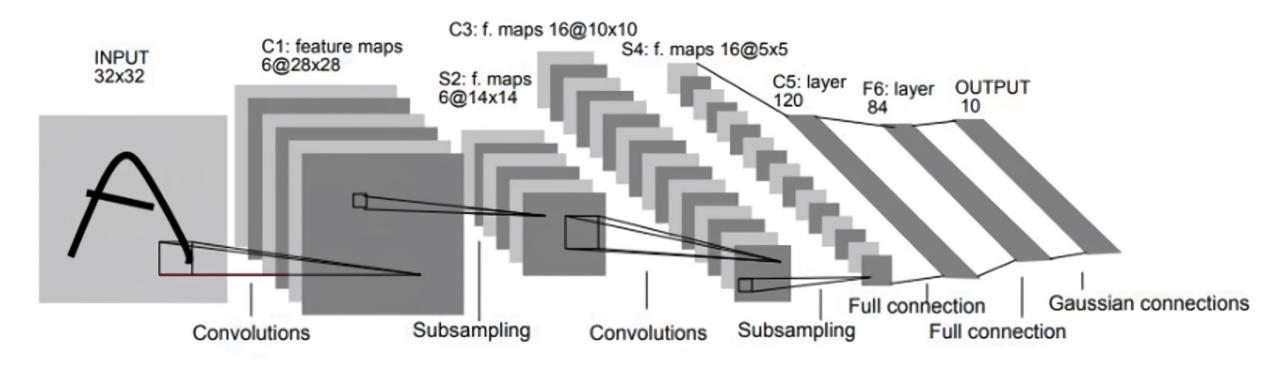
LeNet-5 on ZYBO Z7-10 FPGA

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- Overview of HW Design & SW Driver & Performance
- Future Work
- References

LeNet-5 Introduction

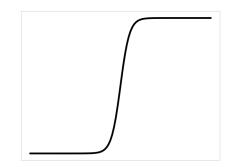


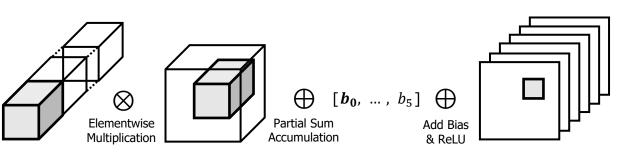
- LeNet-5 is a convolutional neural network (CNN) architecture.
- One of the first neural network architectures to achieve high accuracy on the MNIST handwritten digit recognition.
- Foundational architecture in the development of deep learning.

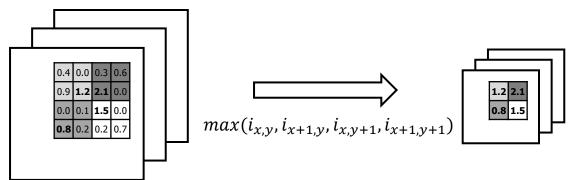
Components of LeNet-5

- Convolution
- Pooling
- Fully connected
- Activation functions
 - ReLU
 - sigmoid
 - tanh

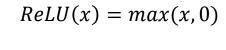
$$tanh(x) = \frac{1 - exp(-x)}{1 + exp(-x)}$$

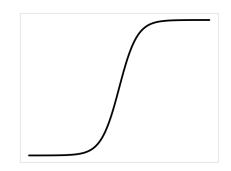


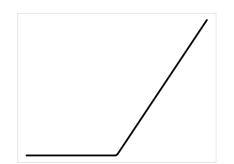


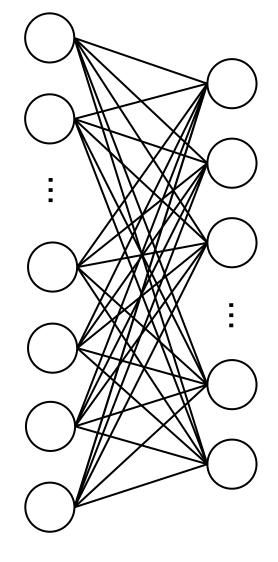


$$sigmoid(x) = \frac{1}{1 + exp(-x)}$$









Parameters of Original LeNet-5

- ZYBO Z7-10 board's resources are not enough to implement Original LeNet-5.
- ZYBO Z7-10 has far fewer resources than the ZYBO Z7-20.

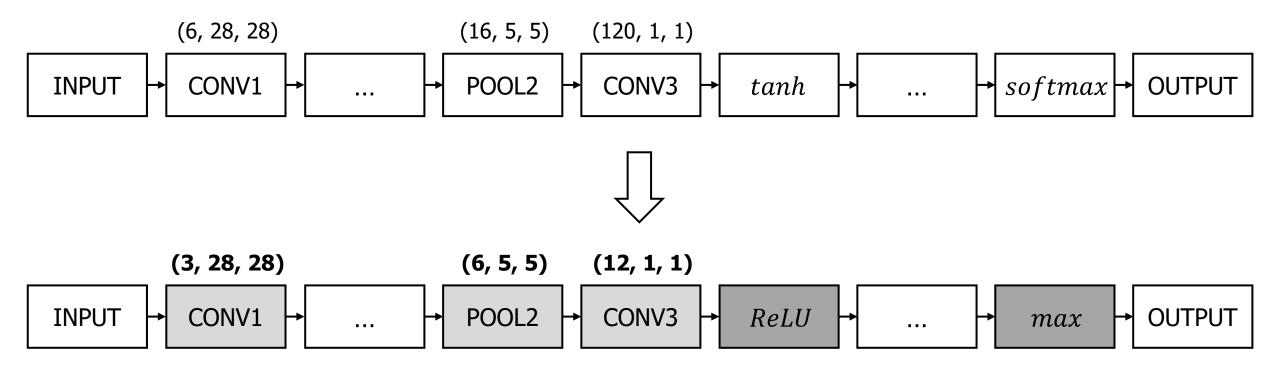
| Layer | С | WxH | Kernel | Stride | Activation | Weight + Bias | Feature map |
|---------|-----|---------|--------|--------|-------------------------|--------------------------|-------------|
| INPUT | 1 | 32 x 32 | - | - | | | 1024 |
| CONV1 | 6 | 28 x 28 | 5x5 | 1 | tanh | tanh 150 + 6 = 156 | |
| A.POOL1 | 6 | 14 x 14 | 2x2 | 2 | sigmoid | sigmoid - | |
| CONV2 | 16 | 10 x 10 | 5x5 | 1 | tanh 2400 + 16 = 2416 | | 1600 |
| A.POOL2 | 16 | 5 x 5 | 2x2 | 2 | sigmoid | sigmoid - | |
| CONV3 | 120 | 1 x 1 | 5x5 | 1 | tanh | tanh 48000 + 120 = 48120 | |
| FC1 | - | 120 | - | - | tanh 10080 + 84 = 10164 | | 84 |
| FC2 | - | 84 | - | - | softmax 840 + 10 = 850 | | 10 |
| Total | - | - | - | - | - | - 61706 | |

| | ZYBO Z7-10 |
|-----------|------------|
| LUT | 17,600 |
| Flip-Flop | 35,200 |
| Block RAM | 270 KB |
| DSP | 80 |
| Slice | 4,400 |
| | |

| | ZYBO Z7-20 |
|-----------|------------|
| LUT | 53,200 |
| Flip-Flop | 106,400 |
| Block RAM | 630 KB |
| DSP | 220 |
| Slice | 13,300 |

Optimization for FPGA Implementation (Model-level)

- Model-level optimization of LeNet-5 from a hardware accelerator perspective.
 - Activation function
 - Model lightening



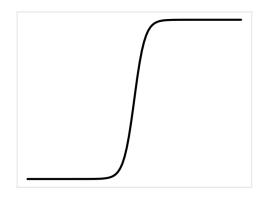
Activation Function (*ReLU* vs. *tanh*, *sigmoid*)

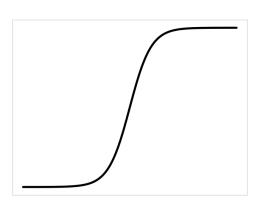
- tanh(x) or sigmoid(x) function in hardware requires additional resources to perform exponentiation and division operations.
- ReLU(x) function can be implemented using basic logical and arithmetic operations, resulting in minimal hardware complexity.
- ReLU(x) helps alleviate the vanishing gradient problem that occurs in activation functions such as tanh(x) or sigmoid(x).

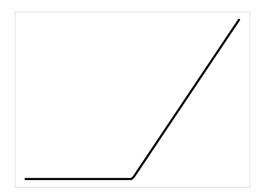
$$tanh(x) = \frac{1 - exp(-x)}{1 + exp(-x)}$$

$$sigmoid(x) = \frac{1}{1 + exp(-x)} \qquad ReLU(x) = max(x, 0)$$

$$ReLU(x) = max(x, 0)$$







Activation Function $(max \ vs. \ softmax)$

- $softmax(\vec{x})$ function in hardware also requires additional resources to perform exponentiation and division operations.
- $max(\vec{x})$ function also can be implemented using basic logical and arithmetic operations, resulting in minimal hardware complexity.
- For both $softmax(\vec{x})$ and $max(\vec{x})$ functions, using the maximum value is the same, so the $max(\vec{x})$ function was used in consideration of efficiency.

$$softmax(\vec{x}) = \frac{exp(x_i)}{\sum_{i=1}^{k} exp(x_i)}, (for \ i = 1, 2, ...k)$$
 $max(\vec{x}) = max(x_0, x_1, ..., x_k)$

Model lightening & Parameters of Light LeNet-5

- Adjust the parameters of each layer to make the model smaller.
- *sigmoid*, *tanh* are replaced by *ReLU*.
- Weights and biases were reduced by **96%**, and feature maps were reduced by **48%**.

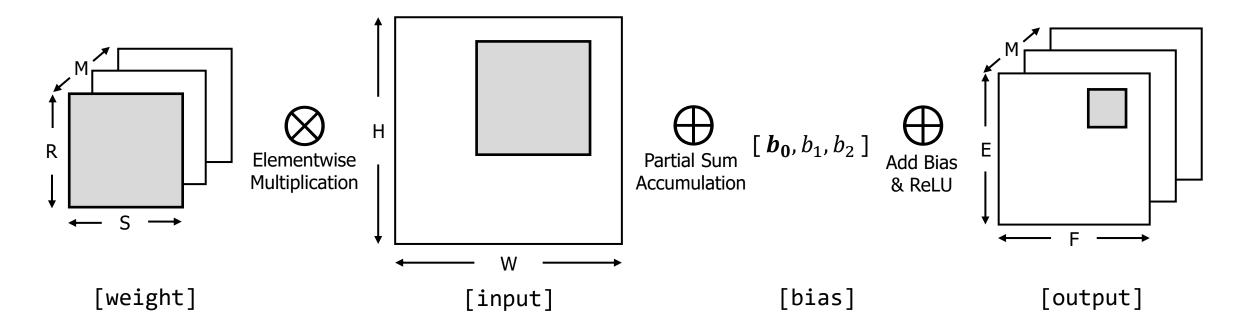
| Layer | С | WxH | Kernel | Stride | Activation | Weight + Bias | Feature map |
|---------|----|---------|--------|--------|------------|------------------|-------------|
| INPUT | 1 | 32 x 32 | - | - | - | - | 1024 |
| CONV1 | 3 | 28 x 28 | 5x5 | 1 | ReLU | 75 + 3 = 78 | 2352 |
| M.POOL1 | 3 | 14 x 14 | 2x2 | 2 | - | - | 588 |
| CONV2 | 6 | 10 x 10 | 5x5 | 1 | ReLU | 450 + 6 = 456 | 600 |
| M.POOL2 | 6 | 5 x 5 | 2x2 | 2 | - | - | 150 |
| CONV3 | 12 | 1 x 1 | 5x5 | 1 | ReLU | 1800 + 12 = 1812 | 12 |
| FC1 | - | 120 | - | - | ReLU | 120 + 10 = 130 | 10 |
| FC2 | - | 84 | - | - | Мах | 100 + 10 = 110 | 10 |
| Total | - | - | - | - | - | 2586 | 4746 |

| | ZYBO Z7-10 |
|-----------|------------|
| LUT | 17,600 |
| Flip-Flop | 35,200 |
| Block RAM | 270 KB |
| DSP | 80 |
| Slice | 4,400 |

| | ZYBO Z7-20 |
|-----------|------------|
| LUT | 53,200 |
| Flip-Flop | 106,400 |
| Block RAM | 630 KB |
| DSP | 220 |
| Slice | 13,300 |

