

TU BERLIN

ADVANCED INFORMATION MANAGEMENT

Homework assignment 1

Programming in Hadoop and Clustering Excercises

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Programming in Hadoop

1. WordCount - "Hello World" of MapReduce

```
package de.tuberlin.dima.aim3.assignment1;
3 import de.tuberlin.dima.aim3.HadoopJob;
4 import org.apache.hadoop.fs.Path;
5 import org.apache.hadoop.io.IntWritable;
6 import org.apache.hadoop.io.Text;
  import org.apache.hadoop.mapreduce.Job;
  import org.apache.hadoop.mapreduce.Mapper;
  import org.apache.hadoop.mapreduce.Reducer;
  import org.apache.hadoop.mapreduce.lib.input.TextInputFormat;
  \frac{import}{org.apache.hadoop.mapreduce.lib.output.TextOutputFormat;\\
  import java.io.IOException;
  import java.util.ArrayList;
14
  import java.util.Arrays;
  import java.util.List;
17 import java.util.Map;
18 import java.util.function.Function;
19 import java.util.regex.Pattern;
  import java.util.stream.StreamSupport;
21
  import static java.util.stream.Collectors.counting;
23
  import static java.util.stream.Collectors.groupingBy;
24
  public class FilteringWordCount extends HadoopJob {
25
26
27
      public int run(String[] args) throws Exception {
28
          Map<String, String> parsedArgs = parseArgs(args);
29
           Path inputPath = new Path(parsedArgs.get("--input"));
           Path\ output Path\ =\ \underline{new}\ Path\ (\,parsed Args.\,get\,(\,"--output\,"\,)\,)\,;
33
           Job wordCount = prepareJob(inputPath, outputPath, TextInputFormat.class,
      FilteringWordCountMapper.class,
                   Text.class, IntWritable.class, WordCountReducer.class, Text.class,
35
      IntWritable.class , TextOutputFormat.class);
36
           wordCount.waitForCompletion(true);
37
38
           return 0;
40
41
      static class FilteringWordCountMapper extends Mapper<Object, Text, Text,
42
      IntWritable> {
43
           private ArrayList<String> filterList = new ArrayList<>();
44
45
46
            * Method to add words that should be filtered out.
47
            * @param fl : the list with filtered words
           public void addWordsToFilter(List<String> fl) {
51
               this.filterList.addAll(fl);
52
53
54
           public List getFilterList() {
               return this.filterList;
56
57
58
```

```
60
                                protected void map(Object key, Text line, Context ctx) throws IOException,
61
                  InterruptedException {
                                            String[] filterList = {"to", "and", "in", "the"};
62
                                            addWordsToFilter(Arrays.asList(filterList));
63
                                            Pattern.compile(" ").splitAsStream(line.toString().replace(",", "")).map(
                  String :: toLowerCase).\ filter (1 \rightarrow ! getFilterList().contains(1)).\ collect(groupingBy(light)) = (1 - light) + (2 - light) +
                  Function.identity(), counting())).forEach((word, count) -> writeToCtx(word, count,
                  ctx));
65
66
                                private void writeToCtx(String word, Long val, Context ctx) {
67
68
                                                        ctx.write(new Text(word), new IntWritable(val.intValue()));
69
                                            } catch (InterruptedException | IOException ignored) {
70
71
72
                                }
73
74
                   }
75
                    static class WordCountReducer extends Reducer < Text, IntWritable, Text, IntWritable >
77
                     {
78
                                @Override
79
                                protected void reduce (Text key, Iterable < IntWritable > values, Context ctx)
                                                        throws IOException, InterruptedException {
81
82
                                            ctx.write(key, new IntWritable(StreamSupport.stream(values.spliterator(),
83
                   false ) . mapToInt(IntWritable :: get ) . sum()));
84
85
86
87
88
```

