

Spillover: Spatial Change Point Estimation Due to Spillover from a Point Source

Spillover_Example

[1] Simulate data from the proposed model:

- Setting the reproducibility seed and initializing packages for data simulation:

```
set.seed(4541)

library(Spillover)
library(geoR) #Spatial covariance functions

## -----
## Analysis of Geostatistical Data
## For an Introduction to geoR go to http://www.leg.ufpr.br/geoR
## geoR version 1.7-5.2.1 (built on 2016-05-02) is now loaded
## -----

library(mnormt) #Multivariate normal distribution
library(boot) #Inverse logit transformation
```

- Setting the global data values:

```
n<-300 #Sample size
m<-100 #Number of unique spatial locations

unique_locations<-matrix(runif(2*m),
                          nrow=m,
                          ncol=2)
ps_location<-unique_locations[1,]
spatial_dists<-as.matrix(dist(unique_locations,
                              diag=TRUE,
                              upper=TRUE))

z<-matrix(0, nrow=n, ncol=m)
distance_to_ps<-rep(0, times=n)
for(j in 1:n){
  loc<-sample(c(1:m),
              size=1)
  if(j <= round(0.10*n)){ #~10% located at the point source
    loc<-1
  }
  z[j, loc]<-1 #Spatial random effect design matrix
  distance_to_ps[j]<-spatial_dists[1, loc]
}

x<-matrix(1, nrow=n, ncol=2)
x[,2]<-rnorm(n) #Covariate design matrix
```

- Setting the values for the statistical model parameters:

```
beta_true<-c(-0.50, 0.30)
lambda_true<-2.00

theta_true<-0.50
x_full_true<-cbind(x,
                   as.numeric(distance_to_ps <= theta_true)*exp(-(distance_to_ps^2)))
```

```

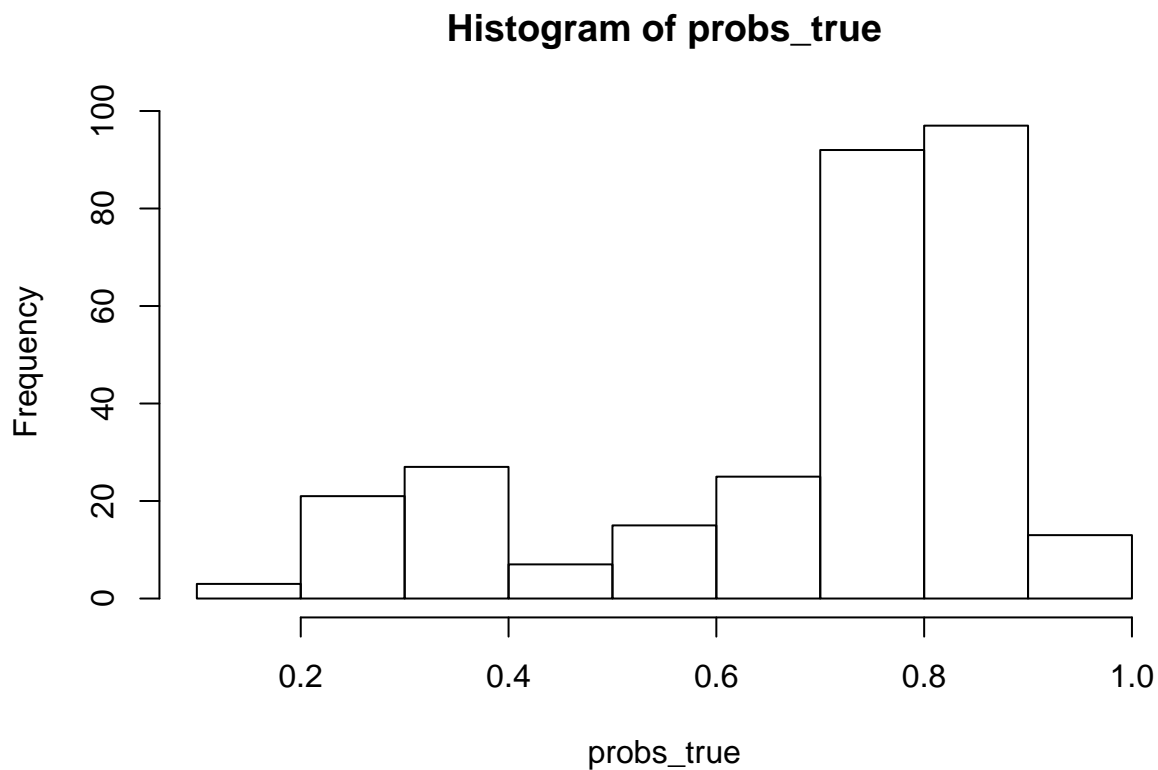
phi_true<-0.70
spatial_corr_true<-spatial_corr<-cov.spatial(spatial_dists,
                                              cov.model="spherical",
                                              cov.pars=c(1, (1/phi_true)))

sigma2_w_true<-0.75
w_true<-c(rmnorm(n=1,
                mean=rep(0, times=m),
                varcov=(sigma2_w_true*spatial_corr_true)))
w_true<-w_true - mean(w_true)

logit_p_true<-x_full_true%%c(beta_true, lambda_true) +
              z%%w_true

probs_true<-inv.logit(logit_p_true)
hist(probs_true)

```



- Simulating the analysis dataset:

```

y<-rbinom(n=n,
          size=1,
          prob=probs_true)

```

[2] Fit Spillover to the Data:

```

results<-Spillover(mcmc_samples = 20000,
                  spillover_covar_def = 3, #1: Change point; 2: Exponential; 3: Gaussian
                  y = y,

