



Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich

# Development of an RF resonator for a double junction ion trap

Semester Project

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**Abstract**

In this report I will describe the modeling, designing and testing of an RF helical resonator suitable for delivering RF signal to a double-junction ion trap in a cryogenic environment.

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## Chapter 1

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# Introduction

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Quantum computing is an exciting and rapidly evolving field of modern science. One of the most promising implementations of a quantum computer is based on the ability to control and measure systems of trapped ions. Those ions are typically confined in Paul (RF) [14] traps by applying static and oscillating RF signals to the trap electrodes, which on average generate a confining electric potential.

### 1.1 Why do we need resonators?

One could potentially couple a radio frequency source directly to an ion's trap. However this creates the following challenges:

- noise from the source may contribute to heating of trapped ions [18],
- in order to maintain efficient cryostat cooling the amount of generated heat within it should be minimized. In order to stabilize ions in the ion trap the confining RF signal must have a reasonably high voltage amplitude. An RF resonator close to the signal consumption area allows to reduce the length of an actively heated (with accordance to the Joule–Lenz law [15]) high voltage wire,
- impedance mismatch between source and trap leads to an additional dissipation of RF power.

These issues can be avoided by placing an amplifier close to the Paul trap, which would filter the incoming signal and output it with a voltage suitable for operating the trap. There are two available options: active and passive amplifiers. The core difference between them is that active amplifiers use an additional power source to increase output power of the signal while passive amplifiers rather modify the shape of the input signal conserving the overall power — in our case the voltage amplitude gain is balanced by the current amplitude decline.

## 1.2. Context of this project

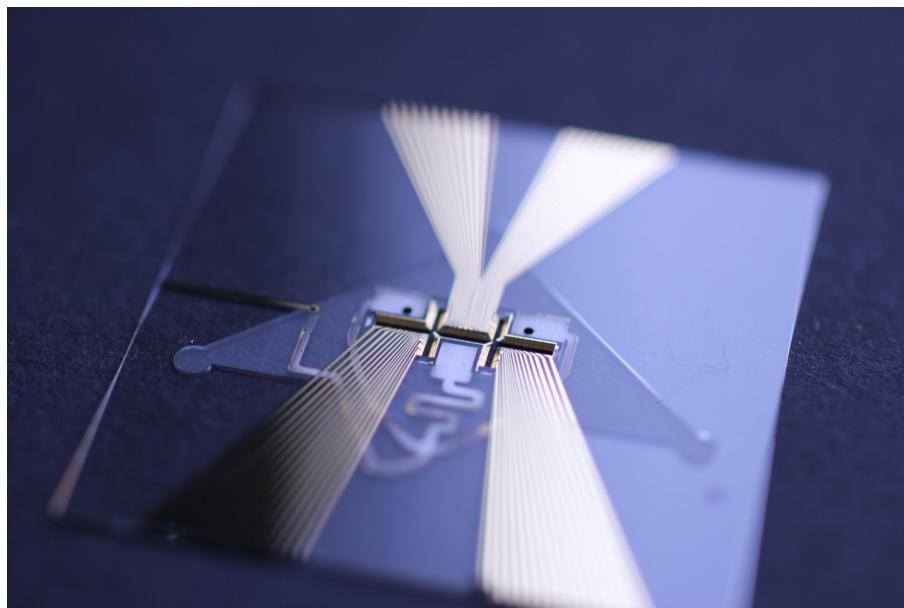
Active amplifiers perform better in terms of voltage gain at room temperatures. However, the aim of this project is to create a resonator used within a cryogenic environment. The properties of transistors powering active amplifiers depend heavily on a combination of densities of free electrons and holes. Lowering the temperature tends to reduce [2] these densities significantly, turning semiconductors at room temperatures into practically dielectrics.

It leaves us with passive amplifiers (resonators).

### **1.2 Context of this project**

This semester project aims to be a part of an attempt to create a scalable quantum computing architecture by Chiara Decaroli. It provides the following benefits compared to existing solutions:

- using subtractive laser writing to manufacture wafers eliminates misalignment effects by allowing a “self assembly” of different wafers,
- double junction ion trap designed for parallel operations, Decoherence Free Subspace (DFS) ion transport across the junctions, and manipulation of long chains of ions,
- potential integrated laser delivery through optical lensed fibers eliminates the need for bulky optics and custom objectives which limit scalability.

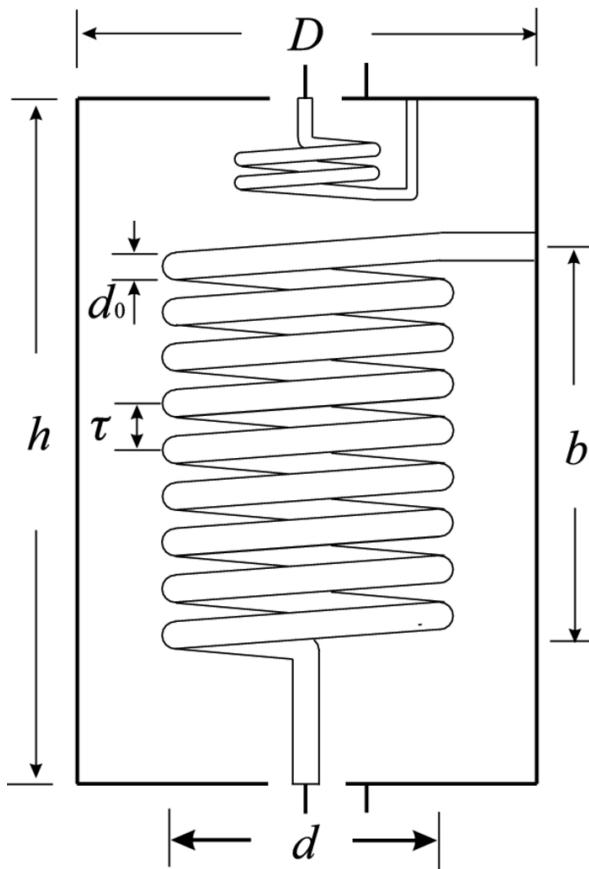


**Figure 11:** Top wafer of the double junction trap

## 1.3 Kinds of resonators

The required frequency of 40 MHz limits our selection to the following types of resonators: helical [6, 7, 19, 10, 9] or, for higher frequencies, coaxial [8], RLC [4, 11, 5], and crystal oscillators. Multiple available solutions require us to do an analysis for a reasoned choice.

### 1.3.1 Helical



**Figure 12:** Schematic diagram of a helical resonator indicating shield diameter  $D$ , shield height  $h$ , coil diameter  $d$ , coil height  $b$ , winding pitch  $\tau$ , and coil wire diameter  $d_0$ . [1]

Helical resonators are commonly selected to be coupled with ion traps due to their high quality factors and ability to operate on high frequencies. It is a perfect option for ion traps operated at room temperatures, since in absence of space constraints they are able to provide  $Q$  values of a couple of thousands. However in order to achieve those  $Q$ , the fabrication process needs to be quite precise to avoid reflections of traveling waves which negatively influence the overall gain.

### 1.3.2 RLC



**Figure 13:** Example of a parallel RLC circuit

RLC amplifiers are a convenient choice for space-bounded environments, such as cryostats. Typical implementation pumps energy between two reactive components — inductor and capacitor. Assembly of RLC circuit is easier than of helical resonator since the physical placement of lumped parts does not influence the resulting quality factor. But it also means that the quality of these components is a major factor for successful creation. Given that units' data sheets rarely provide values for cryogenic or vacuum setup it takes a lot of trial and error to find the right ones [4].

### 1.3.3 Crystal

Unlike helical and RLC resonators, the crystal oscillators do not store energy just in the electric field. This type of resonator utilizes piezoelectric effect to transform applied harmonic voltage into surface mechanical modes and vice versa.

Narrow excitation spectrum is provided by physical dimensions imposing hard constraints on vibrational oscillations and could have made such device an ideal filtering solution for ion traps. Unfortunately, there are some major downsides that seriously limit its applicability:

- after fabrication resonant frequency can not be widely tuned
- limited stability of the crystal does not allow high voltages

### 1.3.4 Choosing the right one

Summarizing constraints for a resonator within the cryostat:

- Helical
  - Max voltage is limited by the size (we want to avoid electrical breakdown between the helix and the shield), generated thermal power (mainly because of the resistance of the solder joints) and the thickness of the coil wire,
  - Max frequency is limited by the manufacturing complexity — high frequencies in small resonators require the coil to be produced from a very thin wire,
  - Resonant frequency tunability depends on the exact design, is typically crude and is achieved by varying capacitive or inductive coupling between the helix and the antenna.
- RLC
  - Max voltage is limited by the quality of components used and generated thermal power,
  - Max frequency is limited by the quality of components used,
  - Resonant frequency can be fine-tuned by using variable electrical components.
- Crystal
  - Max voltage is limited by the mechanical stability of the crystal,
  - Max frequency — no information,
  - Resonant frequency is almost fixed.

Table 11 gives a more visual explanation of above.

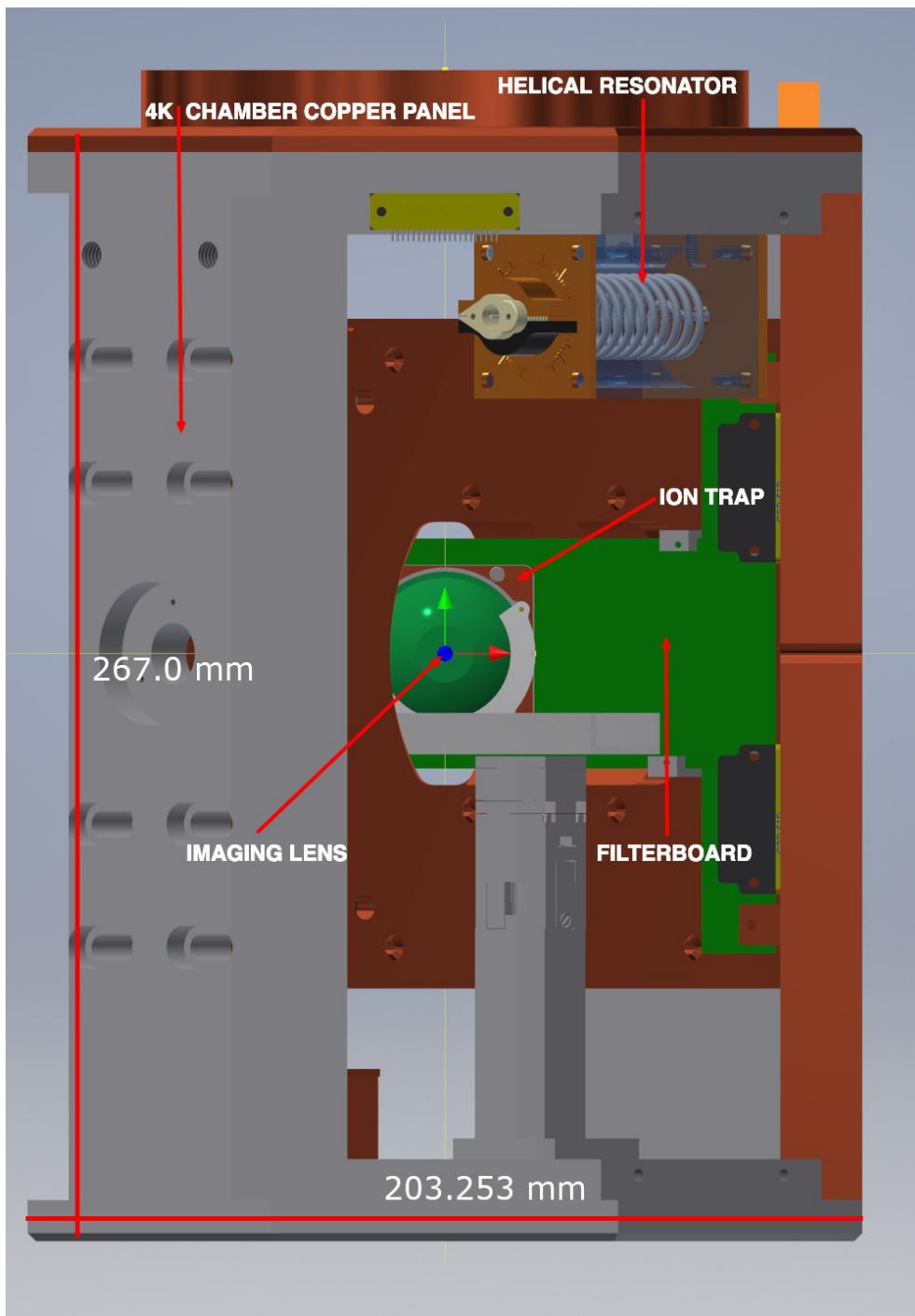
Type	Max voltage	Max frequency	Tunability
Helical	+++	+++	++
RLC	++	++	+++
Crystal	+	?	+

Table 11: Empirical interrelation between parameters of different types of resonators

In our setup, the combination of high voltage and frequency values with our constraints on available space makes helical resonator the optimal option. However, difficulties of assembly do not make it a perfect solution in terms of scalability — for a production-grade setup RLC amplifier might be preferred.

