_wann * num_bands` lines containing the matrix elements (real and imaginary parts) of $\mathbf{U}^{\mathrm{dis}(\mathbf{k})}$. The matrix elements are in column-major order (ie, cycling over rows first and then columns). There is an empty line between each block of data.

```
 written on 15Sep2016 at 16:33:46
          64              8              16

   0.0000000000   +0.0000000000   +0.0000000000
   1.0000000000   +0.0000000000
 +0.0000000000   +0.0000000000
 +0.0000000000   +0.0000000000
 +0.0000000000   +0.0000000000
   .
   .
   .


   0.1250000000    0.0000000000   +0.0000000000
   1.0000000000   +0.0000000000
 +0.0000000000   +0.0000000000
 +0.0000000000   +0.0000000000
 +0.0000000000   +0.0000000000
   .
   .
   .
```

Chapter 9

Some notes on the interpolation

In `wannier90` v.2.1, a new flag `use_ws_distance` has been introduced (and it is set to `.true.` by default since version v3.0). Setting it to `.false.` reproduces the "standard" behavior of `wannier90` in v.2.0.1 and earlier, while setting it to `.true.` changes the interpolation method as described below. In general, this allows a smoother interpolation, helps reducing (a bit) the number of $k-$points required for interpolation, and reproduces the band structure of large supercells sampled at Γ only (setting it to `.false.` produces instead flat bands, which might instead be the intended behaviour for small molecules carefully placed at the centre of the cell).

The core idea rests on the fact that the Wannier functions $w_{n\mathbf{R}}(\mathbf{r})$ that we build from $N \times M \times L$ $k-$points are actually periodic over a supercell of size $N \times M \times L$, but when you use them to interpolate you want them to be *zero* outside this supercell. In 1D it is pretty obvious want we mean here, but in 3D what you really want that they are zero outside the Wigner–Seitz cell of the $N \times M \times L$ superlattice.

The best way to impose this condition is to check that every real-space distance that enters in the $R \to k$ Fourier transform is the shortest possible among all the $N \times M \times L-$periodic equivalent copies.

If the distances were between unit cells, this would be trivial, but the distances are between Wannier functions which are not centred on $\mathbf{R} = 0$. Hence, when you want to consider the matrix element of a generic operator $\mathbf{O}$ (i.e., the Hamiltonian) $\langle w_{i\mathbf{0}}(\mathbf{r})|\mathbf{O}|w_{j\mathbf{R}}(\mathbf{r})\rangle$ you must take in account that the centre $\boldsymbol{\tau}_i$ of $w_{i\mathbf{0}}(\mathbf{r})$ may be very far away from $\mathbf{0}$ and the centre $\boldsymbol{\tau}_j$ of $w_{j\mathbf{R}}(\mathbf{r})$ may be very far away from $\mathbf{R}$.

There are many way to find the shortest possible distance between $w_{i\mathbf{0}}(\mathbf{r})$ and $w_{j\mathbf{R}}(\mathbf{r} - \mathbf{R})$, the one used here is to consider the distance $\mathbf{d}_{ij\mathbf{R}} = \boldsymbol{\tau}_i - (\boldsymbol{\tau}_j + \mathbf{R})$ and all its superlattice periodic equivalents $\mathbf{d}_{ij\mathbf{R}} + \tilde{\mathbf{R}}_{nml}$, with $\tilde{\mathbf{R}}_{nml} = (Nn\mathbf{a}_1 + Mm\mathbf{a}_2 + Ll\mathbf{a}_3)$ and $n, l, m = -L, -L + 1, ...0, ..., L - 1, L$, with L controlled by the parameter `ws_search_size`.

Then,

1. if $\mathbf{d}_{ij\mathbf{R}} + \tilde{\mathbf{R}}_{nml}$ is inside the $N \times M \times L$ super-WS cell, then it is the shortest, take it and quit

2. if it is outside the WS, then it is not the shortest, throw it away

3. if it is on the border/corner of the WS then it is the shortest, but there are other choices of (n, m, l) which are equivalent, find all of them

In all distance comparisons, a small but finite tolerance is considered, which can be controlled with the parameter `ws_distance_tol`.

Because of how the Fourier transform is defined in the `wannier90` code (not the only possible choice) it is only $\mathbf{R} + \tilde{\mathbf{R}}_{nml}$ that enters the exponential, but you still have to consider the distance among the actual centres of the Wannier functions. Using the centres of the unit-cell to which the Wannier functions belong is not enough (but is easier, and saves you one index).

Point 3 is not stricly necessary, but using it helps enforcing the symmetry of the system in the resulting band structure. You will get some small but evident symmetry breaking in the band plots if you just pick one of the equivalent $\tilde{\mathbf{R}}$ vectors.

Note that in some cases, all this procedure does absolutely nothing, for instance if all the Wannier function centres are very close to 0 (e.g., a molecule carefully placed in the periodic cell).

In some other cases, the effect may exist but be imperceptible. E.g., if you use a very fine grid of $k-$points, even if you don't centre each functions perfectly, the periodic copies will still be so far away that the change in centre applied with `use_ws_distance` does not matter.

When instead you use few $k-$points, activating the `use_ws_distance` may help a lot in avoiding spurious oscillations of the band structure even when the Wannier functions are well converged.

Chapter 10

Sample Input Files

10.1   Master input file: `seedname.win`

```
num_wann        : 4
mp_grid         : 4 4 4
num_iter        : 100
postproc_setup  : true

begin unit_cell_cart
ang
-1.61 0.00 1.61
 0.00 1.61 1.61
-1.61 1.61 0.00
end unit_cell_cart

begin atoms_frac
C    -0.125   -0.125   -0.125
C     0.125    0.125    0.125
end atoms_frac

bands_plot        : true
bands_num_points  : 100
bands_plot_format : gnuplot

begin kpoint_path
L 0.50000 0.50000 0.50000 G 0.00000 0.00000 0.00000
G 0.00000 0.00000 0.00000 X 0.50000 0.00000 0.50000
X 0.50000 0.00000 0.50000 K 0.62500 0.25000 0.62500
end kpoint_path

begin projections
C:l=0,l=1
end projections

begin kpoints
```

```
0.00 0.00 0.00
0.00 0.00 0.25
0.00 0.50 0.50
 .
 .
 .
0.75 0.75 0.50
0.75 0.75 0.75
end kpoints
```

10.2   seedname.nnkp

Running `wannier90` on the above input file would generate the following `nnkp` file:

```
File written on  9Feb2006 at 15:13: 9

calc_only_A   :   F

begin real_lattice
  -1.612340    0.000000    1.612340
   0.000000    1.612340    1.612340
  -1.612340    1.612340    0.000000
end real_lattice

begin recip_lattice
  -1.951300   -1.951300    1.951300
   1.951300    1.951300    1.951300
  -1.951300    1.951300   -1.951300
end recip_lattice

begin kpoints
     64
  0.00000    0.00000    0.00000
  0.00000    0.25000    0.00000
  0.00000    0.50000    0.00000
  0.00000    0.75000    0.00000
  0.25000    0.00000    0.00000
   .
   .
   .
  0.50000    0.75000    0.75000
  0.75000    0.00000    0.75000
  0.75000    0.25000    0.75000
  0.75000    0.50000    0.75000
  0.75000    0.75000    0.75000
end kpoints
```

```
begin projections
   8
  -0.12500    -0.12500    -0.12500      0  1  1
     0.000  0.000  1.000    1.000  0.000  0.000    2.00
  -0.12500    -0.12500    -0.12500      1  1  1
     0.000  0.000  1.000    1.000  0.000  0.000    2.00
  -0.12500    -0.12500    -0.12500      1  2  1
     0.000  0.000  1.000    1.000  0.000  0.000    2.00
  -0.12500    -0.12500    -0.12500      1  3  1
     0.000  0.000  1.000    1.000  0.000  0.000    2.00
   0.12500     0.12500     0.12500      0  1  1
     0.000  0.000  1.000    1.000  0.000  0.000    2.00
   0.12500     0.12500     0.12500      1  1  1
     0.000  0.000  1.000    1.000  0.000  0.000    2.00
   0.12500     0.12500     0.12500      1  2  1
     0.000  0.000  1.000    1.000  0.000  0.000    2.00
   0.12500     0.12500     0.12500      1  3  1
     0.000  0.000  1.000    1.000  0.000  0.000    2.00
end projections

begin nnkpts
    8
   1     2      0   0   0
   1     4      0  -1   0
   1     5      0   0   0
   1    13     -1   0   0
   1    17      0   0   0
   1    22      0   0   0
   1    49      0   0  -1
   1    64     -1  -1  -1
   2     1      0   0   0
   2     3      0   0   0
   2     6      0   0   0
   2    14     -1   0   0
   2    18      0   0   0
   2    23      0   0   0
   2    50      0   0  -1
   2    61     -1   0  -1
   .
   .
   .
  64     1      1   1   1
  64    16      0   0   1
  64    43      0   0   0
  64    48      0   0   0
  64    52      1   0   0
  64    60      0   0   0
  64    61      0   1   0
  64    63      0   0   0
```

```
end nnkpts

begin exclude_bands
    4
    1
    2
    3
    4
end exclude_bands
```

Part III

postw90.x

Chapter 11

Parameters

11.1 Introduction

The `wannier90.x` code described in Part II calculates the maximally-localized Wannier functions.

The `postw90.x` executable contains instead a series of modules that take the Wannier functions calculated by `wannier90.x` and use them to calculate different properties. This executable is parallel (by means of MPI libraries), so it can be run on multiple CPUs. The information on the calculated Wannier functions is read from the checkpoint `seedname.chk` file. Note that this is written in an unformatted machine-dependent format. If you need to use this file on a different machine, or you want to use a version of `postw90.x` compiled with a different compiler, refer to Sec. A.2 in the Appendices for a description of how to export/import this file.

11.2 Usage

`postw90.x` can be run in parallel using MPI libraries to reduce the computation time.

For serial execution use: `postw90.x [seedname]`

- `seedname`: If a seedname string is given the code will read its input from a file `seedname.win`. The default value is `wannier`. One can also equivalently provide the string `seedname.win` instead of `seedname`.

For parallel execution use: `mpirun -np NUMPROCS postw90.x [seedname]`

- `NUMPROCS`: substitute with the number of processors that you want to use.

Note that the `mpirun` command and command-line flags may be different in your MPI implementation: read your MPI manual or ask your computer administrator.

Note also that this requires that the `postw90.x` executable has been compiled in its parallel version (follow the instructions in the file `README.install` in the main directory of the wannier90 distribution) and that the MPI libraries and binaries are installed and correctly configured on your machine.

11.3 `seedname.win` File

The `postw90.x` uses the same `seedname.win` input file of `wannier90.x`. The input keywords of `postw90.x` must thus be added to this file, using the same syntax described in Sec. 2.2.

Note that `wannier90.x` checks if the syntax of the input file is correct, but then ignores the value of the flags that refer only to modules of `postw90.x`, so one can safely run `wannier90.x` on a file that contains also `postw90.x` flags.

Similarly, `postw90.x` ignores flags that refer only to `wannier90.x` (as number of iterations, restart flags, . . .). However, some parts of the input file must be there, as for instance the number of Wannier functions, etc.

The easiest thing to do is therefore to simply *add* the `postw90` input keywords to the `seedname.win` file that was used to obtain the Wannier functions.

11.4   List of available modules

The currently available modules in `postw90.x` are:

- `dos`: Calculation of the density of states (DOS), projected density of states (PDOS), net spin etc.

- `kpath`: Calculation of k-space quantities such as energy bands, Berry curvature and Berry curvature-like term of spin Hall conductivity along a piecewise linear path in the BZ (see examples 17, 18 and 29 of the tutorial).

- `kslice`: Calculation of k-space quantities on a planar slice of the BZ (see examples 17, 18 and 29 of the tutorial).

- `berry`: Calculation of properties related to the BZ integral of the Berry curvature, Berry connection and Berry curvature-like term of spin Hall conductivity, including anomalous Hall conductivity, orbital magnetisation, optical conductivity, nonlinear shift current and spin Hall conductivity (see Chap. 12 and examples 18, 19, 25, 29 and 30 of the tutorial). It also includes an option to compute $k \cdot p$ expansion coefficients (see Sec. 12.9 and example 33 of the tutorial).

- `gyrotropic`: Calculation of gyrotropic properties, including natural and current0induced optical rotation, and the current-induced magnetization (see Chap. 13 and examples of the tutorial).

- `BoltzWann`: Calculation of electronic transport properties for bulk materials using the semiclassical Boltzmann transport equation (see Chap. 14 and example 16 of the tutorial).

- `geninterp` (Generic Band Interpolation): Calculation band energies (and band derivatives) on a generic list of k points (see Chap. 15).

11.5   Keyword List

On the next pages the list of available `postw90` input keywords is reported. In particular, Table 11.1 reports keywords that affect the generic behavior of all modules of `postw90`. Often, these are "global"

variables that can be overridden by module-specific keywords (as for instance the `kmesh` flag). The subsequent tables describe the input parameters for each specific module.

A description of the behaviour of the global flags is described Sec. 11.6; the description of the flags specific to the modules can be found in the following sections.

Keyword	Type	Description
Global Parameters of `postw90`		
KMESH	I	Dimensions of the uniform interpolation k-mesh (one or three integers)
KMESH_SPACING	R	Minimum spacing between k points in Å^{-1}
ADPT_SMR	L	Use adaptive smearing
ADPT_SMR_FAC	R	Adaptive smearing prefactor
ADPT_SMR_MAX	P	Maximum allowed value for the adaptive energy smearing (eV)
SMR_TYPE	S	Analytical form used for the broadened delta function
SMR_FIXED_EN_WIDTH	P	Energy smearing (if non-adaptive)
NUM_ELEC_PER_STATE	I	Number of electrons per state
SCISSORS_SHIFT	P	Scissors shift applied to the conduction bands (eV) (deprecated)
NUM_VALENCE_BANDS	I	Number of valence bands
SPIN_DECOMP	L	Decompose various properties into up-spin, down-spin, and possibly spin-flip parts
SPIN_AXIS_POLAR	P	Polar angle of the spin quantization axis (deg)
SPIN_AXIS_AZIMUTH	P	Azimuthal angle of the spin quantization axis (deg)
SPIN_MOMENT*	L	Determines whether to evaluate the spin magnetic moment per cell
uHu_FORMATTED	L	Read a formatted `seedname.uHu` file
SPN_FORMATTED	L	Read a formatted `seedname.spn` file
BERRY_CURV_UNIT	S	Unit of Berry curvature

Table 11.1: `seedname.win` file keywords controlling the general behaviour of the modules in `postw90`. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

The keyword `spin_moment` does not affect the behavior of the modules in `postw90`, and does not really belong to any of them. It is listed here for lack of a better place.

Keyword	Type	Description
`berry` Parameters		
BERRY	L	Calculate Berry-type quantities
BERRY_TASK	S	List of properties to compute
[BERRY_]KMESH	I	Dimensions of the uniform interpolation k-mesh (one or three integers)
[BERRY_]KMESH_SPACING	R	Minimum spacing between k points in Å^{-1}
BERRY_CURV_ADPT_KMESH	I	Linear dimension of the adaptively refined k-mesh used to compute the anomalous/spin Hall conductivity

BERRY_CURV_ADPT_KMESH_THRESH	P	Threshold magnitude of the Berry curvature for adaptive refinement
KUBO_FREQ_MIN	P	Lower limit of the frequency range for optical spectra, JDOS, shift current and spin Hall conductivity (eV)
KUBO_FREQ_MAX	P	Upper limit of the frequency range for optical spectra, JDOS, shift current and spin Hall conductivity (eV)
KUBO_FREQ_STEP	R	Step for increasing the optical frequency in the specified range
KUBO_EIGVAL_MAX	P	Maximum energy eigenvalue included when evaluating the Kubo-Greenwood conductivity, JDOS, shift current and spin Hall conductivity
[KUBO_]ADPT_SMR	L	Use adaptive energy smearing for the optical conductivity, JDOS, shift current and spin Hall conductivity
[KUBO_]ADPT_SMR_FAC	R	Adaptive smearing prefactor
[KUBO_]ADPT_SMR_MAX	P	Maximum allowed value for the adaptive energy smearing (eV)
[KUBO_]SMR_TYPE	S	Analytical form used for the broadened delta function when computing the optical conductivity, JDOS, shift current and spin Hall conductivity
[KUBO_]SMR_FIXED_EN_WIDTH	P	Energy smearing (if non-adaptive) for the optical conductivity, JDOS, shift current and spin Hall conductivity (eV)
SC_ETA	R	Energy broadening of energy differences in the sum over virtual states when computing shift current
SC_PHASE_CONV	I	Convention for phase factor of Bloch states when computing shift current
SC_W_THR	R	Frequency threshold for speeding up delta function integration when computing shift current
SC_USE_ETA_CORR	L	Use finite-eta correction for computing shift current
SHC_FREQ_SCAN	L	Calculate Fermi energy scan or frequency scan of spin Hall conductivity
SHC_METHOD	S	How to obtain the spin current matrix elements for SHC
SHC_ALPHA	I	The spin current direction of spin Hall conductivity
SHC_BETA	I	The direction of applied electrical field of spin Hall conductivity

SHC_GAMMA	I	The spin direction of the spin current of spin Hall conductivity
SHC_BANDSHIFT	L	Rigid bandshift of the conduction bands
SHC_BANDSHIFT_FIRSTBAND	I	Index of the first band to shift
SHC_BANDSHIFT_ENERGYSHIFT	P	Energy shift of the conduction bands (eV)
KDOTP_KPOINT	R	k point for $k \cdot p$ expansion ($2\pi/a$, with a lattice constant in Å)
KDOTP_NUM_BANDS	I	Number of bands for $k \cdot p$ expansion
KDOTP_BANDS	I	Band indexes corresponding to the $k \cdot p$ bands

Table 11.5: `seedname.win` file keywords controlling the `berry` module. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

Keyword	Type	Description
dos Parameters		
DOS	L	Calculate the density of states and related properties
DOS_TASK	S	List of properties to compute
DOS_ENERGY_MIN	P	Lower limit of the energy range for computing the DOS (eV)
DOS_ENERGY_MAX	P	Upper limit of the energy range for computing the DOS (eV)
DOS_ENERGY_STEP	R	Step for increasing the energy in the specified range (eV)
DOS_PROJECT	I	List of WFs onto which the DOS is projected
[DOS_]KMESH	I	Dimensions of the uniform interpolation k-mesh (one or three integers)
[DOS_]KMESH_SPACING	R	Minimum spacing between k points in Å^{-1}
[DOS_]ADPT_SMR	L	Use adaptive smearing for the DOS
[DOS_]ADPT_SMR_FAC	R	Adaptive smearing prefactor
[DOS_]ADPT_SMR_MAX	P	Maximum allowed value for the adaptive energy smearing (eV)
[DOS_]SMR_FIXED_EN_WIDTH	P	Energy smearing (if non-adaptive) for the DOS (eV)
[DOS_]SMR_TYPE	S	Analytical form used for the broadened delta function when computing the DOS.

