

TU BERLIN

ADVANCED INFORMATION MANAGEMENT

Homework assignment 1

Programming in Hadoop and Clustering Excercises

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Programming in Hadoop

1. WordCount - "Hello World" of MapReduce

```
package de.tuberlin.dima.aim3.assignment1;
3 import de.tuberlin.dima.aim3.HadoopJob;
4 import org.apache.hadoop.fs.Path;
5 import org.apache.hadoop.io.IntWritable;
6 import org.apache.hadoop.io.Text;
  import org.apache.hadoop.mapreduce.Job;
  import org.apache.hadoop.mapreduce.Mapper;
  import org.apache.hadoop.mapreduce.Reducer;
  import org.apache.hadoop.mapreduce.lib.input.TextInputFormat;
  \frac{import}{org.apache.hadoop.mapreduce.lib.output.TextOutputFormat;\\
  import java.io.IOException;
  import java.util.ArrayList;
14
  import java.util.Arrays;
  import java.util.List;
17 import java.util.Map;
18 import java.util.function.Function;
19 import java.util.regex.Pattern;
  import java.util.stream.StreamSupport;
21
  import static java.util.stream.Collectors.counting;
23
  import static java.util.stream.Collectors.groupingBy;
24
  public class FilteringWordCount extends HadoopJob {
25
26
27
       public int run(String[] args) throws Exception {
28
          Map<String, String> parsedArgs = parseArgs(args);
29
           Path inputPath = new Path(parsedArgs.get("--input"));
           Path\ output Path\ =\ \underline{new}\ Path\ (\,parsed Args.\,get\,(\,"--output\,"\,)\,)\,;
33
           Job wordCount = prepareJob(inputPath, outputPath, TextInputFormat.class,
      FilteringWordCountMapper.class,
                   Text.class, IntWritable.class, WordCountReducer.class, Text.class,
35
      IntWritable.class , TextOutputFormat.class);
36
           wordCount.waitForCompletion(true);
37
38
           return 0;
40
41
      static class FilteringWordCountMapper extends Mapper<Object, Text, Text,
42
      IntWritable> {
43
           private ArrayList < String > filterList = new ArrayList <>();
44
45
46
            * Method to add words that should be filtered out.
47
            * @param fl : the list with filtered words
           public void addWordsToFilter(List<String> fl) {
51
               this.filterList.addAll(fl);
52
53
54
           public List getFilterList() {
               return this.filterList;
56
57
58
```

```
60
                                protected void map(Object key, Text line, Context ctx) throws IOException,
61
                  InterruptedException {
                                            String[] filterList = {"to", "and", "in", "the"};
62
                                            addWordsToFilter(Arrays.asList(filterList));
63
                                            Pattern.compile(" ").splitAsStream(line.toString().replace(",", "")).map(
                  String :: toLowerCase).\ filter (1 \rightarrow ! getFilterList().contains(1)).\ collect(groupingBy(light)) = (1 - light) + (2 - light) +
                  Function.identity(), counting())).forEach((word, count) -> writeToCtx(word, count,
                  ctx));
65
66
                                private void writeToCtx(String word, Long val, Context ctx) {
67
68
                                                        ctx.write(new Text(word), new IntWritable(val.intValue()));
69
                                            } catch (InterruptedException | IOException ignored) {
70
71
72
                                }
73
74
                   }
75
                    static class WordCountReducer extends Reducer < Text, IntWritable, Text, IntWritable >
77
                     {
78
                                @Override
79
                                protected void reduce (Text key, Iterable < IntWritable > values, Context ctx)
                                                        throws IOException, InterruptedException {
81
82
                                            ctx.write(key, new IntWritable(StreamSupport.stream(values.spliterator(),
83
                   false ) . mapToInt(IntWritable :: get ) . sum()));
84
85
86
87
88
```