### 1.3. Kinds of resonators

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**Figure 14:** 3D model of the 4K cryostat chamber, design by Roland Matt

## Chapter 2

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# Theory

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### 2.1 What is a resonator?

By resonator we mean a harmonic oscillator within which some quantity varies harmonically with time. In case of a helical resonator an alternating current in electrical circuit periodically transfers the inductive energy stored in a magnetic field of the helix into the capacitive electric field energy between the helix and the shield. When being stimulated by an RF signal with a natural frequency of the system, voltage amplitude grows until the damping mechanisms are strong enough to balance the resonant effect.

### 2.2 Helical resonator models

In order to create a helical resonator satisfying our experimental conditions and limitations we inevitably come to a need for a theoretical model that would be able to predict the essential characteristics of the resulting unit. The following sections aim to provide an overview and comparison between the models.

#### 2.2.1 Macalpine & Schildknecht

A well-known approach [13] for describing helical resonators was introduced in the same year as Richard Feynman's idea [3] to use quantum systems for computations. It was motivated by the possibility to reduce volume compared to TEM-mode coaxial-line resonators (90% volume reduction for the reference case [13]). While skipping a detailed theoretical analysis it nevertheless provides a basis for constructing a resonator: such as regions of usefulness, design considerations and a set of parameters' dependencies maximizing  $Q$ .

## 2.2. Helical resonator models

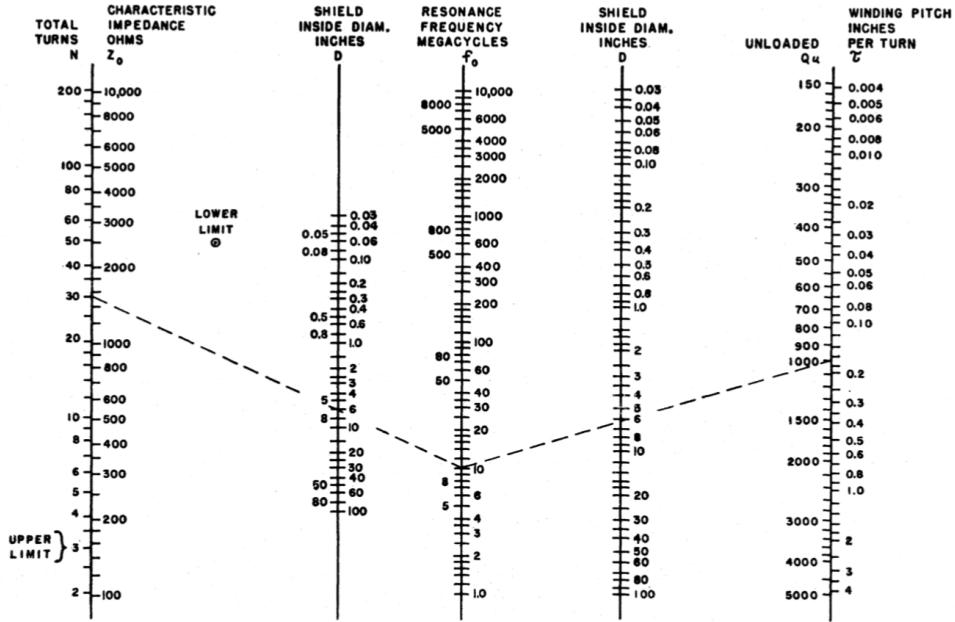


Figure 21: Design chart for quarter-wave helical resonators [13]

While describing essential properties of an unloaded helical quarter-wave resonator, this paper [13] also predicts the shift of resonant frequency if an external load is connected. In order to define a new frequency one can make use of telegraph equations [16] by effectively treating the ion trap as a capacitor.

Important results of [13] can be found in equations 2.1 with parameters named as in the figure 12.

$$\begin{aligned} d/D &= 0.55 \\ b/d &= 1.5 \\ h \approx (b + D/2) \end{aligned} \tag{2.1}$$

### 2.2.2 Sivers et al.

Unfortunately modeling an ion trap as a pure capacitive load is not always accurate. Introducing resistive losses imposes an additional shift of resonant frequency which pushes the deviation from self-resonant frequency even further. It is possible to tune the strength of the inductive coupling between the antenna and the main coil to compensate this shift while losing in efficiency.

These limitations of Macalpine's & Schildknecht's [13] model have been overcome in a newer paper [17] which takes the development of an amplifier, specifically for the needs of quantum computing, one step further. By taking a look at the joint resonator + ion trap system as a whole it aims to

## 2.2. Helical resonator models

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predict the effective  $Q$  and frequency. This model ensures that it's possible to find optimal parameters for given experimental constraints.

While it is heavily recommended to check the original [17] paper to understand the theory behind calculations in appendix B we will provide a short explanation of the exact usage below. All symbols correspond to [17].

In our approach the only varying parameters are the diameter of a shield  $D$  and the diameter of a helix  $d$  with  $\alpha = d/D$ .

Formula for  $Q$  from [17] depends on the inductance of the coil  $L_C$  (2.3), the real part of the total impedance  $Z_{real}$  (2.11) and the target frequency  $\omega_0$  ( $2\pi * 40$  MHz). In the following equations we would expand dependencies until it is possible to express everything through our target and varying parameters.

$$Q = \frac{L_C \omega_0}{Z_{real}} \quad (2.2)$$

Let's start with defining the inductance of the coil  $L_C$ . For a long solenoid as modified by the effect of the shield [13] inductance can be described as linearly dependent on the length of the coil  $b$  (2.4) and a coefficient  $K_{L_c}$  (2.5).

$$L_C = b * K_{L_c} \quad (2.3)$$

The length of the coil  $b$  can be derived [13] from the height  $h$  (56 mm) and the inner diameter  $D$  of the shield. Since  $D$  varies resulting  $b$  might become less than 0 — this case is handled properly in the appendix B.

$$b = h - D/2 \quad (2.4)$$

The coefficient  $K_{L_c}$  depends on the diameter of the helix  $d$ , the inner diameter  $D$  of the shield and the winding pitch  $\tau$  (2.7).

$$K_{L_c} = 39.37 \frac{0.025 d^2 (1 - \alpha^2)}{\tau^2} 10^{-6} \text{ H/m} \quad (2.5)$$

We take  $d_0$  from Macalpine's calculations (see appendix A) and define  $\tau$  as suggested in [13].

$$d_0 = \text{Macalpine's} \quad (2.6)$$

$$\tau = 2 * d_0 \quad (2.7)$$

Looking back at the equation for  $Q$  (2.2) we can see that the only undefined part is  $Z_{real}$  (2.11). Naturally, first we need to define total impedance  $Z_{tot}$  as a sum of the following impedances: coil  $Z_{coil}$  (2.9), equivalent  $Z_E$  (2.10) and resistances: shield  $R_s$  (2.24) and helical coil to shield junction  $R_j$  (2.28).

$$Z_{tot} = Z_{coil} + Z_E + R_s + R_j \quad (2.8)$$

## 2.2. Helical resonator models

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The impedance of the coil is dependent on the coil resistivity  $R_c$  (2.21) and reactances  $X_{L_c}$  (2.12, due to the inductance of the coil) and  $X_{C_c}$  (2.13, due to the the coil self-capacitance).

$$Z_{coil} = \left( (iX_{L_c} + R_c)^{-1} + (X_{C_c}/i)^{-1} \right)^{-1} \quad (2.9)$$

In order to define the equivalent impedance we use the resistance of the ion trap  $R_t$  (expected value of 0.1 Ohm was used) and some reactances, such as  $X_{C_t}$  (2.14, caused by the capacitance of the trap),  $X_{C_w}$  (2.15, caused by the capacitance of the ion trap connecting wires), and  $X_{C_s}$  (2.16, caused by the capacitance between the coil and the shield).

$$Z_E = \left( (X_{C_t}/i + R_t)^{-1} + (X_{C_w}/i)^{-1} + (X_{C_s}/i)^{-1} \right)^{-1} \quad (2.10)$$

By substituting equations 2.9 and 2.10 into 2.8 and extracting the real part we can express  $Z_{real}$ .

$$\begin{aligned} Z_{real} = & \frac{R_c X_{C_c}^2}{R_c^2 + (X_{C_c} - X_{L_c})^2} \\ & + \frac{R_t X_{C_s} X_{C_w}}{R_t^2 (X_{C_s} + X_{C_w})^2 + (X_{C_s} (X_{C_t} + X_{C_w}) + X_{C_t} X_{C_w})^2} \\ & + R_s + R_j \end{aligned} \quad (2.11)$$

Let us expand all reactances of  $Z_{real}$  (2.11). Their definitions would include the target frequency  $\omega_0$ , the inductance of the coil  $L_C$  (2.3) and a group of capacitances: coil self  $C_c$  (2.17), ion trap  $C_t$  (varied parameter of 10, 15, 20 pF), ion trap connecting wires  $C_w$  (expected value of  $1 * 10^{-5}$  pF was used), and coil to shield  $C_s$  (2.18).

$$X_{L_c} = \omega_0 L_C \quad (2.12)$$

$$X_{C_c} = (\omega_0 C_c)^{-1} \quad (2.13)$$

$$X_{C_t} = (\omega_0 C_t)^{-1} \quad (2.14)$$

$$X_{C_w} = (\omega_0 C_w)^{-1} \quad (2.15)$$

$$X_{C_s} = (\omega_0 C_s)^{-1} \quad (2.16)$$

The coil self capacitance  $C_c$  can be calculated as below.

$$C_c = \left( \left( 11.26 \frac{b}{d} \right) + 8 + \left( \frac{27}{\sqrt{b/d}} \right) \right) d \text{ pF} \quad (2.17)$$

## 2.2. Helical resonator models

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In order to express the capacitance between the coil and the shield we use an approach similar to what was used for  $L_C$  (2.3) by introducing a coefficient  $K_{C_s}$  (2.19).

$$C_s = b * K_{C_s} \quad (2.18)$$

The equation for the multiplier  $K_{C_s}$  is shown below.

$$K_{C_s} = 39.37 \frac{0.75}{\log_{10}(D/d)} \text{ pF/m} \quad (2.19)$$

With all capacitances in place the resonant frequency  $\omega_{res}$  can be found. We only use it to determine whether it is close to the target frequency  $\omega_0$  which is actually used in the calculations.

$$\omega_{res} = ((C_s + C_t + C_w + C_c) L_C)^{-1/2} \quad (2.20)$$

In order to complete the derivation of the coil impedance  $Z_{coil}$  (2.9) we need to additionally provide a value for the coil resistance  $R_c$ . It depends on the copper resistivity  $\rho$  ( $1.7 * 10^{-8}$  Ohm\*m), the unwound length of the coil  $l_c$  (2.22), thickness of the coil wire  $d_0$ , and the skin depth of copper  $\delta$  (2.23, since the current would only flow through the skin region).

