

# Filter Design

Me lol

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## Notes

- The question papers for 81 Bhadra, Baisakh, 80 Bhadra, Baisakh and 79 Bhadra may seem repeated but they are not.
- This is because 2 question papers are used: EX606 (our BEI) and EX704 (old BEX course).
- Our EX606 will be highlighted with this font for clarity. EX704 will be kept as is.

# Contents

<b>1</b>	<b>Introduction</b>	<b>4</b>
1.1	Filter and its importance in communication . . . . .	4
1.2	Kinds of filters in terms of frequency response . . . . .	4
1.3	Ideal response and response of practical filters . . . . .	4
1.4	Normalization and denormalization in filter design . . . . .	5
1.5	Impedance (magnitude) scaling and frequency scaling . . . . .	5
1.6	Numericals of EX704 . . . . .	5
<b>2</b>	<b>Approximation Methods</b>	<b>6</b>
2.1	Approximation and its importance in filter design . . . . .	6
2.2	Butterworth response, Butterworth pole locations, Butterworth filter design from specifications . . . . .	6
2.3	Chebyshev and inverse Chebyshev characteristics, network functions and pole zero locations	6
2.4	Characteristics of Cauer (elliptic) response . . . . .	7
2.5	Bessel-Thomson approximation of constant delay . . . . .	7
2.6	Delay Equalization . . . . .	8
<b>3</b>	<b>Frequency transformation</b>	<b>9</b>
3.1	Frequency transformation and its importance in filter design . . . . .	9
3.2	Lowpass to highpass transformation . . . . .	9
3.3	Lowpass to bandpass transformation . . . . .	9
3.4	Lowpass to bandstop transformation . . . . .	10
<b>4</b>	<b>Properties and Synthesis of Passive Networks</b>	<b>11</b>
4.1	One-port passive circuits . . . . .	11
4.1.1	Properties of passive circuits, positive real functions . . . . .	11
4.1.2	Properties of lossless circuits . . . . .	11
4.1.3	Synthesis of LC one-port circuits, Foster and Cauer circuits . . . . .	11
4.1.4	Properties and synthesis of RC one-port circuits . . . . .	12
4.2	Two-port Passive Circuits . . . . .	12
4.2.1	Properties of passive two-port circuits, residue condition, transmission zeros . . . .	12
4.2.2	Synthesis of two-port LC and RC ladder circuits based on zero-shifting by partial pole removal . . . . .	12
<b>5</b>	<b>Design of Resistively-Terminated Lossless Fitter</b>	<b>13</b>
5.1	Properties of resistively-terminated lossless ladder circuits, transmission and reflection coefficients . . . . .	13
5.2	Synthesis of LC ladder circuits to realize all-pole lowpass functions . . . . .	13
5.3	Synthesis of LC ladder circuits to realize functions with finite transmission zeros . . . . .	13
<b>6</b>	<b>Active Filter</b>	<b>14</b>
6.1	Fundamentals of Active Filter Circuits . . . . .	14
6.1.1	Active filter and passive filter . . . . .	14
6.1.2	Ideal and real operational amplifiers, gain-bandwidth product . . . . .	14
6.1.3	Active building blocks: amplifiers, summers, integrators . . . . .	14
6.1.4	First order passive sections and active sections using inverting and non-inverting op-amp configuration . . . . .	14
6.2	Second order active sections (biquads) . . . . .	14

6.2.1	Tow-Thomas biquad circuit, design of active filter using TowThomas biquad . . .	14
6.2.2	Sallen-Key biquad circuit and Multiple-feedback biquad (MFB) circuit . . . . .	14
6.2.3	Cain reduction and gain enhancement . . . . .	15
6.2.4	RC-CR transformation . . . . .	15
<b>7</b>	<b>Sensitivity</b>	<b>16</b>
7.1	Sensitivity and importance of sensitivity analysis . . . . .	16
7.2	Definition of single parameter sensitivity . . . . .	16
7.3	Centre frequency and Q-factor sensitivity . . . . .	16
7.4	Sensitivity properties of biquads . . . . .	16
7.5	Sensitivity of passive circuits . . . . .	16
<b>8</b>	<b>Design of High-Order Active Filters</b>	<b>17</b>
8.1	Cascade of biquads . . . . .	17
8.1.1	Sequencing of filter blocks, center frequency, Q-factor and gain . . . . .	17
8.2	Active simulation of passive filters . . . . .	17
8.2.1	Ladder design with simulated inductors . . . . .	17
8.2.2	Ladder design with frequency dependent negative resistors (FDNR) . . . . .	17
8.2.3	Leapfrog simulation of ladders . . . . .	17
<b>9</b>	<b>Switched-Capacitor Filters</b>	<b>18</b>
9.1	The MOS switch and switched capacitor . . . . .	18
9.2	Simulation of resistor by switched capacitor . . . . .	18
9.3	Switched-capacitor circuits for analog operations: addition, subtraction, multiplication and integration . . . . .	18
9.4	First-order and second-order switched-capacitor circuits . . . . .	18
<b>10</b>	<b>Tables</b>	<b>19</b>
10.0.1	81 Bh/80 Bh . . . . .	19
10.0.2	81 Ba . . . . .	19

# 1 Introduction

(4 Hours/7 Marks)

