# Estimation of Effects of Endogenous Time-Varying Covariates: A Comparison Of Multilevel Linear Modeling and Generalized Estimating Equations

Research Report

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## 1 Introduction

Across a wide range of disciplines, researchers analyze clustered longitudinal, observational data to investigate prospective causal relationships between variables. When analyzing such data, the psychological sciences most commonly resort to the multilevel linear model (MLM, McNeish et al., 2017), which—in the context of longitudinal data analysis—separates observed variance into stable between-person differences and within-person fluctuations (Hamaker & Muthén, 2020). Conversely, other fields, such as biostatistics and econometrics often favour generalized estimating equations (GEE) for the analysis of longitudinal data (McNeish et al., 2017). Despite some cross-disciplinary efforts to compare these methods (McNeish et al., 2017; Muth et al., 2016; Yan et al., 2013), their scarcity may leave researchers with limited guidance in choosing the most suitable approach for their application.

Recent evidence has highlighted an issue present in both methods, where controlling for time-varying endogenous covariates may lead to biased causal estimates (Pepe & Anderson, 1994; Qian et al., 2020). A time-varying covariate is endogenous if it is directly or indirectly influenced by prior treatment or outcome, meaning its value may be determined by earlier stages of the process (Qian et al., 2020). As a result of including these covariates in the mentioned models, ordinary interpretations of the coefficients are no longer valid (Qian et al., 2020, p. 3). According to Diggle (2002), this issue not only pertains GEE and MLM, but all longitudinal data analysis methods.

However, due to a divide between the disciplines that employ these methods, such critiques of the MLM appear to have largely failed to reach the applied researcher in psychology. One specific reason might be that the technical jargon in other disciplines

makes it difficult for researchers to recognize when and how these issues emerge<sup>1</sup>. As a result, researchers may address related problems in disconnected literatures but fail to understand each other. For instance, while the MLM literature emphasizes on the distinction between different centering methods and the effect of cross-level interactions on parameter interpretations (e.g., Hamaker & Muthén, 2020), the GEE literature appears to focus more on the marginal and conditional interpretations of model parameters (e.g., Pepe & Anderson, 1994).

Through a cross-fertilization of these literatures, this project aims to (1) explain the issue of including endogenous covariates in analyses involving GEE, MLM and DSEM (a widely used framework in the social sciences based on MLM) in a psychological context and (2) establish guidelines on how researchers can prevent this issue in their longitudinal data analysis. Accordingly, the following research questions will be addressed: In which cases do the inclusion of endogenous variables in multilevel linear models and generalized estimating equations result in a discrepancy between marginal and conditional estimates? In line with the literature (Diggle, 2002; Pepe & Anderson, 1994; Qian et al., 2020), we expect that the inclusion of endogenous time-varying covariates in longitudinal data analyses may result in bias that—depending on the circumstances—can promote the potential for faulty inferences. To isolate the issue described in Qian et al. (2020), we will focus on the following sub-questions: (1) When removing the interaction  $\beta_1$  from generative model 3, is there a difference between the marginal and conditional estimates of the treatment effect? (2) When removing the random slope  $b_{i2}$  from generative model 3, is there a difference between the marginal and conditional estimates of the treatment effect?

<sup>&</sup>lt;sup>1</sup>For instance, the term 'endogeneity' in econometrics, while related, has a distinct meaning from that of an endogenous variable, which can lead to confusion.

## 2 Methods

To obtain a better understanding of the issue exposed by Qian et al. (2020), two methods were employed. First, graphical methods were used provide insight into the presence and extent of bias with potential violation of assumptions: (a) path diagrams were used to evaluate the conditional independence assumption and (b) directed acyclic graphs (DAGs) were used to evaluate the backdoor criterion (Pearl, 1988, 2009). Second, a simulation study was performed to reproduce the results for the generative models (GMs) from Qian et al. (2020) and to further isolate the issue using additional GMs.

