Estimation of Effects of Endogenous Time-Varying Covariates: A Comparison Of Multilevel Modeling and Generalized Estimating Equations

PROPOSAL

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Introduction

Across a wide range of disciplines, researchers analyze clustered longitudinal, observational data to investigate prospective causal relationships between variables. To address such data, the psychological sciences most commonly resort to the multilevel linear model LM) (McNeish et al., 2017), which is characterized by its separation of stable between-person differences from possible trends in the dynamics of within-person fluctuations (Hamaker & Muthén, 2020). Conversely, other fields, such as biostatistics and econometrics often favour generalized estimating equations (GEE, McNeish et al., 2017). While some interdisciplinary research has introduced and compared these methods (McNeish al., 2017; Muth et al., 2016; Yan et al., 2013), much of it remains superficial, lacking a focus on the specific conditions under which these models can produce meaningful inferences.

Recent evidence has shed light on an issue present in both methods, where controlling for moderators of the treatment effect—that depend on prior treatment—may yield biased causal estimands (Pepe & Anderson, 1994; Qian et al., 2020). Such moderators fall under the umbrella of time-varying endogenous covariates. As a result of including these covariates in the model, ordinary interpretations of the coefficients are no longer valid (Qian et al., 2020, p. 3). According to Diggle (2002), this issue not only pertains GEE and MLM, but all longitudinal data analysis methods. However, due to a schism of the disciplines that employ these methods, such critiques of the MLM not reach the applied researcher. And when it does, the technical nature and jargon of the literature in other fields may prevent these researchers from figuring out how and when these problems occur.

This indicates a need to understand (1) the consequences of including these covariates in analyses on multilevel longitudinal data, such as GEE, MLM and dynamic structural



equation modeling (DSEM; a modeling framework based on MLM) and (2) how this issue may be addressed by researchers that perform longitudinal data analysis. Accordingly, this paper explains how the inclusion of time-varying covariates can yield faulty inferences and intends to establish guidelines on how this may be prevented. More specifically, the current project addresses the following research question: to what extent does the inclusion of endogenous variables in multilevel linear models and generalized estimating equations result in biased estimands? In line with the literature (Diggle, 2002; Pepe & Anderson, 1994; Qian et al., 2020), we expect that the inclusion of endogenous time-varying covariates in longitudinal data analyses that involve marginal interpretation may result in bias that—depending on the circumstances—can promote the potential for faulty inferences.

Analytic Strategy

To uncover the undesirable effects of endogenous covariates and investigate robustness against these effects, we will carry out simulations in which data will be generated according to several increasingly complex causal questions. These scenarios will be visually represented using directed acyclic graphs and analyzed using GEE, MLM and DSEM. We will start out with a scenario of the basic MLM—where a time-varying outcome is regressed on one time-varying predictor and stable between person differences are modeled with a random intercept—and increase the complexity until we reach the scenario discussed by Qian et al. (2020) (i.e., MLM that includes a time-varying endogenous covariate). The primary interest of this simulation study is the comparative performance in terms of bias and the secondary interest is the efficiency in mean squared error (MSE).

occur when using small samples (Bou & Satorra, 2018).

Statistical analyses pertaining to the GEE and basic MLM will be performed in R, version 4.2.0 (R Core Team, 2022). To fit the GEE, the R-packages geepack (Halekoh et al., 2006) and gee (Carey et al., 2024) will evaluate several different working correlation structures, including independent, exchangeable, AR(1) and unstructured. To fit the basic MLM, the R-package lme4 (Bates et al., 2015) will be employed, where we will both evaluate restricted maximum likelihood estimation and ordinary maximum likelihood estimation. Extensions of the MLM from the DSEM framework will be fitted using Mplus, version 8.10 (Muthén & Muthén, 1998).

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