Topic: Dividing multivariable polynomials

Question: Find the quotient.

$$\frac{x^3 + y^3}{x + y}$$

Answer choices:

- $x^2 + xy + y^2$ Α
- $\mathsf{B} \qquad x^2 xy y^2$
- C $x^2 xy + y^2$ D $x^2 + 2xy + y^2$

Solution: C

If we use long division to find the quotient, we get

$$\begin{array}{c}
x^{2} - xy + y^{2} \\
x + y \overline{)x^{3} + 0x^{2}y + 0xy^{2} + y^{3}} \\
-\underline{(x^{3} + x^{2}y)} \\
-x^{2}y + 0xy^{2} \\
-(-x^{2}y - xy^{2}) \\
\underline{(xy^{2} + y^{3})} \\
0
\end{array}$$

Topic: Dividing multivariable polynomials

Question: Find the quotient.

$$\frac{2x^3 + 15yx^2 + 24y^2x - 16y^3}{x + 4y}$$

Answer choices:

- A $2x^2 + 7xy 4y^2$
- B $2x^2 5xy 4y^2$
- C $2x^2 + 3xy 4y^2$
- D $2x^2 4xy 4y^2$

Solution: A

If we use long division to find the quotient, we get

$$\begin{array}{r}
2x^2 + 7xy - 4y^2 \\
x+4y \overline{\smash)2x^3 + 15yx^2 + 24y^2x - 16y^3} \\
-\underline{(2x^3 + 8yx^2)} \\
7yx^2 + 24y^2x \\
-(7yx^2 + 28y^2x) \\
-4y^2x - 16y^3 \\
-(-4y^2x - 16y^3)
\end{array}$$

Topic: Dividing multivariable polynomials

Question: Find the quotient.

$$\frac{3x^3 - 7x^2y - 7xy^2 + 3y^3}{x - 3y}$$

Answer choices:

- A $3x^2 + 2xy 3y^2$
- $\mathsf{B} \qquad 3x^2 2xy 3y^2$
- $C \qquad 3x^2 2xy + y^2$
- D $3x^2 + 2xy y^2$

Solution: D

If we use long division to find the quotient, we get

$$3x^{2}+2xy-y^{2}$$

$$x-3y \overline{)3x^{3}-7x^{2}y-7xy^{2}+3y^{3}}$$

$$-(3x^{3}-9x^{2}y)$$

$$2x^{2}y-7xy^{2}$$

$$-(2x^{2}y-bxy^{2})$$

$$-xy^{2}+3y^{3}$$

$$-(-xy^{2}+3y^{3})$$
0