#### 2.1 Data Generation

In the simulation Qian et al. (2020) considered three generative models (GMs), all of which have an endogenous time-varying covariate. In GM1 and GM2, the endogenous covariate  $X_{it}$  equals the previous outcome  $Y_{it}$  plus some random noise, so the conditional independence assumption is valid. In GM3, the endogenous covariate depends directly on  $b_{i0}$ , violating the assumption. To isolate the issue in GM3, we consider two variations on this model: GM3A, where the random slope  $b_{i2}$  for the treatment  $A_{it}$  is removed; GM3B, where the interaction term  $\beta_1 A_{it} X_{it}$  is removed. Note that the conditional independence assumption is violated in either of these variations. The details of the generative models are described below. We follow the notation of Qian et al. (2020) to allow for direct comparison, but rewrite the equations into within- and between-person models (see Raudenbush & Bryk, 2002). We accompany the equations of the GMs with graphical representations, where random effects are represented by grey circles, observed variables by squares and relationships across variables by arrows. The path diagrams of the three data generating models shows the discrepancies between the different generative models—

especially concerning the interaction effects—more clearly than DAGs.

#### 2.1.1 Generative Model 1

In GM1, we considered a simple case with only a random intercept and a random slope for  $X_{it}$ . The outcome is generated according to the following repeated-observations or within-person model (level 1):

$$Y_{it+1} = \pi_{0i} + \pi_{1i}X_{it} + \pi_{2i}A_{it} + \pi_{3i}A_{it}X_{it} + \epsilon_{it+1}$$

with the person-level or between-person model (level 2):

$$\pi_{0i} = \alpha_0 + b_{i0}, \quad b_{i0} \sim \mathcal{N}(0, \sigma_{b0}^2),$$

$$\pi_{1i} = \alpha_1,$$

$$\pi_{2i} = \beta_0 + b_{i2}, \quad b_{i2} \sim \mathcal{N}(0, \sigma_{b2}^2),$$

$$\pi_{3i} = \beta_1$$
.

By substitution, we get the single equation model:

$$\begin{split} Y_{it+1} &= \pi_{0i} + \pi_{1i} X_{it} + \pi_{2i} A_{it} + \pi_{3i} A_{it} X_{it} + \epsilon_{it+1} \\ &= (\alpha_0 + b_{i0}) + \alpha_1 X_{it} + (\beta_0 + b_{i2}) A_{it} + \beta_1 A_{it} X_{it} + \epsilon_{it+1} \\ &= \alpha_0 + \alpha_1 X_{it} + b_{i0} + A_{it} (\beta_0 + \beta_1 X_{it} + b_{i2}) + \epsilon_{it+1}. \end{split}$$

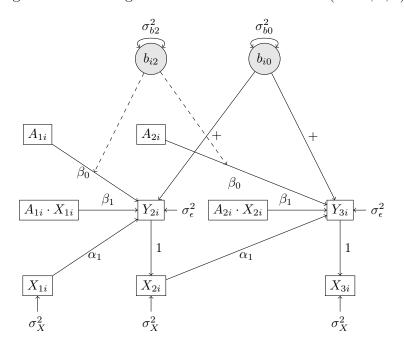
The random effects  $b_{i0} \sim \mathcal{N}(0, \sigma_{b0}^2)$  and  $b_{i2} \sim \mathcal{N}(0, \sigma_{b2}^2)$  are independent of each other. The covariate is generated as  $X_{i1} \sim \mathcal{N}(0, 1)$ , and for  $t \geq 2$ ,

$$X_{it} = Y_{it} + \mathcal{N}(0, 1).$$

The randomization probability  $p_t = P(A_{it} = 1 \mid H_{it})$  is constant at 1/2. Thus,  $A_{it} \sim$  Bernoulli(0.5) for  $i = 1, \ldots, N$  and  $t = 1, \ldots, T$ . The exogenous noise is  $\epsilon_{it+1} \sim \mathcal{N}(0, \sigma_{\epsilon}^2)$ .

Figure 1: Path diagram for Generative Model 1 (t = 1, 2, 3)

Figure 1 shows the path diagram for GM3.



