PHYSICS

1. (C) The image formed by lens will be at centre of curvature of the mirror

For lens

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \frac{1}{(-20)} = -\frac{1}{5}$$

$$\frac{1}{v} = -\frac{1}{20} - \frac{1}{5}$$

$$v = -4cm$$

Hence distance b/n the lens and the mirror will be 5cm

2. (A) For observer in air

$$\frac{n_2}{v} - \frac{n_1}{u} = \frac{(n_2 - n_1)}{R}$$

$$\frac{1}{v} - \frac{3}{2(-5)} = \frac{1 - 15}{(-5)}$$

$$\frac{1}{v} + \frac{3}{10} = \frac{1}{10}$$

$$\frac{1}{v}$$
 $\frac{-2}{10}$

$$v = -5cm$$

For observer in water

$$\frac{n_2}{v} - \frac{n_1}{u} = \frac{(n_2 - n_1)}{R}$$

$$\frac{4}{3v} - \frac{3}{2(-9)} = \frac{\left(\frac{4}{3} - \frac{3}{2}\right)}{\infty}$$

$$\frac{4}{3v} \frac{-1}{6}$$
 $\Rightarrow v = -8cm$

Distance between the image = 14 - (8+5) = 1 cm

$$3. \hspace{1cm} \text{(B)} \hspace{1cm} V = \frac{kq}{d} - \frac{kq}{R_{_1}} + \frac{kq}{R_{_2}}$$

$$= kq \left[\frac{1}{R_2} - \frac{1}{R_1} + \frac{1}{d} \right]$$

4. (D)
$$P_1V_1 P_2V_2$$

$$(P_0)(2V_0) = (P_0 + pgh)V_0$$

$$2P_0 = P_0 + pgh$$

5. (C)
$$I = \frac{I_0}{2} \cos^2 \theta \sin^2 \theta$$

$$I = \frac{I_0}{8} \sin^2 2\theta$$

7. (D)
$$\frac{dv}{dt} = \frac{v^2}{R}$$

$$\int_{v_0}^{2V_0} \frac{dv}{v^2} \int_{0}^{t} dt$$

$$\left[\left(-\frac{1}{v}\right)\right]_{v_0}^{2v_0} = \frac{t}{R}$$

$$+\left(\frac{1}{v_0} - \frac{1}{2v_0}\right) = \frac{t}{R}$$

$$\frac{1}{2v_0} \quad \frac{t}{R}$$

$$t \frac{R}{2v_0}$$

8. (B)
$$x = \frac{u^2 \sin^2 \theta}{g} = \frac{(3)^2 \sin 30^\circ}{10}$$

$$\frac{9}{20}$$
m

9. (D)
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$
 — (1)

$$n_1 \cos \theta_1 w_1 = n_2 \cos \theta_2 w_2$$
 — (2)

Solving (1) & (2) w = 6 rad/s

- 10. (B) Conceptual
- 11. (A) $v_x = 50\cos 53^\circ$

$$=50\left(\frac{3}{5}\right)=30\text{m/s}$$

$$v_{y} = 50\sin 53^{\circ} = 40\text{m/s}$$

Momentum conservation

$$(5)[30\hat{i} + 20\hat{j}] = (2.5)(\vec{v}) + (2.5)(40)\hat{j}$$

$$150\hat{i} + 100\hat{j} = 2.5\vec{v} + 100\hat{j}$$

12. (B)
$$\left(\frac{hc}{\lambda}\right) = \left(\frac{8 \times 10^{-3}}{5 \times 10^{15}}\right) = 1.6 \times 10^{-18} \,\mathrm{J}$$