Table 11.2: `seedname.win` file keywords controlling the `dos` module. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

Keyword	Type	Description
kpath Parameters		
KPATH	L	Calculate properties along a piecewise linear path in the BZ
KPATH_TASK	L	List of properties to evaluate
KPATH_NUM_POINTS	I	Number of points in the first kpath segment
KPATH_BANDS_COLOUR	S	Property used to colour the energy bands along the path

Table 11.3: `seedname.win` file keywords controlling the `kpath` module. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

Keyword	Type	Description
kslice Parameters		
KSLICE	L	Calculate properties on a slice in the BZ
KSLICE_TASK	S	List of properties to evaluate
KSLICE_CORNER	R	Position of the corner of the slice
KSLICE_B1	R	First vector defining the slice
KSLICE_B2	R	Second vector defining the slice
KSLICE_2DKMESH	I	Dimensions of the uniform interpolation k-mesh on the slice (one or two integers)
KSLICE_FERMI_LEVEL	P	This parameter is not used anymore. Use FERMI_ENERGY instead.
KSLICE_FERMI_LINES_COLOUR	S	Property used to colour the Fermi lines

Table 11.4: `seedname.win` file keywords controlling the `kslice` module. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

Keyword	Type	Description
berry Parameters		
GYROTROPIC	L	Calculate gyrotropic quantities
GYROTROPIC_TASK	L	List of properties to compute
[GYROTROPIC_]KMESH	I	Dimensions of the uniform interpolation k-mesh (one or three integers)
[GYROTROPIC_]KMESH_SPACING	R	Minimum spacing between k points in Å^{-1}
GYROTROPIC_FREQ_MIN	P	Lower limit of the frequency range for optical rotation (eV)
GYROTROPIC_FREQ_MAX	P	Upper limit of the frequency range for optical rotation (eV)
GYROTROPIC_FREQ_STEP	P	Step for increasing the optical frequency in the specified range
GYROTROPIC_EIGVAL_MAX	P	Maximum energy eigenvalue included when evaluating the interband natural optical activity
GYROTROPIC_DEGEN_THRESH	P	threshold to exclude degenerate bands from the calculation
[GYROTROPIC_]SMR_TYPE	S	Analytical form used for the broadened delta function
[GYROTROPIC_]SMR_FIXED_EN_WIDTH	P	Energy smearing (eV)
[GYROTROPIC_]BAND_LIST	I	list of bands used in the calculation
GYROTROPIC_BOX_CENTER	R	The center and three basis vectors,
GYROTROPIC_BOX_B1	R	defining the box for integration (in
GYROTROPIC_BOX_B2	R	reduced coordinates, three real
GYROTROPIC_BOX_B3	R	numbers for each vector)

Table 11.6: `seedname.win` file keywords controlling the `gyrotropic` module. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

Keyword	Type	Description
BoltzWann Parameters		
BOLTZWANN	L	Calculate Boltzmann transport coefficients
[BOLTZ_]KMESH	I	Dimensions of the uniform interpolation k-mesh (one or three integers)
[BOLTZ_]KMESH_SPACING	R	Minimum spacing between k points in Å^{-1}
BOLTZ_2D_DIR	S	Non-periodic direction (for 2D systems only)
BOLTZ_RELAX_TIME	P	Relaxation time in fs
BOLTZ_MU_MIN	P	Minimum value of the chemical potential μ in eV
BOLTZ_MU_MAX	P	Maximum value of the chemical potential μ in eV
BOLTZ_MU_STEP	R	Step for μ in eV
BOLTZ_TEMP_MIN	P	Minimum value of the temperature T in Kelvin
BOLTZ_TEMP_MAX	P	Maximum value of the temperature T in Kelvin
BOLTZ_TEMP_STEP	R	Step for T in Kelvin
BOLTZ_TDF_ENERGY_STEP	R	Energy step for the TDF (eV)
BOLTZ_TDF_SMR_FIXED_EN_WIDTH	P	Energy smearing for the TDF (eV)
BOLTZ_TDF_SMR_TYPE	S	Smearing type for the TDF
BOLTZ_CALC_ALSO_DOS	L	Calculate also DOS while calculating the TDF
BOLTZ_DOS_ENERGY_MIN	P	Minimum value of the energy for the DOS in eV
BOLTZ_DOS_ENERGY_MAX	P	Maximum value of the energy for the DOS in eV
BOLTZ_DOS_ENERGY_STEP	R	Step for the DOS in eV
[BOLTZ_DOS_]SMR_TYPE	S	Smearing type for the DOS
[BOLTZ_DOS_]ADPT_SMR	L	Use adaptive smearing for the DOS
[BOLTZ_DOS_]ADPT_SMR_FAC	R	Adaptive smearing prefactor
[BOLTZ_DOS_]ADPT_SMR_MAX	P	Maximum allowed value for the adaptive energy smearing (eV)
[BOLTZ_DOS_SMR_]FIXED_EN_WIDTH	P	Energy smearing (if non-adaptive) for the DOS (eV)
BOLTZ_BANDSHIFT	L	Rigid bandshift of the conduction bands
BOLTZ_BANDSHIFT_FIRSTBAND	I	Index of the first band to shift
BOLTZ_BANDSHIFT_ENERGYSHIFT	P	Energy shift of the conduction bands (eV)

Table 11.7: `seedname.win` file keywords controlling the `BoltzWann` module (calculation of the Boltzmann transport coefficients in the Wannier basis). Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

Keyword	Type	Description
geninterp Parameters		
GENINTERP	L	Calculate bands for given set of k points
GENINTERP_ALSOFIRSTDER	L	Calculate also first derivatives
GENINTERP_SINGLE_FILE	L	Write a single file or one for each process

Table 11.8: `seedname.win` file keywords controlling the Generic Band Interpolation (`geninterp`) module. Argument types are represented by, I for a integer, R for a real number, P for a physical value, L for a logical value and S for a text string.

11.6 Global variables

11.6.1 integer :: kmesh(:)

Dimensions of the interpolation grid used in `postw90.x`.

Not to be confused with the `mp_grid` *input flag, which instead specifies the Monkhorst–Pack grid used in the ab-initio calculation!*

If three integers $l\ m\ n$ are given, the reciprocal-space cell subtended by the three primitive translations is sampled on a uniform $l \times m \times n$ grid (including Γ). If only one integer m is given, an $m \times m \times m$ grid is used.

If you use a module which needs a k-mesh, either `kmesh_spacing` or `kmesh` must be defined.

11.6.2 real(kind=dp) :: kmesh_spacing

An alternative way of specifying the interpolation grid. This flag defines the minimum distance for neighboring k points along each of the three directions in k space.

The units are Å^{-1}.

If you use a module which needs a k-mesh, either `kmesh_spacing` or `kmesh` must be defined.

11.6.3 logical :: adpt_smr

Determines whether to use an adaptive scheme for broadening the DOS and similar quantities defined on the energy axis. If `true`, the values for the smearing widths are controlled by the flag `adpt_smr_fac`.

The default value is `true`.

11.6.4 real(kind=dp) :: adpt_smr_fac

The width $\eta_{n\mathbf{k}}$ of the broadened delta function used to determine the contribution to the spectral property (DOS, ...) from band n at point $\mathbf{k}$ is calculated as

$$\eta_{n\mathbf{k}} = \alpha |\nabla_{\mathbf{k}} \varepsilon_{n\mathbf{k}}| \Delta k,$$

where $\varepsilon_{n\mathbf{k}}$ is the energy eigenvalue and the dimensionless factor α is given by `adpt_smr_fac`. Δk is taken to be the largest of the mesh spacings along the three reciprocal lattice vectors $\mathbf{b_1}$, $\mathbf{b_2}$, and $\mathbf{b_3}$. If the calculated value of $\eta_{n\mathbf{k}}$ exceeds `adpt_smr_max`, the latter value is used.

The default value is $\sqrt{2}$.

11.6.5 real(kind=dp) :: adpt_smr_max

See description given immediately above.

The units are eV. The default value is 1.0.

11.6.6   character(len=120) ::   smr_type

Defines the analytical form used for the broadened delta function in the computation of the DOS and similar quantities defined on the energy axis.

- gauss: Gaussian smearing

- m-pN: derivative of the N-th order Methfessel-Paxton function ($N \geq 0$). Example: m-p2 for the second-order Methfessel-Paxton function. If only m-p is provided, the first-order function is used, i.e., it is equivalent to m-p1.

- m-v or cold: derivative of the Marzari–Vanderbilt cold-smearing function

- f-d: derivative of the Fermi-Dirac distribution function

The default value is gauss.

11.6.7   logical ::   smr_fixed_en_width

Energy width for the smearing function for the DOS. Used only if adpt_smr is false.

The units are eV. The default value is 0 eV. Note that if the width is smaller than twice the energy step (e.g. dos_energy_step for the dos module), the DOS will be unsmeared (thus the default is to have an unsmeared properties when adpt_smr is set to false.).

11.6.8   integer ::   num_elec_per_state

Number of electrons per state. It can only take the values one or two.

The default value is 1 if spinors=true, 2 otherwise.

11.6.9   real(kind=dp) ::   scissors_shift

Scissors shift applied to the conduction bands.

Note! This variable is deprecated and will be removed in future versions of the code. This applies the scissors shift only to the Hamiltonian, but also other matrices might need to be updated if a scissors shift is applied. If you are using BoltzWann, consider using boltz_bandshift instead. If you are calculating spin Hall conductivity, consider using shc_bandshift instead.

The units are eV. The default value is 0 eV (i.e., no scissors shift applied).

11.6.10   integer ::   num_valence_bands

Number of valence bands of the system. Used in different modules and for the scissors shift.

No default value.

11.6.11 logical :: spin_decomp

If `true`, extra columns are added to some output files (such as `seedname-dos.dat` for the `dos` module, and analogously for the `berry` and `BoltzWann` modules).

For the `dos` and `BoltzWann` modules, two further columns are generated, which contain the decomposition of the required property (e.g., total or orbital-projected DOS) of a spinor calculation into up-spin and down-spin parts (relative to the quantization axis defined by the input variables `spin_axis_polar` and `spin_axis_azimuth`). For the `berry` module with `berry_task = kubo`, three extra columns are added to `seedname-jdos.dat`, containing the decomposition of the JDOS into up $\to$ up, down $\to$ down, and spin-flip transitions. In the same way, six extra columns are added to the data files `seedname-kubo*.dat` where the complex optical conductivity is stored.

The file `seedname.spn` must be present at input. Furthermore, if this variable is set to `true` it requires `num_elec_per_state = 1`.

The default value is `false`.

11.6.12 real(kind=dp) :: spin_axis_polar

Polar angle of the spin quantization axis.

The units are degrees. The default value is 0.

11.6.13 real(kind=dp) :: spin_axis_azimuth

Azimuthal angle of the spin quantization axis.

The units are degrees. The default value is 0.

11.6.14 logical :: spin_moment

Determines whether to evaluate the spin moment.

The default value is `false`.

11.6.15 logical :: uHu_formatted

If `uHu_formatted=true`, then the uHu matrix elements will be read from disk as formatted (ie ASCII) files; otherwise they will be read as unformatted files.

The default value of this parameter is `false`.

11.6.16 logical :: spn_formatted

If `spn_formatted=true`, then the spin matrix elements will be read from disk as formatted (ie ASCII) files; otherwise they will be read as unformatted files. Unformatted is generally preferable as the files will take less disk space and I/O is significantly faster. However such files will not be transferable

between all machine architectures and formatted files should be used if transferability is required (i.e., for test cases).

The default value is `false`.

11.6.17 character(len=20) :: berry_curv_unit

Unit in which the Berry curvature is specified at input (in `berry_curv_adpt_kmesh_thresh`) or written to file (when `kpath_task=curv` or `kpath_task=shc` or `kslice_task=curv` or `kslice_task=shc`).

- `ang2`: Angstrom^2

- `bohr2`: Bohr^2 (atomic units)

The default value is `ang2`.

11.6.18 real(kind=dp) :: sc_eta

The width η used to broaden energy differences in denominators of the form

$$\frac{1}{\varepsilon_{n\mathbf{k}} - \varepsilon_{m\mathbf{k}}} \to \mathrm{Re}\frac{1}{\varepsilon_{n\mathbf{k}} - \varepsilon_{m\mathbf{k}} + i\eta}.$$

The above is needed in shift-current calculations in order to avoid numerical problems caused by near-degeneracies in the sum over virtual states.

The units are eV. The default value is 0.4.

11.6.19 integer :: sc_phase_conv

Convention for the expansion of the Bloch states in shift-current calculations. It can only take the values one or two. We follow the convention of Ref. [11]:

- 1: Include Wannier centre $\boldsymbol{\tau}_n = \langle w_{n\mathbf{0}}|\mathbf{r}|w_{n\mathbf{0}}\rangle$ in the phase factor (so-called tight-binding convention):
$$|u_{n\mathbf{k}}\rangle = \sum_{\mathbf{R}} e^{-i\mathbf{k}(\mathbf{r}-\mathbf{R}-\boldsymbol{\tau}_n)}|w_{n\mathbf{R}}\rangle$$

- 2: Do not include Wannier centre in the phase factor (usual `Wannier90` convention):
$$|u_{n\mathbf{k}}\rangle = \sum_{\mathbf{R}} e^{-i\mathbf{k}(\mathbf{r}-\mathbf{R})}|w_{n\mathbf{R}}\rangle$$

If `sc_use_eta_corr=true`, the convention does not affect the full shift-current matrix element, but it does affect the weights of the internal components that compose it (see Ref. [12]). If `sc_use_eta_corr=false`, the convention can affect the full shift-current matrix element (see Ref. [13]).

The default value is 1.

11.6.20 `real(kind=dp) :: sc_w_thr`

Parameter α_t for speeding up the frequency integration in shift-current calculations. It settles the frequency threshold $\omega_t = \alpha_t \eta_{n\mathbf{k}}$ (a factor times the broadening) beyond which the delta functions are taken as zero.

The default value is 5.0.

11.6.21 `logical :: sc_use_eta_corr`

If `sc_use_eta_corr=true`, apply the finite-eta correction of the shift current (Eq. (19) of Ref. [13]). Without the correction, the convention of the Bloch sum (determined by `sc_phase_conv`) can affect the computed shift-current spectra. See Ref. [13] for details.

The default value is `true`.

11.7   DOS

Note that the behavior of the `dos` module is also influenced by the value of some global flags (listed in Table 11.1), as `spin_decomp`, `spin_axis_polar`, `spin_axis_azimuth`, `scissors_shift`, etc. Some of the global flags can be possibly overridden by local flags of the DOS module, listed below, which have the same name of the global flag but are prefixed by `dos_`.

11.7.1   logical :: dos

Determines whether to enter the DOS routines.

The default value is `false`.