#### 2.1.2 Generative Model 2

In GM2, we considered the case with a random intercept and random slopes for (1) covariate  $X_{it}$ , (2) treatment  $A_{it}$ , and (3) the interaction between  $A_{it}$  and  $X_{it}$ ; and with a time-varying randomization probability for treatment. The outcome is generated according to the same repeated-observations model presented in GM1. However, the person-level model is different:

$$\pi_{0i} = \alpha_0 + b_{i0}, \quad b_{i0} \sim \mathcal{N}(0, \sigma_{b0}^2), \label{eq:pi_0i}$$

$$\pi_{1i} = \alpha_1 + b_{i1}, \quad b_{i1} \sim \mathcal{N}(0, \sigma_{b1}^2),$$

$$\pi_{2i} = \beta_0 + b_{i2}, \quad b_{i2} \sim \mathcal{N}(0, \sigma_{b2}^2),$$

$$\pi_{3i} = \beta_1 + b_{i3}, \quad b_{i3} \sim \mathcal{N}(0, \sigma_{b3}^2). \label{eq:pi_3i}$$

By substitution, we get the single equation model:

$$\begin{split} Y_{it+1} &= \pi_{0i} + \pi_{1i} X_{it} + \pi_{2i} A_{it} + \pi_{3i} A_{it} X_{it} + \epsilon_{it+1} \\ &= (\alpha_0 + b_{i0}) + (\alpha_1 + b_{i1}) X_{it} + (\beta_0 + b_{i2}) A_{it} + (\beta_1 + b_{i3}) A_{it} X_{it} + \epsilon_{it+1} \\ &= \alpha_0 + \alpha_1 X_{it} + b_{i0} + b_{i1} X_{it} + A_{it} \left(\beta_0 + \beta_1 X_{it} + b_{i2} + b_{i3} X_{it}\right) + \epsilon_{it+1}. \end{split}$$

The random effects  $b_{ij} \sim \mathcal{N}(0, \sigma_{bj}^2)$ , for j=0,1,2,3, are independent of each other. The covariate is generated as  $X_{i1} \sim \mathcal{N}(0,1)$ , and for  $t \geq 2$ ,

$$X_{it} = Y_{it} + \mathcal{N}(0, 1).$$

The randomization probability depends on  $X_{it}$ :

$$p_t = P(A_{it} = 1 \mid H_{it}) = \begin{cases} 0.7 & \text{if } X_{it} > -1.27, \\ \\ 0.3 & \text{if } X_{it} \leq -1.27, \end{cases}$$

where the cutoff -1.27 was chosen so that  $p_t$  equals 0.7 or 0.3 for about half of the time. In other words, if the value of the covariate for any given person and time point is above the cutoff, the probability of receiving the treatment  $p_t$  is 0.7; otherwise, it is 0.3. Accordingly,  $A_{it} \sim \text{Bernoulli}(p_t)$  for  $i=1,\ldots,N$  and  $t=1,\ldots,T$ . The exogenous noise is  $\epsilon_{it+1} \sim \mathcal{N}(0,\sigma_{\epsilon}^2)$ .

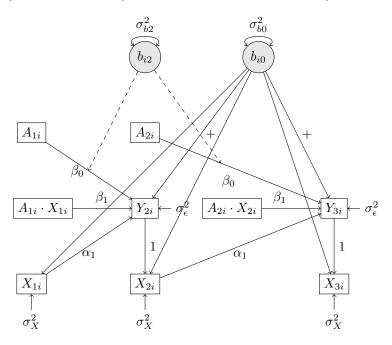
#### 2.1.3 Generative Model 3

GM3 is the same as GM1, except that the covariate  $X_{it}$  depends directly on  $b_{i0}$ :

$$X_{i1} \sim \mathcal{N}(b_{i0}, 1), \quad X_{it} = Y_{it} + \mathcal{N}(b_{i0}, 1) \text{ for } t \geq 2.$$

Figure 2 shows the path diagram for GM3.