Listing 1: FilteringWordCount.java

```
1 16/06/08 23:46:45 WARN mapred. JobClient: Use GenericOptionsParser for parsing the
      arguments. Applications should implement Tool for the same.
  16/06/08 23:46:45 WARN mapred. Job Client: No job jar file set. User classes may not be
      found. See JobConf(Class) or JobConf#setJar(String).
3 16/06/08 23:46:45 INFO input. FileInputFormat: Total input paths to process: 1
4 16/06/08 23:46:45 INFO mapred. JobClient: Running job: job_local_0001
_{5} 16/06/08 23:46:45 INFO mapred.MapTask: io.sort.mb = 100
616/06/0823:46:45 INFO mapred.MapTask: data buffer = 79691776/99614720
7 \cdot 16/06/08 \cdot 23:46:45 INFO mapred.MapTask: record buffer = 262144/327680
8 16/06/08 23:46:45 INFO mapred.MapTask: Starting flush of map output
9 16/06/08 23:46:45 WARN util. NativeCodeLoader: Unable to load native-hadoop library for
      your platform... using builtin-java classes where applicable
10 16/06/08 23:46:45 INFO compress.CodecPool: Got brand-new compressor
11 16/06/08 23:46:45 INFO mapred.MapTask: Finished spill 0
12 \ 16/06/08 \ 23:46:45 \ INFO \ mapred. Task: Task: attempt_local_0001_m_0000000_0 \ is \ done. And is local_0001_m_0000000_0 \ is \ done.
      in the process of commiting
13 16/06/08 23:46:46 INFO mapred. JobClient: map 0% reduce 0%
14 \frac{16}{06} \frac{06}{08} 23:46:48 INFO mapred LocalJobRunner:
15 16/06/08 23:46:48 INFO mapred. Task: Task 'attempt_local_0001_m_000000_0' done.
16 16/06/08 23:46:48 INFO mapred. LocalJobRunner:
17 \ 16/06/08 \ 23:46:48 INFO mapred.Merger: Merging 1 sorted segments
18 16/06/08 23:46:48 INFO compress.CodecPool: Got brand-new decompressor
  16/06/08 23:46:48 INFO mapred. Merger: Down to the last merge-pass, with 1 segments left
       of total size: 80 bytes
20\ 16/06/08\ 23{:}46{:}48\ INFO\ mapred.LocalJobRunner:
  16/06/08 23:46:48 INFO mapred.Task: Task:attempt_local_0001_r_0000000_0 is done. And is
      in the process of committing
22 16/06/08 23:46:48 INFO mapred.LocalJobRunner:
```

```
23 16/06/08 23:46:48 INFO mapred. Task: Task attempt_local_0001_r_0000000_0 is allowed to
      commit now
  16/06/08 23:46:48 INFO output.FileOutputCommitter: Saved output of task '
      attempt_local_0001_r_000000_0 ' to /tmp/mahout-FilteringWordCountTest
      -1822392791331859456/output
_{25} 16/06/08 23:46:49 INFO mapred. JobClient: map 100\% reduce 0\%
_{26} 16/06/08 23:46:51 INFO mapred. LocalJobRunner: reduce > reduce
27 16/06/08 23:46:51 INFO mapred. Task: Task 'attempt_local_0001_r_000000_0' done.
28\ 16/06/08\ 23:46:52 INFO mapred. JobClient: map 100\% reduce 100\%
29 16/06/08 23:46:52 INFO mapred. JobClient: Job complete: job_local_0001
30 16/06/08 23:46:52 INFO mapred. JobClient: Counters: 16
  16/06/08 23:46:52 INFO mapred. JobClient:
                                               Map-Reduce Framework
31
32 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Combine output records=0
  16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Spilled Records=34
34 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Map output materialized bytes=84
  16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Reduce input records=17
36 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Reduce output records=9
37 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Map input records=4
38 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 SPLIT_RAW_BYTES=133
39 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Map output records=17
40 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Map output bytes=153
41 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Reduce shuffle bytes=0
42 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Combine input records=0
43 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Reduce input groups=9
44 16/06/08 23:46:52 INFO mapred. JobClient:
                                               File Input Format Counters
45 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Bytes Read=107
46 16/06/08 23:46:52 INFO mapred. JobClient:
                                               FileSystemCounters
47 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 FILE_BYTES_WRITTEN=64694
48 16/06/08 23:46:52 INFO mapred. JobClient:
                                                 FILE_BYTES_READ=672
49 16/06/08 23:46:52 INFO mapred. JobClient:
                                               File Output Format Counters
  16/06/08 23:46:52 INFO mapred. JobClient:
                                                 Bytes Written=78
  Process finished with exit code 0
```