$$R_c = \frac{\rho l_c}{d_0 \pi \delta} \quad (2.21)$$

From the geometry of the coil we can express the unwound length through the diameter  $d$ , pitch  $\tau$ , and height  $b$ .

$$l_c = 2\pi \sqrt{\left(\frac{d}{2}\right)^2 + \left(\frac{\tau}{2\pi}\right)^2} \frac{b}{\tau} \quad (2.22)$$

Calculations of the skin depth are standard.

$$\delta = \sqrt{\frac{2\rho}{\omega_0 \mu_0}} \quad (2.23)$$

Looking again at the expression for the real part of total impedance  $Z_{real}$  (2.11) we see that the only missing parts are the shield  $R_s$  (2.24) and helical coil to shield junction  $R_j$  (2.28) resistances. Similar to the coil resistance  $R_c$  (2.21) we can define  $R_s$  by accounting for the coil height  $b$  and the "unwound" length  $l_s$  (2.25) that the currents take on the shield inner surface.

$$R_s = \frac{\rho l_s}{b \delta} \quad (2.24)$$

### 2.3. Comparison

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The distance of the path  $l_s$  in the shield is dependent on the number of "turns"  $N_s$  (2.26) the current takes.

$$l_s = N_s \sqrt{\left(\frac{\pi d}{\alpha}\right)^2 + \left(\frac{b}{N_s}\right)^2} \quad (2.25)$$

This number  $N_s$  can be defined as below, with  $r$  (2.27) being the difference between the coil and inner shield radii.

$$N_s = \frac{b l_c}{4\pi r^2} \quad (2.26)$$

Calculations for the difference between radii  $r$  follows naturally from the geometrical considerations.

$$r = \frac{d}{2} (\alpha^{-1} - 1) \quad (2.27)$$

The resistance of the solder joint is dependent on the target frequency  $\omega_0$  with  $3 * 10^{-3}$  Ohm being a typical resistance value for a DC current.

$$R_j = 0.003 \sqrt{\frac{\omega_0}{2\pi 10^5}} \text{ Ohm} \quad (2.28)$$

With these we have everything required for the expression for  $Q$  (2.2).

## 2.3 Comparison

Macalpine's and Schildknecht's [13] model gives insights for designing a helical quarter-wave resonator with a given self-resonant frequency. However major shifts from it can be expected when connecting the ion trap. Sivers' et al. approach [17] investigates connections between various parameters in the total circuit. As a result one could create a resonator which implements a transfer function closer to a desired one. Considering these benefits the Sivers model [17] was selected.

## Chapter 3

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# Design

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This chapter provides a representation of efforts one must face to make a jump from dry theoretical models to a virtually real device.

### 3.1 On a quest to perfect parameters

Our journey begins with a necessity to define restrictions of the problem. The intended environment would be a 4K cryogenic chamber (figure 14), which imposes dimensions restrictions. The ion trap requires a defined frequency for successful confinement of ions and has a capacitance. Summarized restrictions can be found in table 31.

Parameter	Description	Value
$V_{max}$	Maximum volume of the resonator	$(60 \text{ mm})^3$
$\omega_0$	Target frequency of the trap	40 MHz
$C_{trap}$	Capacitance of the trap	10–20 pF

Table 31: Restrictions of a system

#### 3.1.1 First iteration

Siversn's model [17] is dependent on outcomes from Macalpine's model [13] thus one needs to find these beforehand. Exact value of a trap's capacitance is unknown at the moment of calculations so it was decided to use and compare values from a following set of capacitances:  $C_{trap} = [10, 15, 20] \text{ pF}$ . The modified Macalpine's model, found in the appendix A, also predicts resonant frequency shift when connecting a capacitor. The unloaded frequency needed to be varied until the loaded frequency equals target frequency. Results are provided in table 32, naming is consistent with [13].

Parameter	Value		
	10	15	20
$C_{trap}$ , pF			
$B$ , mm (length of a shield)		60.0	
$D$ , mm (diameter of a shield)		45.0	
$b$ , mm (length of a coil)		37.1	
$N_t$ (number of turns)	11.0	9.2	8.1
$d_0$ , mm (diameter of a wire)	1.7	2.0	2.3
$\tau$ , mm (pitch of a helix)	3.4	4.0	4.6
$f_0$ , MHz (unloaded frequency)	97.0	116.0	132.8
$Q$ (unloaded quality factor)	873.2	954.8	1022.4

Table 32: Joint output of the appendix A

### 3.1.2 Precise fit

After defining an approximate region of interest we can proceed to calculations utilizing Siversn's model [17] with implementation provided in the appendix B. Volume requirements were also better clarified with the goal to get the best quality factor by varying coil's parameters. Updated restrictions can be found in the table 33. One could argue that all values of  $d_0$  are lower than the recommended in [17] thickness of 5 mm. This is true and additional measures to handle it can be found in section 3.2.5.

Parameter	Value		
	10	15	20
$C_{trap}$ , pF			
$B$ , mm (length of a shield)		56.0	
$D_{max}$ , mm (max diameter of a shield)		38.0	
$d_0$ , mm (diameter of a wire)	1.7	2.0	2.3
$\tau$ , mm (pitch of a helix)	3.4	4.0	4.6
$\omega_0$ , MHz (resonator frequency)	44.6	45.6	46.9
$Q$	418	360	311

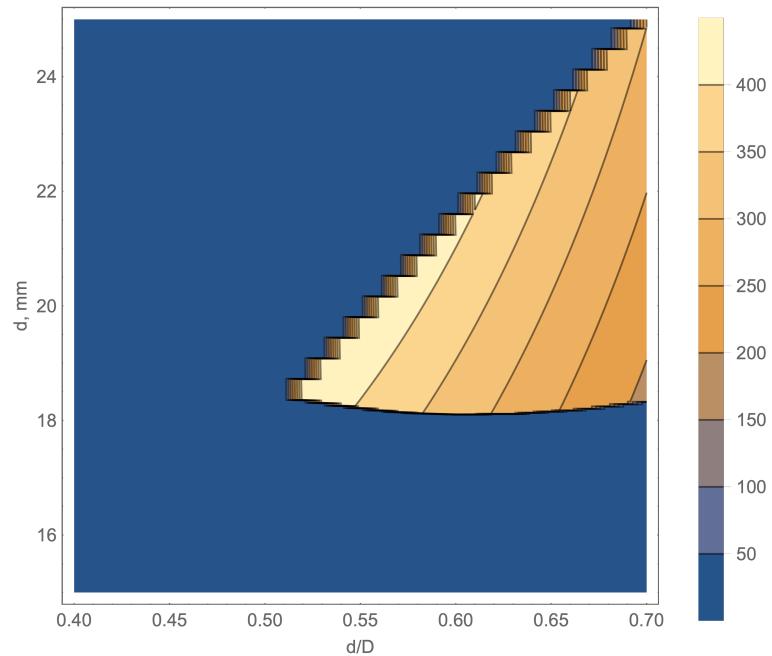
Table 33: Restrictions for the Siversn's model

Fixed values of the table 33 allow us to independently change 2 remaining parameters — diameter of a shield and diameter of a coil. Appendix's B output of  $Q$  values is provided in the figures 31, 32, 33. By selecting a point in a  $\{d, \gamma = d/D\}$  space that maximizes  $Q$  for a set of  $C_{trap}$  values we get final parameters for our RF resonator as defined in the table 34.

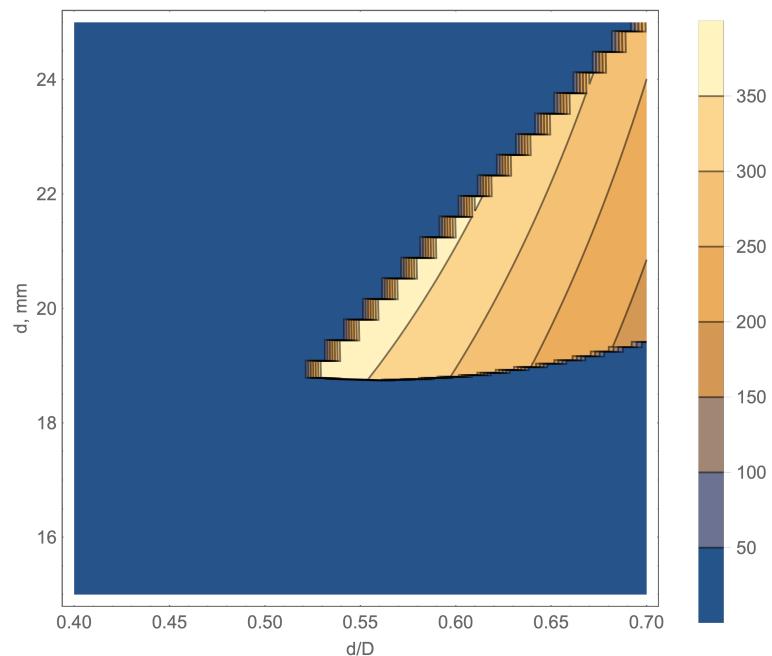
Since selected dimensional parameters in the table 34 correspond to those of  $C_{trap} = 10$  pF we would expect the unloaded frequency  $f_0$  and the unloaded  $Q$  to be equal to ones mentioned in the table 32.

### 3.1. On a quest to perfect parameters

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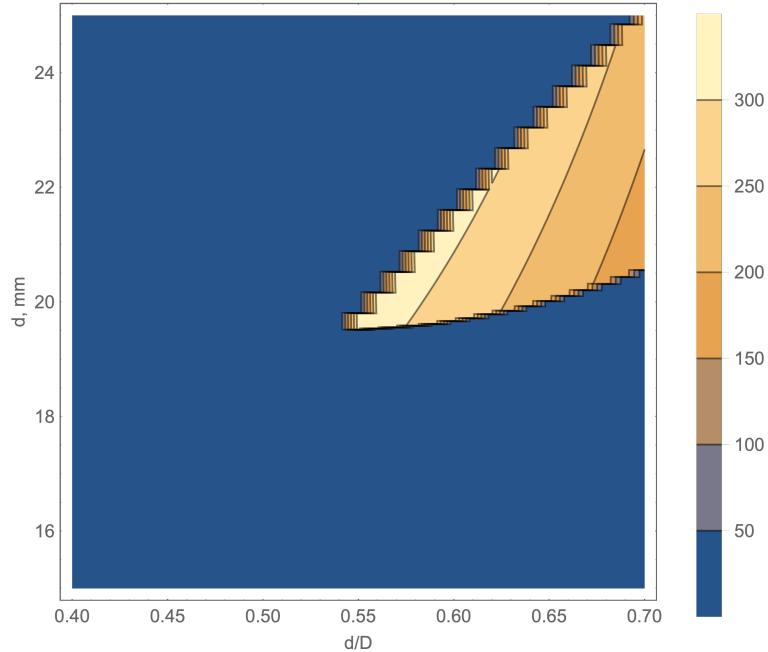
**Figure 31:**  $Q$  values plot for  $C_{trap} = 10$  pF



**Figure 32:**  $Q$  values plot for  $C_{trap} = 15$  pF

### 3.2. Shaping the 3D model

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**Figure 33:**  $Q$  values plot for  $C_{trap} = 20 \text{ pF}$

Parameter	Value
$B$ , mm (length of a shield)	56.0
$D$ , mm (diameter of a shield)	34.5
$d$ , mm (diameter of a coil)	19.0
$b$ , mm (length of a coil)	40.0
$N_t$ (number of turns)	10.0
$d_0$ , mm (diameter of a wire)	2.0
$\tau$ , mm (pitch of a helix)	4.0