Listing 1: FilteringWordCount.java

```
1 16/06/08 23:46:45 WARN mapred. JobClient: Use GenericOptionsParser for parsing the
      arguments. Applications should implement Tool for the same.
  16/06/08 23:46:45 WARN mapred. Job Client: No job jar file set. User classes may not be
      found. See JobConf(Class) or JobConf#setJar(String).
3 16/06/08 23:46:45 INFO input. FileInputFormat: Total input paths to process: 1
4 16/06/08 23:46:45 INFO mapred. JobClient: Running job: job_local_0001
_{5} 16/06/08 23:46:45 INFO mapred.MapTask: io.sort.mb = 100
616/06/0823:46:45 INFO mapred.MapTask: data buffer = 79691776/99614720
7 \cdot 16/06/08 \cdot 23:46:45 INFO mapred.MapTask: record buffer = 262144/327680
8 16/06/08 23:46:45 INFO mapred.MapTask: Starting flush of map output
9 16/06/08 23:46:45 WARN util. NativeCodeLoader: Unable to load native-hadoop library for
      your platform... using builtin-java classes where applicable
10 16/06/08 23:46:45 INFO compress.CodecPool: Got brand-new compressor
11 16/06/08 23:46:45 INFO mapred.MapTask: Finished spill 0
12 \ 16/06/08 \ 23:46:45 \ INFO \ mapred. Task: Task: attempt_local_0001_m_0000000_0 \ is \ done. And is local_0001_m_0000000_0 \ is \ done.
      in the process of commiting
13 16/06/08 23:46:46 INFO mapred. JobClient: map 0% reduce 0%
14 \frac{16}{06} \frac{0}{08} 23:46:48 INFO mapred. LocalJobRunner:
15 16/06/08 23:46:48 INFO mapred. Task: Task 'attempt_local_0001_m_000000_0' done.
16 16/06/08 23:46:48 INFO mapred. LocalJobRunner:
17 \ 16/06/08 \ 23:46:48 INFO mapred.Merger: Merging 1 sorted segments
18 16/06/08 23:46:48 INFO compress.CodecPool: Got brand-new decompressor
  16/06/08 23:46:48 INFO mapred. Merger: Down to the last merge-pass, with 1 segments left
       of total size: 80 bytes
20\ 16/06/08\ 23{:}46{:}48\ INFO\ mapred.LocalJobRunner:
  16/06/08 23:46:48 INFO mapred.Task: Task:attempt_local_0001_r_0000000_0 is done. And is
      in the process of committing
22 16/06/08 23:46:48 INFO mapred.LocalJobRunner:
```

```
23 16/06/08 23:46:48 INFO mapred. Task: Task attempt_local_0001_r_0000000_0 is allowed to
      commit now
  16/06/08 23:46:48 INFO output.FileOutputCommitter: Saved output of task '
      attempt_local_0001_r_000000_0 ' to /tmp/mahout-FilteringWordCountTest
      -1822392791331859456/output
_{25} 16/06/08 23:46:49 INFO mapred. JobClient: map 100\% reduce 0\%
_{26} 16/06/08 23:46:51 INFO mapred.LocalJobRunner: reduce > reduce
27 16/06/08 23:46:51 INFO mapred. Task: Task 'attempt_local_0001_r_000000_0' done.
28\ 16/06/08\ 23:46:52 INFO mapred. JobClient: map 100\% reduce 100\%
29 16/06/08 23:46:52 INFO mapred. JobClient: Job complete: job_local_0001
30 16/06/08 23:46:52 INFO mapred. JobClient: Counters: 16
  16/06/08 23:46:52 INFO mapred. JobClient:
                                               Map-Reduce Framework
31
32 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Combine output records=0
  16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Spilled Records=34
34 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Map output materialized bytes=84
  16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Reduce input records=17
36 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Reduce output records=9
37 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Map input records=4
38 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 SPLIT_RAW_BYTES=133
39 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Map output records=17
40 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Map output bytes=153
41 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Reduce shuffle bytes=0
42 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Combine input records=0
43 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Reduce input groups=9
44 16/06/08 23:46:52 INFO mapred. JobClient:
                                               File Input Format Counters
45 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Bytes Read=107
46 16/06/08 23:46:52 INFO mapred. JobClient:
                                               FileSystemCounters
47 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 FILE_BYTES_WRITTEN=64694
48 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 FILE_BYTES_READ=672
49 16/06/08 23:46:52 INFO mapred. JobClient:
                                               File Output Format Counters
  16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Bytes Written=78
  Process finished with exit code 0
```