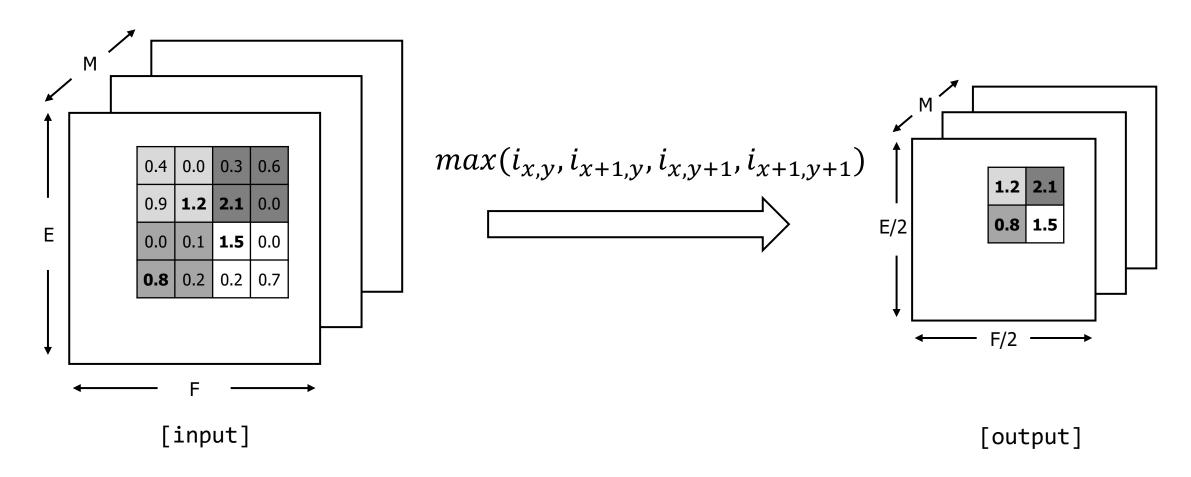
1st Convolution layer

- Input (32 x 32) -> Output (3 x 28 x 28)
- $O[u][x][y] = \sum_{i=0}^{S-1} \sum_{j=0}^{R-1} I[x+i][y+j] * W[u][i][j] + B[u]$
- $0 \le u < M, 0 \le x < F, 0 \le y < E$
- W = F + S 1, H = E + R 1



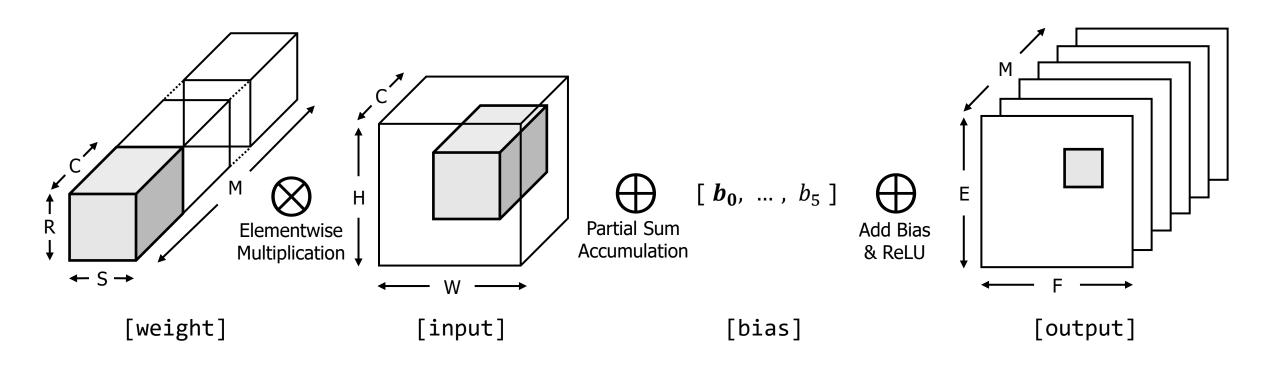
1st Pooling layer

- Input (3 x 28 x 28) -> Output (3 x 14 x 14)
- 2x2 Max pooling, stride 2



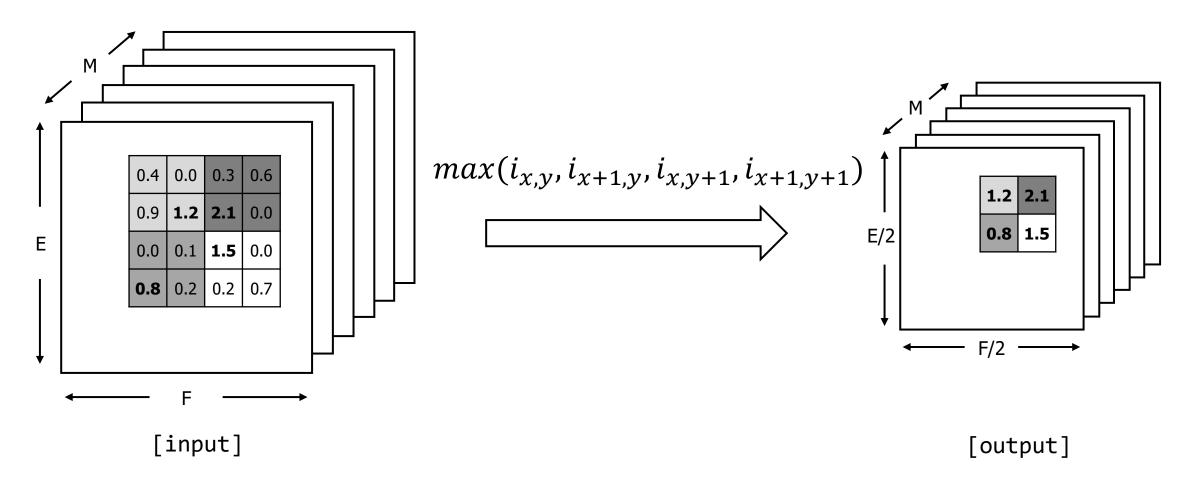
2nd Convolution layer

- Input (3 x 14 x 14) -> Output (6 x 10 x 10)
- $O[u][x][y] = \sum_{k=0}^{C-1} \sum_{i=0}^{S-1} \sum_{j=0}^{R-1} I[k][x+i][y+j] * W[u][k][i][j] + B[u]$
- $0 \le u < M, 0 \le x < F, 0 \le y < E$
- W = F + S 1, H = E + R 1



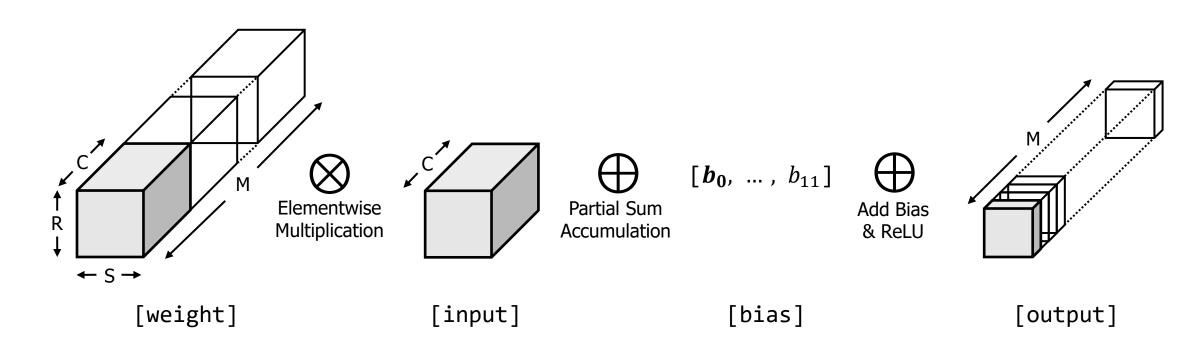
2nd Pooling layer

- Input (6 x 10 x 10) -> Output (6 x 5 x 5)
- 2x2 Max pooling, stride 2



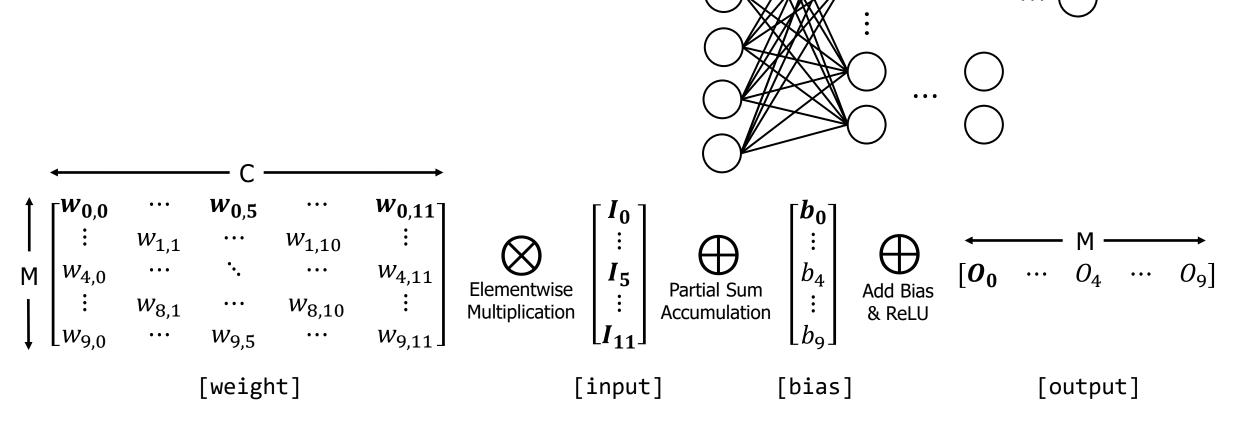
3rd Convolution layer

- Input (6 x 5 x 5) -> Output (12 x 1 x 1)
- $O[u] = \sum_{k=0}^{C-1} \sum_{i=0}^{S-1} \sum_{j=0}^{R-1} I[k][i][j] * W[u][k][i][j] + B[u]$
- $0 \le u < M$
- W = S, H = R, E = F = 1



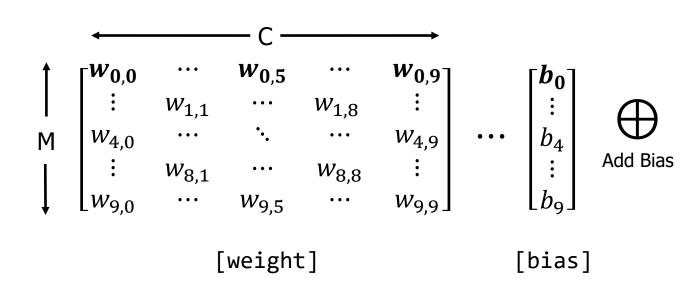
1st Fully Connected layer

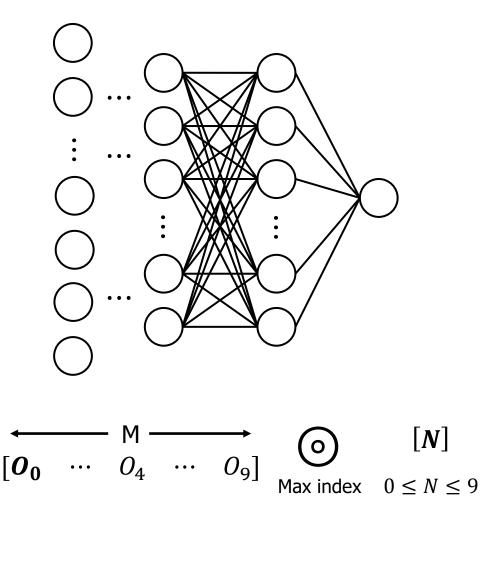
- Input (12) -> Output (10)
- $O[u] = \sum_{k=0}^{C-1} I[k] * W[u][k] + B[u]$
- $0 \le u < M$



2nd Fully Connected layer

- Input (10) -> Output (10)
- $O[u] = \sum_{k=0}^{C-1} I[k] * W[u][k] + B[u]$
- $0 \le u < M$
- Infer a number by finding index of max value.



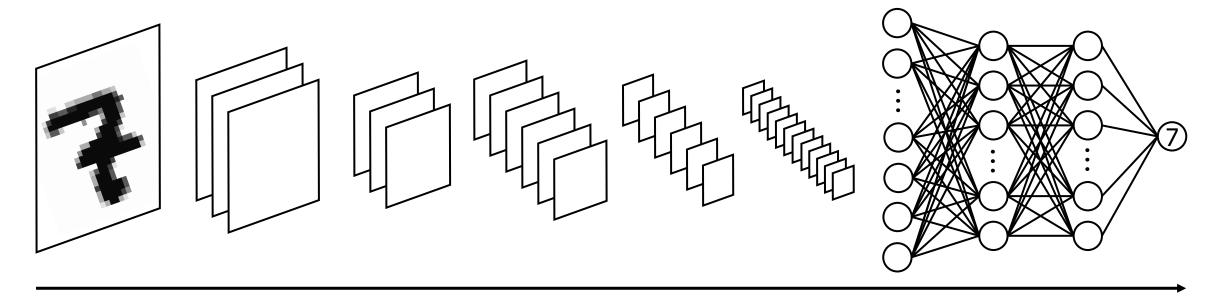


[intermediate output]

[output]

Overview of Optimized LeNet-5 (Light LeNet-5)

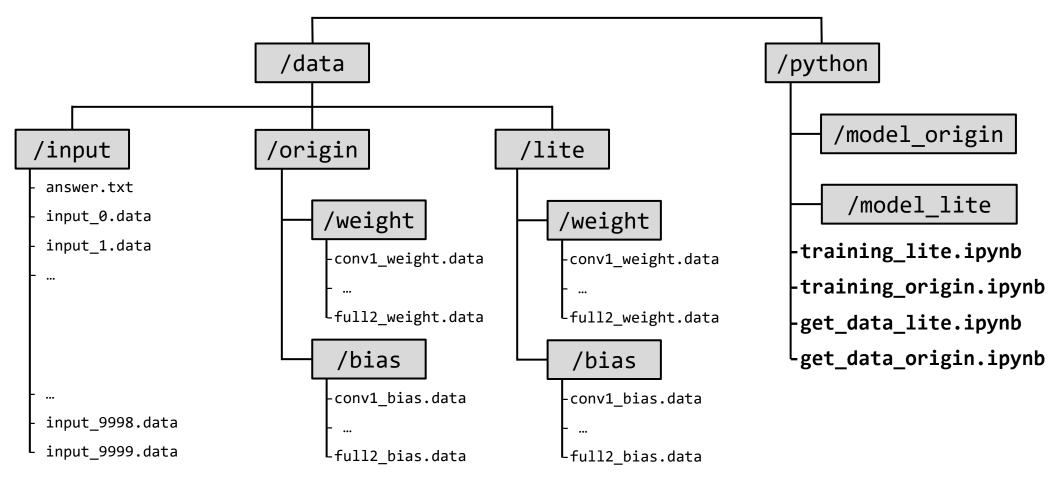
- Feature maps were reduced by 48%, weights and biases were reduced by 96%.
- sigmoid, tanh are replaced by ReLU.



| | INPUT | CONV1 | POOL1 | CONV2 | POOL2 | CONV3 | FULL1 | FULL2 | OUTPUT |
|---------------|---------|-------------|-------------|-------------|-----------|------------|-------|-------|--------|
| Feature Map | 32 x 32 | 3 @ 28 x 28 | 3 @ 14 x 14 | 6 @ 10 x 10 | 6 @ 5 x 5 | 12 @ 1 x 1 | 10 | 10 | 1 |
| Weight + Bias | - | 78 | - | 456 | - | 1812 | 130 | 110 | - |
| Activation | - | ReLU | - | ReLU | - | ReLU | ReLU | Мах | - |

Implementation of LeNet-5 using Python, Cont'd

- TensorFlow is used to build LeNet-5.
- Get data such as pre-trained weights and biases.
- Get data such as inputs and answer.