Figure 2: Path diagram for Generative Model 3 (t=1,2,3)

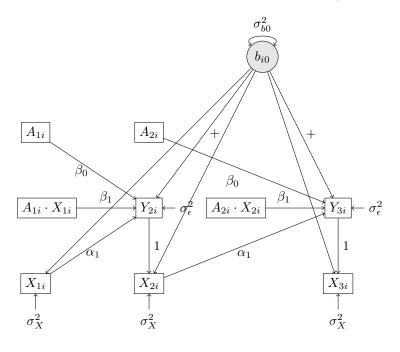


### 2.1.4 Generative Model 3A

GM3A is the same as GM3, except that the random slope  $b_{i2}$  for the treatment  $A_{it}$  is removed. The single equation model then becomes:

$$Y_{it+1} = \alpha_0 + \alpha_1 X_{it} + b_{i0} + A_{it} (\beta_0 + \beta_1 X_{it}) + \epsilon_{it+1}.$$

Figure 3: Path diagram for Generative Model 3A (t=1,2,3)

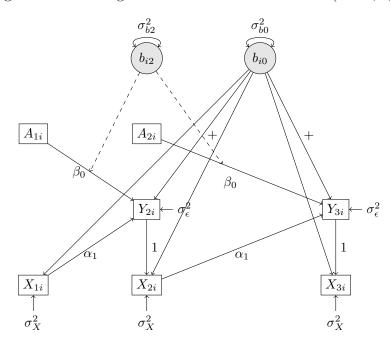


## 2.1.5 Generative Model 3B

GM3B is the same as GM3, except that the interaction term  $\beta_1 A_{it} X_{it}$  is removed. The single equation model then becomes:

$$Y_{it+1} = \alpha_0 + \alpha_1 X_{it} + b_{i0} + A_{it} (\beta_0 + b_{i2}) + \epsilon_{it+1}.$$

Figure 4: Path diagram for Generative Model 3B (t=1,2,3)



### 2.1.6 Parameter Values

The following parameter values were adapted from Qian et al. (2020):

$$\alpha_0 = -2$$
,  $\alpha_1 = -0.3$ ,  $\beta_0 = 1$ ,  $\beta_1 = 0.3$ ,

$$\sigma_{b0}^2 = 4$$
,  $\sigma_{b1}^2 = \frac{1}{4}$ ,  $\sigma_{b2}^2 = 1$ ,  $\sigma_{b3}^2 = \frac{1}{4}$ ,  $\sigma_{\epsilon}^2 = 1$ .

# 2.2 Path Diagrams and Conditional Independence

Qian et al. (2020) proposes the use of the conditional independence assumption to identify whether bias may occur, which is given by:

$$X_{it} \perp (b_{i0}, b_{i1}) \mid H_{it-1}, A_{it-1}, Y_{it}.$$

This allows  $X_{it}$  to be endogenous, but the endogenous covariate  $X_{it}$  can only depend

on the random effects through variables observed prior to  $X_{it}$ . If the only endogenous covariates are functions of prior treatments and prior outcomes, then the assumption automatically holds.

When inspecting Figure 1 and  $?@fig-GM2\_path$ , we may notice that  $X_{it}$  becomes independent of the random effects after conditioning on  $Y_{it}$ . On the other hand, we can see that this assumption is violated in GM3/GM3A/GM3B, as  $X_{it}$  depends directly on  $b_{i0}$  and can thus not be made independent of the random effects by conditioning on prior variables such as  $Y_{it}$  (see Figure 2, Figure 3 and Figure 4)

### 2.3 Backdoor Criterion and DAGs

We formulated the DAGs in dagitty, where the random disturbance  $b_{0i}$  was represented by the node U (e.g., Kim & Steiner, 2021).

"According to the backdoor criterion (Pearl, 1988, 2009) or the adjustment criterion (Shpitser, VanderWeele, & Robins, 2010), identification of causal effects requires that all non-causal paths are blocked by conditioning on middle variables on the non-causal paths (i.e., by controlling for or matching on the variables). If it is not possible to block all non-causal paths due to omitted or unreliably measured variables, the treatment and outcome remain connected via non-causal (or backdoor) paths and the remaining confounding association biases the effect estimators. In Figure 1b, since U is unmeasured, the non-causal path A2 U ! Y 2 cannot be blocked," (Kim and Steiner, 2021)

The DAGs for the first three observations of the three data generating models are presented in Figure ??. The red arrows show the biased paths after controlling for the covariate  $X_{it}$ .

