two\_layer\_nn

February 11, 2024

# 0.1 This is the 2-layer neural network notebook for ECE C147/C247 Homework #3

Please follow the notebook linearly to implement a two layer neural network.

Please print out the notebook entirely when completed.

The goal of this notebook is to give you experience with training a two layer neural network.

```
[143]: import random
  import numpy as np
  from utils.data_utils import load_CIFAR10
  import matplotlib.pyplot as plt

%matplotlib inline
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload\_ext autoreload

## 0.2 Toy example

Before loading CIFAR-10, there will be a toy example to test your implementation of the forward and backward pass. Make sure to read the description of TwoLayerNet class in neural\_net.py file , understand the architecture and initializations

```
[144]: from nndl.neural_net import TwoLayerNet

[145]: # Create a small net and some toy data to check your implementations.
# Note that we set the random seed for repeatable experiments.

input_size = 4
hidden_size = 10
num_classes = 3
num_inputs = 5
```

```
def init_toy_model():
    np.random.seed(0)
    return TwoLayerNet(input_size, hidden_size, num_classes, std=1e-1)

def init_toy_data():
    np.random.seed(1)
    X = 10 * np.random.randn(num_inputs, input_size)
    y = np.array([0, 1, 2, 2, 1])
    return X, y

net = init_toy_model()
X, y = init_toy_data()
```

## 0.2.1 Compute forward pass scores

```
[146]: ## Implement the forward pass of the neural network.
       ## See the loss() method in TwoLayerNet class for the same
       # Note, there is a statement if y is None: return scores, which is why
       # the following call will calculate the scores.
       scores = net.loss(X)
       print('Your scores:')
       print(scores)
       print()
       print('correct scores:')
       correct_scores = np.asarray([
           [-1.07260209, 0.05083871, -0.87253915],
           [-2.02778743, -0.10832494, -1.52641362],
           [-0.74225908, 0.15259725, -0.39578548],
           [-0.38172726, 0.10835902, -0.17328274],
           [-0.64417314, -0.18886813, -0.41106892]])
       print(correct_scores)
       print()
       # The difference should be very small. We get < 1e-7
       print('Difference between your scores and correct scores:')
       print(np.sum(np.abs(scores - correct_scores)))
```

```
Your scores:

[[-1.07260209  0.05083871  -0.87253915]

[-2.02778743  -0.10832494  -1.52641362]

[-0.74225908  0.15259725  -0.39578548]

[-0.38172726  0.10835902  -0.17328274]

[-0.64417314  -0.18886813  -0.41106892]]
```

correct scores:

## 0.2.2 Forward pass loss

```
[147]: loss, _ = net.loss(X, y, reg=0.05)
    correct_loss = 1.071696123862817

# should be very small, we get < 1e-12
    print("Loss:",loss)
    print('Difference between your loss and correct loss:')
    print(np.sum(np.abs(loss - correct_loss)))</pre>
```

Loss: 1.071696123862817 Difference between your loss and correct loss: 0.0

## 0.2.3 Backward pass

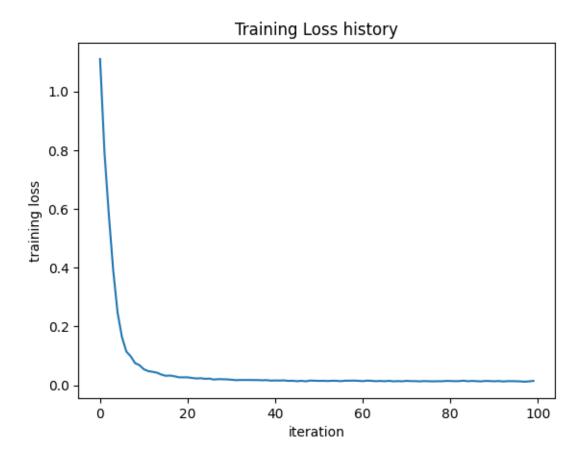
Implements the backwards pass of the neural network. Check your gradients with the gradient check utilities provided.

b2 max relative error: 1.248269635168964e-09 W2 max relative error: 2.96322045694799e-10 b1 max relative error: 3.172679513723066e-09

## 0.2.4 Training the network

Implement neural\_net.train() to train the network via stochastic gradient descent, much like the softmax and SVM.

Final training loss: 0.014497864587765886



## 0.3 Classify CIFAR-10

Do classification on the CIFAR-10 dataset.