Implementation of LeNet-5 using Python, Cont'd

• In training_origin.ipynb, build, train, and evaluate the original model.

| # Build model using Sequential API import tensorflow as tf | <pre># Print model information model.summary()</pre> | | | | |
|--|---|--------------------|---------|--|--|
| <pre>model = models.Sequential()</pre> | Layer (type) | Output Shape | Param # | | |
| <pre>model.add(layers.Conv2D(6, 5, 'tanh')) model.add(layers.AveragePooling2D(2))</pre> | conv1 (Conv2D) | (None, 28, 28, 6) | 156 | | |
| <pre>model.add(layers.Activation('sigmoid'))</pre> | pool1 (AveragePooling2D) | (None, 14, 14, 6) | 0 | | |
| <pre>model.add(layers.Conv2D(16, 5, 'tanh')) model.add(layers.AveragePooling2D(2))</pre> | activation (Activation) | (None, 14, 14, 6) | 0 | | |
| <pre>model.add(layers.Activation('sigmoid')) model.add(layers.Conv2D(120, 16, 'tanh'))</pre> | conv2 (Conv2D) | (None, 10, 10, 16) | 2416 | | |
| model.add(layers.Flatten()) | pool2 (AveragePooling2D) | (None, 5, 5, 16) | 0 | | |
| <pre>model.add(layers.Dense(10, 'tanh')) model.add(layers.Dense(10, 'softmax'))</pre> | activation_1 (Activation) | (None, 5, 5, 16) | 0 | | |
| | conv3 (Conv2D) | (None, 1, 1, 120) | 48120 | | |
| # Training model | flatten (Flatten) | (None, 120) | 0 | | |
| <pre>model.compile() model.fit()</pre> | full1 (Dense) | (None, 84) | 10164 | | |
| | full2 (Dense) | (None, 10) | 850 | | |
| # Get loss value and accuracy model.evaluate() 200/200 [=======] - loss: 0.1888, accuracy: 0.9406 | Total params: 61,706 Trainable params: 61,706 Non-trainable params: 0 | | | | |

Implementation of LeNet-5 using Python, Cont'd

• In training_lite.ipynb, build, train, and evaluate light model.

| <pre># Print model information model.summary()</pre> | | | | | |
|---|-------------------------------|--|--|--|--|
| Layer (type) | Output Shape | Param # | | | |
| conv1 (Conv2D) | (None, 28, 28, 3) | 78 | | | |
| pool1 (MaxPooling2D) | (None, 14, 14, 3) | 0 | | | |
| conv2 (Conv2D) | (None, 10, 10, 6) | 456 | | | |
| pool2 (MaxPooling2D) | (None, 5, 5, 6) | 0 | | | |
| conv3 (Conv2D) | (None, 1, 1, 12) | 1812 | | | |
| flatten (Flatten) | (None, 12) | 0 | | | |
| full1 (Dense) | (None, 10) | 130 | | | |
| full2 (Dense) | (None, 10) | 110 | | | |
| Total params: 2,586 Trainable params: 2,586 Non-trainable params: 0 | | | | | |
| | model.summary() Layer (type) | model.summary() Layer (type) Output Shape | | | |

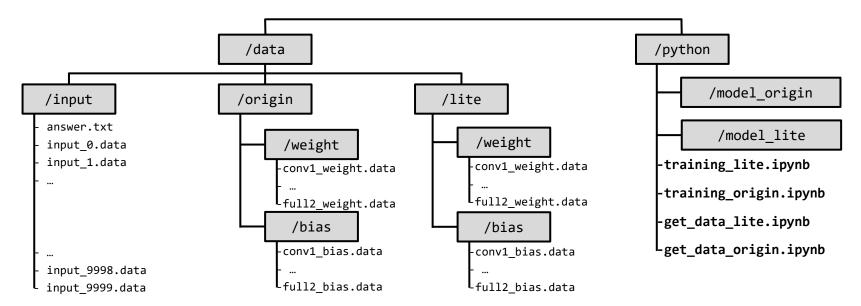
Implementation of LeNet-5 using Python

In get_data_lite.ipynb, get the weights and biases processed for ease of use.

```
# Get weights and biases
                                                           # Shape of weights and biases before processing
weight bias dict = {}
                                                           name: conv1 weight shape: (5, 5, 1, 3) bias shape: (3,)
layer list = []
                                                           name: conv2 weight shape: (5, 5, 3, 6) bias shape: (6,)
                                                           name : conv3 weight shape : (5, 5, 6, 12) bias shape : (12,)
for layer in model.layers:
                                                           name : full1 weight shape : (12, 10)
                                                                                                    bias shape : (10,)
   layer list.append(layer.name)
                                                           name : full2 weight shape : (10, 10)
                                                                                                     bias shape : (10,)
   # No trainable params
   if 'pool' in layer.name or 'flatten' in layer.name:
                                                           # Shape of weights and biases after processing
       continue
                                                           name : conv1 weight shape : (3, 5, 5)
                                                                                                     bias shape : (3,)
   weight bias dict[layer.name] = layer.get weights()
                                                           name: conv2 weight shape: (6, 3, 5, 5) bias shape: (6,)
                                                           name : conv3 weight shape : (12, 6, 5, 5) bias shape : (12,)
                                                           name : full1 weight shape : (10, 12)
                                                                                                    bias shape : (10,)
# Process weights to use easily in C/C++
                                                           name: full2 weight shape: (10, 10)
                                                                                                     bias shape: (10,)
for key, value in weight bias dict.items():
   if 'conv' in key:
                                                           # Flatten and save wegihts and biases
       tp weight = tf.transpose(value[0])
                                                           for key, value in weight bias dict.items()
       weight = tf.transpose(tp weight, [0,1,3,2])
                                                               value[0] = tf.reshape(value[0], [-1]) # -1 means flatten
       value[0] = tf.squeeze(weight)
                                                               # save as txt file
   if 'full' in key:
                                                               np.savetxt('../data/weight/...' value[0], fmt = "%.10f")
       tp weight = tf.transpose(value[0])
                                                               np.savetxt('../data/bias/...' value[1], fmt = "%.10f")
       value[0] = tf.squeeze(tp weight)
```

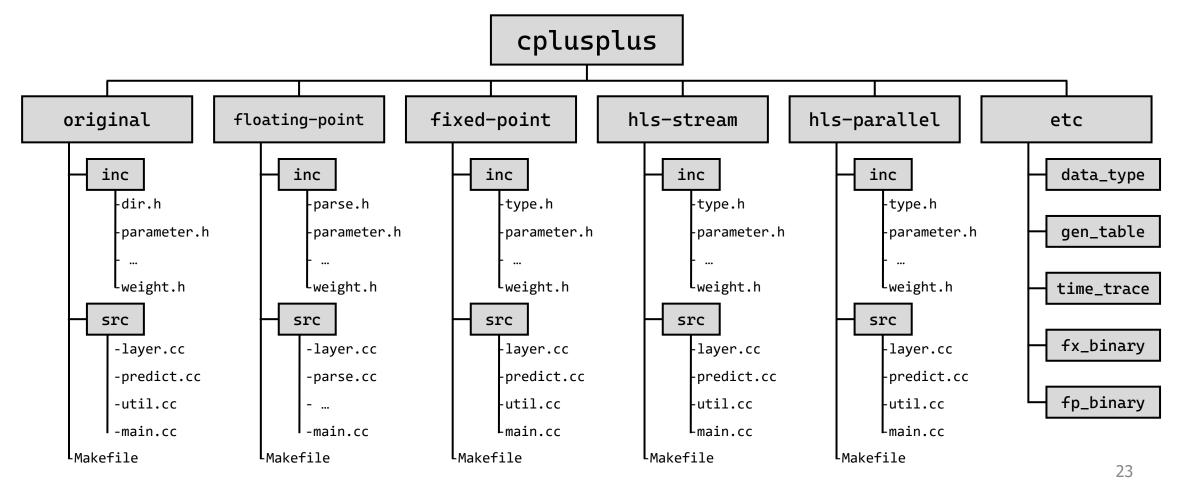
Overview of implementation of LeNet-5 using python

- TensorFlow is used to build LeNet-5.
 - In training_origin.ipynb, build, train, and evaluate the original model.
 - In training_lite.ipynb, build, train, and evaluate light model.
- Get data such as pre-trained weights and biases.
 - In get_data_lite.ipynb, get the weights and biases processed for ease of use.
- Get data such as inputs and answer.
 - In get_data_lite.ipynb, get the inputs and answer.



Implementation of LeNet-5 using C/C++

- cplusplus directory structure.
- Makefile can compile each folder.
- etc directory serves to analyze the result, save input txt file as a binary, or generate weight table.



Fixed-Point vs. Floating-Point, Cont'd

Comparison by data type using Vivado HLS.

```
Tests to determine latency, utilization,
   and max frequency by data type.
*/
#define NUM 32
typedef int data t;
// typedef ap fixed<32, 16> data t;
// typedef half data t;
void test(data t in[NUM], ..., data t out[NUM])
    for (int i = 0; i < NUM; i++) {
        data t result = bias[i];
        for (int j = 0; j < NUM; j++) {
            result += in[j] * weight[i][j];
        out[i] = result;
```

[Latency (clock cycles)]

| | short | fix16 | half | int | fix32 | float |
|---------|-------|-------|-------|------|-------|-------|
| Latency | 3169 | 3169 | 11361 | 4193 | 4193 | 11361 |

[Resource Usage Implementaion]

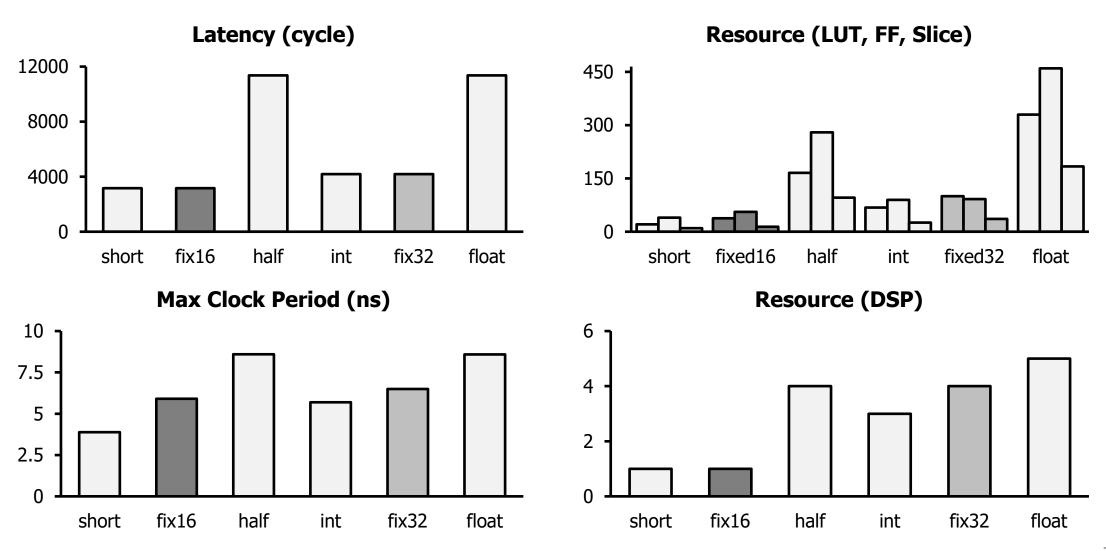
| | short | fixed16 | half | int | fixed32 | float |
|-------|-------|---------|------|-----|---------|-------|
| LUT | 21 | 38 | 166 | 68 | 100 | 330 |
| FF | 40 | 56 | 280 | 90 | 92 | 460 |
| DSP | 1 | 1 | 4 | 3 | 4 | 5 |
| SLICE | 10 | 14 | 96 | 26 | 36 | 184 |

[Final Timing Implementation]

| | short | fix16 | half | int | fix32 | float |
|-----------|--------|--------|--------|--------|--------|--------|
| CP Req. | 10.000 | 10.000 | 10.000 | 10.000 | 10.000 | 10.000 |
| Post-Impl | 3.884 | 5.911 | 8.598 | 5.692 | 6.501 | 8.585 |

Fixed-Point vs. Floating-Point

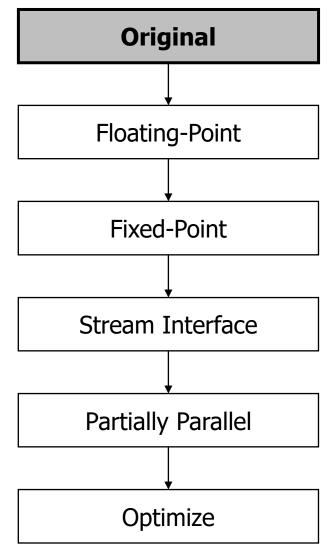
• Results of sysnthesis and implementation using Vivado HLS.