11.7.2   character(len=20) :: dos_task

The quantity to compute when `dos=true`

The valid options for this parameter are:

   – `dos_plot` Density of states. An output data file `seedname-dos.dat` is created, containing the energy values in eV in the first column, and the total DOS per unit cell and unit energy range (in eV^{-1}) in the second. Two additional columns are present if `spin_decomp=true`

The default value is `dos_plot`.

11.7.3   real(kind=dp) :: dos_energy_min

Lower limit of the energy range for computing the DOS. Units are eV.

The default value is the minimum value of the energy eigenvalues stored in `seedname.eig`, minus 0.6667.

11.7.4   real(kind=dp) :: dos_energy_max

Upper limit of the energy range for computing the DOS. Units are eV.

If an inner energy window was specified, the default value is the upper bound of the innter energy window, plus 0.6667. Otherwise it is the maximum value of the energy eigenvalues stored in `seedname.eig`, plus 0.6667.

11.7.5   real(kind=dp) :: dos_energy_step

Energy step for the grid of energies used to plot the dos. Units are eV.

The default value is 0.01 eV.

11.7.6 integer :: dos_project(:)

If present **postw90** computes, instead of the total DOS, the partial DOS projected onto the WFs listed. The WFs are numbered according to the file **seedname.wout**.

For example, to project onto WFs 2, 6, 7, 8, and 12:

`dos_project :  2, 6-8, 12`

The DOS projected onto a set $\mathcal{S}$ of orbitals is calculated as

$$\rho_{\mathcal{S}}(E) = \frac{1}{N_k} \sum_{\mathbf{k}} \sum_{n} \langle \psi_{n\mathbf{k}}^{(\mathrm{H})} | \hat{P}_{\mathbf{k}}(\mathcal{S}) | \psi_{n\mathbf{k}}^{(\mathrm{H})} \rangle \delta(\varepsilon_{n\mathbf{k}} - E) \tag{11.1}$$

$$\hat{P}_{\mathbf{k}}(\mathcal{S}) = \sum_{m \in \mathcal{S}} | \psi_{n\mathbf{k}}^{(\mathrm{W})} \rangle \langle \psi_{n\mathbf{k}}^{(\mathrm{W})} |, \tag{11.2}$$

where N_k is the number of mesh points used to sample the BZ, and the superscript (H) and (W) refer to *Hamiltonian gauge* and *Wannier gauge* [14].

11.7.7 integer :: dos_kmesh(:)

Overrides the **kmesh** global variable (see Sec. 11.6).

11.7.8 real(kind=dp) :: dos_kmesh_spacing

Overrides the **kmesh_spacing** global variable (see Sec. 11.6).

11.7.9 logical :: dos_adpt_smr

Overrides the **adpt_smr** global variable (see Sec. 11.6).

11.7.10 real(kind=dp) :: dos_adpt_smr_fac

Overrides the **adpt_smr_fac** global variable (see Sec. 11.6).

11.7.11 real(kind=dp) :: dos_adpt_smr_max

Overrides the **adpt_smr_max** global variable (see Sec. 11.6).

11.7.12 logical :: dos_smr_fixed_en_width

Overrides the **smr_fixed_en_width** global variable (see Sec. 11.6).

Note that if the width is smaller than twice the energy step **dos_energy_step**, the DOS will be unsmeared (thus the default is to have an unsmeared DOS).

11.7.13 `character(len=20) :: dos_smr_type`

Overrides the `smr_type` global variable (see Sec. 11.6).

11.8 kpath

11.8.1 `logical :: kpath`

Determines whether to enter the kpath routines.

The default value is `false`.

11.8.2 `character(len=20) :: kpath_task`

The quantities to plot when `kpath=true`

The valid options for this parameter are:

- **bands** Energy bands, in eV. The following files are created:
  - · `seedname-bands.dat` (data file)
  - · `seedname-bands.gnu` (`gnuplot` script)
  - · `seedname-bands.py` (`python` script)
  - · `seedname-path.kpt` (list of k-points along the path, written in the `pwscf` format)

- **curv** Minus the Berry curvature given by Eq. (12.18) of Ch. 12, in units of `berry_curv_unit`. The following files are created:
  - · `seedname-curv.dat` (data file)
  - · `seedname-curv_{x,y,z}.gnu` (`gnuplot` scripts)
  - · `seedname-curv_{x,y,z}.py` (`python` scripts)

- **morb** The integrand of the k-space orbital magnetization formula [Eq. (12.20) of Ch. 12] in eV·Å². Four output files are created:
  - · `seedname-morb.dat` (data file)
  - · `seedname-morb_{x,y,z}.gnu` (`gnuplot` scripts)
  - · `seedname-morb_{x,y,z}.py` (`python` scripts)

- **shc** The band-projected Berry curvature-like term of spin Hall conductivity given by Eq. (12.23) of Ch. 12, in units of `berry_curv_unit`. The following files are created:
  - · `seedname-shc.dat` (data file)
  - · `seedname-shc.gnu` (`gnuplot` scripts)
  - · `seedname-shc.py` (`python` scripts)

- Any combination of the above. The following combinations are of special interest

  `kpath_task = bands+curv`

  `kpath_task = bands+morb`

  `kpath_task = bands+shc`

  They generate the following files:

- seedname-bands.dat (data file)

- seedname-{curv,morb,shc}.dat (data file)

- seedname-bands+{curv,morb}_{x,y,z}.py or seedname-bands+shc.py (python scripts)

Two-panel figures are produced, with the energy bands within ± 0.65 eV of the Fermi level in the top panel, and the Berry curvature (or k-space orbital magnetization, or k-resolved Berry curvature-like term of spin Hall conductivity) in the bottom panel.

The default value is bands.

11.8.3 integer :: kpath_num_points

If kpath = true, then the number of points along the first section of the bandstructure plot given by kpoint_path. Other sections will have the same density of k-points.

The default value is 100.

11.8.4 character(len=20) :: kpath_bands_colour

When kpath_task=bands, colour code the energy bands according to the specified quantity.

The valid options for this parameter are:

- spin Spin projection (in units of $\hbar/2$) along the quantization axis defined by the variables spin_axis_polar and spin_axis_azimuth, for a spinor calculation

- shc Band-projected Berry curvature-like term of spin Hall conductivity (in units of berry_curv_unit) defined by the variables shc_alpha, shc_beta and shc_gamma, for a spinor calculation

- none no colour coding

The default value is none.

11.9   kslice

11.9.1   `logical :: kslice`

Determines whether to enter the kslice routines.

The default value is `false`.

11.9.2   `character(len=20) :: kslice_task`

The quantity to plot when `kslice=true`

The valid options for this parameter are:

- `fermi_lines` Lines of intersection between constant-energy surfaces and the slice. The energy level is specified by the keyword `fermi_energy`. Output files:

  - `seedname-kslice-fermi-spn.dat` (data file when `kslice_fermi_lines_colour = spin`)
  - `seedname-bnd_n.dat` (gnuplot data files when `kslice_fermi_lines_colour = none`)
  - `seedname-kslice-coord.dat` (python data files when `kslice_fermi_lines_colour = none`)
  - `seedname-kslice-bands.dat` (python data file when `kslice_fermi_lines_colour = none`)
  - `seedname-kslice-fermi_lines.gnu` (gnuplot script)
  - `seedname-kslice-fermi_lines.py` (python script)

- `curv[+fermi_lines]` Heatmap of the Berry curvature of the occupied states [together with the constant-energy contours]. The unit of Berry curvature is `berry_curv_unit`.
  Output files:

  - `seedname-kslice-coord.dat` (data files)
  - `seedname-kslice-curv.dat` (data file)
  - `[seedname-kslice-bands.dat]` (data file)
  - `seedname-kslice-curv_{x,y,z}[+fermi_lines].py` (python scripts)

- `morb[+fermi_lines]` Heatmap of the k-space orbital magnetization in eV·Å^2 [together with the constant-energy contours]. Output files:

  - `seedname-kslice-coord.dat` (data files)
  - `seedname-kslice-morb.dat` (data file)
  - `[seedname-kslice-bands.dat]` (data file)
  - `seedname-kslice-morb_{x,y,z}[+fermi_lines].py` (python scripts)

- `shc[+fermi_lines]` Heatmap of the Berry curvature-like term of the occupied states [together with the constant-energy contours]. The unit of Berry curvature-like term is `berry_curv_unit`.
  Output files:

  - `seedname-kslice-coord.dat` (data files)

· `seedname-kslice-shc.dat` (data file)

· [`seedname-kslice-bands.dat`] (data file)

· `seedname-kslice-shc[+fermi_lines].py` (python scripts)

The default value is `fermi_lines`.

Note: When `kslice_fermi_lines_colour = none` the `gnuplot` scripts draw the k-slices with a square shape, even when `kslice_b1` and `kslice_b2` below are not at right angles, or do not have equal lengths. (The `python` scripts draw the slices with the correct parallelogram shape.)

11.9.3 `real(kind=dp) :: kslice_corner(3)`

Reduced coordinates of the lower-left corner of the slice in k-space.

The default value is $(0.0, 0.0, 0.0)$

11.9.4 `real(kind=dp) :: kslice_b1(3)`

Reduced coordinates of the first reciprocal-space vector defining the slice.

The default value is $(1.0, 0.0, 0.0)$.

11.9.5 `real(kind=dp) :: kslice_b2(3)`

Reduced coordinates of the second reciprocal-space vector defining the slice.

The default value is $(0.0, 1.0, 0.0)$.

11.9.6 `integer :: kslice_2dkmesh(2)`

Dimensions of the k-point grid covering the slice. If two integers m n are given, the slice is sampled on a uniform $m \times n$ grid. If only one integer m is given, an $m \times m$ grid is used.

The default value for `kslice_kmesh` is 50.

11.9.7 `character(len=20) :: kslice_fermi_lines_colour`

When `kslice_task=fermi_lines` (but not when combined with `curv` or `morb`), colour code the Fermi lines according to the specified quantity.

The valid options for this parameter are:

– `spin` Spin projection (in units of $\hbar/2$) along the quantization axis defined by the variables `spin_axis_polar` and `spin_axis_azimuth`, for a spinor calculation

– `none` no colour coding

The default value is `none`.

11.10   berry

11.10.1   `logical ::  berry`

Determines whether to enter the berry routines.

The default value is `false`.

11.10.2   `character(len=120) ::  berry_task`

The quantity to compute when `berry=true`

The valid options for this parameter are:

- `kubo` Complex optical conductivity and joint density of states. Output files:

  - `seedname-kubo-S_{xx,yy,zz,xy,xz,yz}.dat` (data files). First column: optical frequency $\hbar\omega$ in eV. Second and third columns: real and imaginary parts of the symmetric conductivity $\sigma^{\mathrm{S}}_{\alpha\beta}(\hbar\omega) = \sigma^{\mathrm{S}}_{\beta\alpha}(\hbar\omega)$ in S/cm. Six additional columns are present if `spin_decomp = true`.
  - `seedname-kubo-A_{yz,zx,xy}.dat` (data files). First column: optical frequency $\hbar\omega$ in eV. Second and third columns: real and imaginary parts of the antisymmetric conductivity $\sigma^{\mathrm{A}}_{\alpha\beta}(\hbar\omega) = -\sigma^{\mathrm{A}}_{\beta\alpha}(\hbar\omega)$ in S/cm. Six additional columns are present if `spin_decomp = true`.
  - `seedname-jdos.dat` (data file). First column: energy difference $\hbar\omega$ in eV between conduction (c) and valence (v) states with the same crystal momentum **k**. Second column: joint density of states $\rho_{cv}(\hbar\omega)$ (number of states per unit cell per unit energy range, in eV^{-1}). Three additional columns are present if `spin_decomp = true`.

- `ahc` Anomalous Hall conductivity, in S/cm. The three independent components $\sigma_x = \sigma_{yz}$, $\sigma_y = \sigma_{zx}$, and $\sigma_z = \sigma_{xy}$ are computed. Output files:

  - `seedname-ahc-fermiscan.dat` (data file). The first column contains the Fermi level ε_F in eV, and the following three column the values of $\sigma_{x,y,z}(\varepsilon_F)$. This file is written if a range of Fermi energies is specified via `fermi_energy_min` and `fermi_energy_max`. If a single Fermi energy is given, the AHC is printed in `seedname.wpout` only.

- `morb` Orbital magnetisation, in bohr magnetons per cell.
  Output files:

  - `seedname-morb-fermiscan.dat` (data file). The first column contains the Fermi level ε_F in eV, and the following three column the values of $M^{\mathrm{orb}}_{x,y,z}(\varepsilon_F)$. This file is written if a range of Fermi energies is specified via `fermi_energy_min` and `fermi_energy_max`. If a single Fermi energy is given, $\mathbf{M}^{\mathrm{orb}}$ is printed in `seedname.wpout` only.

- `sc` Nonlinear shift current. Output files:

  - `seedname-sc_{xxx,xxy,xxz,...}.dat` (data files). The shift current is described by a $3\times3\times3$ tensor σ^{abc}. The program outputs a set of 18 files, and the 9 remaining components can be obtained by taking into account that σ^{abc} is symmetric under $b \leftrightarrow c$ index exchange. First column: optical frequency $\hbar\omega$ in eV. Second column: nonlinear shift current $\sigma^{abc}(\hbar\omega)$ in A/V^2.

– `shc` Spin Hall conductivity (SHC), in $(\hbar/e)$S/cm. Output files:

· `seedname-shc-fermiscan.dat` (data file). The first column is the number of entries in the list, the second column contains the Fermi level ε_F in eV, and the last column contains the values of $\sigma_{\alpha\beta}^{\mathrm{spin}\gamma}(\varepsilon_F)$. This file is written if a range of Fermi energies is specified via `fermi_energy_min` and `fermi_energy_max`. If a single Fermi energy is given, the file will contain SHC at this specific energy.

· `seedname-shc-freqscan.dat` (data file). The first column is the number of the entry in the list, the second column contains the frequency $\hbar\omega$ in eV, and the following two columns contain the values of the real part $\Re[\sigma_{\alpha\beta}^{\mathrm{spin}\gamma}(\omega)]$ and imaginary part $\Im[\sigma_{\alpha\beta}^{\mathrm{spin}\gamma}(\omega)]$ of ac SHC. This file is written if a range of frequencies is specified via `kubo_freq_min` and `kubo_freq_max`.

– `kdotp` $k \cdot p$ expansion coefficients. Output files:

· `seedname-kdotp_{0,1,2}.dat` (data files); respectively, the zeroth, first and second order $k \cdot p$ expansion coefficients, in units of eV, eV·Å, and eV·Å^2.

There is no default value.

11.10.3 `integer :: berry_kmesh(:)`

Overrides the `kmesh` global variable (see Sec. 11.6).

11.10.4 `real(kind=dp) :: berry_kmesh_spacing`

Overrides the `kmesh_spacing` global variable (see Sec. 11.6).

11.10.5 `integer :: berry_curv_adpt_kmesh`

If a positive integer n is given and `berry_task=ahc`[or `berry_task=shc`], an $n \times n \times n$ mesh is placed around points on the uniform mesh (defined by either `berry_kmesh` or `berry_kmesh_spacing`) where the magnitude of the k-space Berry curvature[k-space Berry curvature-like term of SHC] exceeds the threshold value specified in `berry_curv_adpt_kmesh_thresh`. This can be used to densify the BZ integration mesh around spikes in the Berry curvature[Berry curvature-like term of SHC].

The default value is 1.

11.10.6 `real(kind=dp) :: berry_curv_adpt_kmesh_thresh`

Magnitude of the Berry curvature[Berry curvature-like term of SHC] (in units of `berry_curv_unit`) that triggers adaptive mesh refinement when `berry_task=ahc`[`berry_task=shc`].

The default value is 100.0.

11.10.7   real(kind=dp) ::   kubo_freq_min

Lower limit of the frequency range for computing the optical conductivity, JDOS and ac SHC. Units are eV.

The default value 0.0.

11.10.8   real(kind=dp) ::   kubo_freq_max

Upper limit of the frequency range for computing the optical conductivity, JDOS and ac SHC. Units are eV.

If an inner energy window was specified, the default value is `dis_froz_max-fermi_energy`+0.6667. Otherwise it is the difference between the maximum and the minimum energy eigenvalue stored in `seedname.eig`, plus 0.6667.

11.10.9   real(kind=dp) ::   kubo_freq_step

Difference between consecutive values of the optical frequency between `kubo_freq_min` and `kubo_freq_max`. Units are eV.

The default value is 0.01.

11.10.10   real(kind=dp) ::   kubo_eigval_max

Maximum energy eigenvalue of the eigenstates to be included in the evaluation of the optical conductivity, JDOS and ac SHC. Units are eV.

If an inner energy window was specified, the default value is the upper bound of the inner energy window plus 0.6667. Otherwise it is the maximum energy eigenvalue stored in `seedname.eig` plus 0.6667.

11.10.11   logical ::   kubo_adpt_smr

Overrides the `adpt_smr` global variable (see Sec. 11.6).

11.10.12   real(kind=dp) ::   kubo_adpt_smr_fac

Overrides the `adpt_smr_fac` global variable (see Sec. 11.6).

