

$$\begin{cases} x'=x-ut\\ t'=t \end{cases}$$

$$v' = \frac{dx'}{dt'}$$

$$= \frac{dx - u dt}{dt}$$

$$= \frac{dx}{dt} - u = v - t$$