Original LeNet-5 with C/C++, Cont'd

- Implementation of original LeNet-5.
- Check accuracy to ensure that it is implemented correctly.
- Use tanh or sigmoid instead of ReLU for activation function.
- Use Average Pooling instead of Max Pooling.

| Layer | С | WxH | Kernel | Stride | Activation | Weight + Bias | Feature map |
|---------|-----|---------|--------|--------|------------|---------------------|-------------|
| INPUT | 1 | 32 x 32 | - | - | - | - | 1024 |
| CONV1 | 6 | 28 x 28 | 5x5 | 1 | tanh | 150 + 6 = 156 | 4704 |
| A.POOL1 | 6 | 14 x 14 | 2x2 | 2 | sigmoid | - | 1176 |
| CONV2 | 16 | 10 x 10 | 5x5 | 1 | tanh | 2400 + 16 = 2416 | 1600 |
| A.POOL2 | 16 | 5 x 5 | 2x2 | 2 | sigmoid | - | 400 |
| CONV3 | 120 | 1 x 1 | 5x5 | 1 | tanh | 48000 + 120 = 48120 | 120 |
| FC1 | - | 120 | - | - | tanh | 10080 + 84 = 10164 | 84 |
| FC2 | - | 84 | - | - | softmax | 840 + 10 = 850 | 10 |
| Total | - | - | - | - | - | 61706 | 9118 |



Original LeNet-5 with C/C++, Cont'd

```
/* layer.cc */
void full1 layer(float input[...][...],
                 float output[...] [...] )
    for (int row = 0; row < ...; ...) {
        float acc = full1 bias[row];
        for (int col = 0; col < ...; ...) {
            acc += input[col] * full1 weight[row][col];
        output[row] = (float)std::tanh(acc); // tanh activation
void pool1 layer(float input[...][...][...],
                float output[...][...])
    for (int num = 0; num < ...; ...) {
        for (int row = 0; row < ...; ...) {
            for (int col = 0; col < ...; ...) {
                float avg = 0.0;
                 avg += input[num][row][col];
                 avg = (float)(avg / 4.0);
               // sigmoid activation
                 output[num][row >> 1][col >> 1] = sigmoid(avg);
```

```
/* predict.cc */
uint8 t predict(float* input) {
   /* Intermediate outputs */
   float conv1 output[...] [...] = { 0.0 };
   float full2 output[...] = { 0.0 };
   /* 1st convolution layer */
   conv1 layer(input, conv1 output);
   /* 1st pooling layer */
   pool1 layer(conv1 output, pool1 output);
   /* 2nd convolution layer */
   conv2 layer(pool1 output, conv2 output);
   /* 2nd pooling layer */
   pool2 layer(conv2 output, pool2 output);
   /* 3th convolution layer */
   conv3 layer(pool2 output, conv3 output);
   /* 1st fully connected layer */
   full1 layer(conv3 output, full1 output);
   /* 2nd fully connected layer */
   full2 layer(full1 output, full2 output);
   /* Return result */
   return softmax(full2 output);
```

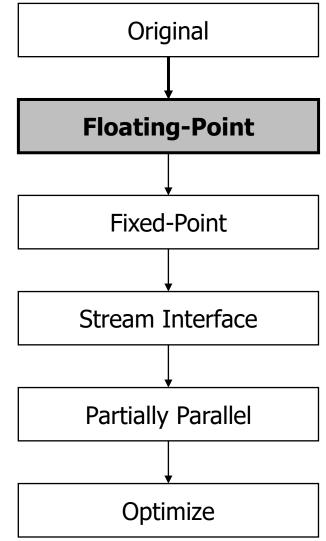
Original LeNet-5 with C/C++

• Similar to the accuracy obtained from python (0.9406)

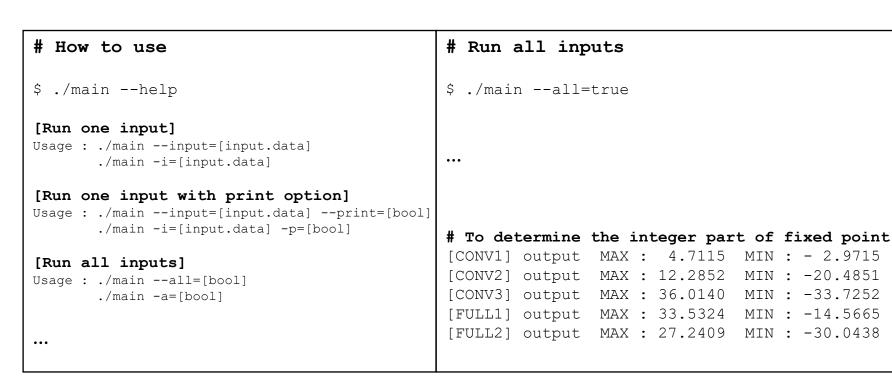
```
/* main.cc */
                                                                     # Run all inputs
                                                                     $ ./main
int main (int argc, char* argv[]) {
    int err cnt = 0;
                                                                            Number Answer Predict
   for (size t i = 0; i < TEST NUM; i++) {
                                                                      [TRUE] [
                                                                                0] 7
                                                                      [TRUE] [ 1] 2
                                                                      [TRUE] [ 2] 1
       my answer[i] = predict(input array);
                                                                      [TRUE] [ 3] 0
       if (my answer != answer[i]) {
          err cnt++;
                                                                      [TRUE] [9996] 3
           cout << "[ FALSE ] " ... << "\n";
                                                                      [TRUE] [9997] 4
                                                                      [TRUE] [9998] 5
       else {
                                                                      [TRUE] [9999] 6
           cout << "[ TRUE ] " ... << "\n";
                                                                      [Original LeNet-5]
                                                                     Accuracy : 94.55 [%]
                                                                     Error : 545 [cases]
    accuracy = ((float)(TEST NUM - err cnt)/(float)TEST NUM) * 100;
    cout << "\n[Original LeNet-5]\n";</pre>
    cout << "Accuracy : " << setw(5) << accuracy << ...;</pre>
    cout << "Error : " << setw(5) << err cnt << ...;</pre>
    return 0;
```

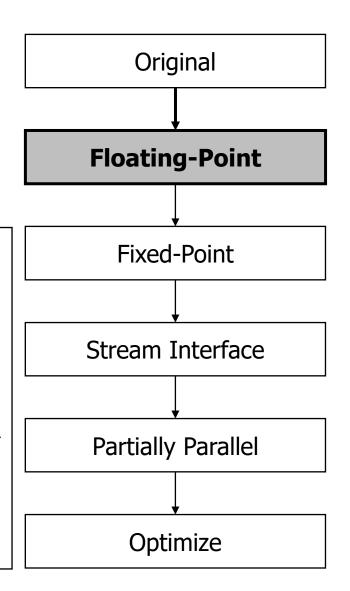
- Implementation of light LeNet-5 using floating point.
- Use *ReLU* instead of *sigmoid* or *tanh* for activation function.
- Use Max Pooling instead of Average Pooling.
- Use max instead of softmax for output layer.

| Layer | С | WxH | Kernel | Stride | Activation | Weight + Bias | Feature map |
|---------|----|---------|--------|--------|------------|------------------|-------------|
| INPUT | 1 | 32 x 32 | - | - | - | - | 1024 |
| CONV1 | 3 | 28 x 28 | 5x5 | 1 | ReLU | 75 + 3 = 78 | 2352 |
| M.POOL1 | 3 | 14 x 14 | 2x2 | 2 | - | - | 588 |
| CONV2 | 6 | 10 x 10 | 5x5 | 1 | ReLU | 450 + 6 = 456 | 600 |
| M.POOL2 | 6 | 5 x 5 | 2x2 | 2 | - | - | 150 |
| CONV3 | 12 | 1 x 1 | 5x5 | 1 | ReLU | 1800 + 12 = 1812 | 12 |
| FC1 | - | 120 | - | - | ReLU | 120 + 10 = 130 | 10 |
| FC2 | - | 84 | - | - | Мах | 100 + 10 = 110 | 10 |
| Total | - | - | - | - | - | 2586 | 4746 |



- Enble to run with 3 options.
 - Run one input.
 - Run one input + Print intermediate results (Debug).
 - Run all (Chcek accuracy and find Max/Min value).
- Integer part of fixed point can be determined through Run all option.





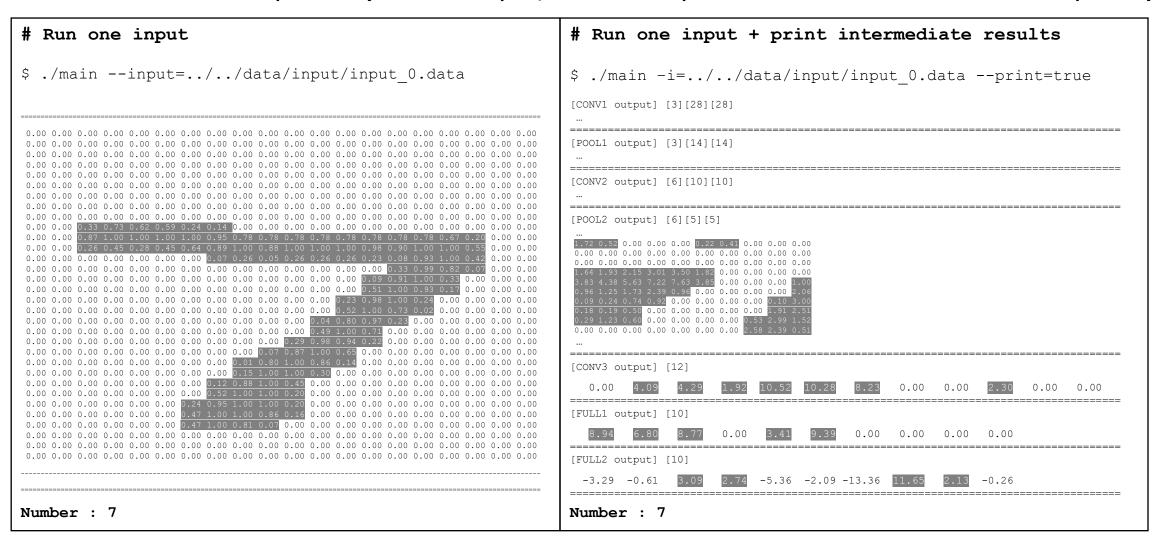
```
/* laver.cc */
void full1 layer(float input[...], float output[...])
    for (int row = 0; row < ...; ...) {
        float acc = full1 bias[row];
        for (int col = 0; col < ...; ...) {
            acc += input[col] * full1 weight[row][col];
... // ReLU function exists to find the MAX/MIN value
void relu4 layer(float input[...], float output[...])
    for (int i = 0; i < ...; ...)
        output[i] = input[i] > 0.0 ? input[i] : 0.0;
void pool1 layer(float input[...][...][...],
                  float output[...] [...] ( ...] (
    for (int num = 0; num < ...; ...) {
        for (int row = 0; row < ...; ...) {
            for (int col = 0; col < ...; ...) {
                max = input[num][row][col];
                ... // find max
                output[num][row >> 1][col >> 1] = max;
```

```
/* predict.cc */
uint8 t predict(float* input, float* conv1 max, float* conv1 min,
                              float* full2 max, float* full2 min) {
    /* Intermediate outputs */
   float conv1 output[...] [...] = { 0.0 };
   float relu1 output[...][...] = { 0.0 };
   float pool1 output[...][...] = { 0.0 };
   float full2 output[...] = { 0.0 };
    /* 1st convolution layer */
    conv1 layer(input, conv1 output);
    /* 1st ReLU layer */
    relu1 layer(conv1 output, relu1 output);
    /* 2nd fully connected layer */
    full2 layer(relu4 output, full2 output);
    /* Find the MAX/MIN value of each intermediate result.
    *conv1 max = *std::max element(conv1 output, ...);
    *full2 max = *std::max element(full2 output, ...);
    *conv1 min = *std::min element(conv1 output, ...);
    *full2 min = *std::min element(full2 output, ...);
    /* Return result */
    return result(full2 output);
                                                                 31
```