11.10.13   real(kind=dp) ::   kubo_adpt_smr_max

Overrides the `adpt_smr_max` global variable (see Sec. 11.6).

11.10.14 logical :: kubo_smr_fixed_en_width

Overrides the `smr_fixed_en_width` global variable (see Sec. 11.6).

11.10.15 character(len=120) :: kubo_smr_type

Overrides the `smr_type` global variable (see Sec. 11.6).

11.10.16 logical :: shc_freq_scan

Determines whether to calculate the frequency scan (i.e. the ac SHC) or the Fermi energy scan (i.e. the dc SHC) of the spin Hall conductivity.

The default value is `false`, which means dc SHC is calculated.

11.10.17 character(len=120) :: shc_method

If it is `qiao/ryoo`, the ac or dc SHC is calculated using Junfeng Qiao's/Jihoon Ryoo's method. To calculate the Kubo formula, the spin current matrix elements are required, and the two methods differ in the degree of approximation. For details, see the section 12.5.

11.10.18 integer :: shc_alpha

The α index of spin Hall conductivity $\sigma^{\text{spin}\gamma}_{\alpha\beta}$, i.e. the direction of spin current. Possible values are 1, 2 and 3, representing the x, y and z directions respectively.

The default value is 1.

11.10.19 integer :: shc_beta

The β index of spin Hall conductivity $\sigma^{\text{spin}\gamma}_{\alpha\beta}$, i.e. the direction of applied electric field. Possible values are 1, 2 and 3, representing the x, y and z directions respectively.

The default value is 2.

11.10.20 integer :: shc_gamma

The γ index of spin Hall conductivity $\sigma^{\text{spin}\gamma}_{\alpha\beta}$, i.e. the spin direction of spin current. Possible values are 1, 2 and 3, representing the x, y and z directions respectively.

The default value is 3.

If all the `shc_alpha`, `shc_beta` and `shc_gamma` are set as default values, the $\sigma^{\text{spin}z}_{xy}$ is computed.

11.10.21 logical :: shc_bandshift

Shift all conduction bands by a given amount (defined by `shc_bandshift_energyshift`).

Note: this flag slightly differs from the global `scissors_shift` flag: with `shc_bandshift`, an exact rigid shift is applied *after* interpolation; `scissors_shift` applies instead the shift *before* interpolation. As a consequence, results may slightly differ (and this is why we provide both possibilities). Note also that with `scissors_shift` you have to provide the number of valence bands `num_valence_bands`, while with `shc_bandshift` you should provide the first band to shift `shc_bandshift_firstband` = `num_valence_bands`+1.

The default value is `false`.

11.10.22   integer ::   shc_bandshift_firstband

Index of the first conduction band to shift.

That means that all bands with index $i \geq$ `shc_bandshift_firstband` will be shifted by `shc_bandshift_energyshift`, if `shc_bandshift` is `true`.

The units are eV. No default value; if `shc_bandshift` is `true`, this flag must be provided.

11.10.23   real(kind=dp) ::   shc_bandshift_energyshift

Energy shift of the conduction bands.

The units are eV. No default value; if `shc_bandshift` is `true`, this flag must be provided.

11.10.24   real(kind=dp) ::   sc_eta

The width η used to broaden energy differences in denominators of the form

$$\frac{1}{\varepsilon_{n\mathbf{k}} - \varepsilon_{m\mathbf{k}}} \to \mathrm{Re}\frac{1}{\varepsilon_{n\mathbf{k}} - \varepsilon_{m\mathbf{k}} + i\eta}.$$

The above is needed in shift-current calculations in order to avoid numerical problems caused by near-degeneracies in the sum over virtual states.

The units are eV. The default value is 0.4.

11.10.25   integer ::   sc_phase_conv

Convention for the expansion of the Bloch states in shift-current calculations. It can only take the values one or two. We follow the convention of Ref. [11]:

- 1: Include Wannier centre $\boldsymbol{\tau}_n = \langle w_{n\mathbf{0}}|\mathbf{r}|w_{n\mathbf{0}}\rangle$ in the phase factor (so-called tight-binding convention):
$$|u_{n\mathbf{k}}\rangle = \sum_{\mathbf{R}} e^{-i\mathbf{k}(\mathbf{r}-\mathbf{R}-\boldsymbol{\tau}_n)}|w_{n\mathbf{R}}\rangle$$

- 2: Do not include Wannier centre in the phase factor (usual `Wannier90` convention):
$$|u_{n\mathbf{k}}\rangle = \sum_{\mathbf{R}} e^{-i\mathbf{k}(\mathbf{r}-\mathbf{R})}|w_{n\mathbf{R}}\rangle$$

The convention does not affect the full shift-current matrix element, but it does affect the weights of the internal components that compose it (see Ref. [12]).

The default value is 1.

11.10.26 real(kind=dp) :: sc_w_thr

Parameter α_t for speeding up the frequency integration in shift-current calculations. It settles the frequency threshold $\omega_t = \alpha_t \eta_{n\mathbf{k}}$ (a factor times the broadening) beyond which the delta functions are taken as zero.

The default value is 5.0.

11.10.27 real(kind=dp) :: kdotp_kpoint(3)

Defines the k point around which the $k \cdot p$ expansion is performed.

The default value is 0.0 0.0 0.0 (Γ).

11.10.28 integer :: kdotp_num_bands

Number of bands forming the $k \cdot p$ basis set.

No default value.

11.10.29 integer :: kdotp_bands(kdotp_num_bands)

Band indexes of bands belonging to $k \cdot p$ basis. Number of entries must be equal to the integer defined in kdotp_num_bands. The band labelling follows that of "wannierised" bands.

No default value.

11.11 Gyrotropic

11.11.1 `logical :: gyrotropic`

Determines whether to enter the gyrotropic routines.

The default value is `false`.

11.11.2 `character(len=120) :: gyrotropic_task`

The quantity to compute when `gyrotropic=true`

May contain one or more of the following valid options (note that each option starts with a '-'):

- `-D0` The Berry-curvature dipole tensor Eq. (13.1) (dimensionless)
  Output file: `seedname-gyrotropic-D.dat` (see Sec. 11.11.3 for file format description)

- `-Dw` The finite-frequency Berry-curvature dipole tensor Eq. (13.2) (dimensionless)
  Output file: `seedname-gyrotropic-tildeD.dat` (see Sec. 11.11.3 for file format description)

- `-C` The ohmic conductivity tensor Eq. (13.4) (Ampere/cm)
  Output file: `seedname-gyrotropic-C.dat` (see Sec. 11.11.3 for file format description)

- `-K` The orbital contribution to the kME tensor Eq. (13.5) (Ampere)
  Output file: `seedname-gyrotropic-K_orb.dat` (see Sec. 11.11.3 for file format description)

  - `-spin` : if this task is present, compute also the spin contribution.
    Output file: `seedname-gyrotropic-K_spin.dat`

- `-NOA` The orbital contribution to the NOA Eq. (13.5) (Å)
  Output file: `seedname-gyrotropic-NOA_orb.dat` (see Sec. 11.11.3 for file format description)

  - `-spin` : if this task is present, compute also the spin contribution.
    Output file: `seedname-gyrotropic-NOA_spin.dat`

- `-dos` the density of states Output file: `seedname-gyrotropic-DOS.dat`. First column - energy
  (eV), second column - DOS $(1/(\text{eV} \times \text{\AA}^3))$

There is no default value.

11.11.3 output data format

The calculated tensors are written as functions of Fermi level E_F (first column) and frequency ω (second column). If the tensor does not denend on ω, the second column is filled by zeros. Data is grouped in blocks of the same ω separated by two blank lines. In case of natural optical activity the columns 3 to 11 contain the independent components of γ_{abc} (antisymmetric in ab): yzx, zxy ,xyz, yzy, yzz, zxz, xyy, yzz and zxx. For tensors C_{ab}, D_{ab}, $\widetilde{D}_{ab}$, K_{ab} the symmetric and antisymmetric components are writted. Thus, the columns 3 to 11 are marked as xx, yy, zz, xy, xz, yz, x, y, z, wich correspond ,e.g., for D_{ab} to D_{xx}, D_{yy}, D_{zz}, $(D_{xy}+D_{yx})/2$, $(D_{xz}+D_{zx})/2$, $(D_{yz}+D_{zy})/2$, $(D_{yz}-D_{zy})/2$, $(D_{zx}-D_{xz})/2$, $(D_{xy}-D_{yx})/2$

11.11.4 integer :: gyrotropic_kmesh(:)

Overrides the kmesh global variable (see Sec. 11.6).

11.11.5 real(kind=dp) :: gyrotropic_kmesh_spacing

Overrides the kmesh_spacing global variable (see Sec. 11.6).

11.11.6 real(kind=dp) :: gyrotropic_freq_min

Lower limit of the frequency range for computing the optical activity.

Units are eV. The default value 0.0.

11.11.7 real(kind=dp) :: gyrotropic_freq_max

Upper limit of the frequency range for computing the optical activity. Units are eV.

If an inner energy window was specified, the default value is dis_froz_max-fermi_energy+0.6667. Otherwise it is the difference between the maximum and the minimum energy eigenvalue stored in seedname.eig, plus 0.6667.

11.11.8 real(kind=dp) :: gyrotropic_freq_step

Difference between consecutive values of the optical frequency between gyrotropic_freq_min and gyrotropic_freq_max.

Units are eV. The default value is 0.01.

11.11.9 real(kind=dp) :: gyrotropic_eigval_max

Maximum energy eigenvalue of the eigenstates to be included in the evaluation of the Natural optical activity. Units are eV.

If an inner energy window was specified, the default value is the upper bound of the inner energy window plus 0.6667. Otherwise it is the maximum energy eigenvalue stored in seedname.eig plus 0.6667.

11.11.10 logical :: gyrotropic_smr_fixed_en_width

Overrides the smr_fixed_en_width global variable (see Sec. 11.6).

11.11.11 character(len=120) :: gyrotropic_smr_type

Overrides the smr_type global variable (see Sec. 11.6).

11.11.12 `character(len=120) :: gyrotropic_degen_thresh`

The threshould to eliminate degenerate bands from the calculation in order to avoid divergences.

Units are eV. The dfault value is 0.

11.11.13 `character(len=120) :: gyrotropic_box_center`

- three real numbers. Optionally the integration may be restricted to a parallelogram, centered at `gyrotropic_box_center` and defined by vectors `gyrotropic_box_b{1,2,3}`

In reduced coordinates. Default value is 0.5 0.5 0.5

11.11.14 `character(len=120) :: gyrotropic_box_b1`

- three real numbers. In reduced coordinates. Default value is 1.0 0.0 0.0

11.11.15 `character(len=120) :: gyrotropic_box_b2`

- three real numbers. In reduced coordinates. Default value is 0.0 1.0 0.0

11.11.16 `character(len=120) :: gyrotropic_box_b3`

- three real numbers. In reduced coordinates. Default value is 0.0 0.0 1.0

11.12 BoltzWann

11.12.1 `logical ::  boltzwann`

Determines whether to enter the `BoltzWann` routines.

The default value is `false`.

11.12.2 `integer ::  boltz_kmesh(:)`

It determines the interpolation k mesh used to calculate the TDF (from which the transport coefficient are calculated). If `boltz_calc_also_dos` is `true`, the same k mesh is used also for the DOS. Overrides the `kmesh` global variable (see Sec. 11.6).

11.12.3 `real(kind=dp) ::  boltz_kmesh_spacing`

Overrides the `kmesh_spacing` global variable (see Sec. 11.6).

11.12.4 `character(len=4) ::  boltz_2d_dir`

For two-dimensional systems, the direction along which the system is non-periodic. It can assume the following values: `x` for a 2D system on the yz plane, `y` for a 2D system on the xz plane, `z` for a 2D system on the xy plane, or `no` for a 3D system with periodicity along all threee directions.

This value is used when calculating the Seebeck coefficient, where the electrical conductivity tensor needs to be inverted. If the value is different from zero, only the relevant 2×2 sub-block of the electrical conductivity is inverted.

The default value is `no`.

11.12.5 `real(kind=dp) ::  boltz_relax_time`

The relaxation time to be used for the calculation of the TDF and the transport coefficients.

The units are fs. The default value is 10 fs.

11.12.6 `real(kind=dp) ::  boltz_mu_min`

Minimum value for the chemical potential μ for which we want to calculate the transport coefficients.

The units are eV. No default value.

11.12.7 `real(kind=dp) ::  boltz_mu_max`

Maximum value for the chemical potential μ for which we want to calculate the transport coefficients.

The units are eV. No default value.

11.12.8 `real(kind=dp) :: boltz_mu_step`

Energy step for the grid of chemical potentials μ for which we want to calculate the transport coefficients.

The units are eV. No default value.

11.12.9 `real(kind=dp) :: boltz_temp_min`

Minimum value for the temperature T for which we want to calculate the transport coefficients.

The units are K. No default value.

11.12.10 `real(kind=dp) :: boltz_temp_max`

Maximum value for the temperature T for which we want to calculate the transport coefficients.

The units are K. No default value.

11.12.11 `real(kind=dp) :: boltz_temp_step`

Energy step for the grid of temperatures T for which we want to calculate the transport coefficients.

The units are K. No default value.

11.12.12 `real(kind=dp) :: boltz_tdf_energy_step`

Energy step for the grid of energies for the TDF.

The units are eV. The default value is 0.001 eV.

11.12.13 `character(len=120) :: boltz_tdf_smr_type`

The type of smearing function to be used for the TDF. The available strings are the same of the global `smr_type` input flag.

The default value is the one given via the `smr_type` input flag (if defined).

11.12.14 `real(kind=dp) :: boltz_tdf_smr_fixed_en_width`

Energy width for the smearing function. Note that for the TDF, a standard (non-adaptive) smearing scheme is used.

The units are eV. The default value is 0 eV. Note that if the width is smaller than twice the energy step `boltz_tdf_energy_step`, the TDF will be unsmeared (thus the default is to have an unsmeared TDF).

11.12.15 `logical :: boltz_calc_also_dos`

Whether to calculate also the DOS while calculating the TDF.

If one needs also the DOS, it is faster to calculate the DOS using this flag instead of using independently the routines of the `dos` module, since in this way the interpolation on the k points will be performed only once.

The default value is `false`.

11.12.16 `real(kind=dp) :: boltz_dos_energy_min`

The minimum value for the energy grid for the calculation of the DOS.

The units are eV. The default value is `minval(eigval)-0.6667`, where `minval(eigval)` i s the minimum eigenvalue returned by the ab-initio code on the ab-initio q me sh.

11.12.17 `real(kind=dp) :: boltz_dos_energy_max`

The maximum value for the energy grid for the calculation of the DOS.

The units are eV. The default value is `maxval(eigval)+0.6667`, where `maxval(eigval)` i s the maximum eigenvalue returned by the ab-initio code on the ab-initio q me sh.

11.12.18 `real(kind=dp) :: boltz_dos_energy_step`

Energy step for the grid of energies for the DOS.

The units are eV. The default value is 0.001 eV.

11.12.19 `character(len=120) :: boltz_dos_smr_type`

Overrides the `smr_type` global variable (see Sec. 11.6).

11.12.20 `logical :: boltz_dos_adpt_smr`

Overrides the `adpt_smr` global variable (see Sec. 11.6).

11.12.21 `real(kind=dp) :: boltz_dos_adpt_smr_fac`

Overrides the `adpt_smr_fac` global variable (see Sec. 11.6).

11.12.22 `real(kind=dp) :: boltz_dos_adpt_smr_max`

Overrides the `adpt_smr_max` global variable (see Sec. 11.6).

11.12.23   `logical :: boltz_dos_smr_fixed_en_width`

Overrides the `smr_fixed_en_width` global variable (see Sec. 11.6).

11.12.24   `logical :: boltz_bandshift`

Shift all conduction bands by a given amount (defined by `boltz_bandshift_energyshift`).

Note: this flag slightly differs from the global `scissors_shift` flag: with `boltz_bandshift`, an exact rigid shift is applied *after* interpolation; `scissors_shift` applies instead the shift *before* interpolation. As a consequence, results may slightly differ (and this is why we provide both possibilities). Note also that with `scissors_shift` you have to provide the number of valence bands `num_valence_bands`, while with `boltz_bandshift` you should provide the first band to shift `boltz_bandshift_firstband` = `num_valence_bands`+1.

The default value is `false`.

11.12.25   `integer :: boltz_bandshift_firstband`

Index of the first conduction band to shift.

That means that all bands with index $i \geq$ `boltz_bandshift_firstband` will be shifted by `boltz_bandshift_ener` if `boltz_bandshift` is `true`.

The units are eV. No default value; if `boltz_bandshift` is `true`, this flag must be provided.

11.12.26   `real(kind=dp) :: boltz_bandshift_energyshift`

Energy shift of the conduction bands.

The units are eV. No default value; if `boltz_bandshift` is `true`, this flag must be provided.

11.13   Generic Band Interpolation

11.13.1   `logical :: geninterp`

Determines whether to enter the Generic Band Interpolation routines.