Listing 2: Output FilteringWordCount

2. A custom Writable

```
package de.tuberlin.dima.aim3.assignment1;
  import org.apache.hadoop.hdfs.util.ByteArray;
  import org.apache.hadoop.io.Writable;
6 import java.io.DataInput;
7 import java.io.DataOutput;
  import java.io.IOException;
  import java.util.Arrays;
  public class PrimeNumbersWritable implements Writable {
11
12
      private int[] numbers;
13
14
      public PrimeNumbersWritable() {
          numbers = new int[0];
17
18
      public PrimeNumbersWritable(int... numbers) {
19
           this.numbers = numbers;
21
22
      @Override
23
      public void write(DataOutput out) throws IOException {
24
           out.writeInt(numbers.length);
25
           Arrays.stream(numbers).forEach((v) -> writeToOut(out, v));
26
27
28
      private void writeToOut(DataOutput out, int i) {
```

```
try {
30
                out.writeInt(i);
31
             catch (IOException ignored) {
32
33
34
35
36
       @Override
37
       public void readFields(DataInput in) throws IOException {
38
           int length = in.readInt();
39
40
           int[] temp = new int[length];
41
           for (int i = 0; i < length; i++) {
42
                temp[i] = in.readInt();
43
44
           this. numbers = temp;
45
       }
46
47
       @Override
48
       public boolean equals(Object obj) {
49
           if (obj instanceof PrimeNumbersWritable) {
50
               PrimeNumbersWritable other = (PrimeNumbersWritable) obj;
51
                return Arrays.equals(numbers, other.numbers);
52
53
           return false;
54
       }
       @Override
57
       public int hashCode() {
58
           return Arrays.hashCode(numbers);
59
60
61
```

Listing 3: PrimeNumbersWritable.java

1 Process finished with exit code 0

Listing 4: Output PrimeNumbersWritable

3. Average temperature per month

```
package de.tuberlin.dima.aim3.assignment1;
2
4 import de.tuberlin.dima.aim3.HadoopJob;
5 import org.apache.hadoop.conf.Configuration;
6 import org.apache.hadoop.fs.Path;
7 import org.apache.hadoop.io.DoubleWritable;
  import org.apache.hadoop.io.IntWritable;
  import org.apache.hadoop.io.Text;
  import org.apache.hadoop.mapreduce.Mapper;
  import org.apache.hadoop.mapreduce.Reducer;
11
  import java.io.IOException;
13
  import java.util.Map;
14
15
  import org.apache.hadoop.mapreduce.Job;
  import org.apache.hadoop.mapreduce.lib.input.TextInputFormat;
17
  import org.apache.hadoop.mapreduce.lib.output.TextOutputFormat;
19
  public class AverageTemperaturePerMonth extends HadoopJob {
20
21
      @Override
22
      public int run(String[] args) throws Exception {
23
          Map<String, String> parsedArgs = parseArgs(args);
24
25
          Path inputPath = new Path(parsedArgs.get("--input"));
```

```
Path outputPath = new Path(parsedArgs.get("-output"));
2.7
2.8
           double minimumQuality = Double.parseDouble(parsedArgs.get("-minimumQuality"));
29
30
           \label{eq:continuous_problem} \mbox{Job averageTemperature} = \mbox{prepareJob (inputPath \, , \, outputPath \, , \, TextInputFormat \, .}
31
      class,
                    AverageTemperatureMapper.class, Text.class, IntWritable.class,
32
                    AverageTemperatureReducer.class, Text.class, DoubleWritable.class,
33
                    TextOutputFormat.class);
34
35
           averageTemperature.getConfiguration().set("minimumQuality", String.valueOf(
36
      minimumQuality));
37
           averageTemperature.waitForCompletion(true);
38
39
           return 0;
40
       }
41
42
43
       static class AverageTemperatureMapper extends Mapper<Object, Text, Text,
44
      IntWritable> {
45
46
           @Override
47
           protected void map(Object key, Text line, Context ctx) throws IOException,
48
      InterruptedException {
                Configuration conf = ctx.getConfiguration();
49
                double minimumQuality = Double.parseDouble(conf.get("minimumQuality"));
50
                String l = line.toString();
52
                String [] ls = 1.split("\t");
53
                if (minimumQuality <= Double.parseDouble(ls[ls.length - 1])) {
54
                    String K = ls[0] + "\t" + ls[1];
                    ctx.write(new Text(K), new IntWritable(Integer.parseInt(ls[2])));
56
                }
57
58
           }
60
       }
61
62
       static class AverageTemperatureReducer extends Reducer < Text, IntWritable, Text,
63
      DoubleWritable> {
           @Override
64
           protected void reduce (Text key, Iterable < IntWritable > values, Context ctx)
65
                    throws IOException, InterruptedException {
66
                int sum = 0;
67
                int length = 0;
                for (IntWritable value : values) {
69
                    sum += value.get();
                    length++;
71
72
                double average = (double) sum / length;
73
                ctx.write(new Text(key), new DoubleWritable(average));
74
           }
75
76
77
```