## 1.1 Filter and its importance in communication

1. What is (analog) Filter? [1] (81 Bh, 80 Bh, 74 Ch, 81 Ba)
2. List out the applications of filter networks. [2] (81 Ba)  
|→ What is its importance of filter in communication? [2] (74 Ch)
3. Explain the basic steps to be followed while designing a filter. [3] (81 Bh, 79 Bh)
4. What are the differences between active filter and passive filter? [3] (79 Ba)

## 1.2 Kinds of filters in terms of frequency response

1. Define the terms: Insertion gain and Insertion loss with neat diagram. [2] (80 Bh)
2. Define the following terms with the help of illustrations: Passband, Stopband, Transition band, Roll-off and bandwidth. [4] (79 Bh)
3. Define all-pass filter. [1] (74 Ch) [2] (76 Ch)
4. Where is all-pass filter used since it passes all the frequency components? [4] (76 Ch)  
|→ Why do we need all pass filter if it passes all the frequency components? [3] (76 Ash)  
|→ What is the importance of all pass filter in filter design? [1] (80 Bh, 74 Ch)
5. Define  $\alpha_{max}$ ,  $\alpha_{min}$ , half power frequency, bandwidth, insertion loss and insertion gain with necessary figures. [6] (75 Ch, 72 Ka)
6. Define and explain the following terms with necessary diagrams:  $\alpha_p$ ,  $\alpha_s$ ,  $\omega_p$ ,  $\omega_s$ . [4] (74 Ash)  
|→ and define passband, stopband and bandwidth with figures. [7] (70 Asa)
7. Define  $\alpha_{max}$ ,  $\alpha_{min}$  and half power bandwidth with necessary diagrams. [3] (70 Ch)

## 1.3 Ideal response and response of practical filters

1. What are the characteristics of ideal filter? [1] (81 Ba)
2. What are the ideal and practical filters? [3] (80 Ba)
3. Explain the ideal response and practical response of filters. [3] (74 Ch)

## 1.4 Normalization and denormalization in filter design

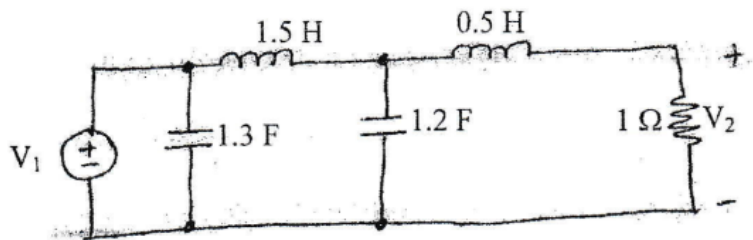
1. Define normalization and denormalization. [2] (73 Shr) [3] (**73 Ch**, 71 Shr)
2. Explain the significance of normalization and denormalization during filter design. [2] (81 Bh, 80 Bh, 80 Ba, **78 Bh**, **72 Ch**, **69 Ch**) [3] (79 Bh, 76 Ash, 71 Shr)

## 1.5 Impedance (magnitude) scaling and frequency scaling

1. Define scaling. [1] (**81 Bh**, 74 Ash)  
|→ What is frequency scaling? [1] (81 Ba)
2. Derive the relations for frequency scaling. [3] (**81 Bh**, 81 Ba)  
|→ Explain magnitude scaling with necessary derivations. [3] (79 Ba)
3. What is the importance of scaling in filter design? [2] (75 Ash, 73 Shr, 71 Ch)  
|→ with examples. [2] (81 Ba) [4] (81 Ba)
4. Derive element scaling equation. [3] (74 Ash) [4] (81 Bh, 79 Bh, **80 Bh**, 81 Ba, 75 Ash) [5] (80 Bh, 71 Ch, **69 Ch**, 80 Ba)

## 1.6 Numericals of EX704

1. At frequency  $f = 20\text{KHz}$  and  $f = 30\text{KHz}$  a filter is designed to attenuate the input signal by 78dB and 90dB respectively. Find the amplitude of the output signal if the 30KHz input signal has amplitude of 1V. [4] (**78 Bh**, **70 Ch**)
2. Following ckt is an LPF designed at normalization frequency of  $\omega_0 = 1\text{rad/s}$ . Apply frequency and magnitude scaling so that  $\omega_0 = 10^5\text{rad/s}$  and practically realizable elements. [4] (**73 Ch**)  
(and no circuit has been found in any source yet)
3. The following is a pass filter with  $\omega_p = 1\text{rad/s}$ . Modify the circuit so that it becomes a low pass filter with a pass band of  $1000\text{rad/s}$  and a load resistance of  $75\Omega$ . [3] (**72 Ch**)



## 2 Approximation Methods

(8 Hours/14 Marks)