The default value is `false`.

11.13.2   `logical :: geninterp_alsofirstder`

Whether to calculate also the first derivatives of the bands at the given k points.

The default value is `false`.

11.13.3 `logical :: geninterp_single_file`

Whether to write a single `seedname_geninterp.dat` file (all I/O is done by the root node); or instead multiple files (one for each node) with names `seedname_geninterp_NNNNN.dat`, where `NNNNN` is the node number. See also the discussion in Sec. 15.1.2 on how to use this flag.

The default value is `true`.

Chapter 12

Overview of the `berry` module

The `berry` module of `postw90` is called by setting `berry = true` and choosing one or more of the available options for `berry_task`. The routines in the `berry` module which compute the k-space Berry curvature, orbital magnetization and spin Hall conductivity are also called when `kpath = true` and `kpath_task = {curv,morb,shc}`, or when `kslice = true` and `kslice_task = {curv,morb,shc}`.

12.1   Background: Berry connection and curvature

The Berry connection is defined in terms of the cell-periodic Bloch states $|u_{n\mathbf{k}}\rangle = e^{-i\mathbf{k}\cdot\mathbf{r}}|\psi_{n\mathbf{k}}\rangle$ as

$$\mathbf{A}_n(\mathbf{k}) = \langle u_{n\mathbf{k}}|i\boldsymbol{\nabla}_{\mathbf{k}}|u_{n\mathbf{k}}\rangle, \tag{12.1}$$

and the Berry curvature is the curl of the connection,

$$\boldsymbol{\Omega}_n(\mathbf{k}) = \boldsymbol{\nabla}_{\mathbf{k}} \times \mathbf{A}_n(\mathbf{k}) = -\mathrm{Im}\langle\boldsymbol{\nabla}_{\mathbf{k}}u_{n\mathbf{k}}| \times |\boldsymbol{\nabla}_{\mathbf{k}}u_{n\mathbf{k}}\rangle. \tag{12.2}$$

These two quantities play a central role in the description of several electronic properties of crystals [15]. In the following we will work with a matrix generalization of the Berry connection,

$$\mathbf{A}_{nm}(\mathbf{k}) = \langle u_{n\mathbf{k}}|i\boldsymbol{\nabla}_{\mathbf{k}}|u_{m\mathbf{k}}\rangle = \mathbf{A}_{mn}^*(\mathbf{k}), \tag{12.3}$$

and write the curvature as an antisymmetric tensor,

$$\Omega_{n,\alpha\beta}(\mathbf{k}) = \epsilon_{\alpha\beta\gamma}\Omega_{n,\gamma}(\mathbf{k}) = -2\mathrm{Im}\langle\nabla_{k_\alpha}u_{n\mathbf{k}}|\nabla_{k_\beta}u_{n\mathbf{k}}\rangle. \tag{12.4}$$

12.2   `berry_task=kubo`: optical conductivity and joint density of states

The Kubo-Greenwood formula for the optical conductivity of a crystal in the independent-particle approximation reads

$$\sigma_{\alpha\beta}(\hbar\omega) = \frac{ie^2\hbar}{N_k\Omega_c}\sum_{\mathbf{k}}\sum_{n,m}\frac{f_{m\mathbf{k}} - f_{n\mathbf{k}}}{\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}}}\frac{\langle\psi_{n\mathbf{k}}|v_\alpha|\psi_{m\mathbf{k}}\rangle\langle\psi_{m\mathbf{k}}|v_\beta|\psi_{n\mathbf{k}}\rangle}{\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}} - (\hbar\omega + i\eta)}. \tag{12.5}$$

Indices α, β denote Cartesian directions, Ω_c is the cell volume, N_k is the number of k-points used for sampling the Brillouin zone, and $f_{n\mathbf{k}} = f(\varepsilon_{n\mathbf{k}})$ is the Fermi-Dirac distribution function. $\hbar\omega$ is the optical frequency, and $\eta > 0$ is an adjustable smearing parameter with units of energy.

The off-diagonal velocity matrix elements can be expressed in terms of the connection matrix [16],

$$\langle \psi_{n\mathbf{k}} | \mathbf{v} | \psi_{m\mathbf{k}} \rangle = -\frac{i}{\hbar} (\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}}) \mathbf{A}_{nm}(\mathbf{k}) \quad (m \neq n). \tag{12.6}$$

The conductivity becomes

$$\sigma_{\alpha\beta}(\hbar\omega) = \frac{1}{N_k} \sum_{\mathbf{k}} \sigma_{\mathbf{k},\alpha\beta}(\hbar\omega) \tag{12.7}$$

$$\sigma_{\mathbf{k},\alpha\beta}(\hbar\omega) = \frac{ie^2}{\hbar\Omega_c} \sum_{n,m} (f_{m\mathbf{k}} - f_{n\mathbf{k}}) \frac{\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}}}{\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}} - (\hbar\omega + i\eta)} A_{nm,\alpha}(\mathbf{k}) A_{mn,\beta}(\mathbf{k}). \tag{12.8}$$

Let us decompose it into Hermitian (dissipative) and anti-Hermitean (reactive) parts. Note that

$$\overline{\delta}(\varepsilon) = \frac{1}{\pi} \mathrm{Im} \left[\frac{1}{\varepsilon - i\eta} \right], \tag{12.9}$$

where $\overline{\delta}$ denotes a "broadended" delta-function. Using this identity we find for the Hermitean part

$$\sigma_{\mathbf{k},\alpha\beta}^{\mathrm{H}}(\hbar\omega) = -\frac{\pi e^2}{\hbar\Omega_c} \sum_{n,m} (f_{m\mathbf{k}} - f_{n\mathbf{k}})(\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}}) A_{nm,\alpha}(\mathbf{k}) A_{mn,\beta}(\mathbf{k}) \overline{\delta}(\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}} - \hbar\omega). \tag{12.10}$$

Improved numerical accuracy can be achieved by replacing the Lorentzian (12.9) with a Gaussian, or other shapes. The analytical form of $\overline{\delta}(\varepsilon)$ is controlled by the keyword `[kubo_]smr_type`.

The anti-Hermitean part of Eq. (12.8) is given by

$$\sigma_{\mathbf{k},\alpha\beta}^{\mathrm{AH}}(\hbar\omega) = \frac{ie^2}{\hbar\Omega_c} \sum_{n,m} (f_{m\mathbf{k}} - f_{n\mathbf{k}}) \mathrm{Re} \left[\frac{\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}}}{\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}} - (\hbar\omega + i\eta)} \right] A_{nm,\alpha}(\mathbf{k}) A_{mn,\beta}(\mathbf{k}). \tag{12.11}$$

Finally the joint density of states is

$$\rho_{cv}(\hbar\omega) = \frac{1}{N_k} \sum_{\mathbf{k}} \sum_{n,m} f_{n\mathbf{k}}(1 - f_{m\mathbf{k}}) \overline{\delta}(\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}} - \hbar\omega). \tag{12.12}$$

Equations (12.9–12.12) contain the parameter η, whose value can be chosen using the keyword `[kubo_]smr_fixed_en_width`. Better results can often be achieved by adjusting the value of η for each pair of states, i.e., $\eta \to \eta_{nm\mathbf{k}}$. This is done as follows (see description of the keyword `adpt_smr_fac`)

$$\eta_{nm\mathbf{k}} = \alpha |\nabla_{\mathbf{k}} (\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}})| \Delta k. \tag{12.13}$$

The energy eigenvalues $\varepsilon_{n\mathbf{k}}$, band velocities $\nabla_{\mathbf{k}} \varepsilon_{n\mathbf{k}}$, and off-diagonal Berry connection $\mathbf{A}_{nm}(\mathbf{k})$ entering the previous four equations are evaluated over a k-point grid by Wannier interpolation, as described in Refs. [14, 17]. After averaging over the Brillouin zone, the Hermitean and anti-Hermitean parts of the conductivity are assembled into the symmetric and antisymmetric tensors

$$\sigma_{\alpha\beta}^{\mathrm{S}} = \mathrm{Re}\sigma_{\alpha\beta}^{\mathrm{H}} + i\mathrm{Im}\sigma_{\alpha\beta}^{\mathrm{AH}} \tag{12.14}$$

$$\sigma_{\alpha\beta}^{\mathrm{A}} = \mathrm{Re}\sigma_{\alpha\beta}^{\mathrm{AH}} + i\mathrm{Im}\sigma_{\alpha\beta}^{\mathrm{H}}, \tag{12.15}$$

whose independent components are written as a function of frequency onto nine separate files.

12.3 `berry_task=ahc`: anomalous Hall conductivity

The antisymmetric tensor $\sigma_{\alpha\beta}^{A}$ is odd under time reversal, and therefore vanishes in non-magnetic systems, while in ferromagnets with spin-orbit coupling it is generally nonzero. The imaginary part $\text{Im}\sigma_{\alpha\beta}^{H}$ describes magnetic circular dichroism, and vanishes as $\omega \to 0$. The real part $\text{Re}\sigma_{\alpha\beta}^{AH}$ describes the anomalous Hall conductivity (AHC), and remains finite in the static limit.

The intrinsic dc AHC is obtained by setting $\eta = 0$ and $\omega = 0$ in Eq. (12.11). The contribution from point $\mathbf{k}$ in the Brillouin zone is

$$\sigma_{\mathbf{k},\alpha\beta}^{AH}(0) = \frac{2e^2}{\hbar\Omega_c}\sum_{n,m} f_{n\mathbf{k}}(1 - f_{m\mathbf{k}})\text{Im}\langle\nabla_{k_\alpha}u_{n\mathbf{k}}|u_{m\mathbf{k}}\rangle\langle u_{m\mathbf{k}}|\nabla_{k_\beta}u_{n\mathbf{k}}\rangle, \tag{12.16}$$

where we replaced $f_{n\mathbf{k}} - f_{m\mathbf{k}}$ with $f_{n\mathbf{k}}(1 - f_{m\mathbf{k}}) - f_{m\mathbf{k}}(1 - f_{n\mathbf{k}})$.

This expression is not the most convenient for *ab initio* calculations, as the sums run over the complete set of occupied and empty states. In practice the sum over empty states can be truncated, but a relatively large number should be retained to obtain accurate results. Using the resolution of the identity $1 = \sum_m |u_{m\mathbf{k}}\rangle\langle u_{m\mathbf{k}}|$ and noting that the term $\sum_{n,m} f_{n\mathbf{k}}f_{m\mathbf{k}}(\ldots)$ vanishes identically, we arrive at the celebrated formula for the intrinsic AHC in terms of the Berry curvature,

$$\sigma_{\alpha\beta}^{AH}(0) = \frac{e^2}{\hbar}\frac{1}{N_k\Omega_c}\sum_{\mathbf{k}}(-1)\Omega_{\alpha\beta}(\mathbf{k}), \tag{12.17}$$

$$\Omega_{\alpha\beta}(\mathbf{k}) = \sum_n f_{n\mathbf{k}}\Omega_{n,\alpha\beta}(\mathbf{k}). \tag{12.18}$$

Note that only *occupied* states enter this expression. Once we have a set of Wannier functions spanning the valence bands (together with a few low-lying conduction bands, typically) Eq. (12.17) can be evaluated by Wannier interpolation as described in Refs. [14, 18], with no truncation involved.

12.4 `berry_task=morb`: orbital magnetization

The ground-state orbital magnetization of a crystal is given by [15, 19]

$$\mathbf{M}^{\text{orb}} = \frac{e}{\hbar}\frac{1}{N_k\Omega_c}\sum_{\mathbf{k}}\mathbf{M}^{\text{orb}}(\mathbf{k}), \tag{12.19}$$

$$\mathbf{M}^{\text{orb}}(\mathbf{k}) = \sum_n \frac{1}{2}f_{n\mathbf{k}}\,\text{Im}\,\langle\boldsymbol{\nabla}_{\mathbf{k}}u_{n\mathbf{k}}|\times(H_{\mathbf{k}} + \varepsilon_{n\mathbf{k}} - 2\varepsilon_F)|\boldsymbol{\nabla}_{\mathbf{k}}u_{n\mathbf{k}}\rangle, \tag{12.20}$$

where ε_F is the Fermi energy. The Wannier-interpolation calculation is described in Ref. [18]. Note that the definition of $\mathbf{M}^{\text{orb}}(\mathbf{k})$ used here differs by a factor of $-1/2$ from the one in Eq. (97) and Fig. 2 of that work.

12.5 `berry_task=shc`: spin Hall conductivity

The Kubo-Greenwood formula for the intrinsic spin Hall conductivity (SHC) of a crystal in the independent-particle approximation reads [20–22]

$$\sigma_{\alpha\beta}^{\text{spin}\gamma}(\omega) = \frac{\hbar}{\Omega_c N_k}\sum_{\boldsymbol{k}}\sum_n f_{n\boldsymbol{k}}\sum_{m\neq n}\frac{2\,\text{Im}[\langle n\boldsymbol{k}|\hat{j}_\alpha^\gamma|m\boldsymbol{k}\rangle\langle m\boldsymbol{k}| - e\hat{v}_\beta|n\boldsymbol{k}\rangle]}{(\epsilon_{n\boldsymbol{k}} - \epsilon_{m\boldsymbol{k}})^2 - (\hbar\omega + i\eta)^2}. \tag{12.21}$$

The spin current operator $\hat{j}_\alpha^\gamma = \frac{1}{2}\{\hat{s}_\gamma, \hat{v}_\alpha\}$ where the spin operator $\hat{s}_\gamma = \frac{\hbar}{2}\hat{\sigma}_\gamma$. Indices α, β denote Cartesian directions, γ denotes the direction of spin, commonly $\alpha = x, \beta = y, \gamma = z$. Ω_c is the cell volume, N_k is the number of k-points used for sampling the Brillouin zone, and $f_{n\mathbf{k}} = f(\varepsilon_{n\mathbf{k}})$ is the Fermi-Dirac distribution function. $\hbar\omega$ is the optical frequency, and $\eta > 0$ is an adjustable smearing parameter with unit of energy.

The velocity matrix element in the numerator is the same as Eq. (12.6), so the only unknown quantity is the spin current matrix $\langle n\mathbf{k}|\hat{j}_\alpha^\gamma|m\mathbf{k}\rangle$. We can use Wannier interpolation technique to efficiently calculate this matrix, and there are two derivation according to the degree of approximation. A noteworthy difference is the way in which two *ab-initio* matrix elements are evaluated,

$$\langle u_{n\mathbf{k}}|\sigma_\gamma H_{\mathbf{k}}|u_{m\mathbf{k+b}}\rangle, \langle u_{n\mathbf{k}}|\sigma_\gamma|u_{m\mathbf{k+b}}\rangle, \gamma = x, y, z \tag{12.22}$$

These are evaluated by `pw2wannier90` using Ryoo's method. In contrast, Qiao's method does not require `pw2wannier90`, but it assumes an approximation $1 \approx \sum_{l\in ab-initio\,\mathrm{bands}} |u_{l\mathbf{k}}\rangle\langle u_{l\mathbf{k}}|$. You can choose which method to evaluate this value with `shc_method` in the input file. For a full derivation please refer to Ref. [20] or Ref. [21].

The Eq. (12.21) can be further separated into band-projected Berry curvature-like term

$$\Omega_{n,\alpha\beta}^{\mathrm{spin}\gamma}(\boldsymbol{k}) = \hbar^2 \sum_{m\neq n} \frac{-2\,\mathrm{Im}[\langle n\boldsymbol{k}|\frac{1}{2}\{\hat{\sigma}_\gamma, \hat{v}_\alpha\}|m\boldsymbol{k}\rangle\langle m\boldsymbol{k}|\hat{v}_\beta|n\boldsymbol{k}\rangle]}{(\epsilon_{n\boldsymbol{k}} - \epsilon_{m\boldsymbol{k}})^2 - (\hbar\omega + i\eta)^2}, \tag{12.23}$$

k-resolved term which sums over occupied bands

$$\Omega_{\alpha\beta}^{\mathrm{spin}\gamma}(\boldsymbol{k}) = \sum_n f_{n\boldsymbol{k}} \Omega_{n,\alpha\beta}^{\mathrm{spin}\gamma}(\boldsymbol{k}), \tag{12.24}$$

and the SHC is

$$\sigma_{\alpha\beta}^{\mathrm{spin}\gamma}(\omega) = -\frac{e^2}{\hbar}\frac{1}{\Omega_c N_k}\sum_{\boldsymbol{k}} \Omega_{\alpha\beta}^{\mathrm{spin}\gamma}(\boldsymbol{k}). \tag{12.25}$$

The unit of the $\Omega_{n,\alpha\beta}^{\mathrm{spin}\gamma}(\boldsymbol{k})$ is length^2 (Angstrom^2 or Bohr^2, depending on your choice of `berry_curv_unit` in the input file), and the unit of $\sigma_{\alpha\beta}^{\mathrm{spin}\gamma}$ is $(\hbar/e)$S/cm (the unit is written in the header of the output file). The case of $\omega = 0$ corresponds to direct current (dc) SHC while that of $\omega \neq 0$ corresponds to alternating current (ac) SHC or frequency-dependent SHC. Note in some papers Eq. (12.23) is called as spin Berry curvature. However, it was pointed out by Ref. [23] that this name is misleading, so we use a somewhat awkward name "Berry curvature-like term" to refer to Eq. (12.23). The k-resolved term Eq. (12.24) can be used to draw `kslice` plot, and the band-projected Berry curvature-like term Eq. (12.23) can be used to color the `kpath` plot.