Enble to run with 3 options. (Run all option)

```
# How to use
                                                                          # Run all inputs
                                                                          $ ./main --all=true
$ ./main --help
[Run one input]
                                                                                  Number Answer Predict
Usage : ./main --input=[input.data]
                                                                                      0 ]
                                                                           [TRUE] [
       ./main -i=[input.data]
                                                                                      11 2
                                                                          [TRUE] [
                                                                          [TRUE] [
[Run one input with print option]
                                                                          [TRUE] [ 3] 0
Usage : ./main --input=[input.data] --print=[bool]
       ./main -i=[input.data] -p=[bool]
                                                                           [TRUE] [9996] 3
[Run all inputs]
                                                                          [TRUE] [9997] 4
Usage : ./main --all=[bool]
                                                                          [TRUE] [9998] 5
       ./main -a=[bool]
                                                                          [TRUE] [9999] 6
--input=[input] | -i=[input]
                           File name to run.
                                                                          [Floating-Point]
                           [input] must be txt file.
                                                                          Accuracy: 97.47 [%]
                           [input] extension must be *.data.
                           This option is required.
                                                                                         253 [cases]
                                                                          Error
--print=[bool] | -p=[bool]
                           Determine whether to print intermediate result.
                                                                          # To determine the integer part of fixed point
                           [bool] must be true or false with small letters.
                           This option is optional.
                                                                          [CONV1] output
                                                                                             MAX : 4.7115
                                                                                                              MIN : - 2.9715
                                                                          [CONV2] output
                                                                                             MAX : 12.2852
                                                                                                              MIN : -20.4851
--all=[bool] | -a=[bool]
                           Determine whether run all test cases.
                                                                                                              MIN : -33.7252
                                                                          [CONV3] output
                                                                                             MAX : 36.0140
                           [bool] must be true or false with small letters.
                                                                                             MAX : 33.5324 MIN : -14.5665
                                                                          [FULL1] output
                           This option is optional.
                                                                          [FULL2] output
                                                                                             MAX : 27.2409
                                                                                                              MIN : -30.0438
--help | -h
                           Display this information.
```

• Enble to run with 3 options. (Run one input, Run one input + Print intermediate results options)



- Compare floating-point and fixed-point in terms of :
 - Latency
 - Resource
 - Max frequency

[Latency (clock cycles)]

| | short | fix16 | half | int | fix32 | float |
|---------|-------|-------|-------|------|-------|-------|
| Latency | 3169 | 3169 | 11361 | 4193 | 4193 | 11361 |

[Resouce Usage Implementaion]

| | short | fixed16 | half | int | fixed32 | float |
|-------|-------|---------|------|-----|---------|-------|
| LUT | 21 | 38 | 166 | 68 | 100 | 330 |
| FF | 40 | 56 | 280 | 90 | 92 | 460 |
| DSP | 1 | 1 | 4 | 3 | 4 | 5 |
| SLICE | 10 | 14 | 96 | 26 | 36 | 184 |

[Final Timing Implementation]

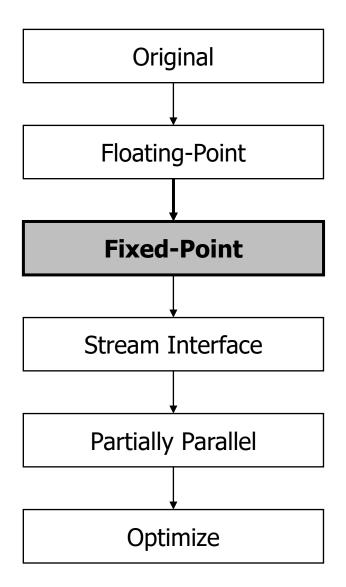
| | short | fix16 | half | int | fix32 | float |
|-----------|--------|--------|--------|--------|--------|--------|
| CP Req. | 10.000 | 10.000 | 10.000 | 10.000 | 10.000 | 10.000 |
| Post-Impl | 3.884 | 5.911 | 8.598 | 5.692 | 6.501 | 8.585 |

[ZYBO Z7-10 Resource]

| | ZYBO Z7-10 |
|-------------|------------|
| LUT | 17,600 |
| Flip-Flop | 35,200 |
| Block RAM | 270 KB |
| DSP | 80 |
| Logic slice | 4,400 |

[ZYBO Z7-20 Resource]

| | ZYBO Z7-20 | | |
|-------------|------------|--|--|
| LUT | 53,200 | | |
| Flip-Flop | 106,400 | | |
| Block RAM | 630 KB | | |
| DSP | 220 | | |
| Logic slice | 13,300 | | |



- Determine integer part of fixed point.
 - Using etc/data_type/
- Include Xilinx HLS library to use <ap_fixed.h>
- For the *Round*, *Convert* formulas,
- Refer to the paper "Deep Learning with Limited Numerical Precision"

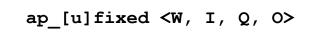
[Round & Saturation formula]

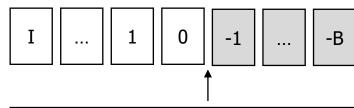
$$Round(x, < I, F >) = \begin{cases} [x] & if [x] \le x \le [x] + \frac{\epsilon}{2} \\ [x] + \epsilon & if [x] + \frac{\epsilon}{2} < x \le [x] + \epsilon \end{cases}$$

where
$$\epsilon = 2^{-F}$$

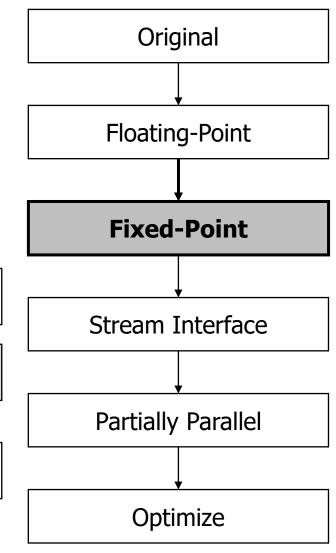
$$Convert(x, < I, F >) = \begin{cases} -2^{I-1} & \text{if } x \le -2^{I-1} \\ 2^{I-1} - 2^{-F} & \text{if } x \ge 2^{I-1} - 2^{-F} \\ Round(x, < I, F >) & \text{otherwise} \end{cases}$$

[Fixed point data type]





Binary Point : W = I + B

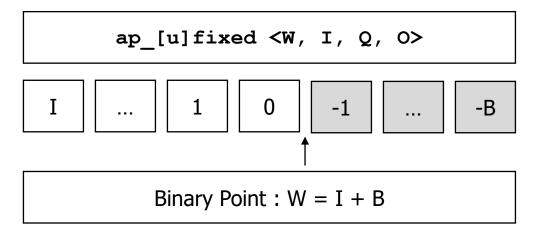


Determine integer part of fixed point using etc/data_type directory.

```
/* data type.cc */
                                                      /* data type.cc */
                                                      conv1 o = fx integer(CONV1 MAX, CONV1 MIN);
// Data from ./main --all=true command output
#define CONV1 MAX 4.71154
                                                      conv3 w = fx integer(max conv3 weight, min conv3 weight);
#define CONV1 MIN -2.97152
#define CONV2 MAX 12.2852
                                                      full2 b = fx integer(max full2 bias, min full2 bias);
#define CONV2 MIN -20.4851
#define CONV3 MAX 36.0140
                                                      # Run data type
#define CONV3 MIN -33.7252
                                                      $ ./data type
#define FULL1 MAX 33.5324
#define FULL1 MIN -14.5665
                                                       [CONV1 OUTPUT] integer part: 4
#define FULL2 MAX 27.2409
                                                       [CONV2 OUTPUT] integer part : 6
#define FULL2 MIN -30.0438
                                                       [CONV3 OUTPUT] integer part: 7
                                                      [FULL1 OUTPUT] integer part : 7
  QI = ceiling(log_2(max(abs[\alpha_{max}, \alpha_{min}]) + 1)) + 1
                                                       [FULL2 OUTPUT] integer part: 6
// Implement the above formula as a function
                                                       [CONV1 WEIGHT] integer part : 2
int fx integer(float m, float n) {
                                                       [CONV2 WEIGHT] integer part : 2
 int OI;
                                                       [CONV3 WEIGHT] integer part : 2
                                                       [FULL1 WEIGHT] integer part : 2
 QI = ceil(log2(max(abs(m),abs(n)) + 1)) + 1;
                                                       [FULL2 WEIGHT] integer part : 3
 return QI;
                                                       [CONV1 BIAS] integer part: 2
                                                       [FULL2 BIAS] integer part: 2
```

Light LeNet-5 with C/C++ (Fixed-Point), Cont'd

- Refer to Xilinx User Guide 902 (High-Level Synthesis)
- Refer to Deep Learning with Limited Numerical Precision



$$Round(x, < I, F >) = \begin{cases} [x] & if [x] \le x \le [x] + \frac{\epsilon}{2} \\ [x] + \epsilon & if [x] + \frac{\epsilon}{2} < x \le [x] + \epsilon \end{cases}$$

$$where \epsilon = 2^{-F}$$

$$Convert(x, < I, F >) = \begin{cases} -2^{I-1} & if x \le -2^{I-1} \\ 2^{I-1} - 2^{-F} & if x \ge 2^{I-1} - 2^{-F} \\ Round(x, < I, F >) & otherwise \end{cases}$$

| Identifer | Description | | |
|-----------|----------------------|--|--|
| W | Word length in bits | | |
| I | The number of bits (| used to represent the integer value. | |
| | Quantization mode | | |
| | Mode | Description | |
| Q | AP_TRN | Truncation to minus infinity (default) | |
| | | | |
| | AP_RND | Rounding to plus inifinity | |
| | Overflow mode | | |
| | Mode | Description | |
| 0 | AP_SAT | Saturation | |
| | | | |
| | AP_WRAP | Wrap around (default) | |

Light LeNet-5 with C/C++ (Fixed-Point), Cont'd

```
/* layer.cc */
void full1 layer(conv3 t input[...], full1 t output[...]) {
    for (int row = 0; row < ...; ...) {
        // Temporary enough width accumulate register (32-bit)
        full1 temp acc = full1 bias[row];
        for (int col = 0; col < ...; ...) {
            acc += input[col] * full1 weight[row][col];
        if (acc > 0) output[row] = (full1 t) acc;
        else
                     output[row] = (full1 t) 0.0;
void pool1 layer(conv1 t input[...][...][...], conv1 t output[...][...]) {
    for (int num = 0; num < ...; ...) {
        for (int row = 0; row < ...; ...) {
            for (int col = 0; col < ...; ...) {
               conv1 t n1 = input[num][row][col];
               conv1 t n4 = input[num][row+1][col+1];
               conv1 t max1 = std::max(n1, n2);
               conv1 t max2 = std::max(n3, n4);
               conv1 t max = std::max(max1, max2);
               output[num][row >> 1][col >> 1] = max;
```

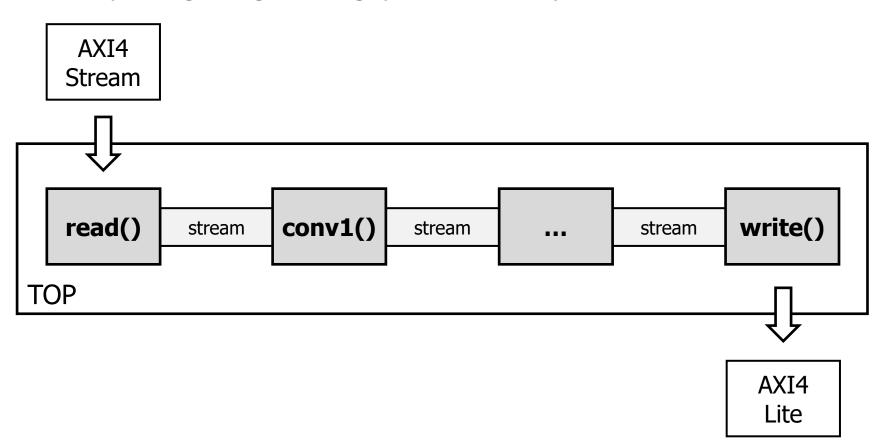
```
/* predict.cc */
uint8 t predict(float* input) {
    /* Intermediate outputs */
    conv1 t conv1 output[...][...] = { 0.0 };
    conv1 t pool1 output[...][...] = { 0.0 };
   full2 t full2 output[...] = { 0.0 };
   /* 1st convolution layer */
    conv1 layer(input, conv1 output);
    /* 1st pooling layer */
    pool1 layer(conv1 output, pool1 output);
   /* 2nd convolution layer */
    conv2 layer(pool1 output, conv2 output);
    /* 2nd pooling layer */
    pool2 layer(conv2 output, pool2 output);
   /* 3rd convolution layer */
    conv3 layer(pool2 output, conv3 output);
    /* 1st fully connected layer */
   full1 layer(conv3 output, full1 output);
   /* 2nd fully connected layer */
   full2 layer(full1 output, full2 output);
    /* Return result */
    return result(full2 output);
```