### 2.1 Approximation and its importance in filter design

1. What is approximation in filter design? [1] (81 Ba)

### 2.2 Butterworth response, Butterworth pole locations, Butterworth filter design from specifications

1. What are the characteristics of Butterworth response? [3] (79 Bh, **73 Ch**)  
|→ What are the characteristics of Butterworth filter? [2] (**75 Ch**)
2. Derive the expression to calculate the order of a Butterworth low pass filter.  
[4] (80 Bh, 79 Bh, **80 Bh, 79 Bh, 78 Bh, 75 Bh**, 75 Ash) [5] (**69 Ch**)
3. Derive the transfer function of a normalized 4<sup>th</sup> Butterworth low pass approximation. [4] (**81 Bh**)  
|→ derive for 5<sup>th</sup> [4] (**73 Ch**)
4. Calculate the minm order of Butterworth filter with the following specifications: [3] (81 Bh)  
 $\omega_p/\omega_s = 1.5$   $\alpha_{max} = 1\text{dB}$ ,  $\alpha_{min} = 25\text{dB}$
5. Estimate the order of Butterworth filter, along with pole locations and transfer functions, having following specifications:  
a.  $\omega_p/\omega_s = 1.5$   $\alpha_{max} = 1\text{dB}$ ,  $\alpha_{min} = 20\text{dB}$  [2+4] (75 Ash)  
b.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 2000\text{rad/s}$   $\alpha_{max} = 0.5\text{dB}$ ,  $\alpha_{min} = 20\text{dB}$  [3+3] (80 Bh, **80 Bh**)
6. Calculate the order of Butterworth filter with the following specifications:  
a.  $\omega_p = 2000\text{rad/s}$ ,  $\omega_s = 3000\text{rad/s}$   $\alpha_{max} = 1\text{dB}$ ,  $\alpha_{min} = 12\text{dB}$  [3] (79 Bh)  
b.  $\omega_p = 2000\text{rad/s}$ ,  $\omega_s = 3000\text{rad/s}$   $\alpha_{max} = 0.5\text{dB}$ ,  $\alpha_{min} = 22\text{dB}$  [3] (**78 Bh**)  
c.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 2000\text{rad/s}$   $\alpha_{max} = 1\text{dB}$ ,  $\alpha_{min} = 20\text{dB}$  [3] (**75 Ch**)  
d.  $\omega_p = 200\text{rad/s}$ ,  $\omega_s = 2000\text{rad/s}$   $\alpha_{max} = 0.1\text{dB}$ ,  $\alpha_{min} = 30\text{dB}$  [3] (**69 Ch**)

### 2.3 Chebyshev and inverse Chebyshev characteristics, network functions and pole zero locations

1. What are the characteristics of chebyshev magnitude response? [3] (81 Ba, 80 Ba)  
|→ characteristics of chebyshev filter. [2] (76 Ash)
2. What are the characteristics of inverse Chebyshev response? [2] (81 Bh, 74 Ash)
3. Derive the expression to calculate the order of a lowpass Chebyshev filter.  
[3] (**81 Bh, 74 Ch**) [4] (**76 Ch**, 80 Ba) [5] (**70 Ch**, 76 Ash, 71 Shr) [6] (79 Ba)  
|→ also derive for response. [7] (**79 Bh**)  
|→ and then prove that locus of its pole is an ellipse centered at origin. [4] (**81 Bh**)  
|→  
|→ Show that the poles of chebyshev filter lie on an ellipse. Also show the major and minor axes.  
[7] (**73 Ch**)
4. Derive the expression to calculate the order of inverse Chebyshev low pass filter. [3] (81 Bh)  
[4] (74 Ash) [5] (**72 Ch, 71 Ch**, 81 Ba, 80 Ba, 70 Asa)

5. Calculate inverse Chebyshev poles and zeros for given specifications:  $\alpha_{min} = 18\text{dB}$ ,  $\alpha_{max} = 0.25\text{dB}$ ,  $\omega_s = 1400\text{rad/sec}$  and  $\omega_p = 1000\text{rad/sec}$ . [5] (81 Bh)
6. Determine the minimum order  $n$  of CLPF for following specifications.  
 $\alpha_p = 1\text{dB}$ ,  $\alpha_s = 25\text{dB}$  and  $(\omega_s/\omega_p) = 1.5$ , where the symbols have their usual meanings.
7. Find the minimum order with its transfer function, of CLPF having the specifications:
  - a.  $\omega_p/\omega_s = 1.5\text{rad/s}$   $\alpha_{max} = 1\text{dB}$ ,  $\alpha_{min} = 25\text{dB}$  [3] (80 Ba)
  - b.  $\omega_p = 1\text{rad/s}$ ,  $\omega_s = 2.33\text{rad/s}$   $\alpha_{max} = 0.5\text{dB}$ ,  $\alpha_{min} = 22\text{dB}$  [8] (72 Ka)
8. Estimate the order of CLPF with the following specifications:
  - a.  $\omega_p = 100\text{Krad/s}$ ,  $\omega_s = 140\text{Krad/s}$   $\alpha_{max} = 0.25\text{dB}$ ,  $\alpha_{min} = 18\text{dB}$  [3] (81 Ba)
  - b.  $\omega_p = 1500\text{rad/s}$ ,  $\omega_s = 4500\text{rad/s}$   $\alpha_{max} = 0.5\text{dB}$ ,  $\alpha_{min} = 20\text{dB}$  [3] (81 Ba)
  - c.  $\omega_p = 2000\text{rad/s}$ ,  $\omega_s = 2000\text{rad/s}$   $\alpha_{max} = 0.5\text{dB}$ ,  $\alpha_{min} = 22\text{dB}$  [3] (79 Bh)
  - d.  $\omega_p = 2000\text{rad/s}$ ,  $\omega_s = 3000\text{rad/s}$   $\alpha_{max} = 0.5\text{dB}$ ,  $\alpha_{min} = 22\text{dB}$  [3] (79 Ba)
  - e.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 1500\text{rad/s}$   $\alpha_{max} = 0.25\text{dB}$ ,  $\alpha_{min} = 20\text{dB}$  [3] (76 Ch)
  - f.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 2500\text{rad/s}$   $\alpha_{max} = 0.25\text{dB}$ ,  $\alpha_{min} = 40\text{dB}$  [3] (76 Ash)
  - g.  $\omega_p = 3200\text{Hz}$ ,  $\omega_s = 9800\text{Hz}$   $\alpha_{max} = 0.4\text{dB}$ ,  $\alpha_{min} = 52\text{dB}$  [3] (74 Ch)
  - h.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 1400\text{rad/s}$   $\alpha_{max} = 0.25\text{dB}$ ,  $\alpha_{min} = 18\text{dB}$  [3] (71 Ch)
  - i.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 2000\text{rad/s}$   $\alpha_{max} = 0.5\text{dB}$ ,  $\alpha_{min} = 20\text{dB}$  [3] (71 Shr)
  - j.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 2500\text{rad/s}$   $\alpha_{max} = 0.1\text{dB}$ ,  $\alpha_{min} = 20\text{dB}$  [3] (70 Ch)
  - k.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 1800\text{rad/s}$   $\alpha_{max} = 0.5\text{dB}$ ,  $\alpha_{min} = 18\text{dB}$  [3] (70 Asa)
9. Estimate the order of ICLPF with the following specifications:
  - a.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 1800\text{rad/s}$   $\alpha_{max} = 0.5\text{dB}$ ,  $\alpha_{min} = 25\text{dB}$  [3] (80 Ba)
  - b.  $\omega_p = 10000\text{rad/s}$ ,  $\omega_s = 20000\text{rad/s}$   $\alpha_{max} = 0.4\text{dB}$ ,  $\alpha_{min} = 16\text{dB}$  [2] (74 Ash)
  - c.  $\omega_p = 1000\text{rad/s}$ ,  $\omega_s = 1400\text{rad/s}$   $\alpha_{max} = 0.25\text{dB}$ ,  $\alpha_{min} = 18\text{dB}$  [2] (72 Ch)