Same as the case of optical conductivity, the parameter η contained in the Eq. (12.23) can be chosen using the keyword `[kubo_]smr_fixed_en_width`. Also, adaptive smearing can be employed by the keyword `[kubo_]adpt_smr` (see Examples 29 and 30 in the Tutorial).

Please cite the following paper [20] or [21] when publishing SHC results obtained using this method:

> Junfeng Qiao, Jiaqi Zhou, Zhe Yuan, and Weisheng Zhao,
> *Calculation of intrinsic spin Hall conductivity by Wannier interpolation,*
> Phys. Rev. B. 98, 214402 (2018), DOI:10.1103/PhysRevB.98.214402.

or

Ji Hoon Ryoo, Cheol-hwan Park, and Ivo Souza,
Computation of intrinsic spin Hall conductivities from first principles using maximally localized Wannier functions,
Phys. Rev. B. 99, 235113 (2019), DOI:10.1103/PhysRevB.99.235113.

12.6   `berry_task=sc`: shift current

The shift-current contribution to the second-order response is characterized by a frequency-dependent third-rank tensor [24]

$$
\sigma^{abc}(0;\omega,-\omega) = -\frac{i\pi e^3}{4\hbar^2\Omega_c N_k} \sum_{\boldsymbol{k}} \sum_{n,m} (f_{n\boldsymbol{k}} - f_{m\boldsymbol{k}}) \times \left(r_{mn}^b(\boldsymbol{k}) r_{nm}^{c;a}(\boldsymbol{k}) + r_{mn}^c(\boldsymbol{k}) r_{nm}^{b;a}(\boldsymbol{k}) \right)
$$
$$
\times \left[\delta(\omega_{mn\boldsymbol{k}} - \omega) + \delta(\omega_{nm\boldsymbol{k}} - \omega) \right],
\tag{12.26}
$$

where a, b, c are spatial indexes and $\omega_{mn\boldsymbol{k}} = (\epsilon_{n\boldsymbol{k}} - \epsilon_{m\boldsymbol{k}})/\hbar$. The expression in Eq. 12.26 involves the dipole matrix element

$$
r_{nm}^a(\boldsymbol{k}) = (1 - \delta_{nm}) A_{nm}^a(\boldsymbol{k}),
\tag{12.27}
$$

and its *generalized derivative*

$$
r_{nm}^{a;b}(\boldsymbol{k}) = \partial_{k_b} r_{nm}^a(\boldsymbol{k}) - i \left(A_{nn}^b(\boldsymbol{k}) - A_{mm}^b(\boldsymbol{k}) \right) r_{nm}^a(\boldsymbol{k}).
\tag{12.28}
$$

The first-principles evaluation of the above expression is technically challenging due to the presence of an extra k-space derivative. The implementation in `wannier90` follows the scheme proposed in Ref. [12], following the spirit of the Wannier-interpolation method for calculating the AHC [14] by reformulating $k \cdot p$ perturbation theory within the subspace of wannierized bands. This strategy inherits the practical advantages of the sum-over-states approach, but without introducing the truncation errors usually associated with this procedure [24].

As in the case of the optical conductivity, a broadened delta function can be applied in Eq. 12.26 by means of the parameter η (see Eq. 12.9) using the keyword `[kubo_]smr_fixed_en_width`, and adaptive smearing can be employed using the keyword `[kubo_]adpt_smr`.

Please cite Ref. [12] when publishing shift-current results using this method.

12.7   `berry_task=ic`: injection current

The injection-current contribution to the second-order response is characterized by a frequency-dependent third-rank tensor [25]

$$
\eta^{abc}(0;\omega,-\omega) = -\frac{\pi e^3}{\hbar^2\Omega_c N_k} \sum_{\boldsymbol{k}} \sum_{n,m} (f_{n\boldsymbol{k}} - f_{m\boldsymbol{k}}) \times \Delta_{nm}^a(\boldsymbol{k}) \left(r_{nm}^b(\boldsymbol{k}) r_{mn}^c(\boldsymbol{k}) \right)
$$
$$
\times \delta(\omega_{mn\boldsymbol{k}} - \omega),
\tag{12.29}
$$

where a, b, c are spatial indexes and $\omega_{mn\boldsymbol{k}} = (\epsilon_{n\boldsymbol{k}} - \epsilon_{m\boldsymbol{k}})/\hbar$. The expression in Eq. 12.29 involves the dipole matrix element, defined in Eq. (12.27) and the difference between the band velocities

$$
\Delta_{nm}^a = \frac{\partial}{\partial k^a} \omega_{nm\boldsymbol{k}},
\tag{12.30}
$$

which is calculated by using the scheme proposed in Ref. [17].

As in the case of the optical conductivity and the shift-current, a broadened delta function can be applied in Eq. 12.29 by means of the parameter η (see Eq. 12.9) using the keyword `[kubo_]smr_fixed_en_width`, and adaptive smearing can be employed using the keyword `[kubo_]adpt_smr`.

The output files related to the injection-current take the form `SEED-ic_S_***.dat` and `SEED-ic_A_***.dat`. The `S` and `A` labels denote the symmetric and antisymmetric parts of Eq. (12.29) with respect to the $b \leftrightarrow c$ exchange, defined as

$$\eta_S^{abc}(\omega) = \frac{1}{2}\left[\eta^{abc}(\omega) + \eta^{acb}(\omega)\right], \tag{12.31a}$$

$$\eta_A^{abc}(\omega) = \frac{1}{2}\left[\eta^{abc}(\omega) - \eta^{acb}(\omega)\right]. \tag{12.31b}$$

The symmetric part is completely real and only nonvanishing in time-reversal lacking systems and the antisymmetric part is purely imaginary, as argued in [25].

Please cite Ref. [25] when publishing injection-current results using this method.

12.8   `berry_task=jc`: **jerk current**

The jerk-current contribution to the third-order response is characterized by a frequency-dependent fourth-rank tensor [25]

$$\iota^{abcd}(0; \omega, -\omega, 0) = \frac{2\pi e^4}{\hbar^3 \Omega_c N_k} \sum_{\boldsymbol{k}} \sum_{n,m} (f_{n\boldsymbol{k}} - f_{m\boldsymbol{k}}) \times \vartheta_{nm}^{ad}(\boldsymbol{k}) \left(r_{nm}^b(\boldsymbol{k}) r_{mn}^c(\boldsymbol{k})\right)$$
$$\times \delta(\omega_{mn\boldsymbol{k}} - \omega), \tag{12.32}$$

where a, b, c, d are spatial indexes and $\omega_{mn\boldsymbol{k}} = (\epsilon_{n\boldsymbol{k}} - \epsilon_{m\boldsymbol{k}})/\hbar$. The expression in Eq. 12.29 involves the dipole matrix element, defined in Eq. (12.27) and the difference between the inverse effective masses

$$\vartheta_{nm}^{ad} = \frac{\partial^2}{\partial k^a \partial k^d} \omega_{nm\boldsymbol{k}}, \tag{12.33}$$

which is calculated by using the scheme proposed in Ref. [17]. The jerk-current photoconductivity tensor ι^{abcd} in (12.32) is symmetric under the $b \leftrightarrow c$ and $a \leftrightarrow d$ exchanges.

As in the case of the optical conductivity, the shift-current and injection-current, a broadened delta function can be applied in Eq. 12.29 by means of the parameter η (see Eq. 12.9) using the keyword `[kubo_]smr_fixed_en_width`, and adaptive smearing can be employed using the keyword `[kubo_]adpt_smr`.

The output files related to the jerk-current take the form `SEED-jc_****.dat`.

Please cite Ref. [25] when publishing jerk-current results using this method.

12.9   `berry_task=kdotp`: $k \cdot p$ **coefficients**

Consider a Hamiltonian

$$H = H^0 + H' \tag{12.34}$$

where the eigenvalues E_n and eigenfunctions $|n\rangle$ of H^0 are known, and H' is a perturbation. In a nutshell, quasi-degenerate perturbation theory assumes that the set of eigenfunctions of H^0 can be

divided into subsets A and B that are weakly coupled by H', and that we are only interested in subset A. This theory asserts that a transformed Hamiltonian $\tilde{H}$ exists within subspace A such that

$$\tilde{H} = \tilde{H}^0 + \tilde{H}^1 + \tilde{H}^2 + \cdots \tag{12.35}$$

where $\tilde{H}^j$ contain matrix elements of H' to the jth power. According to Appendix B of Ref [26], the first three terms are

$$\tilde{H}^0_{mm'} = H^0_{mm'}, \tag{12.36}$$

$$\tilde{H}^1_{mm'} = H'_{mm'}, \tag{12.37}$$

$$\tilde{H}^2_{mm'} = \frac{1}{2} \sum_l H'_{ml} H'_{lm'} \left(\frac{1}{E_m - E_l} + \frac{1}{E_{m'} - E_l} \right), \tag{12.38}$$

where $m, m' \in A$ and $l \in B$. The approximation $\tilde{H} \sim \tilde{H}^0 + \tilde{H}^1$ amounts to truncating H to the A subspace. By further including $\tilde{H}^2$, the coupling to the B subspace is incorporated approximately, "renormalizing" the elements of the truncated matrix.

We adopt the notation described in Sec. III.B of Ref. [14]. We shift the origin of k space to the point where the band edge (or some other band extremum of interest) is located, and Taylor expand around that point the Wannier-gauge Hamiltonian,

$$H^{(W)}(\boldsymbol{k}) = H^{(W)}(0) + \sum_a H^{(W)}_a(0)k_a + \frac{1}{2} \sum_{ab} H^{(W)}_{ab}(0)k_a k_b + \mathcal{O}(k^3) \tag{12.39}$$

where $a, b = x, y, z$, and

$$H^{(W)}_a(0) = \left. \frac{\partial H^{(W)}(\boldsymbol{k})}{\partial k_a} \right|_{\boldsymbol{k}=0} \tag{12.40}$$

$$H^{(W)}_{ab}(0) = \left. \frac{\partial^2 H^{(W)}(\boldsymbol{k})}{\partial k_a \partial k_b} \right|_{\boldsymbol{k}=0} \tag{12.41}$$

We now apply to $H^{(W)}(\boldsymbol{k})$ a similarity transformation $U(0)$ that diagonalizes $H^{(W)}(0)$, and call the transformed Hamiltonian $H(\boldsymbol{k})$,

$$H(\boldsymbol{k}) = \overbrace{\overline{H}}^{H^0} + \overbrace{\sum_a \overline{H}_a k_a + \frac{1}{2} \sum_{ab} \overline{H}_{ab} k_a k_b}^{H'} + \mathcal{O}(k^3), \tag{12.42}$$

where we introduced the notation

$$\overline{\mathcal{O}} = U^\dagger(0) \mathcal{O}^{(W)}(0) U(0), \tag{12.43}$$

and applied it to $\mathcal{O} = H, H_a, H_{ab}$. We can now apply quasi-degenerate perturbation theory by choosing the diagonal matrix $\overline{H}$ as our H^0, and the remaining (nondiagonal) terms in Eq. 12.42 as H'. Collecting terms in Eq. (12.35) up to second order in k we get

$$\tilde{H}_{mm'}(\boldsymbol{k}) = \overline{H}_{mm'} + \sum_a \left(\overline{H}_a \right)_{mm'} k_a + \frac{1}{2} \sum_{a,b} \left[\left(\overline{H}_{ab} \right)_{mm'} + (T_{ab})_{mm'} \right] k_a k_b + \mathcal{O}(k^3), \tag{12.44}$$

where $m, m' \in A$ and we have defined the virtual-transition matrix

$$(T_{ab})_{mm'} = \sum_{l \in B} \left(\overline{H}_a \right)_{ml} \left(\overline{H}_b \right)_{lm'} \times \left(\frac{1}{E_m - E_l} + \frac{1}{E_{m'} - E_l} \right) = (T_{ab})^*_{m'm}. \tag{12.45}$$

(The T_{ab} term in Eq. 12.44 gives an Hermitean contribution to $\tilde{H}(\boldsymbol{k})$ only after summing over a and b, whereas the other terms are Hermitean already before summing.)

The implementation in `wannier90` follows the scheme proposed in Ref. [27], and outputs $\overline{H}_{mm'}$ in `seedname-kdotp_0.dat`, $\left(\overline{H}_a\right)_{mm'}$ in `seedname-kdotp_1.dat`, and $\left[\left(\overline{H}_{ab}\right)_{mm'} + (T_{ab})_{mm'}\right]/2$ in `seedname-kdotp_2.dat`.

Please cite Ref. [27] when publishing $k \cdot p$ results using this method.

12.10   Needed matrix elements

All the quantities entering the formulas for the optical conductivity and AHC can be calculated by Wannier interpolation once the Hamiltonian and position matrix elements $\langle \mathbf{0}n|H|\mathbf{R}m\rangle$ and $\langle \mathbf{0}n|\mathbf{r}|\mathbf{R}m\rangle$ are known [14, 17]. Those matrix elements are readily available at the end of a standard MLWF calculation with `wannier90`. In particular, $\langle \mathbf{0}n|\mathbf{r}|\mathbf{R}m\rangle$ can be calculated by Fourier transforming the overlap matrices in Eq. (1.7),

$$\langle u_{n\mathbf{k}}|u_{m\mathbf{k}+\mathbf{b}}\rangle.$$

Further Wannier matrix elements are needed for the orbital magnetization [18]. In order to calculate them using Fourier transforms, one more piece of information must be taken from the k-space *ab-initio* calculation, namely, the matrices

$$\langle u_{n\mathbf{k}+\mathbf{b}_1}|H_{\mathbf{k}}|u_{m\mathbf{k}+\mathbf{b}_2}\rangle$$

over the *ab-initio* k-point mesh [18]. These are evaluated by `pw2wannier90`, the interface routine between `pwscf` and `wannier90`, by adding to the input file `seedname.pw2wan` the line

$$\text{write\_uHu} = \text{.true.}$$

The calculation of spin Hall conductivity needs the spin matrix elements

$$\langle u_{n\mathbf{k}}|\sigma_\gamma|u_{m\mathbf{k}}\rangle, \gamma = x, y, z$$

from the *ab-initio* k-point mesh. These are also evaluated by `pw2wannier90` by adding to the input file `seedname.pw2wan` the line

$$\text{write\_spn} = \text{.true.}$$

If one uses Ryoo's method to calculate spin Hall conductivity, the further matrix elements are needed:

$$\langle u_{n\mathbf{k}}|\sigma_\gamma H_{\mathbf{k}}|u_{m\mathbf{k}+\mathbf{b}}\rangle, \langle u_{n\mathbf{k}}|\sigma_\gamma|u_{m\mathbf{k}+\mathbf{b}}\rangle, \gamma = x, y, z$$

and these are evaluated by adding to the input file `seedname.pw2wan` the lines

$$\text{write\_sHu} = \text{.true.}$$

$$\text{write\_sIu} = \text{.true.}$$

Chapter 13

Overview of the `gyrotropic` module

The `gyrotropic` module of `postw90` is called by setting `gyrotropic = true` and choosing one or more of the available options for `gyrotropic_task`. The module computes the quantities, studied in [28], where more details may be found.

13.1 `gyrotropic_task=-d0`: the Berry curvature dipole

The traceless dimensionless tensor

$$D_{ab} = \int [d\boldsymbol{k}] \sum_n \frac{\partial E_n}{\partial k_a} \Omega_n^b \left(-\frac{\partial f_0}{\partial E} \right)_{E=E_n}, \tag{13.1}$$

13.2 `gyrotropic_task=-dw`: the finite-frequency generalization of the Berry curvature dipole

$$\widetilde{D}_{ab}(\omega) = \int [d\boldsymbol{k}] \sum_n \frac{\partial E_n}{\partial k_a} \widetilde{\Omega}_n^b(\omega) \left(-\frac{\partial f_0}{\partial E} \right)_{E=E_n}, \tag{13.2}$$

where $\widetilde{\boldsymbol{\Omega}}_{\boldsymbol{k}n}(\omega)$ is a finite-frequency generalization of the Berry curvature:

$$\widetilde{\boldsymbol{\Omega}}_{\boldsymbol{k}n}(\omega) = -\sum_m \frac{\omega_{\boldsymbol{k}mn}^2}{\omega_{\boldsymbol{k}mn}^2 - \omega^2} \text{Im} \left(\boldsymbol{A}_{\boldsymbol{k}nm} \times \boldsymbol{A}_{\boldsymbol{k}mn} \right) \tag{13.3}$$

Contrary to the Berry curvature, the divergence of $\tilde{\boldsymbol{\Omega}}_{\boldsymbol{k}n}(\omega)$ is generally nonzero. As a result, $\widetilde{D}(\omega)$ can have a nonzero trace at finite frequencies, $\tilde{D}_\parallel \neq -2\tilde{D}_\perp$ in Te.