Listing 5: AverageTemperaturePerMonth.java

```
    16/06/08 23:57:44 WARN mapred. JobClient: Use GenericOptionsParser for parsing the arguments. Applications should implement Tool for the same.
    16/06/08 23:57:44 WARN mapred. JobClient: No job jar file set. User classes may not be found. See JobConf(Class) or JobConf#setJar(String).
    16/06/08 23:57:44 INFO input. FileInputFormat: Total input paths to process: 1
    16/06/08 23:57:44 INFO mapred. JobClient: Running job: job_local_0001
    16/06/08 23:57:44 INFO mapred. MapTask: io.sort.mb = 100
```

```
6 \cdot 16/06/08 \cdot 23:57:44 INFO mapred. MapTask: data buffer = 79691776/99614720
 7 \cdot 16/06/08 \cdot 23:57:44 INFO mapred.MapTask: record buffer = 262144/327680
 8 16/06/08 23:57:44 INFO mapred.MapTask: Starting flush of map output
 9 16/06/08 23:57:44 WARN util. NativeCodeLoader: Unable to load native-hadoop library for
          your platform... using builtin-java classes where applicable
10 16/06/08 23:57:44 INFO compress.CodecPool: Got brand-new compressor
11 16/06/08 23:57:44 INFO mapred.MapTask: Finished spill 0
12 \ 16/06/08 \ 23:57:44 \ INFO \ mapred. Task: Task: attempt_local_0001_m_0000000_0 \ is \ done. And is local_0001_m_0000000_0 \ is \ done.
          in the process of commiting
13 16/06/08 23:57:45 INFO mapred. JobClient: map 0% reduce 0%
14 \frac{16}{06} \frac{06}{08} \quad 23:57:47 INFO mapred. Local Job Runner:
15 16/06/08 23:57:47 INFO mapred. Task: Task 'attempt_local_0001_m_000000_0' done.
16/06/08 23:57:47 INFO mapred. LocalJobRunner:
17 16/06/08 23:57:47 INFO mapred. Merger: Merging 1 sorted segments
18 16/06/08 23:57:47 INFO compress. CodecPool: Got brand-new decompressor
    16/06/08 23:57:47 INFO mapred.Merger: Down to the last merge-pass, with 1 segments left
            of total size: 14587 bytes
20 \ 16/06/08 \ 23:57:47 \ INFO \ mapred. Local Job Runner:
    16/06/08 23:57:47 INFO mapred. Task: Task: attempt_local_0001_r_0000000_0 is done. And is
          in the process of commiting
\frac{16}{06} \frac{16}{06} \frac{16}{08} \frac{16}{100} \frac{16}{
   16/06/08 23:57:47 INFO mapred.Task: Task attempt_local_0001_r_0000000_0 is allowed to
          commit now
24 16/06/08 23:57:47 INFO output. FileOutputCommitter: Saved output of task '
          attempt_local_0001_r_0000000_0' to /tmp/mahout-AverageTemperaturePerMonthTest
           -2969850880617501696 output
_{25} 16/06/08 23:57:48 INFO mapred. JobClient: map 100\% reduce 0\%
_{26} 16/06/08 23:57:50 INFO mapred.LocalJobRunner: reduce > reduce
27\ 16/06/08\ 23:57:50\ INFO\ mapred. Task:\ Task\ 'attempt_local_0001\_r_000000_0'\ done.
_{28} 16/06/08 23\!:\!57\!:\!51 INFO mapred.JobClient: map 100\% reduce 100\%
29 16/06/08 23:57:51 INFO mapred. JobClient: Job complete: job_local_0001
30 16/06/08 23:57:51 INFO mapred. JobClient: Counters: 16
31 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                Map-Reduce Framework
32 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Combine output records=0
33 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Spilled Records=14988
34 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Map output materialized bytes=14591
35 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Reduce input records=7494
36 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Reduce output records=72
37 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                   Map input records=10000
_{\rm 38} 16/06/08 23\!:\!57\!:\!51 INFO mapred. JobClient:
                                                                                   SPLIT_RAW_BYTES=149
39 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                   Map output records=7494
40 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                   Map output bytes=84301
41 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Reduce shuffle bytes=0
42 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Combine input records=0
43 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Reduce input groups=72
44 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                 File Input Format Counters
45 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Bytes Read=192657
46 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                FileSystemCounters
47 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    FILE_BYTES_WRITTEN=95989
48 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    FILE_BYTES_READ=400317
49 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                 File Output Format Counters
50 16/06/08 23:57:51 INFO mapred. JobClient:
                                                                                    Bytes Written=1769
52 Process finished with exit code 0
```