## 2.4 Characteristics of Cauer (elliptic) response

1. What are the characteristics of Elliptic Response? [3] (73 Shr, 71 Shr)
2. Compare elliptical response with chebyshev and inverse chebyshev response [2+2] (73 Shr)  
 |→ compare with inverse chebyshev response. [3] (71 Shr)

## 2.5 Bessel-Thomson approximation of constant delay

1. What is constant delay filter?  
 [1] (80 Bh, 70 Ch, 81 Ba, 80 Ba, 79 Ba, 76 Ash, 74 Ash, 73 Shr, 70 Asa) [2] (75 Ch, 69 Ch, 80 Ba, 75 Ash)
2. What is significance of constant delay filter? [1] (76 Ch, 80 Ba, 76 Ash) [2] (79 Ba)
3. What are the characteristics of Bessel-Thomson filter? [2] (78 Bh)
4. Derive a transfer function of a second order constant delay filter.  
 [3] (80 Ba, 73 Shr) [4] (74 Ch, 76 Ash, 74 Ash)
5. Find the transfer function of 3<sup>rd</sup> order Bessel Thomson low pass filter.  
 [3] (79 Bh, 75 Ch, 79 Ba) [4] (80 Bh, 80 Bh, 78 Bh, 76 Ch, 69 Ch, 81 Ba, 75 Ash) [5] (80 Ba)  
 |→ for 4th order. [3] (71 Ch)
6. What are the steps involved in designing constant delay filter? Explain with example. [5] (70 Ch)  
 |→ same question, but with example of 2nd order filter. [5] (70 Asa)

## 2.6 Delay Equalization

1. What is delay and delay equalization? Explain with necessary figures  
|→ What is delay equalization? [2+3] (**79 Bh**)  
[1] (**72 Ch.** 72 Ka)
2. What do you mean by phase and gain equalization. [2] (**81 Bh**)
3. What is the importance of all pass filters in delay equalization? [2] (**79 Bh**) [3] (**71 Ch**)
4. Mention the importance of delay equalization. [3] (74 Ash)
5. How is delay equalization done? Explain with necessary figures. [3] (72 Ka) [4] (**72 Ch**)



### 3 Frequency transformation

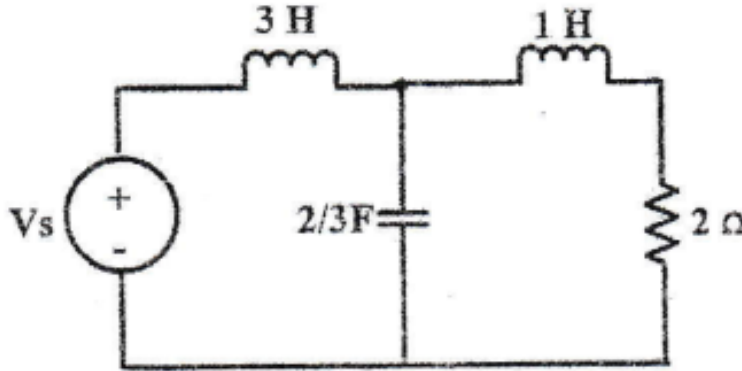
(2 Hours/4 Marks)