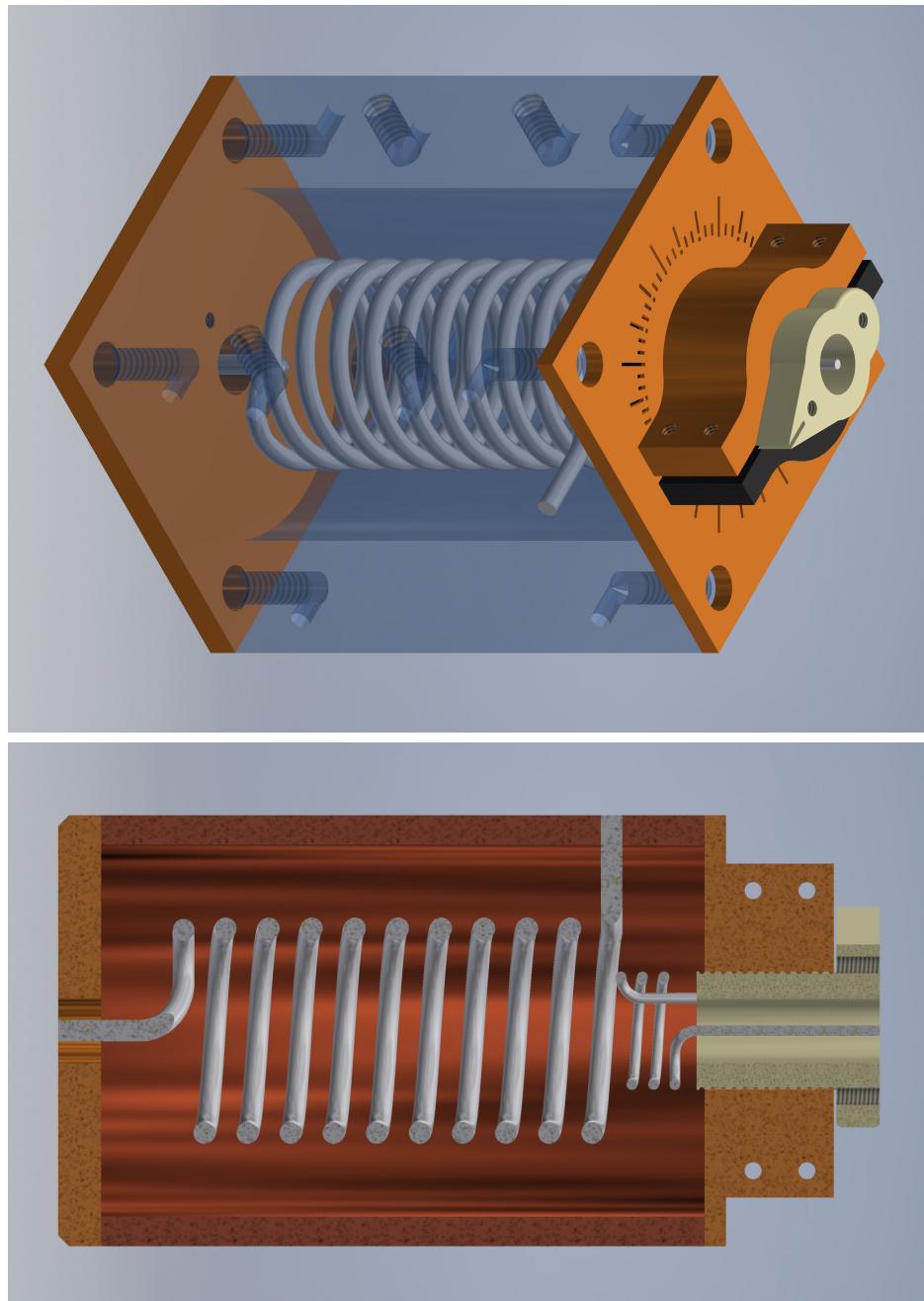
**Table 34:** Final parameters of an RF resonator

## 3.2 Shaping the 3D model

With all dimensions in our hands we can start implementing them in a 3D design for the workshop. This section provides an overview of all parts used, their features and reasonings. One important feature to notice beforehand is the tunability. With the resonator as small as ours the chances that manufacturing complications would shift the target frequency further are rather high. In order to be able to vary it precisely the angular scale on the top cap (3.2.6) and the linear scale on the antenna mount (3.2.8) were designed.

#### 3.2.1 RF resonator

Assembly of the RF resonator is shown on the figure 34. Every part is produced from oxygen-free copper to lower the resistivity. Colors are adjusted for a better perception.



**Figure 34:** 3D model of an RF resonator

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### 3.2. Shaping the 3D model

#### 3.2.2 Bottom cap

Bottom cap as displayed in the figure 35 features:

- output hole for the helix (3.2.4)
- 4xM4 clearance holes to connect to the shield (3.2.3)
- 2xM2 thread holes for a SMA connector (RND 205-00499) for the helix (3.2.4)

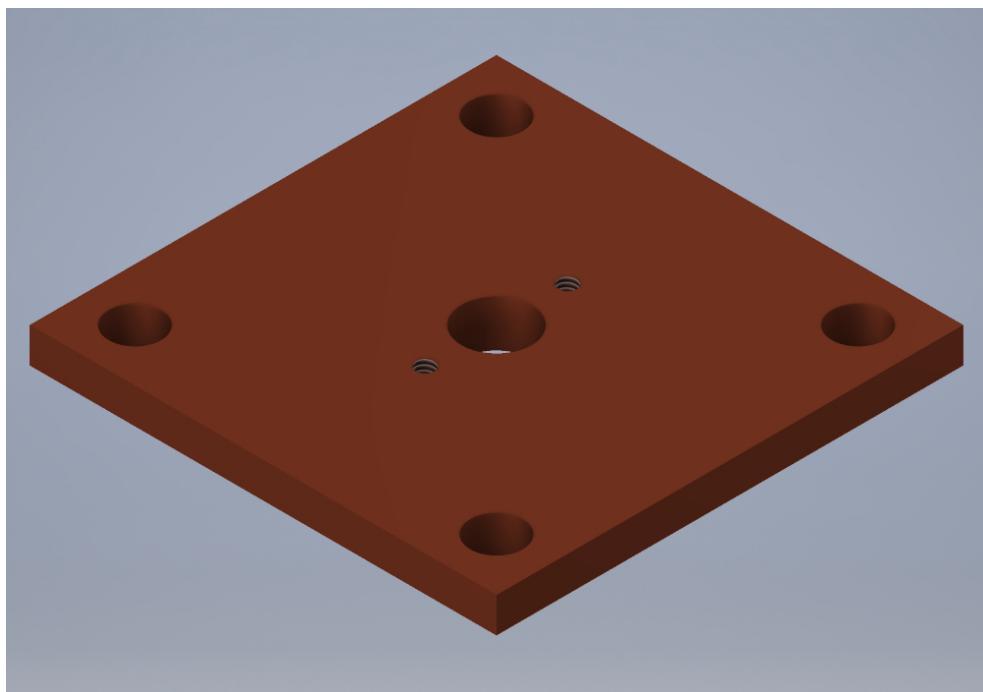
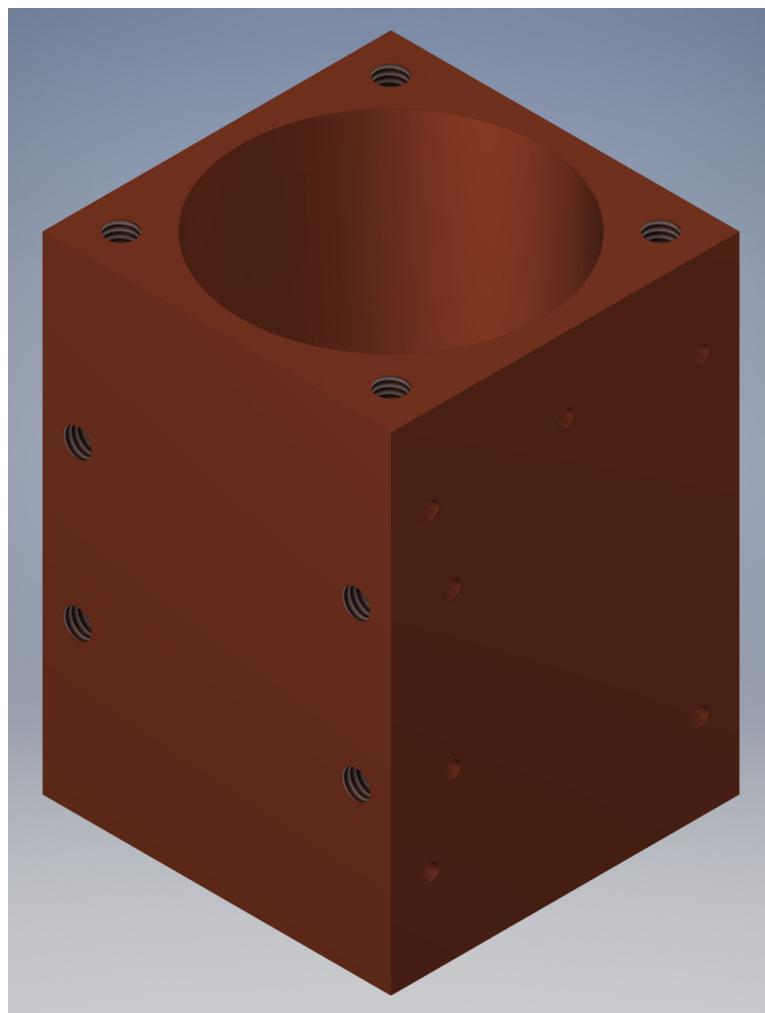


Figure 35: 3D model of a bottom cap

### 3.2.3 Shield

Shield as displayed in the figure 36 features:

- 4xM4 thread holes to connect to the top cap (3.2.6)
- 4xM4 thread holes to connect via a copper adapter to the top cover of the 4K chamber (figure 14)
- 4xM4 thread holes to connect to the bottom cap (3.2.2)
- 12x ventilation holes for M4 thread holes to avoid the slow leakage of the remaining air between the screw and the shield into the vacuum of the cryostat
- hole for the helix connection (3.2.4)

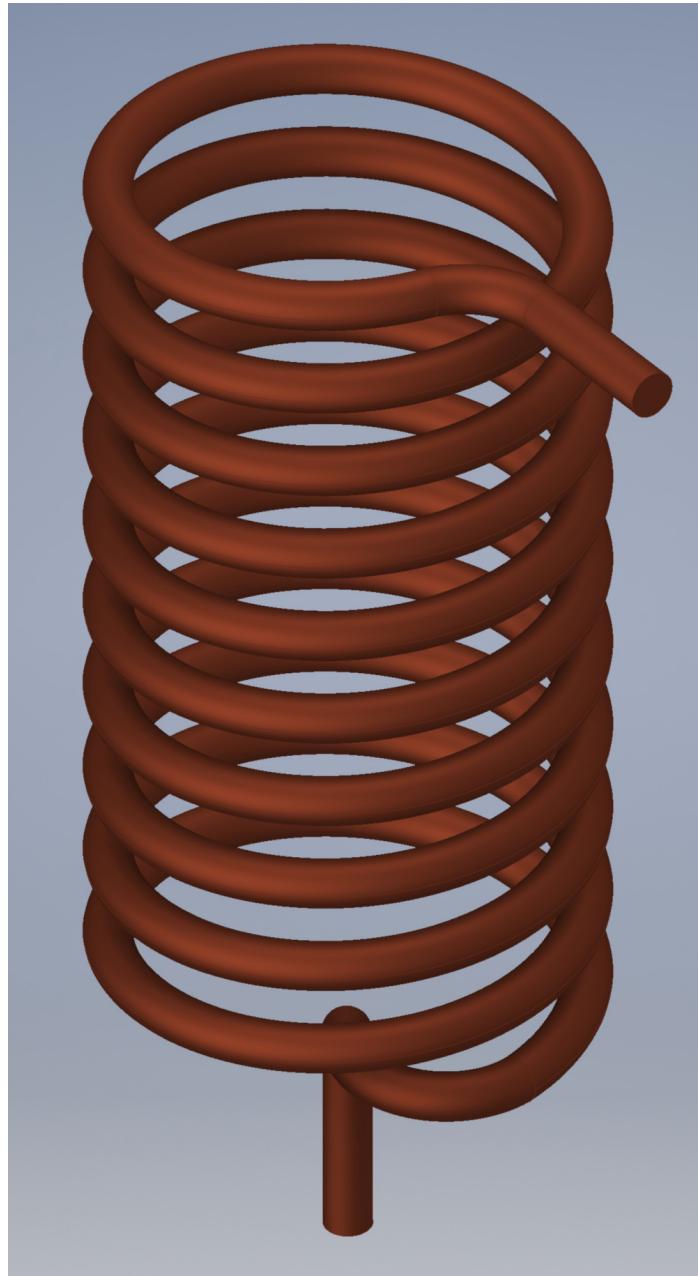


**Figure 36:** 3D model of a shield

### 3.2.4 Helix

Helix as displayed in the figure 37 features:

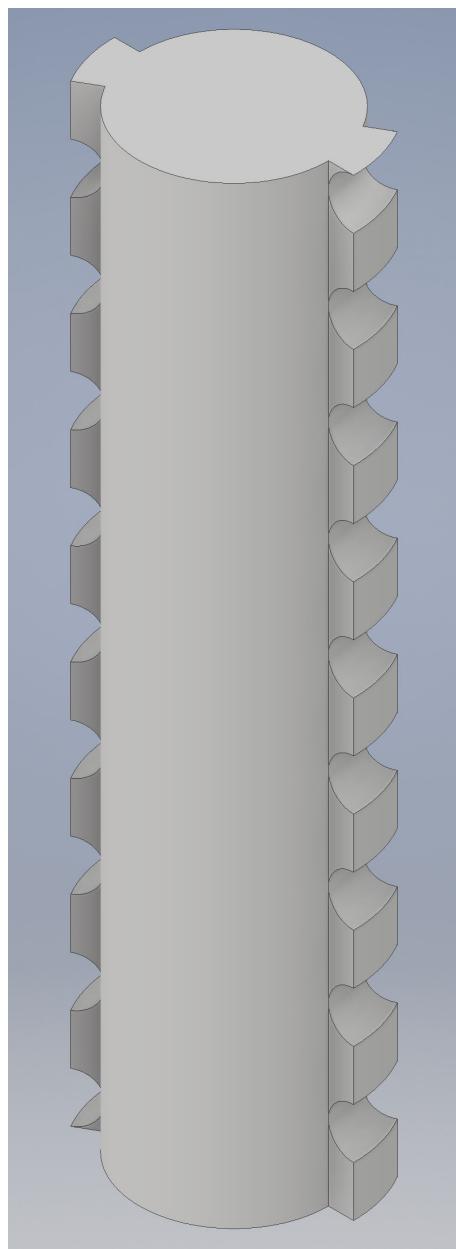
- end soldered to the shield (3.2.3)
- end soldered to a SMA (RND 205-00499) on the bottom cap (3.2.2)



**Figure 37:** 3D model of a helix

### 3.2.5 Helix support

Since  $d_0$  as specified in the table 34 is smaller than recommended thickness of 5 mm the question of mechanical stability arises. In order to eliminate potential mechanical oscillations we introduce a helix support made of PEEK to be inserted inside of the helix (3.2.4). PEEK was selected as a cryogenic compatible insulator thus minimizing its influence on the helix's inductivity.



**Figure 38:** 3D model of a helix support

### 3.2.6 Top cap

Top cap as displayed in the figure 39 features:

- 4xM4 clearance holes to connect to the shield (3.2.3)
- 4xM2 thread holes to connect to the top cap clamp (3.2.7)
- tight hole for an antenna mount (3.2.8)
- angular scale for an antenna mount (3.2.8) as discussed in 3.2

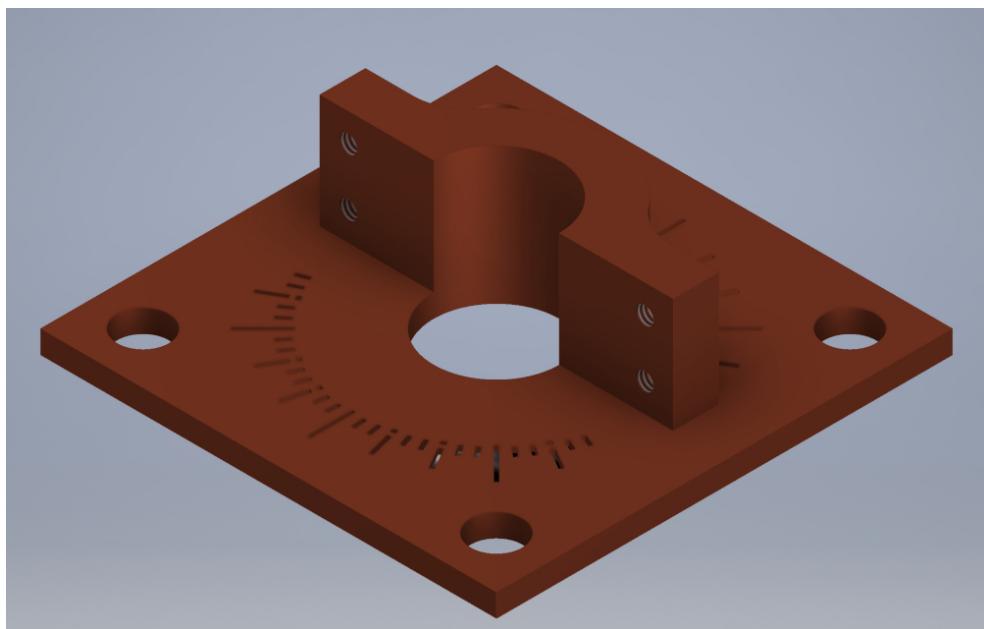
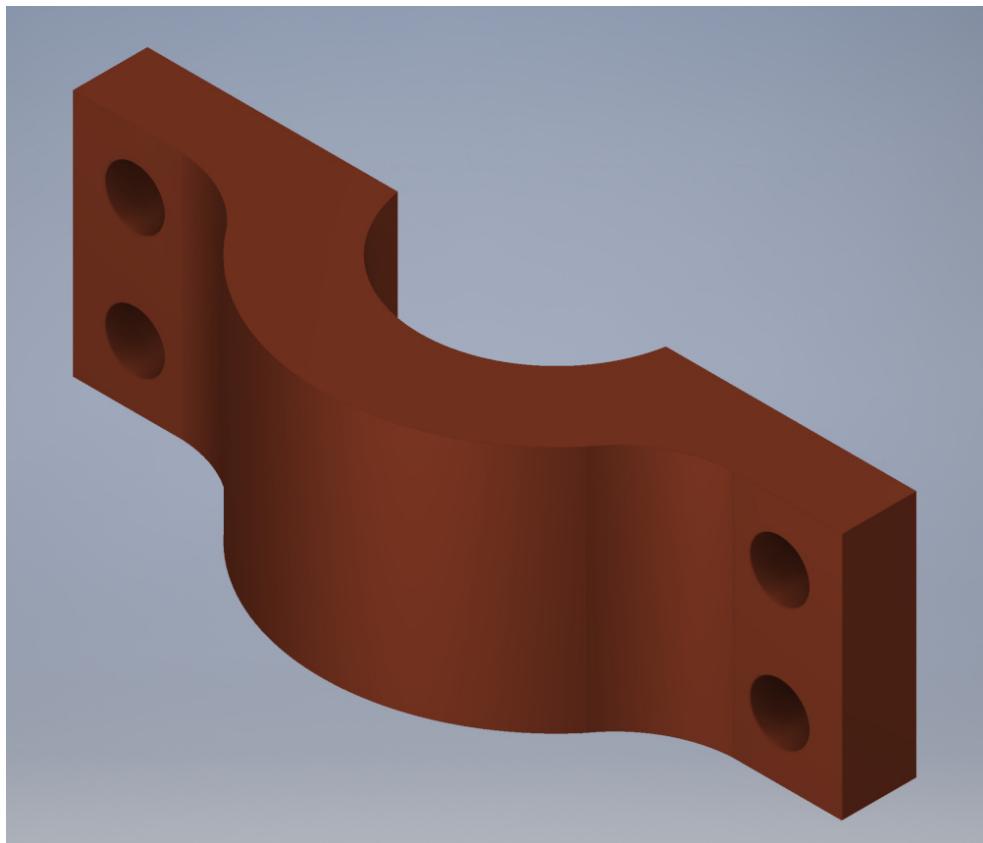


Figure 39: 3D model of a top cap

### 3.2.7 Top cap clamp

Top cap clamp as displayed in the figure 310 features:

- 4xM2 clearance holes to connect to the top cap (3.2.6)
- truncated semicircle to clamp an antenna mount (3.2.8)



**Figure 310:** 3D model of a top cap clamp

### 3.2.8 Antenna mount

Antenna mount as displayed in the figure 311 features:

- 2xM2 thread holes for a SMA (RND 205-00499) connector for the antenna (3.2.9)
- hole for the antenna (3.2.9)
- cut for a precise usage of the angular scale on the top cap (3.2.6)
- 1 mm period cuts to determine the distance to the top cap (3.2.6) as discussed in 3.2

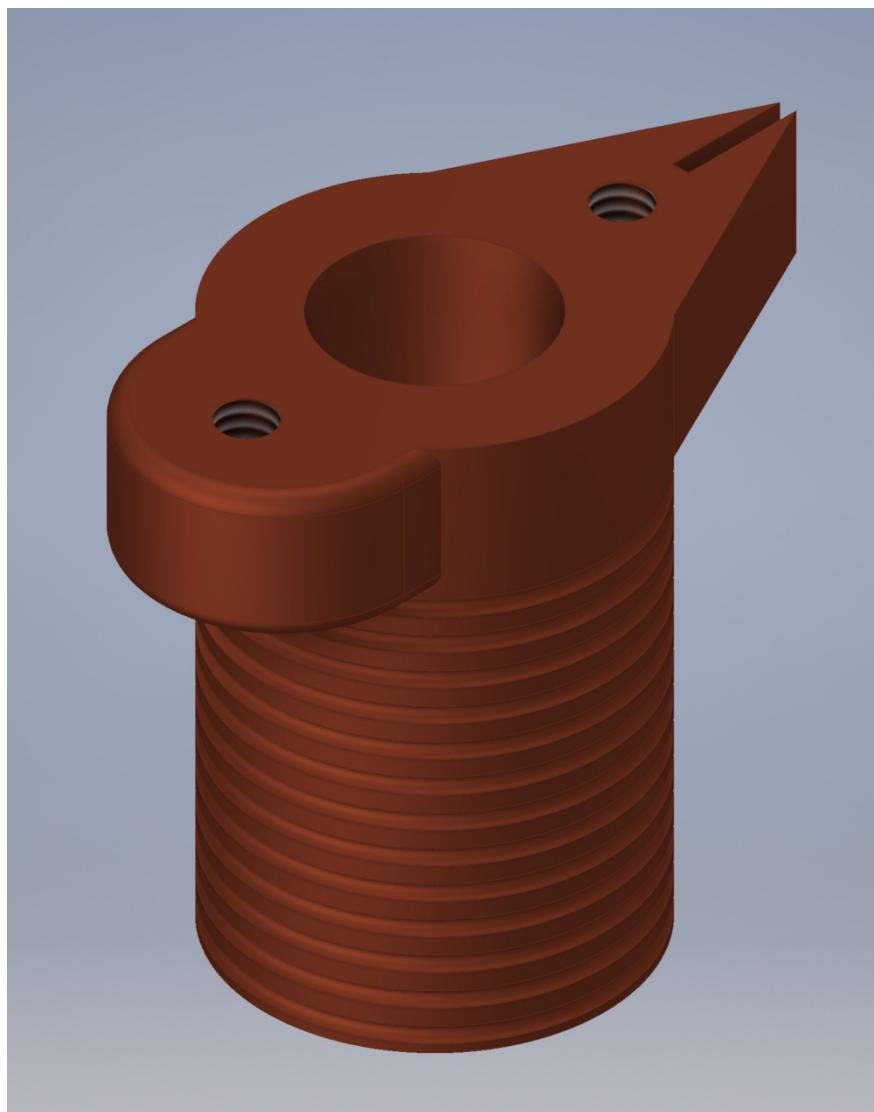


Figure 311: 3D model of an antenna mount

### 3.2.9 Antenna

Antenna as displayed in the figure 312 features:

- end connecting to a SMA (RND 205-00499) on the antenna mount (3.2.8)
- end soldered to the bottom of the antenna mount (3.2.8)
- using empirical estimation from [17] a diameter of 11 mm was selected



**Figure 312:** 3D model of an antenna

### 3.3 Final assembly

An overview of the assembled resonator can be seen in the figure 313.