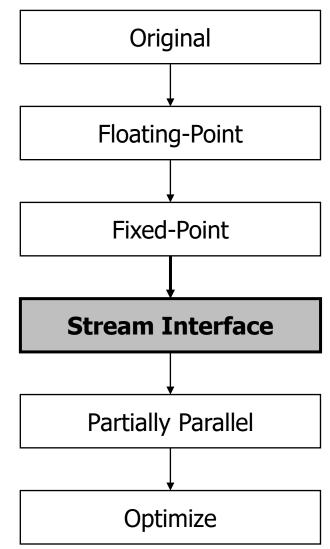
Light LeNet-5 with C/C++ (Fixed-Point)

• Include Xilinx HLS library to use <ap fixed.h>

```
/* type.h */
                                                             /* Makefile */
#include <ap fixed.h> // For fixed-point data type
                                                             CC = q++
                                                             CXXLFAGS = -Wall -Wno-comment -q -02
typedef ap ufixed<16, 1, AP RND, AP SAT> input t;
                                                             LIBS += -I $(XILINX HLS)/include
                                                             $(TARGET): $(OBJECTS)
typedef ap fixed<16, 2, AP RND, AP SAT> weight t;
                                                               $(CC) $(CXXLFAGS) $(OBJECTS) -0 $(TARGET) $(LIBS)
typedef ap fixed<16, 4, AP RND, AP SAT> conv1 t;
typedef ap fixed<16, 5, AP RND, AP SAT> conv2 t;
                                                             # Run all inputs (just one option)
typedef ap fixed<16, 7, AP RND, AP SAT> conv3 t;
                                                             $ ./main
typedef ap fixed<16, 7, AP RND, AP_SAT> full1 t;
typedef ap fixed<16, 7, AP RND, AP SAT> full2 t;
                                                                    Number Answer Predict
                                                             [TRUE] [
                                                             [TRUE] [
  Temporary fixed-point data type with enough width
                                                              [TRUE] [
 to prevent saturation/overflow and avoid any loss of
                                                             [TRUE] [ 3] 0
 precision while accumulating the sum over all products.
  [2*I, 2*F]
                                                             [TRUE] [9996] 3
*/
                                                             [TRUE]
                                                                    [9997] 4
                                                             [TRUE] [9998]
typedef ap fixed<32, 8, AP RND, AP SAT> conv1 temp;
                                                             [TRUE] [9999] 6
typedef ap fixed<32, 10, AP RND, AP SAT> conv2 temp;
typedef ap fixed<32, 14, AP RND, AP SAT> conv3 temp;
                                                             [Fixed-Point]
typedef ap fixed<32, 14, AP RND, AP SAT> full1 temp;
                                                             Accuracy: 97.47 [%]
typedef ap fixed<32, 14, AP RND, AP SAT> full2 temp;
                                                                           253 [cases]
                                                             Error
```

- Implemented as stream interface instead of array interface as before.
- Closer to Vivado HLS canonical form using DATAFLOW optimization.
- For improving design throughput and latency.





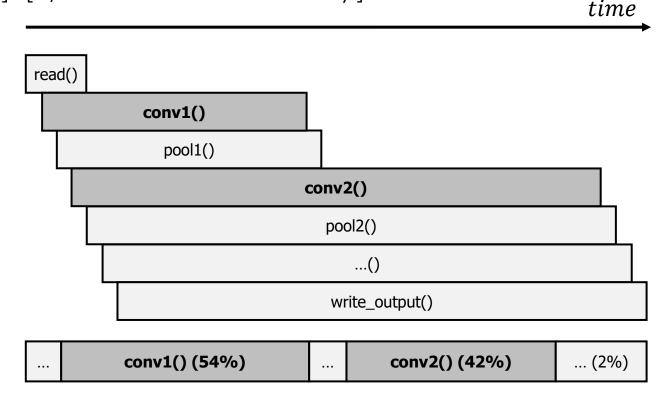
- Vivado HLS C/RTL Cosimulation waveform
- Vivado HLS Performance Estimates.
- It can be seen that conv1() and conv2() are the cause of bottleneck.

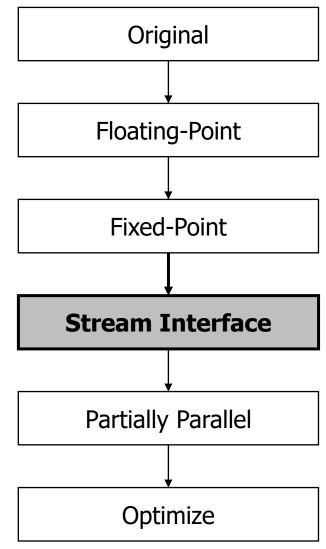
[Performance Estimates] [C/RTL Cosimulation waveform activity]

Latency read() 1025 conv1() 264691 6734 pool1() conv2() 203618 pool2() 1856 conv3() 8324 full1() 524 full2() 442 31 write()

Total

265683





Implemented as stream interface instead of array interface as before.

```
/* type.h */
#include <ap fixed.h> // For fixed-point data type
#include <hls stream.h> // For stream data type
#include <ap axi sdata.h> // For AXI stream data type
// Data type for AXI streaming with side-channel
typedef ap axiu<16, 0, 0, 0> axis t;
typedef ap fixed<16, 1, AP RND, AP SAT> input t;
typedef ap fixed<16, 7, AP RND, AP SAT> full2 t;
typedef ap fixed<32, 8, AP RND, AP SAT> conv1 temp;
typedef ap fixed<32,14, AP RND, AP SAT> full2 temp;
// Stream data type for AXI streaming with side-channel
typedef hls::stream<axis t> stream axis;
typedef hls::stream<input t> stream input;
typedef hls::stream<conv1 t> stream conv1;
typedef hls::stream<full2 t> stream full2;
```

```
/* layer.cc */
void read input(stream axis &input, stream input &output) {
    axis t temp axis;
    input t temp input;
    for (int i = 0; i < IMAGE SIZE; i++) {
        temp axis = input.read();
        // range() selects all bits in normal order
        temp input.range() = temp axis.data.range();
        output.write(temp input);
void write output(stream full2 &input, uint8 t* output) {
    full2 t input 1d[...] = { 0, };
    /* Read input */
    for (int i = 0; i < FULL2 OUTPUT SIZE; i++)</pre>
        input 1d[i] = input.read();
    ... // Find Max and index
    *output = (uint8 t)max index;
```

Implemented as stream interface instead of array interface as before.

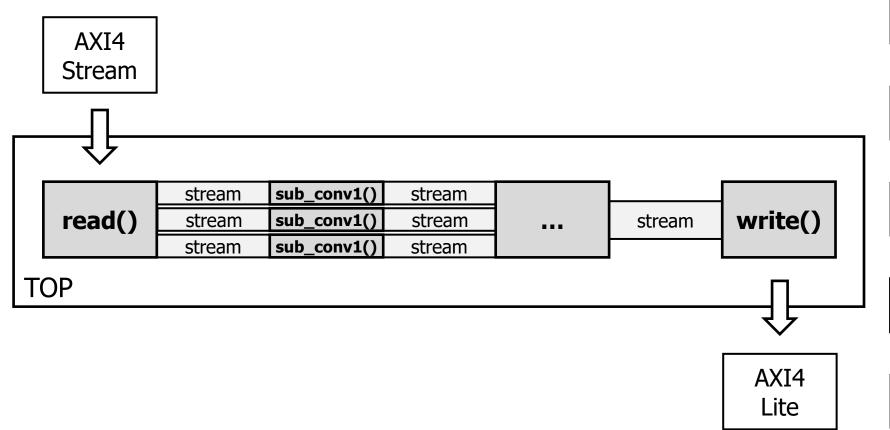
```
/* layer.cc */
void full1 layer(stream conv3 &input, stream full1 &output) {
    conv3 t input 1d[CONV3 OUTPUT NUM] = { 0, };
    /* Read input */
    for (int i = 0; i < CONV3 OUTPUT NUM; <math>i++) {
        input 1d[i] = input.read();
    /* Compute & Write */
    for (int row = 0; row < ...; ...) {
        full1 temp acc = full1 bias[row];
        // Compute
        for (int col = 0; col < ...; ...) {
            acc += (full1 temp) (input 1d[col] * full1 weight[...][...]);
        // ReLU Activation & Write
        if (acc > 0) output.write((full1 t)acc);
        else output.write((full1 t)0.0);
```

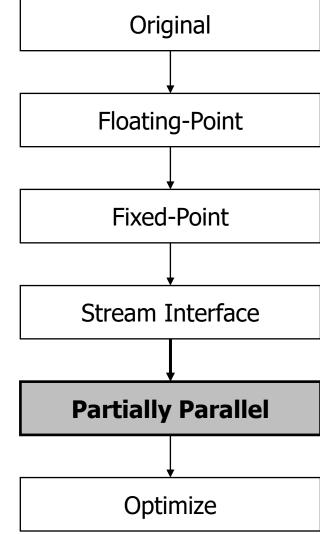
```
/* predict.cc */
void predict(stream axis &input, uint8 t* output) {
    #pragma HLS INTERFACE axis port = input
    #pragma HLS INTERFACE s axilite port = output ...
    #pragma HLS INTERFACE s axilite port = return ...
    #pragma HLS DATAFLOW
    static stream input input stream;
    static stream conv1 conv1 stream;
    static stream full2 full2 stream;
    /* Read input */
    read input(input, input stream);
    /* 1st CONV layer */
    conv1 layer(input stream, conv1 stream);
    /* Write result */
    write output(full2 stream, output);
```

Implemented as stream interface instead of array interface as before.

```
/* main.cc or testbench.cc */
                                                           # Run all inputs (just one option)
int main (int argc, char* argv[]) {
                                                           $ ./main
    int err cnt = 0;
                                                                  Number Answer Predict
                                                           [TRUE] [
    for (size t i = 0; i < TEST NUM; i++) {
                                                           [TRUE] [
                                                           [TRUE] [
        predict(input axi stream, &my answer[i]);
                                                           [TRUE] [
        if (my answer != answer[i]) {
                                                           [TRUE] [9996]
            err cnt++;
                                                           [TRUE] [9997]
            cout << "[ FALSE ] " ... << "\n";
                                                           [TRUE] [9998]
                                                           [TRUE] [9999]
        else ·
            cout << "[ TRUE ] " ... << "\n";
                                                           [Fixed-Point + HLS stream]
                                                           Accuracy : 97.47 [%]
                                                                         253 [cases]
                                                           Error :
    cout << "\n[Fixed-Point + HLS stream]\n";</pre>
    cout << "Accuracy : " << ... << accuracy << ... ;</pre>
    cout << "Error : " << ... << err cnt << ... ;
    return 0;
```

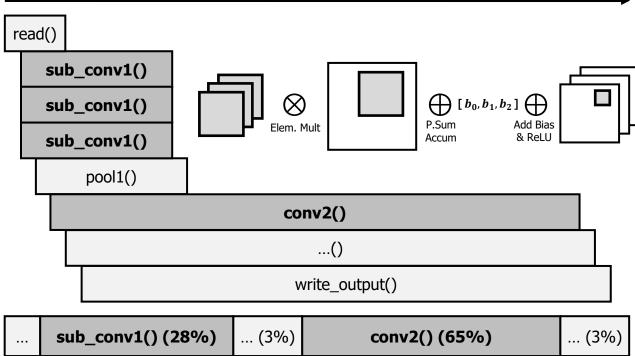
- Longest latency conv1() is divided to be calculated in parallel.
- Since the total latency is bounded by highest latency conv1(),
- Reducing the latency by parallelizing conv1() will reduce total latency.

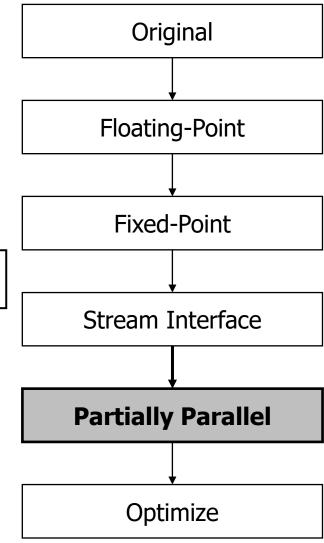




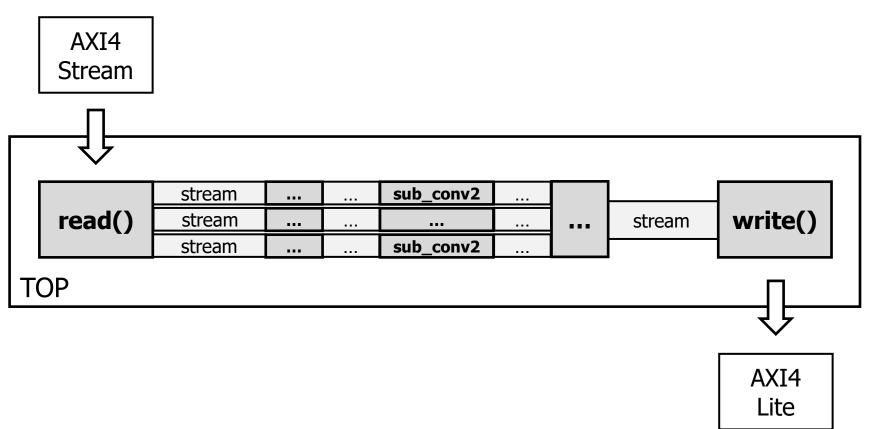
- When conv1() was partially parallelized,
- The latency of conv1() decreased by 66%.
- But, the total latency is bounded to new highest latency conv2().