REMAKE THEM IN TIKZ (USE CHATGPT), MAKE backdoor path ARROW RED FOR GM2.

DAG for Generative Models

According to the backdoor criterion (Pearl, 1988, 2009) or the adjustment criterion (Shpitser, VanderWeele, & Robins, 2010), identification of causal effects requires that all non-causal paths are blocked by conditioning on middle variables on the non-causal paths (i.e., by controlling for or matching on the variables). If it is not possible to block all non-causal paths due to omitted or unreliably measured variables, the treatment and outcome remain connected via non-causal (or backdoor) paths and the remaining confounding association biases the effect estimators

When applying Pearl's backdoor criterion to GM1 and GM3, it may be observed that there exists no backdoor path in the treatment effect  $A_{it} \to Y_{it+1}$ . On the other hand, in GM2, there is a backdoor path in the treatment effect:  $A_{it} \leftarrow X_{it} \to Y_{it+1}$ . Thus, Pearl's backdoor criterion fails to identify when the treatment effect is biased.

Note, however, that limitations to Pearl's backdoor criterion have been voiced by several people, when there are interaction effects/ modification effects.

### 2.4 Data Analysis

We evaluated the performance of the models across a total of 30 different settings, each replicated 1,000 times, by systematically varying the following factors:

- Generative Models (GM): 1, 2, 3, 3A, 3B
- Number of timepoints (T): 10, 30

## • Sample size (N): 30, 100, 200

All data generation and estimation was performed in R, version 4.4.2 (Team, 2024). To fit the standard MLM, the lmer function from the R-package lme4 (Bates et al., 2015) was employed with restricted maximum likelihood estimation. For the MLM, the analytical models were equivalent to each of the respective data-generating models. To fit the GEE with the "exchangeable", "independent" and "AR(1)" working correlation structures, the geeglm function from the R-package geepack (Halekoh et al., 2006) was employed with the identity link function. Since the random effects are not explicitly modelled in GEE, the analytical GEE models simply contain only the fixed effects of the generative model at hand.

## 3 Results

As shown in Table X, GM3 results in bias

Table 1: Simulation results for N=200 over 1000 replications, with T=10 and T=30.

GM	Characteristics	$\hat{\beta}_{0,MLM} - \beta_{0,MLM}$		$\hat{\beta}_{0,GEE-ind} - \beta_{0,MLM}$	
		T = 10	T = 30	T = 10	T = 30
1	Includes random intercept	0.003	0.001	0.086	0.090
	and random slope for treat-				
	ment				
3	Model 1 with dependency	-0.051	-0.023	0.033	0.032
	random intercept and co-				
	variate				
3a	Model 3 without random	0.002	-0.000	-0.001	-0.000
	slope $b_{2i}$				
3b	Model 3 without interaction	0.005	0.001	0.003	0.001
	effect $\beta_1$ (between treat-				
	ment and covariate)				

# 4 Discussion

Despite a violation of the conditional independence assumption in GM 3, 3A and 3B; biased MLM estimates were only found for GM3.

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# 6 Appendix

# 6.1 Original Section from Qian et al. (2020): "4. Simulation"

In the simulation, we considered three generative models (GMs), all of which have an endogenous covariate. In the first two GMs, the endogenous covariate  $X_{it}$  equals the previous outcome  $Y_{it}$  plus some random noise, so the conditional independence assumption (10) is valid. In GM 3, the endogenous covariate depends directly on  $b_i$ , violating assumption (10). The details of the generative models are described below.

In GM1, we considered a simple case with only a random intercept and a random slope for  $A_{it}$ , so that  $Z_{i(t_0)} = Z_{i(t_2)} = 1$  in model (7). The outcome is generated as:

$$Y_{it+1} = \alpha_0 + \alpha_1 X_{it} + b_{i0} + A_{it} (\beta_0 + \beta_1 X_{it} + b_{i2}) + \epsilon_{it+1}.$$

The random effects  $b_{i0} \sim N(0, \sigma_{b0}^2)$  and  $b_{i2} \sim N(0, \sigma_{b2}^2)$  are independent of each other. The covariate is generated as  $X_{i1} \sim N(0,1)$ , and for  $t \geq 2$ ,

$$X_{it} = Y_{it} + N(0, 1).$$

The randomization probability  $p_t$  is constant at 1/2. The exogenous noise is  $\epsilon_{it+1} \sim N(0, \sigma_{\epsilon}^2)$ .