Listing 2: Output FilteringWordCount

2. A custom Writable

```
package de.tuberlin.dima.aim3.assignment1;
  import org.apache.hadoop.hdfs.util.ByteArray;
  import org.apache.hadoop.io.Writable;
6 import java.io.DataInput;
7 import java.io.DataOutput;
  import java.io.IOException;
  import java.util.Arrays;
  public class PrimeNumbersWritable implements Writable {
11
12
      private int[] numbers;
13
14
      public PrimeNumbersWritable() {
          numbers = new int[0];
17
18
      public PrimeNumbersWritable(int... numbers) {
19
           this.numbers = numbers;
21
22
      @Override
23
      public void write(DataOutput out) throws IOException {
24
           out.writeInt(numbers.length);
25
           Arrays.stream(numbers).forEach((v) -> writeToOut(out, v));
26
27
28
      private void writeToOut(DataOutput out, int i) {
```

```
try {
30
                out.writeInt(i);
31
             catch (IOException ignored) {
32
33
34
35
36
       @Override
37
       public void readFields(DataInput in) throws IOException {
38
           int length = in.readInt();
39
40
           int[] temp = new int[length];
41
           for (int i = 0; i < length; i++) {
42
                temp[i] = in.readInt();
43
44
           this. numbers = temp;
45
       }
46
47
       @Override
48
       public boolean equals(Object obj) {
49
           if (obj instanceof PrimeNumbersWritable) {
50
               PrimeNumbersWritable other = (PrimeNumbersWritable) obj;
51
                return Arrays.equals(numbers, other.numbers);
52
53
           return false;
54
       }
       @Override
57
       public int hashCode() {
58
           return Arrays.hashCode(numbers);
59
60
61
```

Listing 3: PrimeNumbersWritable.java

1 Process finished with exit code 0

Listing 4: Output PrimeNumbersWritable

3. Average temperature per month

```
package de.tuberlin.dima.aim3.assignment1;
2
4 import de.tuberlin.dima.aim3.HadoopJob;
5 import org.apache.hadoop.conf.Configuration;
6 import org.apache.hadoop.fs.Path;
7 import org.apache.hadoop.io.DoubleWritable;
  import org.apache.hadoop.io.IntWritable;
  import org.apache.hadoop.io.Text;
  import org.apache.hadoop.mapreduce.Mapper;
  import org.apache.hadoop.mapreduce.Reducer;
11
  import java.io.IOException;
13
  import java.util.Map;
14
15
  import org.apache.hadoop.mapreduce.Job;
  import org.apache.hadoop.mapreduce.lib.input.TextInputFormat;
17
  import org.apache.hadoop.mapreduce.lib.output.TextOutputFormat;
19
  public class AverageTemperaturePerMonth extends HadoopJob {
20
21
      @Override
22
      public int run(String[] args) throws Exception {
23
          Map<String, String> parsedArgs = parseArgs(args);
24
25
          Path inputPath = new Path(parsedArgs.get("--input"));
```

```
Path outputPath = new Path(parsedArgs.get("-output"));
2.7
2.8
           double minimumQuality = Double.parseDouble(parsedArgs.get("-minimumQuality"));
29
30
           \label{eq:continuous_problem} \mbox{Job averageTemperature} = \mbox{prepareJob (inputPath \, , \, outputPath \, , \, TextInputFormat \, .}
31
      class,
                    AverageTemperatureMapper.class, Text.class, IntWritable.class,
32
                    AverageTemperatureReducer.class, Text.class, DoubleWritable.class,
33
                    TextOutputFormat.class);
34
35
           averageTemperature.getConfiguration().set("minimumQuality", String.valueOf(
36
      minimumQuality));
37
           averageTemperature.waitForCompletion(true);
38
39
           return 0;
40
       }
41
42
43
       static class AverageTemperatureMapper extends Mapper<Object, Text, Text,
44
      IntWritable> {
45
46
           @Override
47
           protected void map(Object key, Text line, Context ctx) throws IOException,
48
      InterruptedException {
                Configuration conf = ctx.getConfiguration();
49
                double minimumQuality = Double.parseDouble(conf.get("minimumQuality"));
50
                String l = line.toString();
52
                String [] ls = l.split("\t");
53
                if (minimumQuality <= Double.parseDouble(ls[ls.length - 1])) {
54
                    String K = ls[0] + "\t" + ls[1];
                    ctx.write(new Text(K), new IntWritable(Integer.parseInt(ls[2])));
56
                }
57
58
           }
60
       }
61
62
       static class AverageTemperatureReducer extends Reducer < Text, IntWritable, Text,
63
      DoubleWritable> {
           @Override
64
           protected void reduce (Text key, Iterable < IntWritable > values, Context ctx)
65
                    throws IOException, InterruptedException {
66
                int sum = 0;
67
                int length = 0;
                for (IntWritable value : values) {
69
                    sum += value.get();
                    length++;
71
72
                double average = (double) sum / length;
73
                ctx.write(new Text(key), new DoubleWritable(average));
74
           }
75
76
77
```

