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Section: 7

The following programming assignment measures the ability to analyze and implement Kruskal's algorithm to find MST of a network. You are required to work with your colleagues in a teamwork (Maximum Two– Three members).

a. Write all required algorithms needed to find MST using Kruskal's Algorithm.

Kruskal(g):

 mst = ()

 edges = g.edges

 sort(edges)

 disjoinset(g.vertices)

 for edge in edges:

 u, v, weight = edge

 if find(u) != find(v):

 add edge to mst

 union(u, v)

 if len(mst) == g.vertices - 1:

 break

 return mst

find(v):

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if parent[v] != v:
    parent[v] = find(parent[v])
return parent[v]

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Union(vertex u, vertex v):

root_u = Find(u)

root_v = Find(v)

IF rank(root_u) < rank(root_v):

Set parent of root_u to root_v

Else if rank(root_u) > rank(root_v):

Set parent of root_v to root_u

else:

Set parent of root_v to root_u

Increment rank of root_u

b. Analyze in detail your written algorithms in Part (a).

Each of union is $O(\log V E)$

The loop is $O(E)$

Sorting all edges $O(E \log V E)$

Find and union operation is total

$O(E \log V E)$

Time complexity is $O(E \log V E)$

E is the number of edge.