In GM2, we considered the case where  $Z_{i(t_0)}=Z_{i(t_2)}=1$ , with time-varying randomization probability. The outcome is generated as:

$$Y_{it+1} = \alpha_0 + \alpha_1 X_{it} + b_{i0} + b_{i1} X_{it} + A_{it} (\beta_0 + \beta_1 X_{it} + b_{i2} + b_{i3} X_{it}) + \epsilon_{it+1}.$$

The random effects  $b_{ij} \sim N(0, \sigma_{b_j}^2)$ , for  $0 \le j \le 3$ , are independent of each other. The covariate is generated as  $X_{i1} \sim N(0, 1)$ , and for  $t \ge 2$ ,

$$X_{it} = Y_{it} + N(0, 1).$$

The randomization probability depends on  $X_{it}$ :

$$p_t = 0.7 \cdot 1(X_{it} > -1.27) + 0.3 \cdot 1(X_{it} \le -1.27),$$

where  $1(\cdot)$  represents the indicator function, and the cutoff -1.27 was chosen so that  $p_t$  equals 0.7 or 0.3 for about half of the time. The exogenous noise is  $\epsilon_{it+1} \sim N(0, \sigma_{\epsilon}^2)$ .

GM3 is the same as GM 1, except that the covariate  $X_{it}$  depends directly on  $b_i$ :

$$X_{i1} \sim N(b_{i0},1), \quad X_{it} = Y_{it} + N(b_{i0},1) \text{ for } t \geq 2.$$

We chose the following parameter values:

$$\alpha_0 = -2, \quad \alpha_1 = -0.3, \quad \beta_0 = 1, \quad \beta_1 = 0.3,$$

$$\sigma_{b0}^2 = 4, \quad \sigma_{b1}^2 = \frac{1}{4}, \quad \sigma_{b2}^2 = 1, \quad \sigma_{b3}^2 = \frac{1}{4}, \quad \sigma_{\epsilon}^2 = 1.$$

## 6.2 Overview of Variations on Generative Model 3

Table 2: Models with 1 Parameter Less

Generative	random slope	interactie $\beta_1$	fixed slope	bias
Model	treatment $b_{i2}$		covariate $\alpha_1$	
3	yes	yes	yes	yes, negative
3a	no	yes	yes	no
3d	yes	no	yes	no
3h	yes	yes	no	yes, positive
Generative	random slope	interactie $\beta_1$	fixed slope	bias
Model	treatment $b_{i2}$		covariate $\alpha_1$	
3	yes	yes	yes	yes, negative
3b	no	no	yes	no
3i	no	yes	no	
3j	yes	no	no	

## 6.3 Simulation Plan Proposal

To uncover the undesirable effects of endogenous covariates and investigate robustness against these effects, we will carry out simulations in which data will be generated according to several increasingly complex scenarios. These scenarios will be visually represented using directed acyclic graphs and analyzed using GEE, MLM and DSEM. We will start out with a scenario of the basic MLM—where a time-varying outcome Y is regressed on a single time-varying predictor X and in the presence of stable between person differences

in the intercept—and increase the complexity until we reach the scenario that includes a time-varying endogenous covariate. The primary interest of this simulation study is the comparative performance of different specifications of the MLM and GEE in terms of bias in the estimation of the effect of X to Y. The secondary interest is the efficiency in mean squared error (MSE). We consider settings with timepoints T=10,30 and sample size N=30,100,200.

Statistical analyses pertaining to the GEE and basic MLM will be performed in R, version 4.4.2 (Team, 2024). To fit the GEE, the R-package geepack (Halekoh et al., 2006) will evaluate several different working correlation structures, including independent, exchangeable, AR(1) and unstructured. To fit the basic MLM, the R-package lme4 (Bates et al., 2015) will be employed, where we will use restricted maximum likelihood estimation.