```
[150]: from utils.data_utils import load_CIFAR10
       def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1000):
           Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
           it for the two-layer neural net classifier.
           # Load the raw CIFAR-10 data
           cifar10_dir = './cifar-10-batches-py' # remember to use correct path
           X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
           # Subsample the data
           mask = list(range(num_training, num_training + num_validation))
           X_val = X_train[mask]
           y_val = y_train[mask]
           mask = list(range(num_training))
           X_train = X_train[mask]
           y_train = y_train[mask]
           mask = list(range(num_test))
           X_test = X_test[mask]
           y_test = y_test[mask]
           # Normalize the data: subtract the mean image
           mean_image = np.mean(X_train, axis=0)
           X_train -= mean_image
           X val -= mean image
           X_test -= mean_image
           # Reshape data to rows
           X_train = X_train.reshape(num_training, -1)
           X_val = X_val.reshape(num_validation, -1)
           X_test = X_test.reshape(num_test, -1)
           return X_train, y_train, X_val, y_val, X_test, y_test
       # Invoke the above function to get our data.
       X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
       print('Train data shape: ', X_train.shape)
       print('Train labels shape: ', y_train.shape)
       print('Validation data shape: ', X_val.shape)
       print('Validation labels shape: ', y_val.shape)
```

```
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
```

Train data shape: (49000, 3072)
Train labels shape: (49000,)
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)
Test data shape: (1000, 3072)
Test labels shape: (1000,)

## 0.3.1 Running SGD

If your implementation is correct, you should see a validation accuracy of around 28-29%.

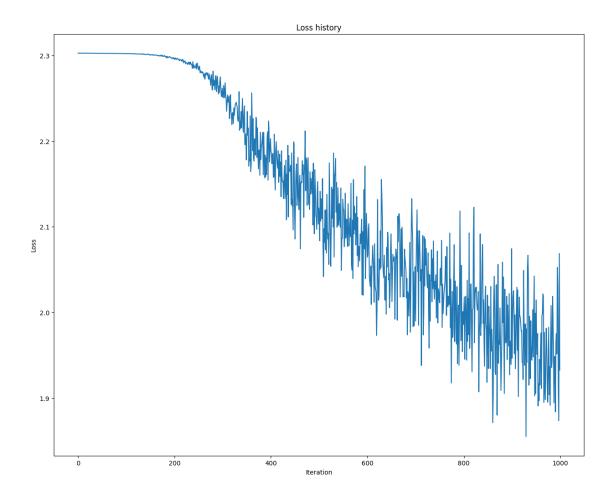
```
iteration 0 / 1000: loss 2.302757518613176
iteration 100 / 1000: loss 2.302120159207236
iteration 200 / 1000: loss 2.2956136007408703
iteration 300 / 1000: loss 2.2518259043164135
iteration 400 / 1000: loss 2.188995235046776
iteration 500 / 1000: loss 2.1162527791897747
iteration 600 / 1000: loss 2.064670827698217
iteration 700 / 1000: loss 1.9901688623083942
iteration 800 / 1000: loss 2.002827640124685
iteration 900 / 1000: loss 1.9465176817856495
Validation accuracy: 0.283
```

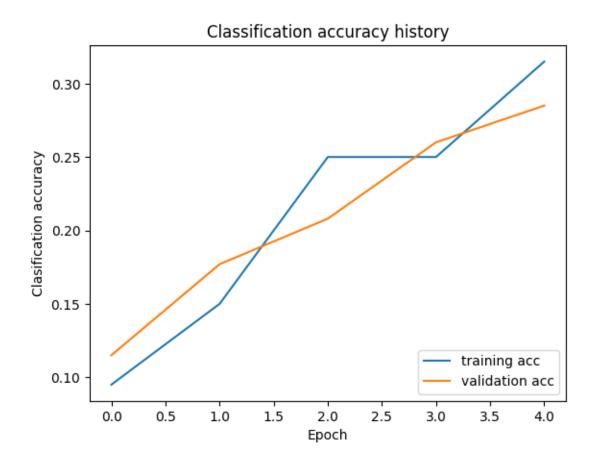
## 0.4 Questions:

The training accuracy isn't great.

- (1) What are some of the reasons why this is the case? Take the following cell to do some analyses and then report your answers in the cell following the one below.
- (2) How should you fix the problems you identified in (1)?

