GPCW: Gaussian Process for Estimating Crtical Windows of Susceptibility

Statistical Model

$$y_i|\boldsymbol{\beta}, \boldsymbol{\theta} \stackrel{\text{iid}}{\sim} \text{Bernoulli}\left(p_i\left(\boldsymbol{\beta}, \boldsymbol{\theta}\right)\right), \ i=1,...,n;$$

$$\log \left(\frac{p_i\left(\boldsymbol{\beta}, \boldsymbol{\theta}\right)}{1 - p_i\left(\boldsymbol{\beta}, \boldsymbol{\theta}\right)} \right) = \mathbf{x}_i^{\mathrm{T}} \boldsymbol{\beta} + \sum_{j=1}^{m_i} \mathbf{z}_{ij} \theta\left(j\right);$$

$$\boldsymbol{\theta} = \left(\theta\left(1\right),...,\theta\left(m\right)\right)^{\mathrm{T}} | \sigma_{\theta}^{2}, \phi \sim \text{MVN}\left(\mathbf{0}_{m}, \sigma_{\theta}^{2} \Sigma\left(\phi\right)\right)$$

- p: Length of \mathbf{x}_i vector (same for all i)
- $m = \max\{m_i : i = 1, ..., n\}$

Prior Information

$$\beta_j \stackrel{\text{iid}}{\sim} \mathcal{N}\left(0, \sigma_\beta^2\right), \ j = 1, ..., p$$

- Default setting: $\sigma_{\beta}^2 = 10,000$
- $\sigma_{\theta}^2 \sim \text{Inverse Gamma}(\alpha, \beta)$
 - Default setting: $\alpha = 3, \beta = 2$
- $\phi \sim \text{Uniform}\left(a_{\phi}, b_{\phi}\right)$
 - Default setting: $a_{\phi} = d, b_{\phi} = d$

Default Initial Values

$$\beta_j = 0$$
 for all j

$$\theta_j = 0$$
 for all j

$$\sigma_{\theta}^2 = 0.50$$

$$\phi = 0.50$$