10eV

$$eV_0 = K_{max} = \frac{hc}{\lambda} - \phi$$

$$\phi = \frac{hc}{\lambda} - eV_0$$

$$=10eV-3eV$$

7eV

13. (C)
$$v = \sqrt{2g(5-h)}$$

$$x=\sqrt{2g(5-4)}\sqrt{\frac{2h}{g}}$$

$$x=2\sqrt{4(5-h)}$$

$$9 = 4(h)(5 - h)$$

h
$$\frac{1}{2}$$
m, $4\frac{1}{2}$ m

$$a \quad \frac{90}{25} \text{m/s}^2$$

$$\frac{18}{5}$$
m/s²

$$150 - T_1 = (15) \left(\frac{18}{5}\right)$$

$$T_2 - 50 = 5a$$

$$T_2 - 50 = (5) \left(\frac{18}{5}\right)$$

$$\frac{T_1}{T_2} = \frac{6x}{17} = \frac{96}{68}$$

$$x = 4$$

15. (A)
$$_{z}P^{A} \longrightarrow_{(z-2)} Q^{(A-4)} +_{2} He^{4}$$

P & S are isotopes

16. (B)
$$N N_0 e^{-\lambda t}$$

$$\left.\frac{dN}{dt}\right|_{t~0}=-\lambda N_{0}$$

$$(\lambda N_0)T = N_0$$

$$T = \frac{1}{\lambda} = t_{avg}$$

17. (C)
$$dI (dm)x^2$$

$$dm = \sigma dA$$

$$dI = \int_{0}^{R} (kx)(2\pi x) dx x^{2}$$

$$M = \int_{0}^{R} (kx)(2\pi x) dx$$

$$I = \int_{0}^{R} (2\pi x) x^4 dx$$

$$I=2\pi k\,\frac{R^5}{5}$$

$$I_d \quad \frac{I}{2}$$

$$\left(\frac{\pi k R^5}{5}\right)$$

$$M = 2\pi \frac{kx^3}{3} \bigg]_0^R = (2\pi K) \frac{R^3}{3}$$

$$\pi k = \frac{3}{2} \frac{M}{R^3}$$

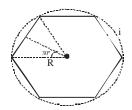
$$I_{d} = \left(\frac{3}{2}\right) \frac{M}{R_{3}} - \frac{R^{5}}{5}$$

$$\frac{3}{10}$$
MR²

18. (B)
$$\frac{1}{2}mv^2 - \frac{1}{2}(4m)\left(\frac{v}{4}\right)^2 = x\left(\frac{1}{2}mv^2\right)$$

$$\left(1-\frac{1}{4}\right)=x$$

$$x = \frac{3}{4}$$



$$B = 6 \left[\frac{\mu_0}{4\pi} \left(\frac{i}{R\cos 30^\circ} \right) (\sin 30^\circ + \sin 30^\circ) \right]$$

$$=\frac{3\mu_0i}{2\pi R}\frac{1}{\left(\sqrt{\frac{3}{2}}\right)}=\frac{\sqrt{3}\mu_0i}{\pi R}$$

$$\left(\frac{1}{4}\right) \leq 1 - \frac{T_L}{T_H}$$

$$\left(\frac{T_L}{T_H}\right) \! \leq \! \left(\frac{3}{4}\right)$$

$$(T_L)\frac{4}{3} \leq T_H$$

$$T_{_H} \geq 200^{\circ}C$$

22. (C)
$$3\left(\frac{\lambda}{2}\right)$$
 L

$$\lambda = \frac{2L}{3}$$

$$\mathbf{v} = \mathbf{v} \, \lambda$$

$$v\left(\frac{2L}{3}\right)$$

23. (B)
$$2T\left[\frac{1}{r_1} - \frac{1}{r_2}\right] = pgh$$

- 24. (A) Conceptual
- 25. (A) Conceptual
- 26. (C)

Balanced Wheatstone bridge

$$C_{eq} = \frac{18 \times 6}{18 + 6} + \frac{6 \times 2}{6 + 2}$$
$$= 4.5 + 1.5$$

$$=6\mu F$$

27. (D) Volume of cavity will also expand on heating

28. (A)
$$\varepsilon = \int_{1/2}^{31/2} Bv dx$$

$$\int\!\frac{\mu_0}{2\pi}\frac{i}{x}vdx$$

$$\frac{\mu_0}{2\pi}$$
iv ln 3

29. (C)
$$i = \sqrt{i_1^2 + i_2^2} \sin(wt + \phi)$$

$$i_{rms} \quad \frac{10}{\sqrt{2}}$$

$$\frac{\sqrt{i_1^2+i_2^2}}{\sqrt{2}}$$

30. (A) Conceptual

Chemistry

31 (C) Volume increase with rise in temperature

32 (C) Marshall's acid; H₂S₂O₈

$$HO - S - O - O - S - OH$$

33 (D)

C≡O BO = 3

O BO = 3

BO =
$$\frac{4}{3}$$

O=C=O BO = 2

BO = $\frac{1}{8}$

BO $\alpha = \frac{1}{8}$

Bond length

34 (D)
$$\Delta G = \Delta H - T\Delta S \Rightarrow +\Delta H - T(-\Delta S) \Rightarrow +\Delta H + T(\Delta S)$$

35 (A) NaHCO₃ has an acidic hydrogen which reacts with basic NaOH.

