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Topic: Multiplying polynomials

Question: Expand the expression.

$$(x + 3)(x + 2)$$

# Answer choices:

- A  $2x^2 + 5x + 5$
- B  $x^2 + 3x + 2$
- C  $x^2 + 5x + 6$
- D  $x^2 + x^2 + 3x + 2x$

# Solution: C

We'll use the FOIL method to expand this, and then we'll simplify.

$$(x + 3)(x + 2)$$

$$(x)(x) + (x)(2) + (3)(x) + (3)(2)$$

$$x^2 + 2x + 3x + 6$$

$$x^2 + 5x + 6$$

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Topic: Multiplying polynomials

Question: Expand the expression.

$$\left(m^{\frac{1}{3}} + y^{-\frac{1}{2}}\right)^2$$

# **Answer choices:**

- A  $m^{\frac{2}{3}} + 2m^{\frac{1}{3}}y^{-\frac{1}{2}} + y^{-1}$
- B  $m^{\frac{1}{3}} + y^{\frac{1}{4}}$
- C  $m^{\frac{2}{3}} + 2m^{\frac{1}{3}}y^{-\frac{1}{2}}y^{-\frac{1}{4}}$
- D m + 2my + y

#### Solution: A

First, we realize that we can rewrite the expression

$$\left(m^{\frac{1}{3}} + y^{-\frac{1}{2}}\right)^2$$

as

$$\left(m^{\frac{1}{3}} + y^{-\frac{1}{2}}\right) \left(m^{\frac{1}{3}} + y^{-\frac{1}{2}}\right)$$

We'll use the FOIL method to expand this, and then we'll simplify.

$$\begin{split} & m^{\frac{1}{3}} \left( m^{\frac{1}{3}} + y^{-\frac{1}{2}} \right) + y^{-\frac{1}{2}} \left( m^{\frac{1}{3}} + y^{-\frac{1}{2}} \right) \\ & m^{\frac{1}{3}} \left( m^{\frac{1}{3}} \right) + m^{\frac{1}{3}} \left( y^{-\frac{1}{2}} \right) + y^{-\frac{1}{2}} \left( m^{\frac{1}{3}} \right) + y^{-\frac{1}{2}} \left( y^{-\frac{1}{2}} \right) \end{split}$$

Remember that when we have something like  $m^{1/3}(m^{1/3})$  or  $y^{-1/2}(y^{-1/2})$  (the first and fourth terms in this expression), we keep the base and add the exponents.

$$\begin{split} & m^{\frac{1}{3}+\frac{1}{3}} + m^{\frac{1}{3}}y^{-\frac{1}{2}} + m^{\frac{1}{3}}y^{-\frac{1}{2}} + y^{-\frac{1}{2}+\left(-\frac{1}{2}\right)} \\ & m^{\frac{2}{3}} + m^{\frac{1}{3}}y^{-\frac{1}{2}} + m^{\frac{1}{3}}y^{-\frac{1}{2}} + y^{-1} \\ & m^{\frac{2}{3}} + 2m^{\frac{1}{3}}y^{-\frac{1}{2}} + y^{-1} \end{split}$$

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Topic: Multiplying polynomials

Question: Simplify the expression.

$$(r-4)(r+3)(2r+5)$$

## Answer choices:

$$A = 2r^3 - 7r^2 - 19r - 60$$

B 
$$2r^3 + 3r^2 - 29r - 60$$

C 
$$2r^3 + 3r^2 - 19r - 60$$

D 
$$2r^3 - 7r^2 - 29r - 60$$

## Solution: B

Given the polynomial,

$$(r-4)(r+3)(2r+5)$$

we'll use the FOIL method on just the first two terms (r-4)(r+3).

$$(r-4)(r+3)$$

$$r^2 + 3r - 4r - 12$$

$$r^2 - r - 12$$

Now we'll bring in the third binomial and multiply this result by (2r + 5).

$$(r^2 - r - 12)(2r + 5)$$

$$r^{2}(2r) - r(2r) - 12(2r) + r^{2}(5) - r(5) - 12(5)$$

$$2r^3 - 2r^2 - 24r + 5r^2 - 5r - 60$$

Collect like terms.

$$2r^3 + 3r^2 - 29r - 60$$