Huge thanks to the ETH Workshop for their help in fitting the final apparatus into machinery constrains and for producing this delicate device.



**Figure 313:** Assembled resonator

## Chapter 4

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# Validation

---

Two parameters defining the assembled resonator are the central frequency  $\omega_0$  and the quality factor  $Q$ . In this chapter we measure their experimental values and compare to those defined in the table 33.

### 4.1 Measurements

In order to determine  $\omega_0$  and  $Q$  we would take a look at the reflection spectrum of the system consisting of resonator + coaxial cable + capacitor. For every configuration the depth of the resonance was optimized by changing the distance and the angle between the antenna mount 3.2.8 and the top cap 3.2.6, effectively adjusting the antenna to coil coupling.

Parameter	Definition	Values	Units
$C_{load}$	External capacitive load	10, 15, 22	pF
$L_{coax}$	Length of the coaxial cable	10, 20, 50	cm

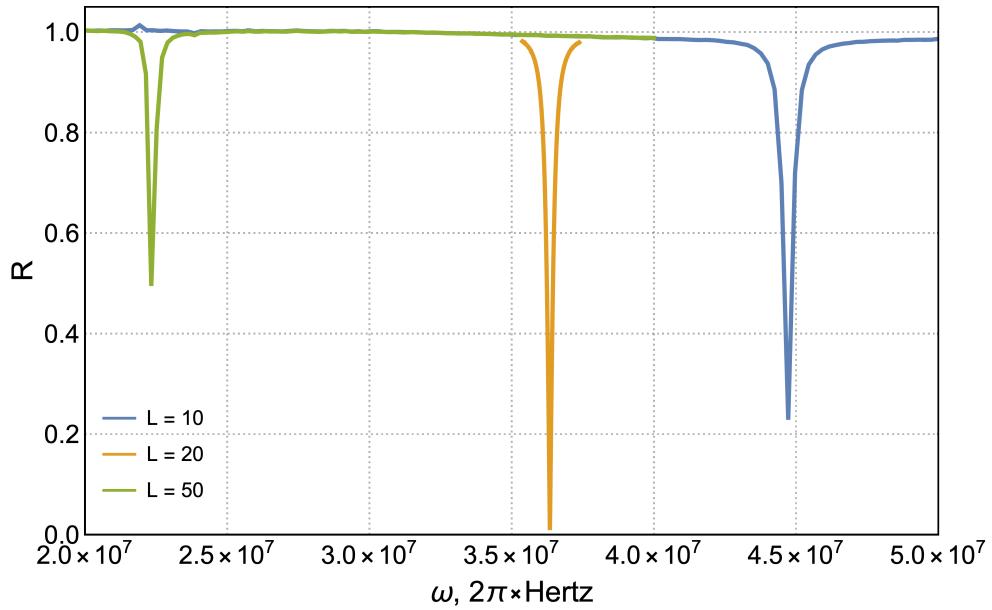
**Table 41:** Additional experimental parameters

At the time of writing there is no clear values for the capacitance of the trap and the length of the wires connecting it with the resonator. By using a set of parameters defined in the table 4.1 we aim to measure  $\omega_0$  and  $Q$  in the region similar to the one used for the numerical calculations and broad enough to include the point  $\{C_{load} = C_{trap}; L_{coax}\}$  of the final setup.

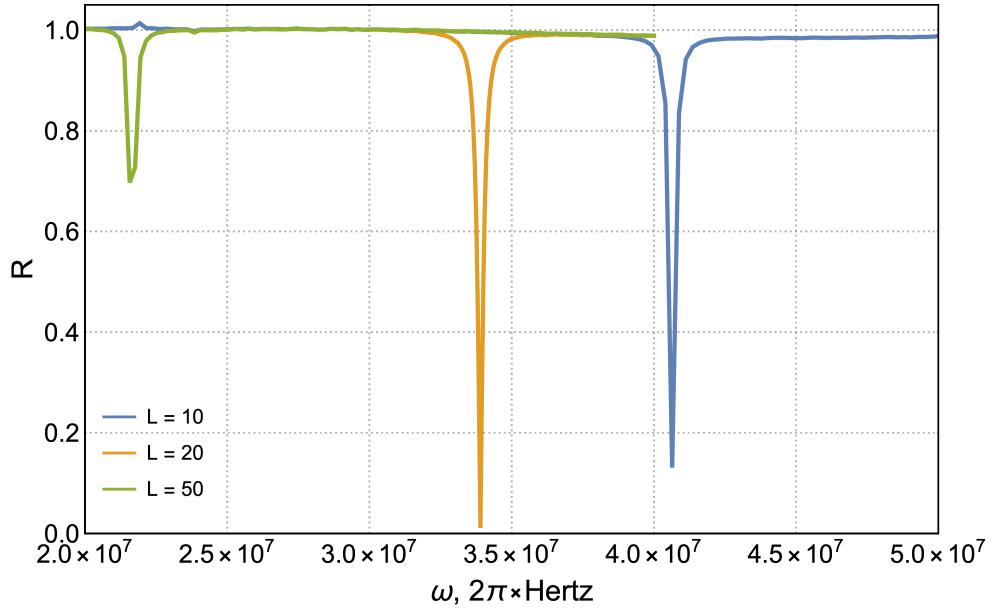
- For  $L_{coax} = 50$  two coaxial cables were connected, introducing 2 additional SMA connectors to the contour
- Available SMA connectors were of the male type. Unfortunately it is also the type commonly used for the wires, so we had to use an additional female-female adapter (+1 for  $L_{coax} = 50$ )

#### 4.1. Measurements

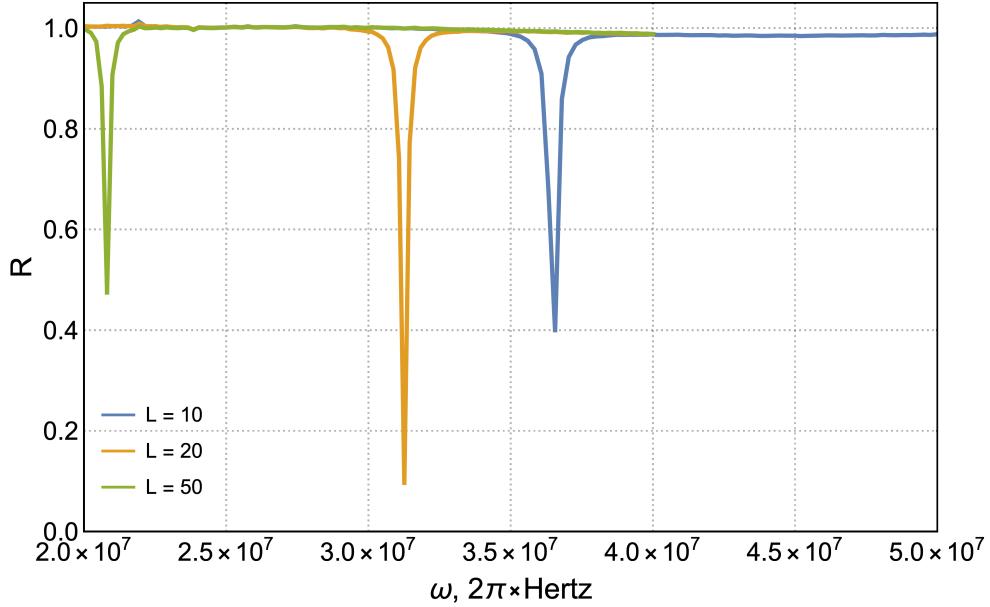
---



**Figure 41:** Reflection spectrum for  $C = 10$



**Figure 42:** Reflection spectrum for  $C = 15$


 Figure 43: Reflection spectrum for  $C = 22$ 

## 4.2 Analysis

Finding  $\omega_0$  from experimental data is trivial, it is the central frequency of the peak. For the transmission spectrum  $Q$  can be defined as

$$Q = \frac{\omega_0}{\Delta\omega}, \quad (4.1)$$

where  $\Delta\omega$  is the width of the peak at the  $1/\sqrt{2}$  height. Since we are working with the reflection spectrum we need to adjust the height using the following expression

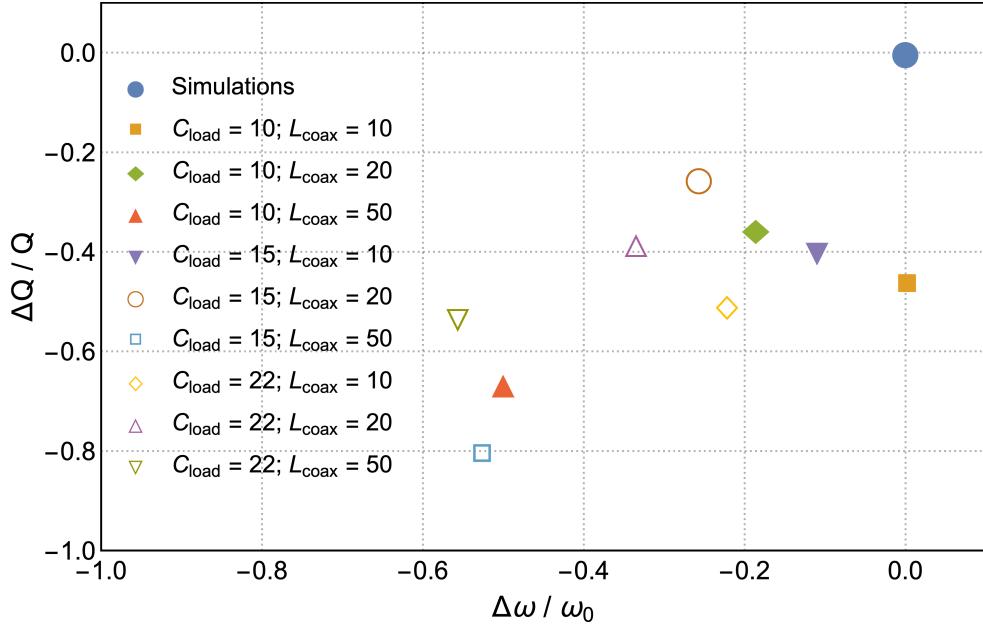
$$R_{1/\sqrt{2}} = 1 - \frac{1 - R_{peak}}{\sqrt{2}}. \quad (4.2)$$

Measured values of  $\omega_0$  and  $Q$  are presented in the table 4.2. Visual comparison with the predicted values from the table 33 is shown in the chart 4.2.  $C_{load} = 22$  pF is not equal to the simulated  $C_{trap} = 20$  pF but was considered being close enough. The closer experimental data is to the point  $\{0; 0\}$  the better it reflects the simulations. It can be seen that increased capacitance due to both  $C_{load}$  and  $L_{coax}$  tends to increase deviations from predictions.