Listing 6: Output AverageTemperature

Clustering

1. Metrics I

We have 3 points A(4,8), B(9,5) and C(2,2).

The *centroid* is then:

$$(x,y) = \left(\frac{4+9+2}{3}, \frac{8+5+2}{3}\right) = (5,5)$$

We now calculate the error towards the centroid for every point:

A(4,8):

$$\sqrt{(4-5)^2 + (8-5)^2} = \sqrt{10}$$

B(9,5):

$$\sqrt{(9-5)^2 + (5-5)^2} = \sqrt{16} = 4$$

C(2,2):

$$\sqrt{(2-5)^2 + (2-5)^2} = \sqrt{18} = 3 \cdot \sqrt{2}$$

The SSE is then:

$$\sqrt{10}^2 + 4^2 + 3 \cdot \sqrt{2}^2 = 44$$

2. Metrics II

If you partition 3 points into 2 clusters, there's one with one element and one with two. The SSE of 1 point is always 0. So the total SSE is only determined by the SSE of the possible combinations of two points.

$$Centroid((3,0),(0,7)) = (1.5,3.5)$$

$$SSE((3,0),(0,7)) = \sqrt{2.25 + 12.25}^2 + \sqrt{2.25 + 12.25}^2 = 29$$

$$Centroid(((0,7),(6,5)) = (3,6)$$

$$SSE(((0,7),(6,5)) = \sqrt{9+1}^2 + \sqrt{9+1}^2 = 20$$

$$Centroid((3,0),(6,5)) = (4.5,2.5)$$

$$SSE((3,0),(6,5)) = \sqrt{2.25 + 6.25}^2 + \sqrt{2.25 + 6.25}^2 = 17$$

The SSE is the smallest in the last configuration therefore the most optimal split in two groups is the following:

Cluster 1: [(0,7)]

Cluster 2: [(3,0),(6,5)]

3. CURE Algorithm

x = (0,0); y = (10,10), a = (1,6); b = (3,7); c = (4,3); d = (7,7), e = (8,2); f = (9,5) As was stated in the question, the two furthest points are x and y. So we start by calculating the distance to them.

D(.,.)	a	b	c	d	е	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
у	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$

Of all the points the minimum value for e is a maximum, so e is added first. \rightarrow (b) is false.

Now we do the same again for e:

D(.,.)	a	b	с	d	е	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
У	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$
е	$\sqrt{65}$	$\sqrt{50}$	$\sqrt{17}$	$\sqrt{26}$	///	$\sqrt{10}$

Of all the points the minimum value for b is a maximum, so b is added next. \rightarrow (d) is true.

We calculate the distance w.r.t. b:

D(.,.)	a	b	c	d	e	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
У	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$
е	$\sqrt{65}$	$\sqrt{50}$	$\sqrt{17}$	$\sqrt{26}$	///	$\sqrt{10}$
b	$\sqrt{5}$	///	$\sqrt{17}$	$\sqrt{16}$	$\sqrt{50}$	$\sqrt{40}$

Of all the points the minimum value for c is a maximum, so c is added third. \rightarrow (a) and (c) are false.

We calculate the distance w.r.t. c:

D(.,.)	a	b	c	d	е	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
У	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$
e	$\sqrt{65}$	$\sqrt{50}$	$\sqrt{17}$	$\sqrt{26}$	///	$\sqrt{10}$
b	$\sqrt{5}$	///	$\sqrt{17}$	$\sqrt{16}$	$\sqrt{50}$	$\sqrt{40}$
С	$\sqrt{18}$	$\sqrt{17}$	///	5	$\sqrt{17}$	$\sqrt{29}$

Of all the points the minimum value for d is a maximum, so d is added fourth.