36 (B) N₂O₄(1 Mole)
$$\frac{P_1}{T_1} = \frac{P_2}{T_2} \Rightarrow \frac{1}{300} = \frac{P_2}{600} \Rightarrow P_2 = 2atm$$

 N_2O_4 \square $2NO_2$

Initial; 1mole 0

Final 0.8 0.4 Total Moles = 1.2

37 (C) $MO_x + H_2 \longrightarrow H + H_2O$ Equivalent of metal = equivalent of oxygen

$$\frac{1.05}{E}$$
 $\frac{3.15-1.05}{8}$

38 (D)
$$M_{eq}$$
 of Ag = 200 X 0.1 = 20 M_{eq} of Ag to be deposited = $\frac{20}{2}$ 10

$$M_{eq}$$
 of Ag = $\frac{i \times t}{96500} \times 1000 \Rightarrow t = 9650 \text{sec}$

39 (A) Smaller is the size of particle, faster is motion.

40 (D) Conceptual

41 (C) Ring expansion

$$\begin{array}{c|c}
 & \xrightarrow{C} & \xrightarrow{C} & \xrightarrow{+} \\
 & \xrightarrow{-H_2O} & \xrightarrow{-H^+} & \xrightarrow{-H^+} & \\
\end{array}$$

42 (C)
$$M_1V_1X_1=M_2V_2X_2$$
 0.02 x V_1 x 5 = 0.1 x 30 x 1 V_1 = 30 mL

43 (D)
$$\Delta H - \Delta U = \Delta n_g RT \Rightarrow 3 \times 8.314 \times 298 \times 10^{-3} \, KJ = +7.43 \, \text{KJ}$$

44 (B) Conceptual

45 (B)
$$CH_3 - C = H \xrightarrow{HSO_4(dil.)} CH_3 - C = H \xrightarrow{HSO_4(dil.)} CH_3 - C - C \xrightarrow{OH} H \xrightarrow{-H_2O} CH_3 - C - CH_3$$

46 (A)
$$A \rightarrow B + C + D$$

Initial
$$P_0$$
 0 0 0 Dis. x x x x

Left at t
$$P_0 - x + x + x$$

$$\mathbf{P}_0 - \mathbf{x} + \mathbf{x} + \mathbf{x} + \mathbf{x} = \mathbf{P}$$

$$P_0 + 2x = P$$

$$x = \frac{P - P_0}{2} \qquad P_x = P_0 - \left(\frac{P - P_0}{2}\right) = \frac{3P_0 - P}{2}$$

$$K \quad \frac{2.303}{t}log \quad \frac{\left(P_{_{0}}\right)}{P_{_{0}}-x}$$

$$K = \frac{2.303}{t} log \frac{P_0}{\frac{3P_0 - P}{2}}$$

$$K \quad \frac{2.303}{t} log \left(\frac{2P_0}{3P_0 - P} \right)$$

47 (D) 3° Carbo Cation are more stable, React faster

$$CH_{3}-CH_{2}-O-CH_{2}CH_{3} \\ CH_{3}-C-CH_{2}-CH_{3} \\ C_{4}H_{10}O \\ C_{4}H_{8}O$$

49 (D) Grignard's Reagent reacts easily with carbonyl group

50 (C)
$$X_B = \frac{n_B}{n_A + n_B} = \frac{1}{1 + \frac{1000}{18}}$$
 Molality = 1 molal, $n_B = 1$, $W_A = 1$ kg = 1000 g, $n_A = \frac{1000}{18}$

- 51 (C) Less electronegative element will easily donate.
- 52 (B) Bordeaux = CaO + CuSO₄ (Insecticide for grapes)
- 53 (B) Fluorescein is prepared from phthalic anhydride and resorcinol.

- 55 (D) All these are the test of protein
 - (A). Biuret Test
- (B). Ninhydrin Test (C). Xanthoprotein test

56 (B)
$$n(CH_2 = CH)$$
 Polymerise $-(CH_2 = CH)_n^ CN$ CN Polyacrylonitrile $=(PAN)$ Orlon

57 (D) AgCl is soluble in NH₃ due to complex formation.

$$AgCI + 2NH_3 \longrightarrow [Ag(NH_3)_2]CI$$

58 (C)

- 59 (C) IV is least basic because lone pair of hydrogen is in resonance and hence less available for donation.
- 60 (A) An Experimental fact depending upon the ability of the ligand to cause crystal field splitting.