#### 3.1 Frequency transformation and its importance in filter design

1. What is frequency transformation (**FT**)?  
[1] (79 Bh, 81 Ba, 78 Bh, 76 Ch, 75 Ch, 69 Ch, 80 Ba, 79 Ba, 76 Ash, 74 Ash, 72 Kar) [2] (74 Ch, 73 Ch)
2. What is the importance of FT? [1] (78 Bh, 75 Ch, 70 Ch, 81 Ba, 76 Ash, 75 Ash, 70 Asa) [2] (71 Ch)
3. How FT reduces the design steps required to design a filter? [1] (80 Bh)
4. What are the application of FT in filter design? [1] (80 Ba) [2] (72 Ch)

#### 3.2 Lowpass to highpass transformation

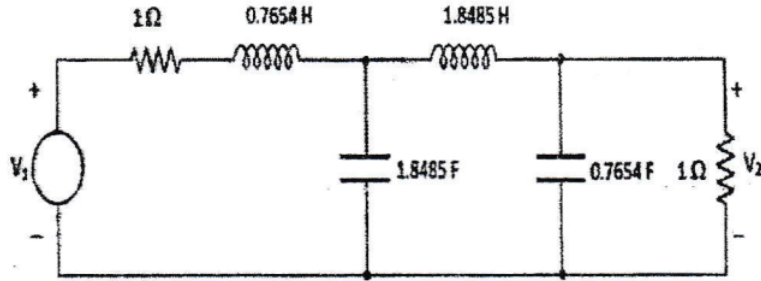
1. How can you obtain a high pass filter from a given low pass filter? Explain with suitable example. [4] (72 Ch, 80 Ba, 80 Ba)
2. The following LPF has passband frequency  $\omega_p$  of 1 rad/s. Transform it into a highpass filter having passband frequency of 2KHz. [4] (73 Shr)



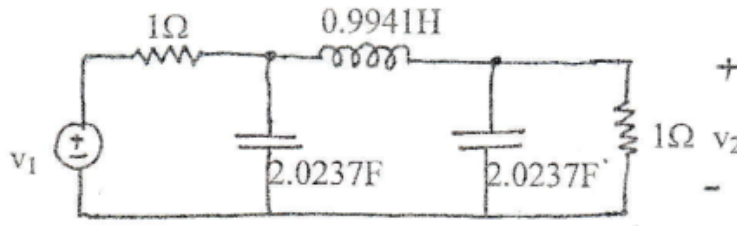
#### 3.3 Lowpass to bandpass transformation

1. Describe the frequency transformation from LPF to BPF with a suitable example.  
[3] (70 Ch, 69 Ch) [4] (74 Ash, 70 Asa) [5] (81 Ba, 81 Ba, 71 Shr)  
|→ Derive the expression of RLC for FT from normalized LPF to BPF. [5] (79 Bh)
2. Design a Band pass filter having center frequency at 1500 rad/sec and bandwidth 300 rad/sec from a 4<sup>th</sup> order Butterworth low pass resistively terminated lossless filter. [Refer Table].  
[4] (81 Bh)  
|→  $\omega_0 = 1\text{ Krad/s}$ , BW = 100 rad/s. [5] (78 Bh)
3. Obtain the BPF from LPF given in figure 1 having center frequency  $10^4\text{ rad/s}$  and bandwidth of  $9.9 \times 10^4\text{ rad/s}$ . [4] (73 Ch)

4. Obtain a bandpass filter having  $\omega_1 = 100$  rad/s and  $\omega_2 = 1000$  rad/s from following LPF at normalized frequency. [4] (74 Ash)

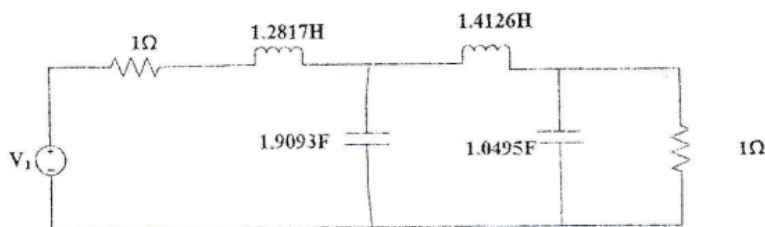


5. The ckt given below is an LPF having passband frequency of 1 rad/s. Obtain a bandpass filter having  $\omega_0 = 2000$  rad/s and  $B = 400$  rad/s. [3] (71 Ch)

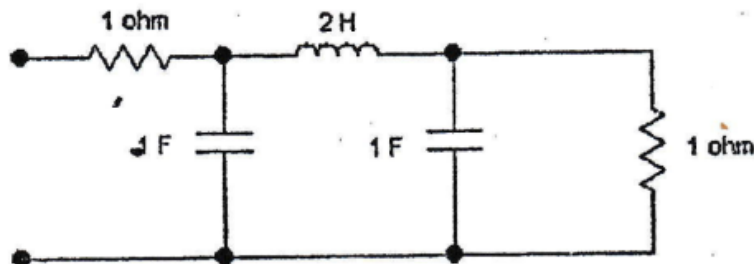


### 3.4 Lowpass to bandstop transformation

1. Explain the frequency transformation technique from a prototype LPF to BSF with necessary derivations. [3] (72 Kar) [4] (81 Bh, 74 Ch, 79 Ba)
2. Design a bandstop filter having center frequency 2000 rad/s and bandwidth 400 rad/s from a 3<sup>rd</sup> order Butterworth low pass filter. [Refer Table] [4] (80 Bh, 79 Bh, 76 Ch, 75 Ch)  
|→ from fourth order. [4] (75 Ash)
3. Following circuit is a low pass filter having  $\alpha_p = 1$  dB and  $\omega_p = 1$  rad/s. Obtain a bandpass filter  $\omega_0 = 400$  rad/s and bandwidth of 150 rad/s. [4] (80 Bh)