Listing 5: AverageTemperaturePerMonth.java

```
    16/06/08 23:57:44 WARN mapred. JobClient: Use GenericOptionsParser for parsing the arguments. Applications should implement Tool for the same.
    16/06/08 23:57:44 WARN mapred. JobClient: No job jar file set. User classes may not be found. See JobConf(Class) or JobConf#setJar(String).
    16/06/08 23:57:44 INFO input. FileInputFormat: Total input paths to process: 1
    16/06/08 23:57:44 INFO mapred. JobClient: Running job: job_local_0001
    16/06/08 23:57:44 INFO mapred. MapTask: io.sort.mb = 100
```

```
6 \cdot 16/06/08 \cdot 23:57:44 INFO mapred. MapTask: data buffer = 79691776/99614720
 7 \cdot 16/06/08 \cdot 23:57:44 INFO mapred.MapTask: record buffer = 262144/327680
 8 16/06/08 23:57:44 INFO mapred.MapTask: Starting flush of map output
 9 16/06/08 23:57:44 WARN util. NativeCodeLoader: Unable to load native-hadoop library for
          your platform... using builtin-java classes where applicable
10 16/06/08 23:57:44 INFO compress.CodecPool: Got brand-new compressor
11 16/06/08 23:57:44 INFO mapred.MapTask: Finished spill 0
12 \ 16/06/08 \ 23:57:44 \ INFO \ mapred. Task: Task: attempt_local_0001_m_0000000_0 \ is \ done. And is local_0001_m_0000000_0 \ is \ done.
          in the process of commiting
13 16/06/08 23:57:45 INFO mapred. JobClient: map 0% reduce 0%
14 \frac{16}{06} \frac{06}{08} \quad 23:57:47 INFO mapred. Local Job Runner:
15 16/06/08 23:57:47 INFO mapred. Task: Task 'attempt_local_0001_m_000000_0' done.
16/06/08 23:57:47 INFO mapred. LocalJobRunner:
17 16/06/08 23:57:47 INFO mapred. Merger: Merging 1 sorted segments
18 16/06/08 23:57:47 INFO compress. CodecPool: Got brand-new decompressor
    16/06/08 23:57:47 INFO mapred.Merger: Down to the last merge-pass, with 1 segments left
            of total size: 14587 bytes
20 \ 16/06/08 \ 23:57:47 \ INFO \ mapred. Local Job Runner:
    16/06/08 23:57:47 INFO mapred. Task: Task: attempt_local_0001_r_0000000_0 is done. And is
          in the process of commiting
\frac{16}{06} \frac{16}{06} \frac{16}{08} \frac{16}{100} \frac{16}{
   16/06/08 23:57:47 INFO mapred.Task: Task attempt_local_0001_r_0000000_0 is allowed to
          commit now
24 16/06/08 23:57:47 INFO output. FileOutputCommitter: Saved output of task '
          attempt_local_0001_r_0000000_0' to /tmp/mahout-AverageTemperaturePerMonthTest
           -2969850880617501696 output
_{25} 16/06/08 23:57:48 INFO mapred. JobClient: map 100\% reduce 0\%
_{26} 16/06/08 23:57:50 INFO mapred.LocalJobRunner: reduce > reduce
27\ 16/06/08\ 23:57:50\ INFO\ mapred. Task:\ Task\ 'attempt_local_0001\_r_000000_0'\ done.
_{28} 16/06/08 23\!:\!57\!:\!51 INFO mapred.JobClient: map 100\% reduce 100\%
29 16/06/08 23:57:51 INFO mapred. JobClient: Job complete: job_local_0001
30 16/06/08 23:57:51 INFO mapred. JobClient: Counters: 16
31 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                Map-Reduce Framework
32 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Combine output records=0
33 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Spilled Records=14988
34 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Map output materialized bytes=14591
35 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Reduce input records=7494
36 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Reduce output records=72
37 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                   Map input records=10000
_{\rm 38} 16/06/08 23\!:\!57\!:\!51 INFO mapred. JobClient:
                                                                                   SPLIT_RAW_BYTES=149
39 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                   Map output records=7494
40 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                   Map output bytes=84301
41 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Reduce shuffle bytes=0
42 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Combine input records=0
43 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Reduce input groups=72
44 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                 File Input Format Counters
45 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Bytes Read=192657
46 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                FileSystemCounters
47 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    FILE_BYTES_WRITTEN=95989
48 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    FILE_BYTES_READ=400317
49 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                 File Output Format Counters
50 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Bytes Written=1769
52 Process finished with exit code 0
```