13.3 `gyrotropic_task=-C`: the ohmic conductivity

In the constant relaxation-time approximation the ohmic conductivity is expressed as $\sigma_{ab} = (2\pi e\tau/\hbar)C_{ab}$, with

$$C_{ab} = \frac{e}{h} \int [d\boldsymbol{k}] \sum_n \frac{\partial E_n}{\partial k_a} \frac{\partial E_n}{\partial k_b} \left(-\frac{\partial f_0}{\partial E} \right)_{E=E_n} \tag{13.4}$$

a positive quantity with units of surface current density (A/cm).

13.4 `gyrotropic_task=-K`: the kinetic magnetoelectric effect (kME)

A microscopic theory of the intrinsic kME effect in bulk crystals was recently developed [29, 30].

The response is described by

$$K_{ab} = \int [d\boldsymbol{k}] \sum_n \frac{\partial E_n}{\partial k_a} m_n^b \left(-\frac{\partial f_0}{\partial E} \right)_{E=E_n}, \tag{13.5}$$

which has the same form as Eq. (13.1), but with the Berry curvature replaced by the intrinsic magnetic moment $\boldsymbol{m}_{\boldsymbol{k}n}$ of the Bloch electrons, which has the spin and orbital components given by [15]

$$m_{\boldsymbol{k}n}^{\text{spin}} = -\frac{1}{2} g_s \mu_{\text{B}} \langle \psi_{\boldsymbol{k}n} | \sigma | \psi_{\mathbf{k}\mathbf{n}} \rangle \tag{13.6}$$

$$\boldsymbol{m}_{\boldsymbol{k}n}^{\text{orb}} = \frac{e}{2\hbar} \text{Im} \langle \partial_{\boldsymbol{k}} u_{\boldsymbol{k}n} | \times (H_{\boldsymbol{k}} - E_{\boldsymbol{k}n}) | \partial_{\boldsymbol{k}} u_{\boldsymbol{k}n} \rangle, \tag{13.7}$$

where $g_s \approx 2$ and we chose $e > 0$.

13.5 `gyrotropic_task=-dos`: the density of states

The density of states is calculated with the same width and type of smearing, as the other properties of the `gyrotropic` module

13.6 `gyrotropic_task=-noa`: the interband contributionto the natural optical activity

Natural optical rotatory power is given by [31]

$$\rho_0(\omega) = \frac{\omega^2}{2c^2} \text{Re}\, \gamma_{xyz}(\omega). \tag{13.8}$$

for light propagating ling the main symmetry axis of a crystal z. Here $\gamma_{xyz}(\omega)$ is an anti-symmetric (in xy) tensor with units of length, which has both inter- and intraband contributions.

Following Ref. [32] for the interband contribution we writewe write, with $\partial_c \equiv \partial/\partial k_c$,

$$\text{Re}\, \gamma_{abc}^{\text{inter}}(\omega) = \frac{e^2}{\varepsilon_0 \hbar^2} \int [d\boldsymbol{k}] \sum_{n,l}^{o,e} \left[\frac{1}{\omega_{ln}^2 - \omega^2} \text{Re} \left(A_{ln}^b B_{nl}^{ac} - A_{ln}^a B_{nl}^{bc} \right) \right.$$
$$\left. - \frac{3\omega_{ln}^2 - \omega^2}{(\omega_{ln}^2 - \omega^2)^2} \partial_c (E_l + E_n) \text{Im} \left(A_{nl}^a A_{ln}^b \right) \right]. \tag{13.9}$$

The summations over n and l span the occupied (o) and empty (e) bands respectively, $\omega_{ln} = (E_l - E_n)/\hbar$, and $\boldsymbol{A}_{ln}(\boldsymbol{k})$ is given by (12.3) Finally, the matrix B_{nl}^{ac} has both orbital and spin contributions given by

$$B_{nl}^{ac\,(\text{orb})} = \langle u_n | (\partial_a H) | \partial_c u_l \rangle - \langle \partial_c u_n | (\partial_a H) | u_l \rangle \tag{13.10}$$

and

$$B_{nl}^{ac\,(\text{spin})} = -\frac{i\hbar^2}{m_e} \epsilon_{abc} \langle u_n | \sigma_b | u_l \rangle. \tag{13.11}$$

The spin matrix elements contribute less than 0.5% of the total ρ_0^{inter} of Te. Expanding $H = \sum_m |u_m\rangle E_m \langle u_m|$ we obtain for the orbital matrix elements

$$B_{nl}^{ac\,(\text{orb})} = -i\partial_a(E_n + E_l)A_{nl}^c \sum_m \Big\{ (E_n - E_m)A_{nm}^a A_{ml}^c - (E_l - E_m)A_{nm}^c A_{ml}^a \Big\}. \qquad (13.12)$$

This reduces the calculation of $B^{(\text{orb})}$ to the evaluation of band gradients and off-diagonal elements of the Berry connection matrix. Both operations can be carried out efficiently in a Wannier-function basis following Ref. [17].

13.7 `gyrotropic_task=-spin`: compute also the spin component of NOA and KME

Unless this task is specified, only the orbital contributions are calcuated in NOA and KME, thus contributions from Eqs. (13.6) and (13.11) are omitted.

Chapter 14

Electronic transport calculations with the `BoltzWann` module

By setting `boltzwann = TRUE`, `postw90` will call the `BoltzWann` routines to calculate some transport coefficients using the Boltzmann transport equation in the relaxation time approximation.

In particular, the transport coefficients that are calculated are: the electrical conductivity $\boldsymbol{\sigma}$, the Seebeck coefficient $\mathbf{S}$ and the coefficient $\mathbf{K}$ (defined below; it is the main ingredient of the thermal conductivity).

The list of parameters of the `BoltzWann` module are summarized in Table 11.7. An example of a Boltzmann transport calculation can be found in the `wannier90` Tutorial.

Note: By default, the code assumes to be working with a 3D bulk material, with periodicity along all three spatial directions. If you are interested in studying 2D systems, set the correct value for the `boltz_2d_dir` variable (see Sec. 11.12.4 for the documentation). This is important for the evaluation of the Seebeck coefficient.

Please cite the following paper [33] when publishing results obtained using the `BoltzWann` module:

> G. Pizzi, D. Volja, B. Kozinsky, M. Fornari, and N. Marzari,
> *BoltzWann: A code for the evaluation of thermoelectric and electronic transport properties with a maximally-localized Wannier functions basis,*
> Comp. Phys. Comm. 185, 422 (2014), DOI:10.1016/j.cpc.2013.09.015.

14.1 Theory

The theory of the electronic transport using the Boltzmann transport equations can be found for instance in Refs. [34–36]. Here we briefly summarize only the main results.

The current density $\mathbf{J}$ and the heat current (or energy flux density) $\mathbf{J}_Q$ can be written, respectively, as

$$\mathbf{J} = \boldsymbol{\sigma}(\mathbf{E} - \mathbf{S}\boldsymbol{\nabla}T) \tag{14.1}$$

$$\mathbf{J}_Q = T\boldsymbol{\sigma}\mathbf{S}\mathbf{E} - \mathbf{K}\boldsymbol{\nabla}T, \tag{14.2}$$

where the electrical conductivity $\boldsymbol{\sigma}$, the Seebeck coefficient $\mathbf{S}$ and $\mathbf{K}$ are 3×3 tensors, in general.

Note: the thermal conductivity $\boldsymbol{\kappa}$ (actually, the electronic part of the thermal conductivity), which is defined as the heat current per unit of temperature gradient in open-circuit experiments (i.e., with $\mathbf{J} = 0$) is not precisely $\mathbf{K}$, but $\boldsymbol{\kappa} = \mathbf{K} - \mathbf{S}\boldsymbol{\sigma}\mathbf{S}T$ (see for instance Eq. (7.89) of Ref. [34] or Eq. (XI-57b) of Ref. [35]). The thermal conductivity $\boldsymbol{\kappa}$ can be then calculated from the $\boldsymbol{\sigma}$, $\mathbf{S}$ and $\mathbf{K}$ tensors output by the code.

These quantities depend on the value of the chemical potential μ and on the temperature T, and can be calculated as follows:

$$[\boldsymbol{\sigma}]_{ij}(\mu, T) = e^2 \int_{-\infty}^{+\infty} d\varepsilon \left(-\frac{\partial f(\varepsilon, \mu, T)}{\partial \varepsilon} \right) \Sigma_{ij}(\varepsilon), \tag{14.3}$$

$$[\boldsymbol{\sigma}\mathbf{S}]_{ij}(\mu, T) = \frac{e}{T} \int_{-\infty}^{+\infty} d\varepsilon \left(-\frac{\partial f(\varepsilon, \mu, T)}{\partial \varepsilon} \right) (\varepsilon - \mu) \Sigma_{ij}(\varepsilon), \tag{14.4}$$

$$[\mathbf{K}]_{ij}(\mu, T) = \frac{1}{T} \int_{-\infty}^{+\infty} d\varepsilon \left(-\frac{\partial f(\varepsilon, \mu, T)}{\partial \varepsilon} \right) (\varepsilon - \mu)^2 \Sigma_{ij}(\varepsilon), \tag{14.5}$$

where $[\boldsymbol{\sigma}\mathbf{S}]$ denotes the product of the two tensors $\boldsymbol{\sigma}$ and $\mathbf{S}$, $f(\varepsilon, \mu, T)$ is the usual Fermi–Dirac distribution function

$$f(\varepsilon, \mu, T) = \frac{1}{e^{(\varepsilon - \mu)/K_B T} + 1}$$

and $\Sigma_{ij}(\varepsilon)$ is the Transport Distribution Function (TDF) tensor, defined as

$$\Sigma_{ij}(\varepsilon) = \frac{1}{V} \sum_{n,\mathbf{k}} v_i(n, \mathbf{k}) v_j(n, \mathbf{k}) \tau(n, \mathbf{k}) \delta(\varepsilon - E_{n,k}).$$

In the above formula, the sum is over all bands n and all states $\mathbf{k}$ (including spin, even if the spin index is not explicitly written here). $E_{n,\mathbf{k}}$ is the energy of the $n-$th band at $\mathbf{k}$, $v_i(n, \mathbf{k})$ is the $i-$th component of the band velocity at $(n, \mathbf{k})$, δ is the Dirac's delta function, $V = N_k \Omega_c$ is the total volume of the system (N_k and Ω_c being the number of k-points used to sample the Brillouin zone and the unit cell volume, respectively), and finally τ is the relaxation time. In the *relaxation-time approximation* adopted here, τ is assumed as a constant, i.e., it is independent of n and $\mathbf{k}$ and its value (in fs) is read from the input variable `boltz_relax_time`.

14.2   Files

14.2.1   `seedname_boltzdos.dat`

OUTPUT. Written by `postw90` if `boltz_calc_also_dos` is `true`. Note that even if there are other general routines in `postw90` which specifically calculate the DOS, it may be convenient to use the routines in `BoltzWann` setting `boltz_calc_also_dos = true` if one must also calculate the transport coefficients. In this way, the (time-demanding) band interpolation on the k mesh is performed only once, resulting in a much shorter execution time.

The first lines are comments (starting with # characters) which describe the content of the file. Then, there is a line for each energy ε on the grid, containing a number of columns. The first column is the energy ε. The following is the DOS at the given energy ε. The DOS can either be calculated using the adaptive smearing scheme[1] if `boltz_dos_adpt_smr` is `true`, or using a "standard" fixed smearing, whose

---

[1]Note that in `BoltzWann` the adaptive (energy) smearing scheme also implements a simple adaptive $k-$mesh scheme: if at any given k point one of the band gradients is zero, then that k point is replaced by 8 neighboring k points. Thus, the final results for the DOS may be slightly different with respect to that given by the `dos` module.

type and value are defined by `boltz_dos_smr_type` and `boltz_dos_smr_fixed_en_width`, respectively. If spin decomposition is required (input flag `spin_decomp`), further columns are printed, with the spin-up projection of the DOS, followed by spin-down projection.

14.2.2 `seedname_tdf.dat`

OUTPUT. This file contains the Transport Distribution Function (TDF) tensor $\boldsymbol{\Sigma}$ on a grid of energies.

The first lines are comments (starting with # characters) which describe the content of the file. Then, there is a line for each energy ε on the grid, containing a number of columns. The first is the energy ε, the followings are the components if $\boldsymbol{\Sigma}(\varepsilon)$ in the following order: Σ_{xx}, Σ_{xy}, Σ_{yy}, Σ_{xz}, Σ_{yz}, Σ_{zz}. If spin decomposition is required (input flag `spin_decomp`), 12 further columns are provided, with the 6 components of $\boldsymbol{\Sigma}$ for the spin up, followed by those for the spin down.

The energy ε is in eV, while $\boldsymbol{\Sigma}$ is in $\dfrac{1}{\hbar^2} \cdot \dfrac{\text{eV} \cdot \text{fs}}{\text{Å}}$.

14.2.3 `seedname_elcond.dat`

OUTPUT. This file contains the electrical conductivity tensor $\boldsymbol{\sigma}$ on the grid of T and μ points.

The first lines are comments (starting with # characters) which describe the content of the file. Then, there is a line for each (μ, T) pair, containing 8 columns, which are respectively: μ, T, σ_{xx}, σ_{xy}, σ_{yy}, σ_{xz}, σ_{yz}, σ_{zz}. (The tensor is symmetric).

The chemical potential is in eV, the temperature is in K, and the components of the electrical conductivity tensor ar in SI units, i.e. in $1/\Omega/\text{m}$.

14.2.4 `seedname_sigmas.dat`

OUTPUT. This file contains the tensor $\boldsymbol{\sigma}\mathbf{S}$, i.e. the product of the electrical conductivity tensor and of the Seebeck coefficient as defined by Eq. (14.4), on the grid of T and μ points.

The first lines are comments (starting with # characters) which describe the content of the file. Then, there is a line for each (μ, T) pair, containing 8 columns, which are respectively: μ, T, $(\sigma S)_{xx}$, $(\sigma S)_{xy}$, $(\sigma S)_{yy}$, $(\sigma S)_{xz}$, $(\sigma S)_{yz}$, $(\sigma S)_{zz}$. (The tensor is symmetric).

The chemical potential is in eV, the temperature is in K, and the components of the tensor ar in SI units, i.e. in A/m/K.

14.2.5 `seedname_seebeck.dat`

OUTPUT. This file contains the Seebeck tensor $\mathbf{S}$ on the grid of T and μ points.

Note that in the code the Seebeck coefficient is defined as zero when the determinant of the electrical conductivity $\boldsymbol{\sigma}$ is zero. If there is at least one (μ, T) pair for which $\det \boldsymbol{\sigma} = 0$, a warning is issued on the output file.

The first lines are comments (starting with # characters) which describe the content of the file. Then, there is a line for each (μ, T) pair, containing 11 columns, which are respectively: μ, T, S_{xx}, S_{xy}, S_{xz}, S_{yx}, S_{yy}, S_{yz}, S_{zx}, S_{zy}, S_{zz}.

NOTE: therefore, the format of the columns of this file is different from the other three files (elcond, sigmas and kappa)!

The chemical potential is in eV, the temperature is in K, and the components of the Seebeck tensor ar in SI units, i.e. in V/K.

14.2.6   `seedname_kappa.dat`

OUTPUT. This file contains the tensor $\mathbf{K}$ defined in Sec. 14.1 on the grid of T and μ points.

The first lines are comments (starting with # characters) which describe the content of the file. Then, there is a line for each (μ, T) pair, containing 8 columns, which are respectively: μ, T, K_{xx}, K_{xy}, K_{yy}, K_{xz}, K_{yz}, K_{zz}. (The tensor is symmetric).

The chemical potential is in eV, the temperature is in K, and the components of the $\mathbf{K}$ tensor are the SI units for the thermal conductivity, i.e. in W/m/K.

Chapter 15

Generic Band interpolation

By setting `geninterp = TRUE`, `postw90` will calculate the band energies (and possibly the band derivatives, if also `geninterp_alsofirstder` is set to `TRUE`) on a generic list of k points provided by the user.

The list of parameters of the Generic Band Interpolation module are summarized in Table 11.8. The list of input k points for which the band have to be calculated is read from the file named `seedname_geninterp.kpt`. The format of this file is described below.

15.1 Files

15.1.1 seedname_geninterp.kpt

INPUT. Read by `postw90` if `geninterp` is `true`.

The first line is a comment (its maximum allowed length is 500 characters).

The second line must contain `crystal` (or `frac`) if the k-point coordinates are given in crystallographic units, i.e., in fractional units with respect to the primitive reciprocal lattice vectors. Otherwise, it must contain `cart` (or `abs`) if instead the $k-$point coordinates are given in absolute coordinates (in units of $1/\text{Å}$) along the k_x, k_y and k_z axes.