4. Following filter has cutoff frequency at 1 rad/s. Transform it into a band pass filter having center frequency at 1000 rad/s and bandwidth of 1000 rad/s. [3] (76 Ash)



## 4 Properties and Synthesis of Passive Networks

(7 Hours/13 Marks)

### 4.1 One-port passive circuits

#### 4.1.1 Properties of passive circuits, positive real functions

#### 4.1.2 Properties of lossless circuits

1. Write the properties of lossless one port network. [2] (81 Bh)
2. How can you determine whether the given function is a valid lossless function or not? [3] (81 Ba)

#### 4.1.3 Synthesis of LC one-port circuits, Foster and Cauer circuits

1. What are the properties of LC driving point impedance function? [3] (79 Bh, 81 Ba)
2. Which of the function is LC driving point impedance function? [2+3] (79 Bh)

$$Z(s) = \frac{8s^3 + 10s}{s^4 + 6s^2 + 5}, \quad Z(s) = \frac{s^4 + 5s^2 + 4}{s^3 + 9s}$$

3. Which of the following function is lossless and why? Find the Cauer-I and Foster-I expansion for the corresponding lossless function. [2+3+3] (81 Bh)

$$Z(S) = \frac{S^2 + 10S + 24}{S^2 + 8S + 15}$$
$$Z(S) = \frac{S^5 + 10S^3 + 24S}{S^4 + 6S^2 + 5}$$

4. Synthesize the given LC function in Foster I and Foster II networks: [6] (81 Bh)

$$F(s) = \frac{s(s^2 + 2)(s^2 + 4)}{(s^2 + 1)(s^2 + 3)}$$

5. Synthesize the given LC impedance in Foster II and Caer I networks: [3+3] (79 Bh)

$$Z(s) = \frac{(s^2 + 1)(s^2 + 3)}{s(s^2 + 2)}$$

6. Which of the following function is valid LC driving point impedance function? State with reason.

$$Z(s) = \frac{8s^3 + 10s}{s^4 + 6s^2 + 5}, \quad Z(s) = \frac{(s^2 + 4)(s^2 + 9)}{(s^2 + 16)(s^2 + 25)} \quad [3+3] (81 Ba)$$

Find the Cauer second form of valid driving point impedance function.

7. Which of the following functions are the valid LC impedance function? State with reason.

$$Z(s) = \frac{(s^2 + 2)(s^2 + 4)}{s(s^2 + 1)(s^2 + 3)}, \quad Z(s) = \frac{(s^2 + 1)(s^2 + 3)}{(s^2)(s^2 + 4)}, \quad Z(s) = \frac{(s^2 + 1)(s^2 + 3)}{s(s^2 + 2)(s^2 + 4)}$$

Pick one valid LC impedance function and realize it in Foster I and Cauer II form. [3+3+3] (81 Ba)

8. Which of the following is valid lossless function? State with reason.

$$Z(s) = \frac{(s^2 + 4)(s^2 + 5)}{(s^2 + s^2)(s^2 + 10)}, \quad Z(s) = \frac{s^4 + 4s^2 + 3}{s(s^2 + 2)}, \quad Z(s) = \frac{s^6 + 4s^4 + 8s^2}{s^3 + 3s}$$

Pick one of the valid LC lossless functions and synthesize it using

→ Foster II and Cauer II methods.

[3+3+3] (80 Bh)

→ Foster series and Cauer I methods.

[2+3+3] (80 Bh)

#### 4.1.4 Properties and synthesis of RC one-port circuits

1. What are the properties of RC impedance function? [3] (80 Ba, 80 Ba)
2. Which of the following are valid RC driving point impedance function and why? [5] (80 Ba)  
$$Z(s) = \frac{(s+3)(s+6)}{(s+1)(s+5)}, \quad Z(s) = \frac{2(s+1)(s+3)}{(s+2)(s+4)}$$

Find Foster form of valid RC driving point impedance function.
3. Synthesize the given RC impedance in Foster and Cauer form. [3+3] (80 Ba)  
$$Z(s) = \frac{3(s+2)(s+4)}{s(s+3)}$$

#### 4.2 Two-port Passive Circuits

1. What do you mean by 2-port network? [1] (81 Bh)

##### 4.2.1 Properties of passive two-port circuits, residue condition, transmission zeros

1. What is called poles and transmission poles. [1] (80 Bh)
2. Define transmission zeros in two port network. [1] (80 Bh, 80 Bh, 81 Ba, 80 Ba, 79 Ba) [2] (79 Bh)
3. How can zeros of transmission be realized in ckts? Explain with suitable diagrams. [4] (79 Bh) [5] (81 Ba)
4. What are the different ways of producing zeros in a network realization? [3] (80 Bh)  
|→ Explain with examples. [5] (80 Ba)
5. Explain the conversion of Z parameters in terms of Y parameters with necessary derivation for a two port passive network. [5] (81 Bh)
6. Explain the series connection of two 2 port networks with figure and derivation. [4] (81 Bh)