### 4.3. Ideal drive

$C_{load}$ , pF	$L_{coax}$ , cm	$\omega_0^{simul}$ , $2\pi * \text{MHz}$	$\omega_0$ , $2\pi * \text{MHz}$	$Q^{simul}$	$Q$
10	10	44.6	44.7	418	223.5
10	20	—  —	36.3	—  —	269.9
10	50	—  —	22.3	—  —	140.4
15	10	45.6	40.6	360	216.5
15	20	—  —	33.9	—  —	268.6
15	50	—  —	21.6	—  —	69.7
22	10	46.9	36.5	311	153.5
22	20	—  —	31.2	—  —	192.3
22	50	—  —	20.8	—  —	145.6

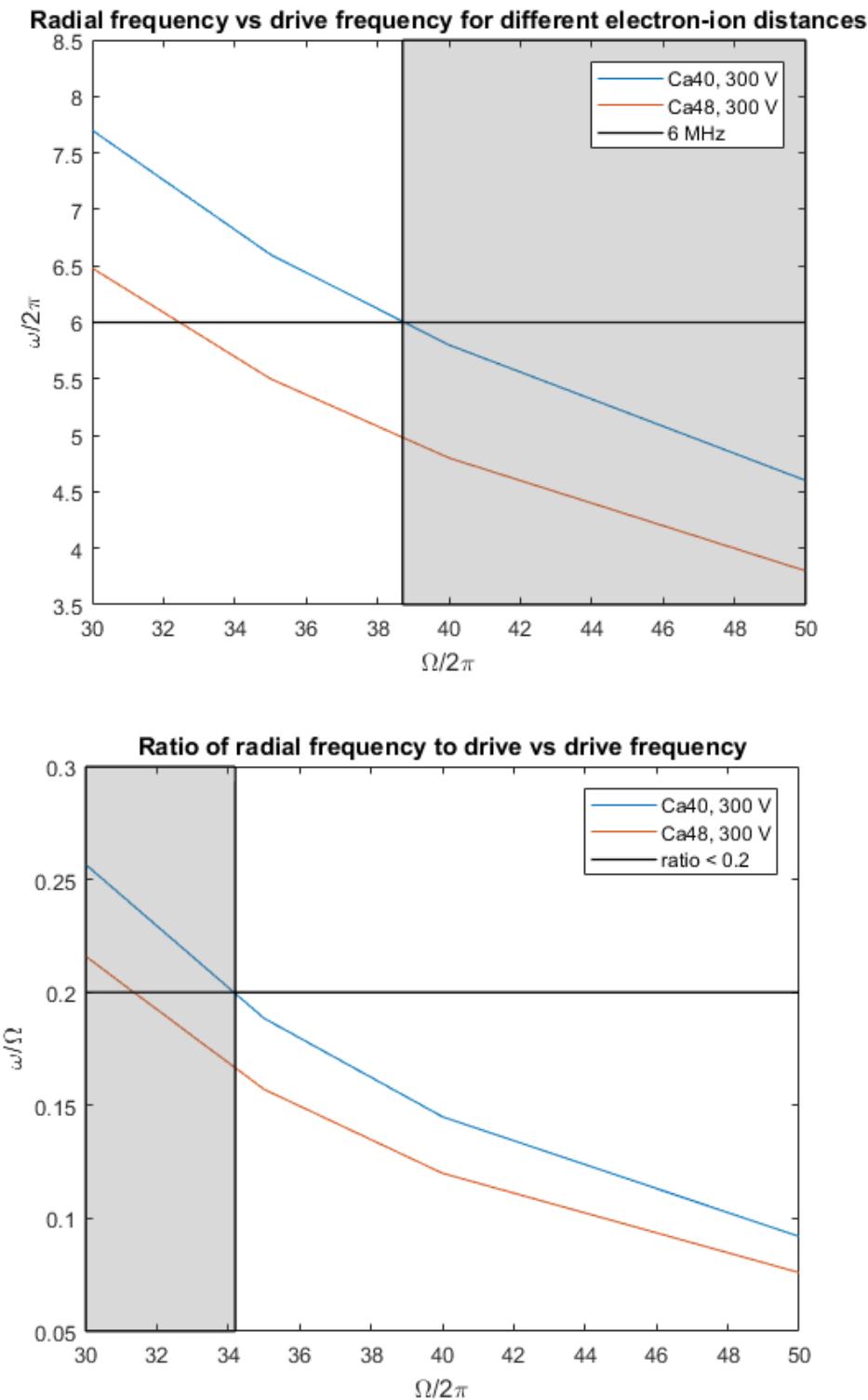
**Table 42:** Measured  $Q$  and  $\omega_0$  for various configurations



**Figure 44:** Relative deviations of  $Q$  and  $\omega_0$

### 4.3 Ideal drive

This section includes simulations of the ideal drive for a 300 and 320 V drive by Chiara Decaroli, figures 4.3 and 4.3 respectively. Let's take a look at the figure 4.3. If the resonator frequency is below  $\approx 2\pi * 34$  MHz the ion trap becomes unstable. On the other hand, with frequencies larger than  $\approx 2\pi * 39$  MHz the secular frequency of the ion itself drops below  $2\pi * 6$  MHz which does not allow certain quantum operations. Thus it is desired for the  $\omega_0$  to be below the intersection of the white areas. We show what measured points respect this condition in the table 4.3.



**Figure 45:** Simulation of the ideal drive for 300V

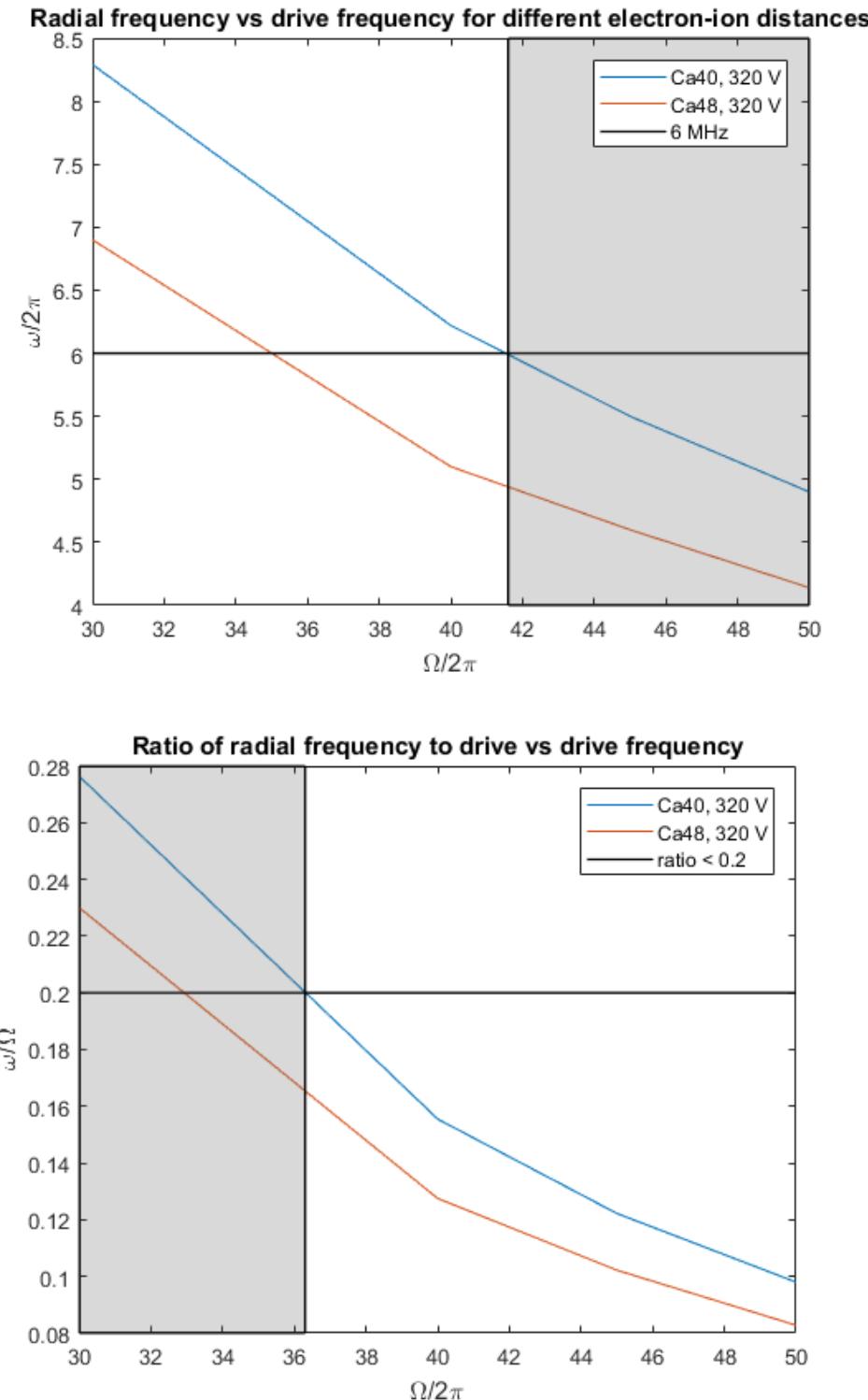


Figure 46: Simulation of the ideal drive for 320V

#### 4.4. Voltage gains

---

$C_{load}$ , pF	$L_{coax}$ , cm	Compatible with 300V	Compatible with 320V
10	10	✗	✗
10	20	✓	✓
10	50	✗	✗
15	10	✗	✓
15	20	✓	✗
15	50	✗	✗
22	10	✓	✓
22	20	✗	✗
22	50	✗	✗

**Table 43:** Fitting the experimental data into the ion trap constrains

## 4.4 Voltage gains

According to [12] average dissipated power  $P$  can be written as

$$P = \frac{I_0^2 R}{2} = \frac{(U_0 \omega_0 C)^2 R}{2} = \frac{U_0^2}{2\omega_0 Q L} \quad (4.3)$$

with a peak current  $I_0$ , peak voltage  $U_0$ , inductance of the resonator  $L$ , and capacitance of the system  $C$ . Since in the section 4.1 we made measurements with various known values of a capacitive load it is possible to give an estimation of  $L = 600$  nH. By picking the values from the table 4.3 that are compatible with  $U_0 = 300$  or 320V we present results for the needed input power in the table 4.4.

$C_{load}$ , pF	$L_{coax}$ , cm	$U_0$ , V	$P$ , W
10	20	300	1.20
10	20	320	1.37
15	10	320	1.53
15	20	300	1.30
22	10	300	2.11
22	10	320	2.40

**Table 44:** Estimated input power  $P$  for various configurations

## Chapter 5

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# Conclusion

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As a result of this project we were able to implement a delicate helical resonator with reasonable  $Q$  and  $\omega_0$  values. There is definitely room for improvement:

- Angular tuning didn't prove to work, which is also good since it shows that structure is fairly symmetrical to rotations.
- Distance tuning almost didn't work, for an optimal tuning the distance between the antenna mount was kept close to 0. Possible solution would be either to add another turn to the antenna itself or extend the length of the antenna mount to gain more flexibility.
- Helical resonator has spent a fair share of time being in contact with air. Cleaning the internal surface of the shield with sanding or acid should remove oxidized layer of copper and improve conductivity.
- SMA adapters are good for testing and probing the device, but add additional capacitance — for a usage with a real trap it would be recommended to solder the wires directly.
- Coaxial cables also add capacitance, better results might be achieved with using regular wires.
- Theoretical calculations used conductivity at cryogenic temperatures, moving the helical resonator into the cryostat should provide results closer to those expected from the model.