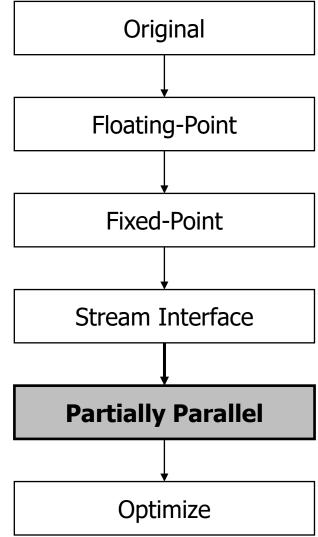
| | Latency |
|-------------|---------|
| read() | 1025 |
| sub_conv1() | 88954 |
| pool1() | 10536 |
| conv2() | 203618 |
| pool2() | 1856 |
| conv3() | 8324 |
| full1() | 524 |
| full2() | 442 |
| write() | 31 |
| Total | 207716 |





- New highest latency conv2() also divided to be calculated in parallel.
- Since the total latency is bounded by highest latency conv2(),
- Reducing the latency by parallelizing conv2() will reduce total latency.

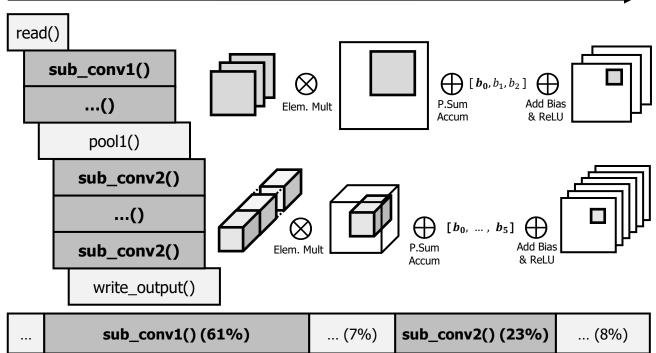


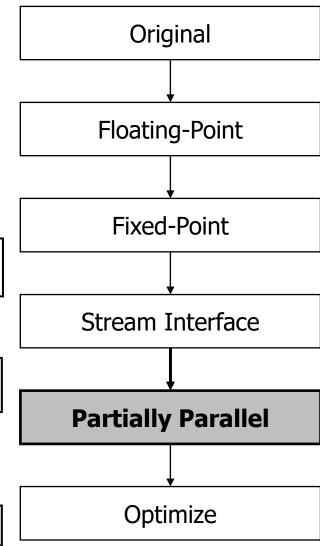


- When conv2() was partially parallelized,
- The latency of conv2() decreased by 83%.
- Total latency decreased by **66%** compared to the [Stream Interface].

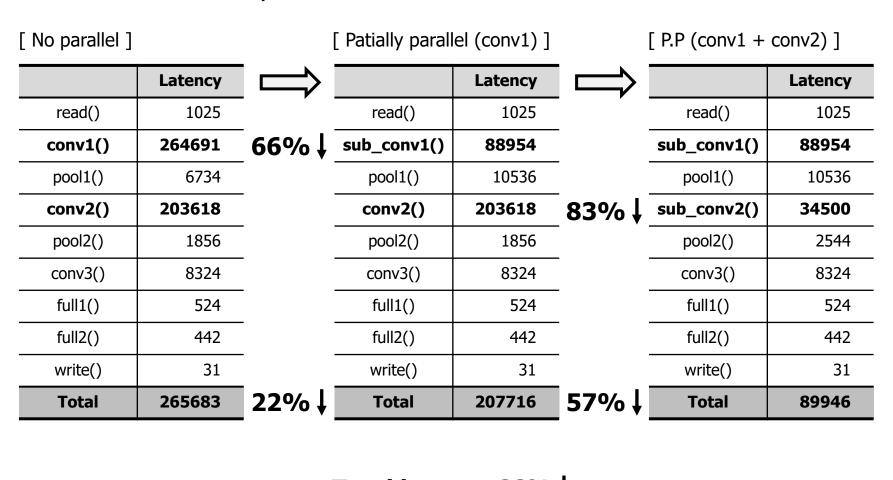
[Performance Estimates] [Partially parallel (conv1 + conv2) C/RTL Cosimulation waveform] time

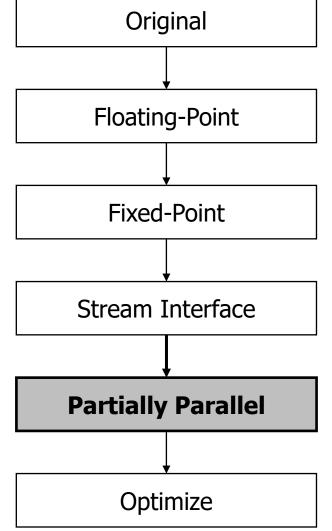
| | Latency |
|-------------|---------|
| read() | 1025 |
| sub_conv1() | 88954 |
| pool1() | 10536 |
| sub_conv2() | 34500 |
| pool2() | 2544 |
| conv3() | 8324 |
| full1() | 524 |
| full2() | 442 |
| write() | 31 |
| Total | 89946 |





Overview of latency reduction.





Overview of resource utilization.

[No parallel]

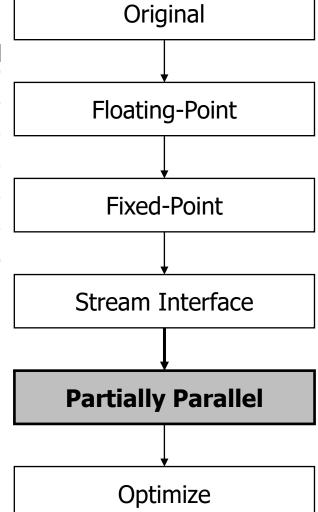
| | Usage | Usage (%) |
|-------|-------|-----------|
| LUT | 2125 | 12.07 |
| FF | 1504 | 4.27 |
| DSP | 5 | 6.25 |
| BRAM | 14 | 11.67 |
| SLICE | 808 | 18.36 |

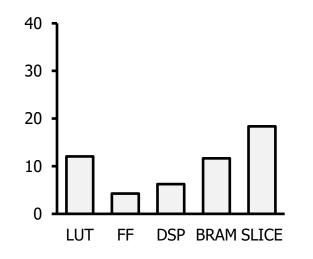
[Patially parallel (conv1)]

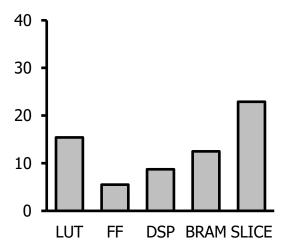
| | Usage | Usage (%) |
|-------|-------|-----------|
| LUT | 2713 | 15.41 |
| FF | 1946 | 5.53 |
| DSP | 7 | 8.75 |
| BRAM | 15 | 12.50 |
| SLICE | 1008 | 22.91 |

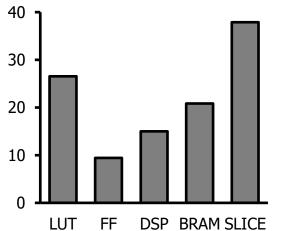
[Patially parallel (conv1 + conv2)]

| | Usage | Usage (%) |
|-------|-------|-----------|
| LUT | 4671 | 26.54 |
| FF | 3324 | 9.44 |
| DSP | 12 | 15.00 |
| BRAM | 25 | 20.83 |
| SLICE | 1667 | 37.89 |









Divide existing functions to be excuted in parallel.

```
/* predict.cc */
void predict(stream axis &input, uint8 t* output r) {
    stream input sub0 input; stream conv1 sub0 conv1;
    stream input sub1 input; stream conv1 sub1 conv1;
    stream input sub2 input; stream conv1 sub2 conv1;
    stream conv1 sub0 pool1;
    stream conv1 sub5 pool1;
    stream conv2 sub0 conv2;
    stream conv2 sub5 conv2;
    read input(input, sub0 input,
                      sub1 input,
                      sub2 input);
    /* 1st CONV layer */
    sub0 conv1 layer(sub0 input, sub0 conv1);
    sub1 conv1 layer(sub1 input, sub1 conv1);
    sub2 conv1 layer(sub2 input, sub2 conv1);
    /* 1st POOL layer */
    pool1 layer(sub0 conv1, sub1 conv1, sub2 conv1,
                sub0 pool1, sub1 pool1, sub2 pool1,
                sub3 pool1, sub4 pool1, sub5 pool1);
```

```
/* predict.cc */
    /* 2nd CONV layer */
    sub0 conv2 layer(sub0 pool1, sub0 conv2);
    sub5 conv2 layer(sub5 pool1, sub5 conv2);
    /* 2nd POOL layer */
    pool2 layer(sub0 conv2,
                sub1 conv2,
                sub2 conv2,
                sub3 conv2,
                sub4 conv2,
                sub5 conv2, pool2 stream);
   /* 3rd CONV layer */
    conv3 layer(pool2 stream, conv3 stream);
   /* 1st FULL laver */
   full1 layer(conv3 stream, full1 stream);
   /* 2nd FULL layer */
   full2 layer(full1 stream, full2 stream);
    /* Return result */
    write output(full2 stream, output r);
```

Divide existing functions to be excuted in parallel.

```
/* layer.cc */
void read input (stream axis &input,
                stream input &sub0,
                stream input &sub1,
                stream input &sub2)
    axis t temp axis;
    input t temp input;
    for (int i = 0; i < IMAGE SIZE; i++) {</pre>
        temp axis = input.read();
        temp input.range() = temp axis.data.range();
        sub0.write(temp input);
        sub1.write(temp input);
        sub2.write(temp input);
```

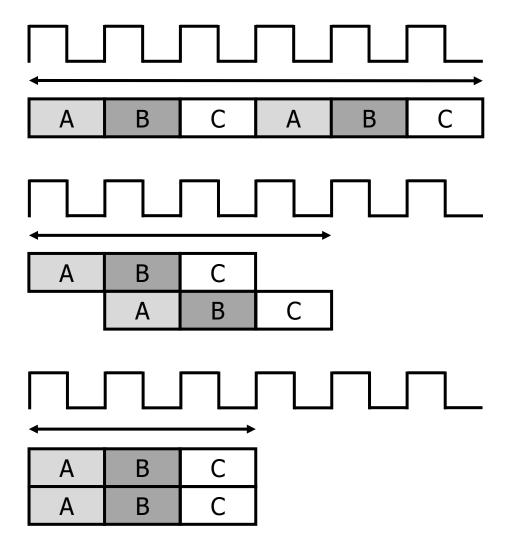
```
/* layer.cc */
void sub0 conv1 layer(stream input &input, stream conv1 &output)
  input t input 2d[IMAGE ROW][IMAGE COL] = { 0, };
  /* Read input */
  /* Compute & Write */
  for (int orow = 0; orow < ...; ...) {
    for (int ocol = 0; ocol < ...; ...) {
      conv1 temp acc = conv1 bias[0];
      for (int wr = 0; wr < ...; ...) {
        for (int wc = 0; wc < ...; ...) {
          // Compute
          acc += (conv1 temp) (input 2d[...] [...] * weight_0[...][...]);
      // ReLU Activation & Write
      if (acc > 0) output.write((conv1 t)acc);
      else
                   output.write((conv1 t)0.0);
```

• Divide existing functions to be excuted in parallel.

```
/* laver.cc */
                                                                                      # Run all inputs (just one option)
void pool1 layer(stream conv1 &input0, stream conv1 &input1, stream conv1 &input2,
                                                                                      $ ./main
                stream conv1 &output0, stream conv1 &output1, stream conv1 &output2,
                stream conv1 &output3, stream conv1 &output4, stream conv1 &output5)
                                                                                             Number Answer Predict
                                                                                      [TRUE] [
    conv1 t input 3d[CONV1 OUTPUT NUM][CONV1 OUTPUT ROW][CONV1 OUTPUT COL] = { 0, };
                                                                                      [TRUE] [
                                                                                      [TRUE] [ 2] 1
    /* Read input */
    for (int i = 0; i < ...; ...) {
                                                                                      [TRUE] [ 3] 0
       for (int j = 0; j < ...; ...) {
           for (int k = 0; k < ...; ...) {
                                                                                      [TRUE] [9996]
                       (k == 0) input 3d[k][i][j] = input0.read();
                                                                                      [TRUE] [9997]
               else if (k == 1) input 3d[k][i][j] = input1.read();
                                                                                      [TRUE] [9998]
                                input 3d[k][i][j] = input2.read();
                                                                                      [TRUE] [9999] 6
                                                                                      [Fixed-Point + HLS stream + Parallel]
                                                                                     Accuracy : 97.47 [%]
                                                                                                    253 [cases]
                                                                                      Error
                                                                                            :
    /* Compute & Write */
    for (int num = 0; num < ...; ...) {
       for (int row = 0; row < ...; ...) {
            for (int col = 0; col < ...; ...) {
               ... // Find Max
               output0.write(max);
               output5.write(max);
                                                                                                                           53
```

Light LeNet-5 with HLS (Optimize), Cont'd

Compare no pragma, HLS PIPELINE, HLS UNROLL



No pragma

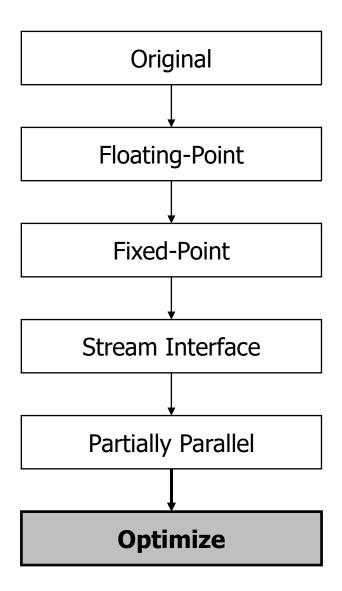
- High latency
- Low resource
- Low throughput

HLS PIPELINE

- Medium latency
- Medium resource
- Medium throughput

HLS UNROLL

- Low latency
- High resource
- High throughput



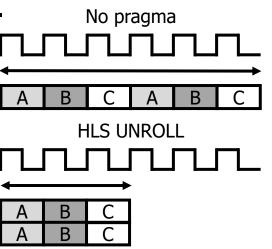
Light LeNet-5 with HLS (Optimize), Cont'd

- When UNROLL pragma is applied to conv1() and conv2(),
- The latency of conv1() is decreased by 62%.
- The latency of conv2() is decreased by 57%.
- The total latency is decreased by 62%.