```
[152]: stats['train_acc_history']
[152]: [0.095, 0.15, 0.25, 0.25, 0.315]
[153]: | # ============ #
     # YOUR CODE HERE:
       Do some debugging to gain some insight into why the optimization
     # isn't great.
     # ----- #
     # Plot the loss function and train / validation accuracies
     plt.plot(stats['loss_history'])
     plt.title('Loss history')
     plt.xlabel('Iteration')
     plt.ylabel('Loss')
     plt.gcf().set_size_inches(15, 12)
     plt.show()
     fig, ax = plt.subplots()
     plt.plot(stats['train_acc_history'], label='training acc')
     plt.plot(stats['val_acc_history'], label='validation acc')
     plt.title('Classification accuracy history')
     plt.xlabel('Epoch')
     plt.ylabel('Clasification accuracy')
     plt.legend(loc='lower right')
     plt.show()
     # END YOUR CODE HERE
     # ------ #
```





#### 0.5 Answers:

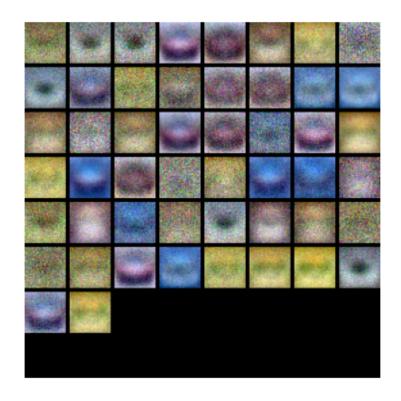
- (1) Both the training and validation accuracy seem to increase every 1000 iterations. Since it doesn't seem like we have overfitting yet (training accuracy increases while validation accuracy decreases), most likely SGD hasn't done enough iterations to find a local minimum.
- (2) We can fix the problems in (1) by optimizing hyperparameters (e.g. learning rate, batch size, etc).

## 0.6 Optimize the neural network

Use the following part of the Jupyter notebook to optimize your hyperparameters on the validation set. Store your nets as best\_net.

```
accuracy you get. Your score on this question will be multiplied by:
      min(floor((X - 28\%)) / \%22, 1)
#
   where if you get 50% or higher validation accuracy, you get full
#
   points.
#
  Note, you need to use the same network structure (keep hidden_size = 50)!
# ------ #
satisfy = 0.5
batches = np.arange(250 , 300, 10).tolist()
learning_rates = (10**np.arange(-3,-2, 0.5)).tolist()
lr_decays = np.arange(0.1,0.3, 0.05).tolist()
flag = False
for batch in batches:
   for learning_rate in learning_rates:
       for lr_decay in lr_decays:
           nn = TwoLayerNet(input_size, hidden_size, num_classes)
           nn.train(X_train, y_train, X_val, y_val,
                    num_iters=2000, batch_size=batch,
                    learning_rate=learning_rate, reg=lr_decay)
           val_acc = (nn.predict(X_val) == y_val).mean()
           print('val acc: ', val_acc,
                 'batch: ', batch,
                 'lr: ', learning_rate,
                 'lr_decay: ', regression)
           if satisfy <= val_acc:</pre>
               print('\nbest val acc: ', val_acc,
                 '\nbest batch: ', batch,
                   '\nnum_iters: ', 2000,
                 '\nbest lr: ', learning_rate,
                 '\nbest lr_decay: ', regression)
               best_net = nn
               flag = True
               break
       if flag:
           break
   if flag:
       break
```

```
# ----- #
      # END YOUR CODE HERE
      val_acc = (best_net.predict(X_val) == y_val).mean()
     print('Validation accuracy: ', val_acc)
     val acc: 0.479 batch: 250 lr: 0.001 lr_decay: 0.25000000000000006
     val acc: 0.488 batch: 250 lr: 0.001 lr_decay: 0.2500000000000000
     val acc: 0.499 batch: 250 lr: 0.001 lr decay: 0.25000000000000000
     val acc: 0.502 batch: 250 lr: 0.001 lr_decay: 0.2500000000000000
     best val acc: 0.502
     best batch: 250
     num_iters: 2000
     best lr: 0.001
     best lr_decay: 0.25000000000000006
     Validation accuracy: 0.502
[177]: from utils.vis_utils import visualize_grid
     # Visualize the weights of the network
     def show_net_weights(net):
         W1 = net.params['W1']
         W1 = W1.T.reshape(32, 32, 3, -1).transpose(3, 0, 1, 2)
         plt.imshow(visualize_grid(W1, padding=3).astype('uint8'))
         plt.gca().axis('off')
         plt.show()
     show_net_weights(subopt_net)
     show net weights(best net)
```





### 0.7 Question:

(1) What differences do you see in the weights between the suboptimal net and the best net you arrived at?

## 0.8 Answer:

(1) The suboptimal net's weights all look similar to each other, implying that it hasn't learned too many distinct/discriminating features. The best net we arrived at has pronounced visual features, which means that it has begun to learn discriminating features of the dataset. This makes it more accurate when classifying since we can identify/recognize patterns now.

#### 0.9 Evaluate on test set