Note on units: In the case of absolute coordinates, if a_{lat} is the lattice constant expressed in angstrom, and you want to represent for instance the point $X = \frac{2\pi}{a_{lat}}[0.5, 0, 0]$, then you have to input for its x coordinate $k_x = 0.5 * 2 * \pi/a_{lat}$. As a practical example, if $a_{lat} = 4\text{Å}$, then $k_x = 0.78539816339745$ in absolute coordinates in units of $1/\text{Å}$.

The third line must contain the number n of following k points.

The following n lines must contain the list of k points in the format

```
kpointidx k1 k2 k3
```

where `kpointidx` is an integer identifying the given k point, and `k1`, `k2` and `k3` are the three coordinates of the k points in the chosen units.

15.1.2   `seedname_geninterp.dat` or `seedname_geninterp_NNNNN.dat`

OUTPUT. This file/these files contain the interpolated band energies (and also the band velocities if the input flag `geninterp_alsofirstder` is `true`).

If the flag `geninterp_single_file` is `true`, then a single file `seedname_geninterp.dat` is written by the code at the end of the calculation. If instead one sets `geninterp_single_file` to `false`, each process writes its own output file, named `seedname_geninterp_00000.dat`, `seedname_geninterp_00001.dat`, . . .

This flag is useful when one wants to parallelize the calculation on many nodes, and it should be used especially for systems with a small number of Wannier functions, when one wants to compute the bands on a large number of k points (if the flag `geninterp_single_file` is `true`, instead, all the I/O is made by the root node, which is a significant bottleneck).

Important! The files are not deleted before the start of a calculation, but only the relevant files are overwritten. Therefore, if one first performs a calculation and then a second one with a smaller number of processors, care is needed to avoid to mix the results of the older calculations with those of the new one. In case of doubt, either check the date stamp in the first line of the `seedname_geninterp_*.dat` files, or simply delete the `seedname_geninterp_*.dat` files before starting the new calculation.

To join the files, on can simply use the following command:

```
cat seedname_geninterp_*.dat > seedname_geninterp.dat
```

or, if one wants to remove the comment lines:

```
rm seedname_geninterp.dat
for i in seedname_geninterp_*.dat ; do grep -v \# "$i" >> \
seedname_geninterp.dat ; done
```

The first few lines of each files are comments (starting with #), containing a datestamp, the comment line as it is read from the input file, and a header. The following lines contain the band energies (and derivatives) for each band and k point (the energy index runs faster than the k-point index). For each of these lines, the first four columns contain the k-point index as provided in the input, and the k coordinates (always in absolute coordinates, in units of $1/\text{Å}$). The fifth column contains the band energy.

If `geninterp_alsofirstder` is `true`, three further columns are printed, containing the three first derivatives of the bands along the k_x, k_y and k_z directions (in units of eV·Å).

The k point coordinates are in units of $1/\text{Å}$, the band energy is in eV.

Part IV

Appendices

Appendix A

Utilities

The `wannier90` code is shipped with a few utility programs that may be useful in some occasions. In this chapter, we describe their use.

A.1 kmesh.pl

The `wannier90` code requires the definition of a full Monkhorst–Pack grid of k points. In the input file the size of this mesh is given by means of the `mp_grid` variable. E.g., setting

```
mp_grid = 4 4 4
```

tells `wannier90` that we want to use a $4 \times 4 \times 4$ k grid.

One has then to specify (inside the `kpoints` block in the the `seedname.win` file) the list of k points of the grid. Here, the `kmesh.pl` Perl script becomes useful, being able to generate the required list.

The script can be be found in the `utility` directory of the `wannier90` distribution. To use it, simply type:

```
./kmesh.pl nx ny nz
```

where `nx`, `ny` and `nz` define the size of the Monkhorst–Pack grid that we want to use (for instance, in the above example of the $4 \times 4 \times 4$ k grid, `nx=ny=nz=4`).

This produces on output the list of k points in Quantum Espresso format, where (apart from a header) the first three columns of each line are the k coordinates, and the fourth column is the weight of each k point. This list can be used to create the input file for the ab-initio `nscf` calculation.

If one wants instead to generate the list of the k coordinates without the weight (in order to copy and paste the output inside the `seedname.win` file), one simply has to provide a fourth argument on the command line. For instance, for a $4 \times 4 \times 4$ k grid, use

```
./kmesh.pl 4 4 4 wannier
```

and then copy the output inside the in the `kpoints` block in the `seedname.win` file.

We suggest to always use this utility to generate the k grids. This allows to provide the k point coordinates with the accuracy required by `wannier90`, and moreover it makes sure that the k grid used in the ab-initio code and in `wannier90` are the same.

A.2 `w90chk2chk.x`

During the calculation of the Wannier functions, `wannier90` produces a `.chk` file that contains some information to restart the calculation.

This file is also required by the `postw90` code. In particular, the `postw90` code requires at least the `.chk` file, the `.win` input file, and (almost always) the `.eig` file. Specific modules may require further files: see the documentation of each module.

However, the `.chk` file is written in a machine-dependent format. If one wants to run `wannier90` on a machine, and then continue the calculation with `postw90` on a different machine (or with `postw90` compiled with a different compiler), the file has to be converted first in a machine-independent "formatted" format on the first machine, and then converted back on the second machine.

To this aim, use the `w90chk2chk.x` executable. Note that this executable is not compiled by default: you can obtain it by executing

```
make w90chk2chk
```

in the main `wannier90` directory.

A typical use is the following:

1. Calculate the Wannier functions with `wannier90`

2. At the end of the calculation you will find a `seedname.chk` file. Run (in the folder with this file) the command

   ```
   w90chk2chk.x -export seedname
   ```

   or equivalently

   ```
   w90chk2chk.x -u2f seedname
   ```

   (replacing `seedname` with the seedname of your calculation).

   This command reads the `seedname.chk` file and creates a formatted file `seedname.chk.fmt` that is safe to be transferred between different machines.

3. Copy the `seedname.chk.fmt` file (together with the `seedname.win` and `seedname.eig` files) on the machine on which you want to run `postw90`.

4. On this second machine (after having compiled `w90chk2chk.x`) run

   ```
   w90chk2chk.x -import seedname
   ```

   or equivalently

```
w90chk2chk.x -f2u seedname
```

This command reads the `seedname.chk.fmt` file and creates an unformatted file `seedname.chk` ready to be used by `postw90`.

5. Run the `postw90` code.

A.3   PL_assessment

The function of this utility is to assess the length of a principal layer (in the context of a Landauer-Buttiker quantum conductance calculation) of a periodic system using a calculation on a single unit cell with a dense k-point mesh.

The utility requires the real-space Hamiltonian in the MLWF basis, `seedname_hr.dat`.

The `seedname_hr.dat` file should be copied to a directory containing executable for the utility. Within that directory, run:

```
\$> ./PL_assess.x  nk1 nk2 nk3 num_wann
```

where:

`nk1` is the number of k-points in x-direction `nk2` is the number of k-points in y-direction `nk3` is the number of k-points in z-direction `num_wann` is the number of wannier functions of your system

e.g.,

```
\$> ./PL_assess.x  1 1 20 16
```

Note that the current implementation only allows for a single k-point in the direction transverse to the transport direction.

When prompted, enter the seedname.

The programme will return an output file `seedname_pl.dat`, containing four columns

1. Unit cell number, R

2. Average 'on-site' matrix element between MLWFs in the home unit cell, and the unit cell R lattice vectors away

3. Standard devaition of the quantity in (2)

4. Maximum absolute value in (2)

A.4   w90vdw

This utility provides an implementation of a method for calculating van der Waals energies based on the idea of density decomposition via MLWFs.

For theoretical details, please see the following publication and references therein:

Lampros Andrinopoulos, Nicholas D. M. Hine and Arash A. Mostofi, "Calculating dispersion interactions using maximally localized Wannier functions", *J. Chem. Phys.* **135**, 154105 (2011).

For further details of this program, please see the documentation in `utility/w90vdw/doc/` and the related examples in `utility/w90vdw/examples/`.

A.5   `w90pov`

An utility to create Pov files (to render the Wannier functions using the PovRay utility) is provided inside `utility/w90pov`.

Please refer to the documentation inside `utility/w90pov/doc` for more information.

A.6   `k_mapper.py`

The `wannier90` code requires the definition of a full Monkhorst–Pack grid of **k**-vectors, which can be obtained by means of the `kmesh.pl` utility. In order to perform a GW calculation with the Yambo code, you need to perform a nscf calculation on a grid in the irreducible BZ. Moreover, you may need a finer grid to converge the GW calculation than what you need to interpolate the band structure. The `k_mapper.py` tools helps in finding the **k**-vectors indexes of a full grid needed for interpolation into the reduced grid needed for the GW calculation with Yambo.

Usage:

```
path/k_mapper.py nx ny nz QE_nscf_output
```

where `path` is the path of `utility` folder, `QE_nscf_output` is the path of the QE nscf output file given to Yambo.

A.7   `gw2wannier90.py`

This utility allows to sort in energy the input data of `wannier90` (e.g. overlap matrices and energy eigenvalues). `gw2wannier90.py` allows to use `wannier90` at the G_0W_0 level, where quasi-particle corrections can change the energy ordering of eigenvalues (Some `wannier90` modules require states to be ordered in energy).

Usage:

```
path/gw2wannier90.py seedname options
```

where `path` is the path of `utility` folder.

Available options are:

```
mmn, amn, spn, unk, uhu, uiu,
spn_formatted, unk_formatted, uhu_formatted, uiu_formatted,
write_formatted
```

If no options are specified, all the files (`mmn`, `amn`, `spn`, `UNK`, `uHu`, `uIu`) are considered.

Binary (unformatted Fortran) files are supported, though not reccommended, since they are compiler-dependent. A safer choice is to use (bigger) formatted files, with options:

```
spn_formatted, uiu_formatted, uhu_formatted, unk_formatted
```

In default, the output format is the same as the input format. To generate formatted files with unformatted input, use option: `write_formatted`

A.8 w90spn2spn.x

The interface between ab-initio code and `wannier90` (e.g. `pw2wannier90.x`) can produce a `.spn` file that is used by `postw90` to calculate some spin related quantities.

The `.spn` file can be written in a machine-dependent or a machine-independent format depending on the input parameter `spn_formatted` (the default is `false` which means the `.spn` file is machine-dependent) of the `pw2wannier90.x`. If a `.spn` file has been generated on a machine with machine-dependent format, and then one wants to continue the calculation with `postw90` on a different machine (or with `postw90` compiled with a different compiler), the file has to be converted first in a machine-independent "formatted" format on the first machine.

To this aim, use the `w90spn2spn.x` executable. Note that this executable is not compiled by default: you can obtain it by executing

```
make w90spn2spn
```

in the main `wannier90` directory.

A typical use is the following:

1. Calculate the `.spn` file, e.g. by `pw2wannier90.x`

2. At the end of the calculation you will find a `seedname.spn` file. If the file is "unformatted", run (in the folder with this file) the command

   ```
   w90spn2spn.x -export seedname
   ```

   or equivalently

   ```
   w90spn2spn.x -u2f seedname
   ```

   (replacing `seedname` with the seedname of your calculation).

   This command reads the `seedname.spn` file and creates a formatted file `seedname.spn.fmt` that is safe to be transferred between different machines.

3. Copy the `seedname.spn.fmt` file on the machine on which you want to run `postw90`.

4. On this second machine (after having compiled `w90spn2spn.x`) run

    `w90spn2spn.x -import seedname`

    or equivalently

    `w90spn2spn.x -f2u seedname`

    This command reads the `seedname.spn.fmt` file and creates an unformatted file `seedname.spn` ready to be used by `postw90`.

5. Run the `postw90` code.

Note if `spn_formatted` is set to `true` in both `pw2wannier90.x` and `postw90` input files, then the `.spn` file will be written and read as "formatted", so `w90spn2spn.x` is not needed. However, if an "unformatted" `seedname.spn` has been created and you do not want to rerun `pw2wannier90.x`, then `w90spn2spn.x` can be useful. Also, once a "formatted" `seedname.spn` has been generated, the step 4 can be skipped if `spn_formatted` is set to `true` in `postw90` input file `seedname.win`.

Appendix B

Frequently Asked Questions

B.1   General Questions

B.1.1   What is `wannier90`?

`wannier90` is a computer package, written in Fortran90, for obtaining maximally-localised Wannier functions, using them to calculate bandstructures, Fermi surfaces, dielectric properties, sparse Hamiltonians and many things besides.

B.1.2   Where can I get `wannier90`?

The most recent release of `wannier90` is always available on our website `http://www.wannier.org`.

B.1.3   Where can I get the most recent information about `wannier90`?

The latest news about `wannier90` can be followed on our website `http://www.wannier.org`.

B.1.4   Is `wannier90` free?

Yes! `wannier90` is available for use free-of-charge under the GNU General Public Licence. See the file `LICENSE` that comes with the `wannier90` distribution or the GNU hopepage at `http://www.gnu.org`.

B.2   Getting Help

B.2.1   Is there a Tutorial available for `wannier90`?

Yes! The `examples` directory of the `wannier90` distribution contains input files for a number of tutorial calculations. The `doc` directory contains the accompanying tutorial handout.

B.2.2 Where do I get support for `wannier90`?

There are a number of options:

1. The `wannier90` User Guide, available in the `doc` directory of the distribution, and from the webpage (`http://www.wannier.org/user_guide.html`)

2. The `wannier90` webpage for the most recent announcements (`http://www.wannier.org`)

3. The `wannier90` mailing list (see `http://www.wannier.org/forum.html`)

B.2.3 Is there a mailing list for `wannier90`?

Yes! You need to register: go to `http://www.wannier.org/forum.html` and follow the instructions.

B.3 Providing Help: Finding and Reporting Bugs

B.3.1 I think I found a bug. How do I report it?

- Check and double-check. Make sure it's a bug.

- Check that it is a bug in `wannier90` and not a bug in the software interfaced to `wannier90`.

- Check that you're using the latest version of `wannier90`.

- Send us an email. Make sure to describe the problem and to attach all input and output files relating to the problem that you have found.

B.3.2 I have got an idea! How do I report a wish?

We're always happy to listen to suggestions. Email your idea to the `wannier90` developers.

B.3.3 I want to help! How can I contribute to `wannier90`?

Great! There's always plenty of functionality to add. Email us to let us know about the functionality you'd like to contribute.

B.3.4 I like `wannier90`! Should I donate anything to its authors?

Our Swiss bank account number is... just kidding! There is no need to donate anything, please just cite our paper in any publications that arise from your use of `wannier90`:

> [ref] G. Pizzi, V. Vitale, R. Arita, S. Blügel, F. Freimuth, G. Géranton, M. Gibertini, D. Gresch, C. Johnson, T. Koretsune, J. Ibañez-Azpiroz, H. Lee, J.M. Lihm, D. Marchand, A. Marrazzo, Y. Mokrousov, J.I. Mustafa, Y. Nohara, Y. Nomura, L. Paulatto, S. Poncé, T. Ponweiser, J. Qiao, F. Thöle, S.S. Tsirkin, M. Wierzbowska, N. Marzari, D. Vanderbilt, I.

Souza, A.A. Mostofi, J.R. Yates,
Wannier90 as a community code: new features and applications, *J. Phys. Cond. Matt.* **32**, 165902 (2020)
`https://doi.org/10.1088/1361-648X/ab51ff`

If you are using versions 2.x of the code, cite instead:

[ref] A. A. Mostofi, J. R. Yates, G. Pizzi, Y.-S. Lee, I. Souza, D. Vanderbilt and N. Marzari, An updated version of `wannier90`: A Tool for Obtaining Maximally-Localised Wannier Functions, *Comput. Phys. Commun.* **185**, 2309 (2014)
`http://doi.org/10.1016/j.cpc.2014.05.003`

B.4 Installation

B.4.1 How do I install `wannier90`?

Follow the instructions in the file `README.install` in the main directory of the `wannier90` distribution.

B.4.2 Are there `wannier90` binaries available?

Not at present.

B.4.3 Is there anything else I need?

Yes. `wannier90` works on top of an electronic structure calculation.

At the time of writing there are public, fully functioning, interfaces between `wannier90` and PWSCF, ABINIT (`http://www.abinit.org`), SIESTA (`http://www.icmab.es/siesta/`), VASP (`https://www.vasp.at`), WIEN2K (`http://www.wien2k.at`), FLEUR (`http://www.fleur.de`), OpenMX (`http://www.openmx-square.org/`), GPAW (`https://wiki.fysik.dtu.dk/gpaw/`).

To use `wannier90` in combination with PWSCF code (a plane-wave, pseudopotential, density-functional theory code, which is part of the `quantum-espresso` package) you will need to download PWSCF from the webpage `http://www.quantum-espresso.org`. Then compile PWSCF and the `wannier90` interface program `pw2wannier90`. For instructions, please refer to the documentation that comes with the `quantum-espresso` distribution.

For examples of how to use PWSCF and `wannier90` in conjunction with each other, see the `wannier90` Tutorial.

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