Listing 6: Output AverageTemperature

Clustering

1. Metrics I

We have 3 points A(4,8), B(9,5) and C(2,2).

The *centroid* is then:

$$(x,y) = \left(\frac{4+9+2}{3}, \frac{8+5+2}{3}\right) = (5,5)$$

We now calculate the error towards the centroid for every point:

A(4,8):

$$\sqrt{(4-5)^2 + (8-5)^2} = \sqrt{10}$$

B(9,5):

$$\sqrt{(9-5)^2 + (5-5)^2} = \sqrt{16} = 4$$

C(2,2):

$$\sqrt{(2-5)^2 + (2-5)^2} = \sqrt{18} = 3 \cdot \sqrt{2}$$

The SSE is then:

$$\sqrt{10}^2 + 4^2 + 3 \cdot \sqrt{2}^2 = 44$$

2. Metrics II

If you partition 3 points into 2 clusters, there's one with one element and one with two. The SSE of 1 point is always 0. So the total SSE is only determined by the SSE of the possible combinations of two points.

$$Centroid((3,0),(0,7)) = (1.5,3.5)$$

$$SSE((3,0),(0,7)) = \sqrt{2.25 + 12.25}^2 + \sqrt{2.25 + 12.25}^2 = 29$$

$$Centroid(((0,7),(6,5)) = (3,6)$$

$$SSE(((0,7),(6,5)) = \sqrt{9+1}^2 + \sqrt{9+1}^2 = 20$$

$$Centroid((3,0),(6,5)) = (4.5,2.5)$$

$$SSE((3,0),(6,5)) = \sqrt{2.25 + 6.25}^2 + \sqrt{2.25 + 6.25}^2 = 17$$

The SSE is the smallest in the last configuration therefore the most optimal split in two groups is the following:

Cluster 1: [(0,7)]

Cluster 2: [(3,0),(6,5)]

3. CURE Algorithm

x = (0,0); y = (10,10), a = (1,6); b = (3,7); c = (4,3); d = (7,7), e = (8,2); f = (9,5) As was stated in the question, the two furthest points are x and y. So we start by calculating the distance to them.

D(.,.)	a	b	c	d	е	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
у	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$

Of all the points the minimum value for e is a maximum, so e is added first. \rightarrow (b) is false.