```
[179]: test_acc = (best_net.predict(X_test) == y_test).mean()
print('Test accuracy: ', test_acc)
```

Test accuracy: 0.482

# 1 neural\_net.py

```
[]: import numpy as np
     import matplotlib.pyplot as plt
     class TwoLayerNet(object):
       A two-layer fully-connected neural network. The net has an input dimension of
       D, a hidden layer dimension of H, and performs classification over C classes.
       We train the network with a softmax loss function and L2 regularization on the
       weight matrices. The network uses a ReLU nonlinearity after the first fully
       connected layer.
       In other words, the network has the following architecture:
       input - fully connected layer - ReLU - fully connected layer - softmax
       The outputs of the second fully-connected layer are the scores for each class.
       def __init__(self, input_size, hidden_size, output_size, std=1e-4):
         Initialize the model. Weights are initialized to small random values and
         biases are initialized to zero. Weights and biases are stored in the
         variable self.params, which is a dictionary with the following keys:
         W1: First layer weights; has shape (H, D)
         b1: First layer biases; has shape (H,)
```

```
W2: Second layer weights; has shape (C, H)
  b2: Second layer biases; has shape (C,)
 Inputs:
  - input_size: The dimension D of the input data.
  - hidden_size: The number of neurons H in the hidden layer.
  - output_size: The number of classes C.
  11 11 11
 self.params = {}
 self.params['W1'] = std * np.random.randn(hidden_size, input_size)
 self.params['b1'] = np.zeros(hidden_size)
 self.params['W2'] = std * np.random.randn(output_size, hidden_size)
 self.params['b2'] = np.zeros(output_size)
def loss(self, X, y=None, reg=0.0):
  Compute the loss and gradients for a two layer fully connected neural
  network.
 Inputs:
  - X: Input data of shape (N, D). Each X[i] is a training sample.
  - y: Vector of training labels. y[i] is the label for X[i], and each y[i] is
   an integer in the range 0 \le y[i] \le C. This parameter is optional; if it
   is not passed then we only return scores, and if it is passed then we
   instead return the loss and gradients.
  - reg: Regularization strength.
 Returns:
  If y is None, return a matrix scores of shape (N, C) where scores[i, c] is
  the score for class c on input X[i].
 If y is not None, instead return a tuple of:
  - loss: Loss (data loss and regularization loss) for this batch of training
  - grads: Dictionary mapping parameter names to gradients of those parameters
   with respect to the loss function; has the same keys as self.params.
  # Unpack variables from the params dictionary
 W1, b1 = self.params['W1'], self.params['b1']
 W2, b2 = self.params['W2'], self.params['b2']
 N, D = X.shape
 # Compute the forward pass
 scores = None
  # ------- #
```

```
# YOUR CODE HERE:
  Calculate the output scores of the neural network. The result
# should be (N, C). As stated in the description for this class,
  there should not be a ReLU layer after the second FC layer.
 The output of the second FC layer is the output scores. Do not
 use a for loop in your implementation.
# ------ #
h1 = np.maximum(0, X.dot(W1.T) + b1)
z = h1.dot(W2.T) + b2
scores = z
# END YOUR CODE HERE
# ------ #
# If the targets are not given then jump out, we're done
if v is None:
 return scores
# Compute the loss
loss = None
# ----- #
# YOUR CODE HERE:
# Calculate the loss of the neural network. This includes the
  softmax loss and the L2 regularization for W1 and W2. Store the
# total loss in teh variable loss. Multiply the regularization
# loss by 0.5 (in addition to the factor req).
# ============= #
# scores is num_examples by num_classes
12_{reg} = 0.5 * reg * (np.sum(W1**2) + np.sum(W2**2))
scores = z - np.max(z, axis=1, keepdims=True)
p = np.exp(scores)
p /= np.sum(p, axis=1, keepdims=True)
loss = -np.sum(np.log(p[range(N), y])) / N + 12_reg
# ------ #
# END YOUR CODE HERE
# ------ #
grads = {}
# ------ #
# YOUR CODE HERE:
```