MATHEMATICS

61. (A) Given;
$$(\vec{a} + 3\vec{b}) \cdot (7\vec{a} - 5\vec{b}) = 0 \Rightarrow 7\vec{a}^2 - 15\vec{b}^2 + 16\vec{a} \cdot \vec{b} = 0 \rightarrow (1)$$

Also,
$$7\vec{a}^2 + 8\vec{b}^2 - 30\vec{a}.\vec{b} = 0 \rightarrow (2)$$
 , From (1) & (2), $\vec{a}.\vec{b} = \frac{\vec{b}^2}{2} \rightarrow (3)$

Putting in (1), $\left| \vec{a} \right| \ \left| \vec{b} \right|$, so $\vec{a}.\vec{b} = ab\cos\theta \Rightarrow \theta = 60^\circ$

62. (B)
$$e = \sqrt{1 + \frac{a^2}{h^2}} \Rightarrow \sqrt{1 + \frac{1}{4}} \Rightarrow \frac{\sqrt{5}}{2}$$

63. (A)
$$\frac{ds}{dt} = (6t+3)m/s$$

$$d_1 = \int_0^1 (6t+3).dt = 6 \Rightarrow \tan \theta_1 = \frac{6}{\sqrt{3}} \Rightarrow \theta_1 = 30^\circ$$

$$d_2 = \int_0^2 (6t + 3) \cdot dt \Rightarrow \tan \theta_2 = \frac{18}{6\sqrt{3}} \Rightarrow \theta = 60^\circ \Rightarrow \theta = \theta_2 - \theta_1 = 30^\circ$$

- 64. (D) 184
- 65. (C) Use direct formula for equation of plane
- 66. (C)

67. (A)
$$\alpha\beta = \frac{c}{a} \Rightarrow \text{Length of tangent} \quad \sqrt{\frac{c}{a}}$$

- 68. (B) multiply numerator and denominator by $(1-\cos 2x)$
- 69. (A) Calculate unit vector and then find distance
- 70. (C) Use $a^{\frac{1}{2}}$ p then apply binomial expansion

71. (C)
$$T_n = (n^2 - n + 1)n! \Rightarrow (n^2 - 1)n! - (n - 2)n!$$

$$=(n-1)(n+1)!-(n-2)n!$$

$$\Rightarrow$$
 sum = $(n-1)(n+1)!$, here n=20, so sum=19(21!)

72. (B) The area of the region bounded by curve is $\frac{8a^2}{3m^3}$

Here a=3, So,
$$\frac{3}{8} = \frac{8(3)^2}{3(m)^3} \Rightarrow m = 4$$

73. (D) Pre-multiply both sides with
$$\begin{pmatrix} 5 & 0 \\ -k & 5 \end{pmatrix}$$
, So that $\frac{-2k}{5} + 25a = 0 \Rightarrow a = \frac{2k}{125}$

74. (C) Here
$$\frac{|z_1|}{2} = \frac{|z_2|}{3} = \frac{|z_3|}{4} = k = \frac{|z_1| + |z_2| + |z_3|}{2 + 3 + 4}$$

75. (A)
$$e^2x^2 - 2\pi e^2x + \pi^2 e^2 + \pi^2 y^2 - 2\pi^2 ey + e^2\pi^2 = e^2\pi^2$$

$$\Rightarrow \frac{\left(x-\pi\right)^2}{\pi^2} + \frac{\left(y-e\right)^2}{e^2} = 1 \text{ , ellipse, } a = \pi, b = e, \text{ So, } AS_1 + AS_2 = 2\pi$$

76. (D) No of five digit numbers having at least one digit repeated = $10^5 - 30240 = 69760$

77. (B) Solving the asymptotes, the centre is x=1 and y=0, since $e^{-\sqrt{2}}$

$$\frac{(x-1)^2}{a^2} - \frac{(y-0)^2}{a^2} = 1 \Rightarrow (x-1) - y \cdot \frac{dy}{dx} = 0 \quad \text{Or, } yy^1 = (x-1)$$

78. (A)
$$f(f(x))$$
 x So, $g(x) = f\left(\frac{x^2}{x}\right) = f(x)$

$$\frac{dg}{dx} = \frac{df}{dx} = -\left(\pi - x^n\right)^{\frac{1-n}{n}} x^{n-1}$$

79.(A)
$$\frac{b}{a} = \frac{c}{b} \Rightarrow \frac{b^2}{a} = c$$
 and $a+b+c=mb$

Combining above,
$$\left(\frac{b}{a}\right)^2 + (1-m)\left(\frac{b}{a}\right) + 1 = 0$$