Now we do the same again for e:

D(.,.)	a	b	с	d	е	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
У	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$
е	$\sqrt{65}$	$\sqrt{50}$	$\sqrt{17}$	$\sqrt{26}$	///	$\sqrt{10}$

Of all the points the minimum value for b is a maximum, so b is added next. \rightarrow (d) is true.

We calculate the distance w.r.t. b:

D(.,.)	a	b	c	d	e	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
У	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$
е	$\sqrt{65}$	$\sqrt{50}$	$\sqrt{17}$	$\sqrt{26}$	///	$\sqrt{10}$
b	$\sqrt{5}$	///	$\sqrt{17}$	$\sqrt{16}$	$\sqrt{50}$	$\sqrt{40}$

Of all the points the minimum value for c is a maximum, so c is added third. \rightarrow (a) and (c) are false.

We calculate the distance w.r.t. c:

D(.,.)	a	b	c	d	е	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
У	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$
e	$\sqrt{65}$	$\sqrt{50}$	$\sqrt{17}$	$\sqrt{26}$	///	$\sqrt{10}$
b	$\sqrt{5}$	///	$\sqrt{17}$	$\sqrt{16}$	$\sqrt{50}$	$\sqrt{40}$
С	$\sqrt{18}$	$\sqrt{17}$	///	5	$\sqrt{17}$	$\sqrt{29}$

Of all the points the minimum value for d is a maximum, so d is added fourth.

We calculate the distance w.r.t. d:

D(.,.)	a	b	c	d	e	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
У	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$
e	$\sqrt{65}$	$\sqrt{50}$	$\sqrt{17}$	$\sqrt{26}$	///	$\sqrt{10}$
b	$\sqrt{5}$	///	$\sqrt{17}$	4	$\sqrt{50}$	$\sqrt{40}$
c	$\sqrt{18}$	$\sqrt{17}$	///	5	$\sqrt{17}$	$\sqrt{29}$
d	$\sqrt{37}$	$\sqrt{16}$	$\sqrt{17}$	///	$\sqrt{26}$	$\sqrt{8}$

Of all the points, now the minimum value for f is a maximum, so f is added fifth. Obviously a is added as last.

4. A Comparative Analysis of Clustering Algorithms

	K-Means	CURE: Clustering Using Representatives	BIRCH: Balanced Iterative Reducing and Clustering using Hierarchies	DBSCAN: Density-based Spatial Clustering of Applications with Noise
Type	Partitioning methodPoint assignment	PartitioningHierarchical methodRandom sampling	Hierarchical method	Density-based method
Space complexity	5	$\mathcal{O}(n)$	A little more than one scan of the data, i.e. almost linear.	$\mathcal{O}(n)$
Time complexity	$\mathcal{O}(kind)$ with i number of iterations, n number of points, k number of clusters and d the dimensionality of the data.	$\mathcal{O}(n^2 \log n)$ if the dimensionality is low it reduces to $\mathcal{O}(n^2)$	$\mathcal{O}(n^2)$	• $\mathcal{O}(n \log n)$: with KD-trees • $\mathcal{O}(n^2)$: without KD-trees
Applicability	Easy and simple to implement. You get pure subclusters if specify a high enough number of clusters	5	Does not require whole data set in advance. Can handle noise	5
Limitations	 Does not work for really big datasets. Some optimisation is needed then. Cannot handle outliers 	5	Cannot correct erroneous merges or splits	5

References

- [1] Hendrik Blockeel. "Machine Learning and Inductive Inference". In: ACCO Leuven (2010).
- [2] Martin Ester et al. "A density-based algorithm for discovering clusters in large spatial databases with noise." In: *Kdd.* Vol. 96. 34. 1996, pp. 226–231.
- [3] Sudipto Guha, Rajeev Rastogi, and Kyuseok Shim. "CURE: an efficient clustering algorithm for large databases". In: *ACM SIGMOD Record.* Vol. 27. 2. ACM. 1998, pp. 73–84.
- [4] k-means clustering Wikipedia, the free encyclopedia. https://en.wikipedia.org/wiki/K-means_clustering. Accessed: June 2016.