```

```

x = x,
distance_to_ps = distance_to_ps,
z = z,
spatial_dists = spatial_dists,
metrop_var_phi_trans = 0.35,
metrop_var_theta_trans = 0.10)

```

```

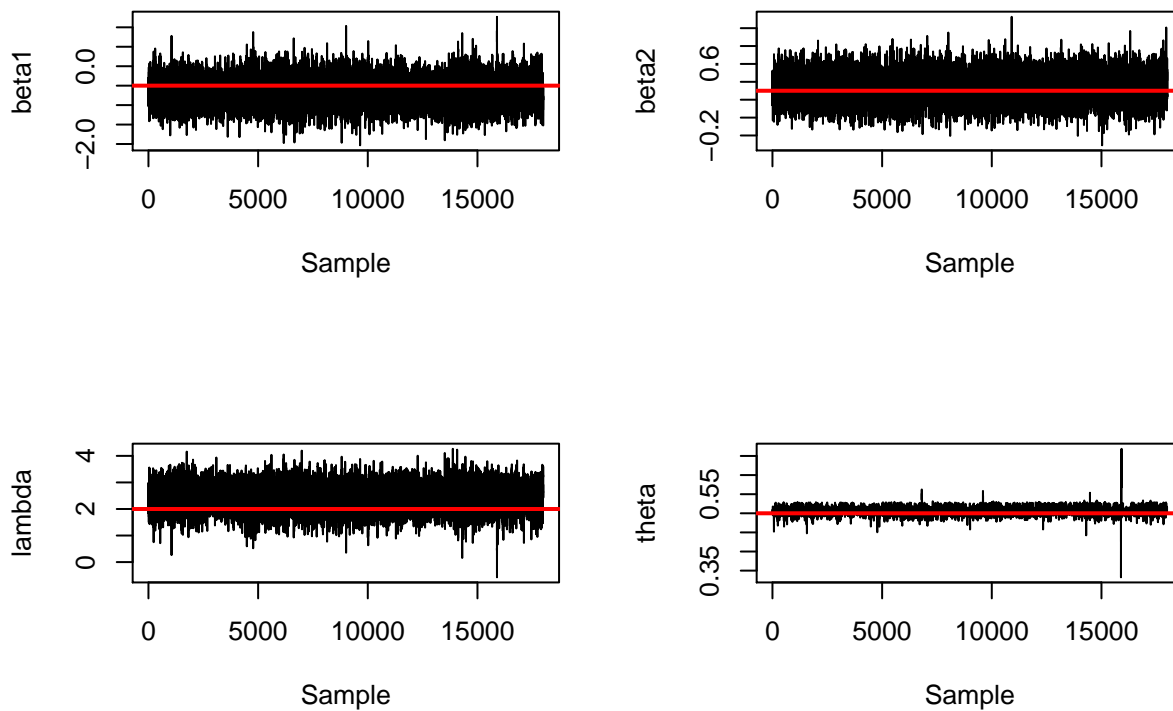
## *****
## Gaussian Spillover
## Progress: 10%
## phi Acceptance: 30%
## theta Acceptance: 22%
## *****
## Gaussian Spillover
## Progress: 20%
## phi Acceptance: 29%
## theta Acceptance: 22%
## *****
## Gaussian Spillover
## Progress: 30%
## phi Acceptance: 28%
## theta Acceptance: 22%
## *****
## Gaussian Spillover
## Progress: 40%
## phi Acceptance: 28%
## theta Acceptance: 23%
## *****
## Gaussian Spillover
## Progress: 50%
## phi Acceptance: 28%
## theta Acceptance: 23%
## *****
## Gaussian Spillover
## Progress: 60%
## phi Acceptance: 28%
## theta Acceptance: 23%
## *****
## Gaussian Spillover
## Progress: 70%
## phi Acceptance: 28%
## theta Acceptance: 22%
## *****
## Gaussian Spillover
## Progress: 80%
## phi Acceptance: 28%
## theta Acceptance: 22%
## *****
## Gaussian Spillover
## Progress: 90%
## phi Acceptance: 28%
## theta Acceptance: 23%
## *****
## Gaussian Spillover

```

```
## Progress: 100%  
## phi Acceptance: 28%  
## theta Acceptance: 22%
```

[3] Analyzing Output:

```
par(mfrow=c(2,2))  
plot(results$beta[1, 2001:20000],  
      type="l",  
      ylab="beta1",  
      xlab="Sample")  
abline(h=beta_true[1],  
       col="red",  
       lwd=2) #True value  
plot(results$beta[2, 2001:20000],  
      type="l",  
      ylab="beta2",  
      xlab="Sample")  
abline(h=beta_true[2],  
       col="red",  
       lwd=2) #True value  
plot(results$lambda[2001:20000],  
      type="l",  
      ylab="lambda",  
      xlab="Sample")  
abline(h=lambda_true,  
       col="red",  
       lwd=2) #True value  
plot(results$theta[2001:20000],  
      type="l",  
      ylab="theta",  
      xlab="Sample")  
abline(h=theta_true,  
       col="red",  
       lwd=2) #True value
```



```
par(mfrow=c(2,2))
plot(results$sigma2_w[2001:20000],
     type="l",
     ylab="sigma2_w",
     xlab="Sample")
abline(h=sigma2_w_true,
      col="red",
      lwd=2) #True value
plot(results$phi[2001:20000],
     type="l",
     ylab="phi",
     xlab="Sample")
abline(h=phi_true,
      col="red",
      lwd=2) #True value
plot(rowMeans(results$w[,2001:20000]), w_true,
     pch=16,
     ylab="True w",
     xlab="Estimated w")
abline(a=0,
      b=1)
```