Since,
$$\frac{b}{a}$$
 is real, $(1-m)^2 - 4(1)(1) > 0$ $\Rightarrow m < -1$ or $m > 3 \Rightarrow m_{\min} = 4$

80. (C)
$$\Box (\Box sv(\Box r \land s)) \Rightarrow s \land (\Box (\Box r \land s)) \Rightarrow s \land (rv \Box s) \Rightarrow (s \land r)v(s \land \Box s)$$

 $(s \land r)vf \Rightarrow s \land r$

81.(B) Put $x \cos^2 \theta$ or $dx = -2\cos\theta\sin\theta.d\theta$

$$\Rightarrow f(x) = \sqrt{x}$$
 and $k = -4$ $\Rightarrow f(-k) = \sqrt{4} = 2$

- 82. (A) On the left of x=99
- 83. (B) Use $\sin^{-1} x = y \Rightarrow 2y^2 y 6 = 0$

$$\Rightarrow y = 2$$
 or $y = \frac{-3}{2} \Rightarrow \sin^{-1} x \neq 2 > \frac{\pi}{2}$ So, $x = \sin^{-1} \left(\frac{-3}{2}\right) \Rightarrow$ one solution

- 84. (D)
- 85. (A) Let the number be 1,2,3,...... 9, 10, a, b

Then
$$\frac{1+2+3+....+10+a+b}{12} = 12 \Rightarrow 55+a+b=144 \Rightarrow a+b=89 \Rightarrow a=45 \& b=44$$
 Possible

86. (C)
$$I = \int_{-\pi}^{\pi} \frac{\cos^2 x}{1 + a^x} . dx \Rightarrow 2I = \int_{-\pi}^{\pi} \cos^2 x . dx$$

$$2I = \frac{1}{2} \int_{-\pi}^{\pi} \left(1 + \cos^2 x \right) . dx \Rightarrow 2I = \frac{1}{2} \left[x + \frac{\sin^2 x}{2} \right]_{-\pi}^{\pi} \Rightarrow I = \frac{\pi}{2}$$

87. (C) We observe that,
$$\left[\frac{x}{39}\right] = \left[\frac{x}{41}\right] = 0 \text{ if } x \in \{1, 2, ..., 38\}$$

$$\left[\frac{x}{39}\right] = \left[\frac{x}{41}\right] = 1 \text{ if } x \in \left\{41....77\right\}, \qquad \left[\frac{x}{39}\right] = \left[\frac{x}{41}\right] = 2 \text{ if } x \in \left\{82....116\right\}$$

$$\left[\frac{x}{39}\right] = \left[\frac{x}{41}\right] = 3 \text{ if } x \in \left\{123, \dots, 155\right\}, \qquad \left[\frac{x}{39}\right] = \left[\frac{x}{41}\right] = 19 \text{ if } x \in \left\{779\right\}$$

$$Total = 38 + (1+3+.....+37) \Rightarrow 38 + \sum_{n=1}^{19} (2n-1) = 38 + (19)^2 = 399$$

88. (A)
$$\lim_{x \to \frac{1}{2}} \left(\sin^2 \pi x \right)^{\frac{\alpha \sin^2 \pi x}{\beta \cos^2 \pi x}} \quad e^{2016} \quad \Rightarrow e^{\lim_{x \to \frac{1}{2}} \left[\frac{\alpha \sin^2 \pi x}{\beta (1 - \sin^2 \pi x)} \right] \left\{ - \left(1 - \sin^2 \pi x \right) \right\}} = e^{2016}$$

$$\frac{-\alpha}{\beta} = 2016 \Rightarrow \alpha + 2016\beta = 0$$

89. (A) Using section formula, we get, $\left(h, \frac{-b}{3}\right)$ on the circle

Therefore,
$$h^2 + \left(\frac{-b}{3}\right)^2 - ah - b\left(\frac{-b}{3}\right) = 0 \Rightarrow h^2 - ah + \frac{4b^2}{9} = 0$$

Must get distinct real roots, $D > 0 \Rightarrow a^2 - 4.4 \cdot \frac{b^2}{9} > 0 \Rightarrow 9a^2 > 16b^2$

90. (B) n(s) = No of ways of selecting 3 tickets out of (2n+1) tickets consecutively numbered = $\frac{2n+1}{3}C_3 = \frac{n(4n^2-1)}{3}$, $n(E)=1+3+....+(2n-1)=n^2$

Required Probability =
$$\frac{n(E)}{n(S)} = \frac{n^2}{n(4n^2 - 1)} 3 = \frac{3n}{4n^2 - 1}$$