## Appendix A

---

### Mathematica code for Macalpine's model

---

This is a relevant part of the script supporting calculations in [12].

```
In[1]:= (* Physical Constants and Units *)
μ0 = 4*π*10-7;
ε0 = 8.854187817*10-12;
c = 299792458;
AMU = 1.6605402*10-27;
h = 6.6260755*10-34;
ℏ =  $\frac{h}{2\pi}$ ;
μB = 9.2740154*10-24;
kB = 1.380658*10-23;
grav = 9.8;
a0 = 0.5291772108*10-10;
me = 9.1093826*10-31;
ee = 1.60217733*10-19; eV = ee;
Eh =  $\frac{\hbar^2}{me a_0^2}$ ;
m=1; μm=10-6m; mm=10-3m; cm=10-2m; nm=10-9m; km=103m;
in=2.54cm; ft=12in; mi=5280*ft;
K=1; mK=10-3K; μK=10-6; nK=10-9K; pK=10-12;
T=1; mT=10-3K; G=10-4; mG=10-3G; μG=10-6;
sec=1; s=1; ms=10.0-3s; μs=10-6s; ns=10-9s;
Ω=1; mΩ=10-3; kΩ=103; MΩ=106;
A=1; mA=10-3A; μA=10-6; nA=10-9;
W=1; mW=10-3; μW=10-6; nW=10-9;
Hz=1; kHz=103; MHz=106; GHz=109;
nF=10-9; pF=10-12;
nH=10-9; pH=10-12;
```

---

```

In[2]:= (* Calculations for Cu resonator *)
Ds[Bs_]:= 0.75Bs; (*diameter of shield*)
d[Bs_]:= 0.55Ds[Bs]; (*diameter of helix*)
b[Bs_]:= 1.5d[Bs]; (*length of helix*)

Nt[Bs_,f0_]:=  $\frac{48.26 \cdot 10^6}{f0 \cdot Ds[Bs]}$ ; (*number of turns*)
d0[Bs_,f0_]:= 0.5  $\frac{b[Bs]}{Nt[Bs, f0]}$ ; (*diameter of wire*)
 $\tau[Bs_, f0_] := \frac{b[Bs]}{Nt[Bs, f0]}$ ; (*pitch*)

(*effective inductance*)
Leff[Bs_,f0_]:=  $9.84 \cdot 10^{-7} \cdot \left( \frac{Nt[Bs, f0] \cdot d[Bs]}{b[Bs]} \right)^2 \cdot \left( 1 - \left( \frac{d[Bs]}{Ds[Bs]} \right)^2 \right)$ ;
Ceoff[Bs_]:=  $\frac{2.95 \cdot 10^{-11}}{\log_{10} \frac{Ds[Bs]}{d[Bs]}}$ ; (*effective capacitance*)

Z0[Bs_,f0_]:=  $\sqrt{\frac{Leff[Bs, f0]}{Ceoff[Bs]}}$ ; (*characteristic impedance*)
v[Bs_,f0_]:=  $\frac{1}{\sqrt{Leff[Bs, f0] \cdot Ceoff[Bs]}}$ ; (*velocity*)
 $\lambda[Bs_, f0_] := \frac{v[Bs, f0]}{f0}$ ; (*wavelength*)

Q[Bs_,f0_]:= 1.97 Ds[Bs]  $\sqrt{f0}$ ;

omega[Bs_,f0_,Cl_]:= Module[{w},
  w =  $v/.FindRoot[\frac{1}{2\pi \cdot Z0[Bs, f0] \cdot Cl \cdot v} == \tan(\frac{2\pi v \cdot b[Bs]}{v[Bs, f0]})]$ , {v, f0}] [[1]];
  Return@w;
]

In[3]:= Bs = 60mm; (*length of shield*)
(* This frequency needs to be varied
until loaded frequency is close to target frequency*)
f0 = 97.023MHz; (*center frequency*)
Cl = 10pF; (*trap capacitance*)

Print["Bs = ", Bs/mm, " mm (length of shield)"]
Print["Ds = ", Ds[Bs]/mm, " mm (diameter of shield)"]
Print["d = ", d[Bs]/mm, " mm (diameter of helix)"]
Print["b = ", b[Bs]/mm, " mm (length of helix)"]
Print["Nt = ", Nt[Bs,f0], " (number of turns)"]
Print["d0 = ", d0[Bs,f0]/mm, " mm (diameter of wire)"]

```

---

```

Print["τ = ",τ[Bs,f0]/mm," mm (pitch of helix)"]
Print["Z₀ = ",Z₀[Bs,f0]/ω," ω (characteristic impedance)"]
Print["Lᵅᵅᵅ = ",Lᵅᵅᵅ[Bs,f0]/(nH/mm)," nH/mm (effective inductance)"]
Print["Cᵅᵅᵅ = ",Cᵅᵅᵅ[Bs]/(pF/mm)," pF/mm (effective capacitance)"]
Print["v = ",v[Bs,f0]/(m/s)," m/s (velocity)"]
Print["λ = ",λ[Bs,f0]/mm," mm (wavelength)"]
Print["f₀ = ",f₀/MHz," MHz (unloaded frequency)"]
Print["Q = ",Q[Bs,f0]," (quality factor)"]
Print["ν₀ = ",omega[Bs,f0,C1]/MHz," MHz (loaded frequency)"]

Clear[Bs,f0,C1];
Bs = 60 mm (length of shield)
Ds = 45. mm (diameter of shield)
d = 24.75 mm (diameter of helix)
b = 37.125 mm (length of helix)
Nt = 11.0535 (number of turns)
d₀ = 1.67933 mm (diameter of wire)
τ = 3.35866 mm (pitch of helix)
Z₀ = 572.731 Ω (characteristic impedance)
Lᵅᵅᵅ = 37.2698 nH/mm (effective inductance)
Cᵅᵅᵅ = 0.11362 pF/mm (effective capacitance)
v = 1.53672*10^7 m/s (velocity)
λ = 158.387 mm (wavelength)
f₀ = 97.023 MHz (unloaded frequency)
Q = 873.205 (quality factor)
ν₀ = 40. MHz (loaded frequency)

```

## Appendix B

### Mathematica code for Siversns' model

Following calculations are heavily based on a script generously provided by James David Siversns. All variables and references correspond to [17].

```
In[1]:= (* Units and constants *)
MHz = 106;
pF = 10-12;
Ω = 1;
mm = 10-3;
m = 1;
H = 1;
μ0 = 4π*10-7;

In[2]:= (* Trap and wire values *)
Cw = 0.00001 pF; (* Wire to trap capacitance *)
Rt = 0.1 Ω; (* Trap resistance *)
CΣ[Ct_] := Cw + Ct; (* Sum of above *)

In[3]:= calculateQ[dMillimeters_, γ_]:=Module[{
(* Arguments naming as in Siversns paper *)
d0, τ, d, De, α, ρ, eN, b, Cc, KLC, KCs, Cs, LC, ω0, δ, lc, r, Ns, ls, a,
Rs, Rc, Rj, XLc, XCc, Xct, Xcw, XCs, Zcoil, ZE, Ztot, RealZ, Q,
maxSize, log, ωRes, Capacitance
},
Capacitance = 20pF;
(* Switch log function for plotting *)
log = Print;
log = (#)&

(* Resonator parameters *)
(* Coil wire diameter, we take it from Macalpine *)
d0 = 1.95mm;
```

---

```

 $\tau = 2*d0$ ; (* Winding pitch *)
 $d = d\text{Millimeters}*\text{mm}$ ; (* Diameter of coil *)
 $De = d/\gamma$ ; (* Diameter of a shield *)
 $\alpha = d/De$ ;
(* Resistivity of resonator material *)
 $\rho = 1.7*10^{-8}*\Omega*\text{m}$ ;
(* Given by the 4K chamber design *)
maxSize = 36mm;
b = 56mm - De/2;
(* Handling case of a too large resonator *)
If[d>maxSize || De>maxSize || b<=0, Return@0];

log["b = ", b/mm, "mm"];
log["d = ", d/mm, "mm"];
log["D = ", De/mm, "mm"];

eN = b/tau;(* Number of turns in the coil *)
log["N = ", eN];
(* Coil self capacitance - equation 25 *)

Cc = ((11.26  $\frac{b}{d}$ ) + 8 + ( $\frac{27}{\sqrt{\frac{b}{d}}}$ ))d pF;

KLC = 39.37  $\frac{0.025 \left(\frac{d}{\tau}\right)^2 (1-\alpha^2)}{\left(\frac{d}{\tau}\right)^2}$  10-6 H/m;
KCs = 39.37  $\frac{0.75}{\text{Log}[10, \frac{1}{\alpha}]}$  pF/m;

(* Shield-coil capacitance - equation 26 *)
Cs = b KCs;
(* Inductance of coil inside a shield - equation 27 *)
LC = b KLC;
(* Resonant frequency - equation 21 *)
ωRes[Ct_] :=  $\frac{1}{\sqrt{(Cs+Ct+Cw+Cc)LC}}$ ;

log["ω = ", ωRes[Capacitance]/(2π MHz), "MHz"];

ω0[Ct_] := 2π*40 MHz; (* This is a target frequency *)
(* Allowing 15% accuracy for the frequency *)
If[
     $\frac{\text{Abs}[\omega_0[\text{Capacitance}] - \omega_{\text{Res}}[\text{Capacitance}]]}{\omega_0[\text{Capacitance}]}$  > 0.15,
    Return@0
];

```

---

```

δ[Ct_] := Sqrt[ $\frac{2 \rho}{(\omega_0[Ct] \mu_0)}$ ]; (* Skin depth *)
(* Unwound length of the coil *)
lc =  $2\pi \sqrt{\left(\frac{d}{2}\right)^2 + \left(\frac{\tau}{2\pi}\right)^2} \frac{b}{\tau}$ ;
r =  $\frac{d}{2} \left(\frac{1}{\alpha} - 1\right)$ ;
(* Number of "turns" in the currents path in the shield
- equation 31 *)
Ns =  $\frac{b \ lc}{4\pi r^2}$ ;
(* Distance of current path in the shield - equation 32 *)
ls = Ns Sqrt[ $\pi^2 \left(\frac{d}{\alpha}\right)^2 + \left(\frac{b}{Ns}\right)^2$ ];
Rs[Ct_] :=  $\frac{\rho \ ls}{b \ \delta[Ct]}$ ;
Rc[Ct_] :=  $\frac{\rho \ lc}{d_0 \ \pi \ \delta[Ct]}$ ;
(* Resistance of solder joint as a function of frequency -
the 0.003 is the DC resistance of a typical solder joint
between shield and coil, however this can vary
and is best to measure *)
Rj[Ct_] := 0.003 Sqrt[ $\frac{\omega_0[Ct]}{2\pi \cdot 10^5}$ ] Ω;
(* Q calculations *)
XLc[Ct_] := ω0[Ct] LC;
XCc[Ct_] :=  $\frac{1}{\omega_0[Ct] Cc}$ ;
Xct[Ct_] :=  $\frac{1}{\omega_0[Ct] Ct}$ ;
Xcw[Ct_] :=  $\frac{1}{\omega_0[Ct] Cw}$ ;
XCs[Ct_] :=  $\frac{1}{\omega_0[Ct] Cs}$ ;
Zcoil[Ct_] :=  $\left( \frac{1}{(i \ XLc[Ct] + Rc[Ct])} + \frac{1}{\frac{1}{i} XCc[Ct]} \right)^{-1}$ ;
ZE[Ct_] :=  $\left( \frac{1}{\left(\frac{1}{i} Xct[Ct] + Rj[Ct]\right)} + \frac{1}{\frac{1}{i} Xcw[Ct]} + \frac{1}{\frac{1}{i} XCs[Ct]} \right)^{-1}$ ;
Ztot[Ct_] := Zcoil[Ct] + ZE[Ct] + Rs[Ct] + Rj[Ct];

```

---

```

RealZ[Ct_] := 
$$\frac{\frac{Rc[Ct] \ XCc[Ct]^2}{Rc[Ct]^2 + (XCc[Ct] - XLc[Ct])^2} +$$


$$\frac{Rt \ XCs[Ct]^2 \ Xcw[Ct]^2}{Rt^2(XCs[Ct] + Xcw[Ct])^2 + (XCs[Ct](Xct[Ct] + Xcw[Ct]) + Xct[Ct]Xcw[Ct])^2}$$


$$+ \ Rs[Ct] + Rj[Ct];$$


Q[Ct_] := 
$$\frac{LC \ \omega_0[Ct]}{RealZ[Ct]};$$


Return@Q[Capacitance];
]

In[4]:= SetDirectory[NotebookDirectory[]];
contourData = Table[
  {γ, d, calculateQ[d, γ]},
  {d, 15, 25, 0.01},
  {γ, 0.4, 0.7, 0.01}
] // Flatten[#, 1]&

ListContourPlot[
  contourData,
  PlotLegends → Automatic,
  FrameLabel → {"d/D", "d, mm"}
]

In[5]:= (* Final parameters *)
calculateQ[19, 0.55]

b = 38.7273mm
d = 19mm
D = 34.5455mm
N = 9.93007
ω = 39.7919MHz

Out[5]= 362.188

```

---

## Bibliography

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