##### 4.2.2 Synthesis of two-port LC and RC ladder circuits based on zero-shifting by partial pole removal

1. What is zero shifting? [2] (81 Ba)
2. How is zero shifting useful for two port networks synthesis? Explain with examples. [4] (81 Ba)
3. What is zero shifting by partial removal of pole? Explain w/ suitable example. [3] (80 Bh)  
[5] (80 Ba)
4. What do you mean by partial removal and complete of pole in the synthesis of 2-port lossless ladder network? Explain w/ examples. [6] (79 Bh)

## 5 Design of Resistivity-Terminated Lossless Fitter

(4 Hours/7 Marks)

### 5.1 Properties of resistively-terminated lossless ladder circuits, transmission and reflection coefficients

1. Describe the significance of reflection coefficient. [2] (80 Bh)
2. What information do you get when the value of reflection coefficient is zero? [1] (81 Ba)
3. Derive the expression for reflection coefficient for a resistively terminated LC ladder network. [5] (80 Ba)
4. What is transmission coefficient? What information do we get from it? [2] (80 Ba)
5. Realize the 3<sup>rd</sup> order Butterworth high pass filter using transfer function of LPF as  $T(S) = \frac{1}{(S+1)(S^2+S+1)}$  in the form of doubly terminated LC ladder with  $R_1 = R_2 = 1 \Omega$ . [5] (81 Bh)
6. Design a third order Butterworth low pass filter using Resistively terminated lossless ladder with equal termination of  $1\omega$ . [Refer Table] [6] (81 Ba)
7. Derive the 3<sup>rd</sup> order Butterworth low pass filter resistively-terminated lossless network with unequal termination of  $R_1 = 1\omega$  and  $R_2 = 4\omega$ . [5] (80 Bh)

### 5.2 Synthesis of LC ladder circuits to realize all-pole lowpass functions

1. (assumed) What is GIC? How can it be used to avoid shunt inductors in LC ladder circuit? [5] (81 Bh)

### 5.3 Synthesis of LC ladder circuits to realize functions with finite transmission zeros

## 6 Active Filter

(7 Hours/12 Marks)

### 6.1 Fundamentals of Active Filter Circuits

#### 6.1.1 Active filter and passive filter

1. Differentiate active and passive filter. [2] (80 Bh)

#### 6.1.2 Ideal and real operational amplifiers, gain-bandwidth product

#### 6.1.3 Active building blocks: amplifiers, summers, integrators

#### 6.1.4 First order passive sections and active sections using inverting and non-inverting op-amp configuration

1. Realize a system using non-inverting op-amp configuration with zero at -5 and pole at -3 and having high frequency gain of 2. [5] (81 Bh)
2. Design circuit of the transfer function  $T(s) = \frac{s+8}{s+2}$  using non inverting op-amp configuration. [4] (81 Ba)
3. Realize the following transfer function using non-inverting op-amp configuration. [3] (80 Bh)  
$$T(s) = \frac{4(s+2)}{s+1}$$

### 6.2 Second order active sections (biquads)

#### 6.2.1 Tow-Thomas biquad circuit, design of active filter using TowThomas biquad

1. Draw the circuit diagram of Tow-Thomas Biquad circuit and derive its transfer function. Design a low pass filter using Tow Thomas Biquad circuit with poles at  $-450 \pm j 893.03$  and dc gain of 1.5. The final circuit should contain practically realizable values. [8] (80 Bh)
2. Design a second order low pass filter with poles at  $-10000 \pm j 17320.51$  and DC gain of 2.5 using Tow Thomas Biquad Circuit. Your final circuit should have capacitors of value  $0.001\mu\text{F}$ . [6] (80 Ba)

#### 6.2.2 Sallen-Key biquad circuit and Multiple-feedback biquad (MFB) circuit

1. How is excess gain compensated in Sallen-Key circuit? Explain with necessary derivations and diagrams. [5] (80 Ba)
2. Draw the circuit diagram of Sallen and Key LP biquad and derive its transfer function. [5] (81 Bh)
3. Design a MFB LP biquad for the transfer function as  $T(s) = \frac{5}{s^2 + 1.2s + 1}$  [4] (81 Bh)
4. Derive the transfer function of low pass sallen-key biquad filter [Refer Table]. The half power frequency should be 10KHz. Make the largest capacitance  $0.01\mu\text{F}$  and overall gain be 1. [5] (81 Bh)

**6.2.3**    Cain reduction and gain enhancement

**6.2.4**    RC-CR transformation

## 7 Sensitivity

(3 Hours/5 Marks)

### 7.1 Sensitivity and importance of sensitivity analysis

1. What is sensitivity analysis in filter design? [1] (81 Bh)
2. What is the importance of sensitivity analysis in filter design? [2] (80 Ba)
3. What information do you get when the sensitivity of y with respect to x is 0.1? [1] (80 Bh)

### 7.2 Definition of single parameter sensitivity

### 7.3 Centre frequency and Q-factor sensitivity

1. Perform sensitivity analysis for center frequency  $\omega_0$  of Tow Thomas low pass filter with respect to all the resistors and capacitors present in the circuit. [3] (80 Bh)