We calculate the distance w.r.t. d:

D(.,.)	a	b	c	d	e	f
X	$\sqrt{37}$	$\sqrt{58}$	5	$\sqrt{98}$	$\sqrt{68}$	$\sqrt{106}$
У	$\sqrt{97}$	$\sqrt{58}$	$\sqrt{85}$	$\sqrt{18}$	$\sqrt{68}$	$\sqrt{26}$
e	$\sqrt{65}$	$\sqrt{50}$	$\sqrt{17}$	$\sqrt{26}$	///	$\sqrt{10}$
b	$\sqrt{5}$	///	$\sqrt{17}$	4	$\sqrt{50}$	$\sqrt{40}$
c	$\sqrt{18}$	$\sqrt{17}$	///	5	$\sqrt{17}$	$\sqrt{29}$
d	$\sqrt{37}$	$\sqrt{16}$	$\sqrt{17}$	///	$\sqrt{26}$	$\sqrt{8}$

Of all the points, now the minimum value for f is a maximum, so f is added fifth. Obviously a is added as last.

4. A Comparative Analysis of Clustering Algorithms

	K-Means	CURE: Clustering Using Representatives	BIRCH: Balanced Iterative Reducing and Clustering using Hierarchies	DBSCAN: Density-based Spatial Clustering of Applications with Noise
Type	Partitioning methodPoint assignment	PartitioningHierarchical methodRandom sampling	Hierarchical method	Density-based method
Space complexity	$\mathcal{O}((n+k)d)$	$\mathcal{O}(n)$	A little more than one scan of the data, i.e. almost linear.	$\mathcal{O}(n)$
Time complexity	$\mathcal{O}(kind)$ with i number of iterations, n number of points, k number of clusters and d the dimensionality of the data.	 \$\mathcal{O}(n^2 \log n)\$ if the dimensionality is low it reduces to \$\mathcal{O}(n^2)\$ 	$\mathcal{O}(n^2)$	• $\mathcal{O}(n \log n)$: with KD-trees • $\mathcal{O}(n^2)$: without KD-trees
Applicability	Easy and simple to implement. You get pure subclusters if specify a high enough number of clusters	 Clusters can have any shape Assumes points are in euclidean space 	Does not require whole data set in advance. Can handle noise	 Can handle clusters of arbitrary size Assumes points are in euclidean space
Limitations	 Does not work for really big datasets. Some optimisation is needed then. Cannot handle outliers K needs to be predetermined 	5	 Cannot identify clusters that have non-spherical shapes Cannot correct erroneous merges or splits 	5

References

- [1] Hendrik Blockeel. "Machine Learning and Inductive Inference". In: ACCO Leuven (2010).
- [2] Clustering Algorithms: K-means. http://www.cs.princeton.edu/courses/archive/spr08/cos435/Class_notes/clustering2_toPost.pdf. Accessed: June 2016.
- [3] Martin Ester et al. "A density-based algorithm for discovering clusters in large spatial databases with noise." In: *Kdd.* Vol. 96. 34. 1996, pp. 226–231.
- [4] Sudipto Guha, Rajeev Rastogi, and Kyuseok Shim. "CURE: an efficient clustering algorithm for large databases". In: *ACM SIGMOD Record*. Vol. 27. 2. ACM. 1998, pp. 73–84.
- [5] k-means clustering Wikipedia, the free encyclopedia. https://en.wikipedia.org/wiki/K-means_clustering. Accessed: June 2016.
- [6] Topic9: Density-based Clustering. https://www.google.de/url?sa=t&rct=j&q=&esrc=s&source=web&cd=3&cad=rja&uact=8&ved=OahUKEwiSxpyT-pvNAhUKWxQKHbcvBVYQFgguMAI&url=http%3A%2F%2Fwww2.cs.uh.edu%2F~ceick%2FML%2FTopic9.ppt&usg=AFQjCNFKy1_wYTyBBIJugNLQWO8plGUgeA&sig2=14LQVkrcFJPbIgGVBiUnsA&bvm=bv.124088155,d.d24. Accessed: June 2016.