```
Implement the backward pass. Compute the derivatives of the
  # weights and the biases. Store the results in the grads
  # dictionary. e.q., grads['W1'] should store the gradient for
    W1, and be of the same size as W1.
  # ----- #
 one_hot = np.zeros_like(p)
 one_hot[range(N), y] = 1
 dz = (1 / N) * (p - one_hot)
 grads['b2'] = np.sum(dz, axis=0)
 grads['W2'] = dz.T.dot(h1) + reg * W2
 dh1 = dz.dot(W2) * (h1 > 0)
 grads['b1'] = np.sum(dh1, axis=0)
 grads['W1'] = dh1.T.dot(X) + reg * W1
 # ------ #
  # END YOUR CODE HERE
  # ----- #
 return loss, grads
def train(self, X, y, X_val, y_val,
         learning_rate=1e-3, learning_rate_decay=0.95,
         reg=1e-5, num_iters=100,
         batch_size=200, verbose=False):
  11 11 11
  Train this neural network using stochastic gradient descent.
 Inputs:
  - X: A numpy array of shape (N, D) giving training data.
 -y: A numpy array f shape (N,) giving training labels; y[i] = c means that
   X[i] has label c, where 0 \le c \le C.
  - X_val: A numpy array of shape (N_val, D) giving validation data.
  - y_val: A numpy array of shape (N_val,) giving validation labels.
  - learning_rate: Scalar giving learning rate for optimization.
 - learning_rate_decay: Scalar giving factor used to decay the learning rate
   after each epoch.
 - reg: Scalar giving regularization strength.
  - num_iters: Number of steps to take when optimizing.
  - batch_size: Number of training examples to use per step.
  - verbose: boolean; if true print progress during optimization.
 num_train = X.shape[0]
 iterations_per_epoch = max(num_train / batch_size, 1)
```

```
# Use SGD to optimize the parameters in self.model
loss_history = []
train_acc_history = []
val_acc_history = []
for it in np.arange(num_iters):
 X_batch = None
 y_batch = None
 # ----- #
 # YOUR CODE HERE:
 # Create a minibatch by sampling batch_size samples randomly.
 # ----- #
 mask = np.random.choice(num_train, batch_size)
 X_batch = X[mask]
 y_batch = y[mask]
 # ------ #
 # END YOUR CODE HERE
 # ----- #
  # Compute loss and gradients using the current minibatch
 loss, grads = self.loss(X_batch, y=y_batch, reg=reg)
 loss_history.append(loss)
 # ----- #
 # YOUR CODE HERE:
 # Perform a gradient descent step using the minibatch to update
   all parameters (i.e., W1, W2, b1, and b2).
 self.params['W1'] += (-learning_rate * grads['W1'])
 self.params['b1'] += (-learning_rate * grads['b1'])
 self.params['W2'] += (-learning_rate * grads['W2'])
 self.params['b2'] += (-learning_rate * grads['b2'])
 # ------ #
 # END YOUR CODE HERE
 # ----- #
 if verbose and it % 100 == 0:
  print('iteration {} / {}: loss {}'.format(it, num_iters, loss))
 # Every epoch, check train and val accuracy and decay learning rate.
 if it % iterations_per_epoch == 0:
   # Check accuracy
  train_acc = (self.predict(X_batch) == y_batch).mean()
```

```
val_acc = (self.predict(X_val) == y_val).mean()
     train_acc_history.append(train_acc)
     val_acc_history.append(val_acc)
     # Decay learning rate
     learning_rate *= learning_rate_decay
 return {
   'loss_history': loss_history,
   'train_acc_history': train_acc_history,
   'val_acc_history': val_acc_history,
 }
def predict(self, X):
 Use the trained weights of this two-layer network to predict labels for
 data points. For each data point we predict scores for each of the C
 classes, and assign each data point to the class with the highest score.
 Inputs:
 - X: A numpy array of shape (N, D) giving N D-dimensional data points to
   classify.
 Returns:
 - y_pred: A numpy array of shape (N,) giving predicted labels for each of
   the elements of X. For all i, y_pred[i] = c means that X[i] is predicted
   to have class c, where 0 <= c < C.
 11 11 11
 y_pred = None
 # ------ #
 # YOUR CODE HERE:
 # Predict the class given the input data.
 # =========== #
 y_pred = np.zeros(X.shape[1])
 h1 = np.maximum(0, self.params['W1'].dot(X.T).T + self.params['b1'])
 scores = self.params['W2'].dot(h1.T).T + self.params['b2']
 y_pred = np.argmax(scores.T, axis=0)
 # ------ #
 # END YOUR CODE HERE
 # ----- #
 return y_pred
```