### 7.4 Sensitivity properties of biquads

1. Perform the sensitivity analysis of quality factor (Q) in Tow Thomas low pass biquad. [5] (81 Bh)
2. Explain the importance of sensitivity analysis in the design of filter. [2] (81 Ba)
3. Perform the sensitivity analysis of  $\Omega_0$  of sallén-key lowpass biquad filter. [5] (81 Ba)  
[4] (80 Ba)

### 7.5 Sensitivity of passive circuits



## 8 Design of High-Order Active Filters

(6 Hours/11 Marks)

### 8.1 Cascade of biquads

#### 8.1.1 Sequencing of filter blocks, center frequency, Q-factor and gain

### 8.2 Active simulation of passive filters

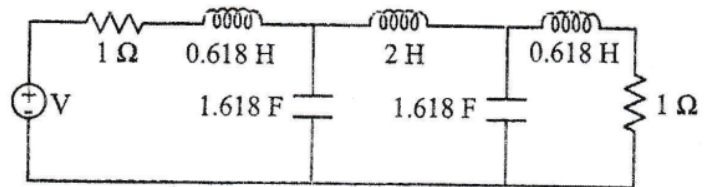
#### 8.2.1 Ladder design with simulated inductors

#### 8.2.2 Ladder design with frequency dependent negative resistors (FDNR)

1. What is FDNR? How can you use FDNR to avoid the inductor in filter design? [4] (80 Bh)
2. What is FDNR? How can it be realized? [1+3] (80 Ba)
3. What is Bruton Transformation? Design the 4<sup>th</sup> order Butterworth low pass filter with half power frequency 2,000 rad/sec and practically realizable elements using FDNR. [Refer Table]. [2+4] (81 Bh)
4. Design third order Butterworth low pass filter having half power frequency 4000rad/s using FDNR. [Refer Table]. [6] (80 Bh)
5. Realize the following passive filter using FDNR, having  $\omega_0 = 25000\text{rad/s}$  and practical element

values in your final circuit.

[5] (80 Ba)



#### 8.2.3 Leapfrog simulation of ladders

1. Design the 4<sup>th</sup> order Butterworth LPF in doubly-terminated network using Leapfrog simulation. The necessary information is listed in the given table below: [8] (81 Ba) 

Order(n)=4 and LPF
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## 9 Switched-Capacitor Filters

(4 Hours/7 Marks)

### 9.1 The MOS switch and switched capacitor

1. Why do we need switched capacitor to simulate resistor in MOS technology? [2] (80 Ba)

### 9.2 Simulation of resistor by switched capacitor

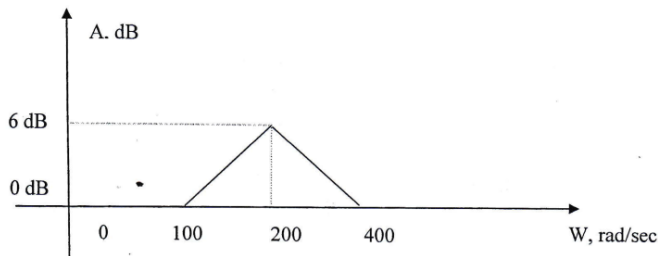
1. What is Switch capacitor filter? Design a switched capacitor filter to realize the transfer function.  
[6] (81 Ba)

$$T(s) = \frac{(s + 200)(s + 800)}{(s + 400)^2}$$

2. Why are resistors are replaced by switched capacitors in modern IC technology? [1] (81 Bh)  
[2] (80 Bh)
3. How can you simulate a resistor using switched capacitor? Explain w/ necessary derivations.  
[4] (80 Ba)

### 9.3 Switched-capacitor circuits for analog operations: addition, subtraction, multiplication and integration

1. Design a switched capacitor filter to realize the magnitude response given by the plot below:  
13. Design a switched – capacitor MOS filter from the given Bode Plot:



[6] (81 Bh)

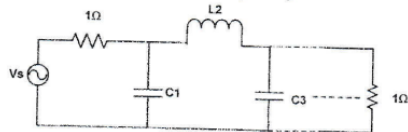
2. How summer, inverting integrator and non-inverting integrator can be realized using switched capacitor? Explain with necessary diagrams and expressions. [4] (80 Bh)

### 9.4 First-order and second-order switched-capacitor circuits

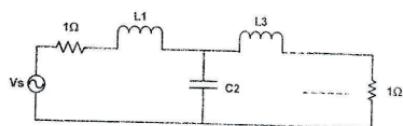
## 10 Tables

### 10.0.1 81 Bh/80 Bh

Table: Elements values for doubly terminated Butterworth low pass filter normal to half power frequency of 1 rad/Sec



n	C1	L2	C3	L4	C5
2	1.414	1.414			
3	1	2	1		
4	0.7654	1.848	1.848	0.7654	
5	0.618	1.618	2	1.618	0.618
n	L1	C2	L3	C4	L5



### 10.0.2 81 Ba

Pole location for Butterworth low pass filter with half power frequency 1 rad/s

n=2	n=3	n=4	n=5
- 0.7071068	- 0.50	- 0.3826834	- 0.809017
$\pm j 0.7071068$	$\pm j 0.86603$	$\pm j 0.9238795$	$\pm j 0.5877852$
	- 1.0	- 0.9238795	- 0.309017
		$\pm j 0.3826834$	$\pm j 0.9510565$
			-1.0