[Before apply pragma]

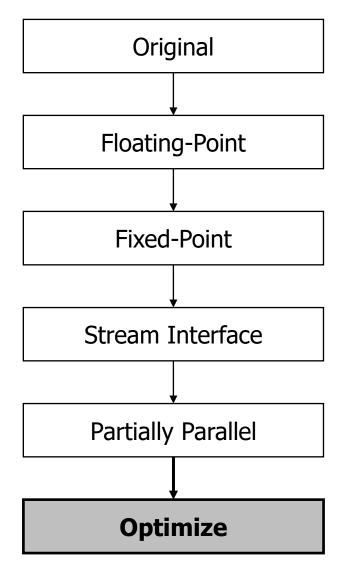
[After apply pragma]

| | Latency | | | Latency |
|-------------|---------|------|-------------|---------|
| read() | 1025 | | read() | 1025 |
| sub_conv1() | 88954 | 62%↓ | sub_conv1() | 34011 |
| pool1() | 10536 | _ | pool1() | 10536 |
| sub_conv2() | 34500 | 57%↓ | sub_conv2() | 14912 |
| pool2() | 2544 | | pool2() | 2544 |
| conv3() | 8324 | | conv3() | 8324 |
| full1() | 524 | | full1() | 524 |
| full2() | 442 | | full2() | 442 |
| write() | 31 | | write() | 31 |
| Total | 89946 | 62%↓ | Total | 34011 |



[Resource Usage]

| | Usage | Usage (%) |
|-------|-------|-----------|
| LUT | 8310 | 47.22 |
| FF | 4727 | 13.43 |
| DSP | 48 | 60.00 |
| BRAM | 19 | 15.83 |
| SLICE | 2935 | 66.70 |



Light LeNet-5 with HLS (Optimize)

Apply optimization each block.

```
/* layer.cc */
void sub0 conv1 layer(stream input &input, stream conv1 &output) {
   input t input 2d[IMAGE ROW][IMAGE COL] = { 0, };
   /* Read input */
   for (int i = 0; i < IMAGE ROW; i++) {
       for (int j = 0; j < IMAGE COL; j++)
            #pragma HLS PIPELINE II=1
                                           // Read input in pipeline manner to reduce this function latency.
           input 2d[i][j] = input.read();
   /* Compute & Write */
   for (int orow = 0; orow < CONV1 OUTPUT ROW; orow++) {</pre>
       for (int ocol = 0; ocol < CONV1 OUTPUT COL; ocol++) {
           // Compute
            conv1 temp acc = conv1 bias[0];
           for (int wr = 0; wr < WEIGHT ROW; wr++) {
                for (int wc = 0; wc < WEIGHT COL; wc++)
                    #pragma HLS UNROLL // The loop is unrolled by WEIGHT COL(5) and fully parallelized.
                    acc += (conv1 temp) (input 2d[orow + wr][ocol + wc] * conv1 weight sub0[wr][wc]);
           // ReLU Activation & Write
           if (acc > 0) output.write((conv1 t)acc);
                        output.write((conv1 t)0.0);
```

Overview of Impl. of LeNet-5 using C/C++ and HLS

Original → Floating-Point

- Change activation function (sigmoid, tanh to ReLU).
- Adjust the parameters of each layer to make the model smaller.

Floating-Point → Fixed-Point

- Confirmed that fixed-point has more benefits than floating-point.
- Determine fixed-point identifier, for using fixed-point data type.

Fixed-Point → Stream interface

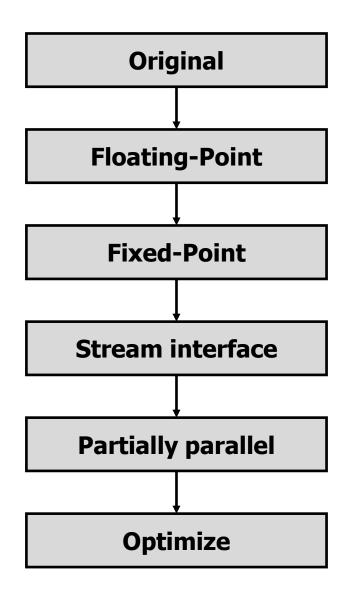
- Implemented as stream interface instead of array interface as before.
- Closer to Vivado HLS canonical form using DATAFLOW optimization.

Stream interface → Partially parallel

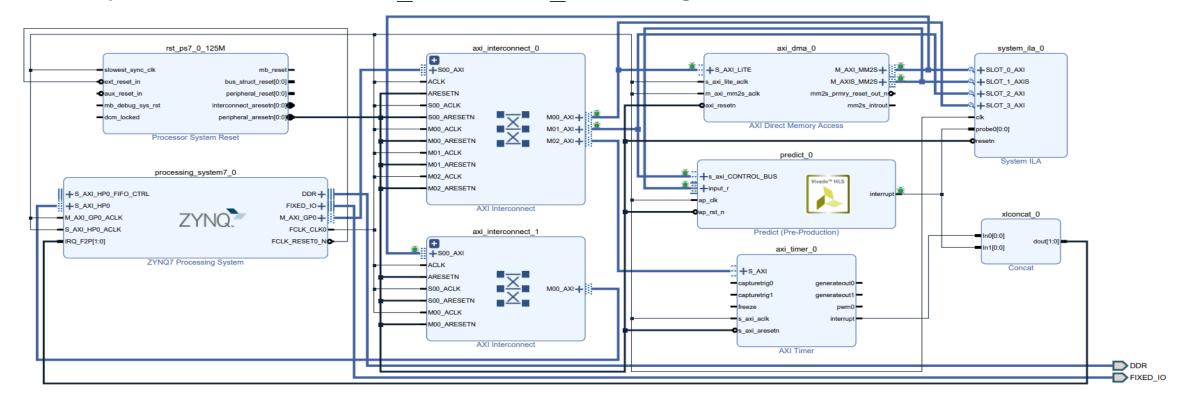
- Reducing the latency by parallelizing conv1() and conv2().
- Increase the throughput by parallelizing conv1() and conv2().

• Partially parallel \rightarrow Optimize

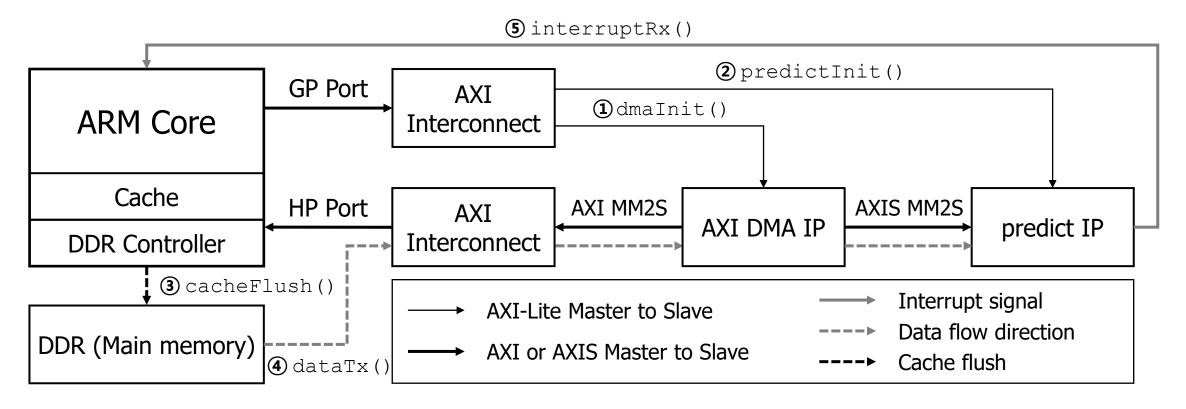
- Confirmed that UNROLL is more benefits than PIPELINE.
- Apply optimization and confirmed reduced total latency.



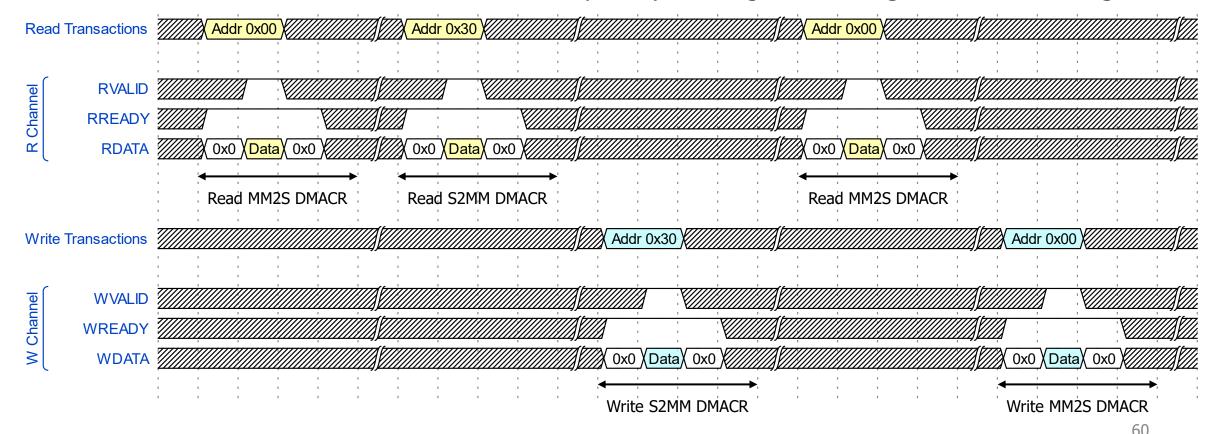
- The AXI DMA provides high-speed data movement between system memory and an AXI4-Streambased taget IP.
- The Integrated Logic Analyzer (ILA) IP core is logic analyzer core that can be used to monitor the internal signals of a design.
- The AXI Timer provides an AXI4-Lite interface to communicate with the Processing System.
- Interrupt is driven when the ap done or ap_ready signals are HIGH.



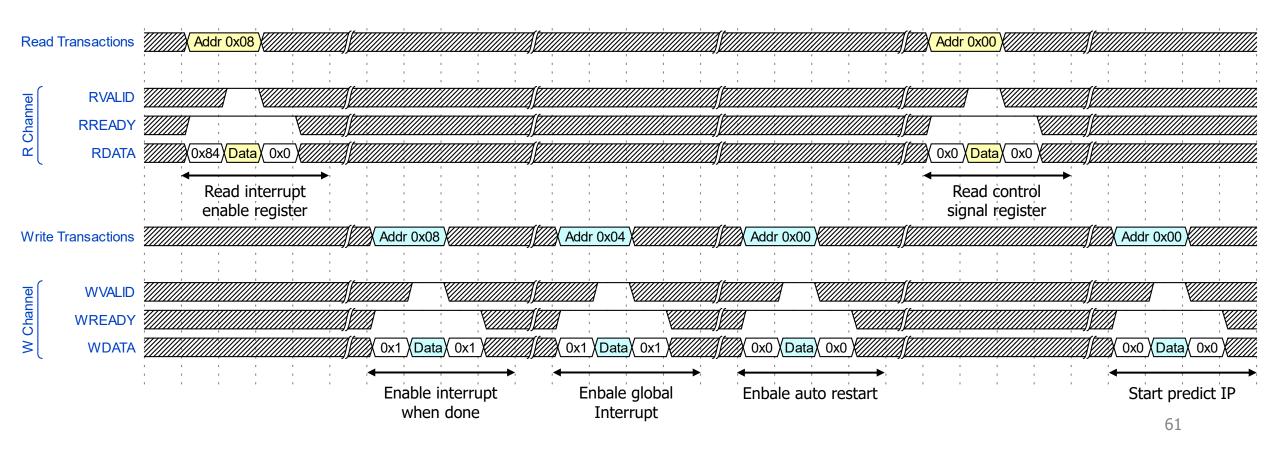
- Initialize AXI DMA IP and predict IP through dmaInit() and predictInit().
- Flush the cache before transferring data via DMA through cacheFlush().
- AXI DMA IP reads data through DDR and transfers it to predict IP through dataTx().
- Wait for the predict IP to process, and read the result when interrupt signal is raised.



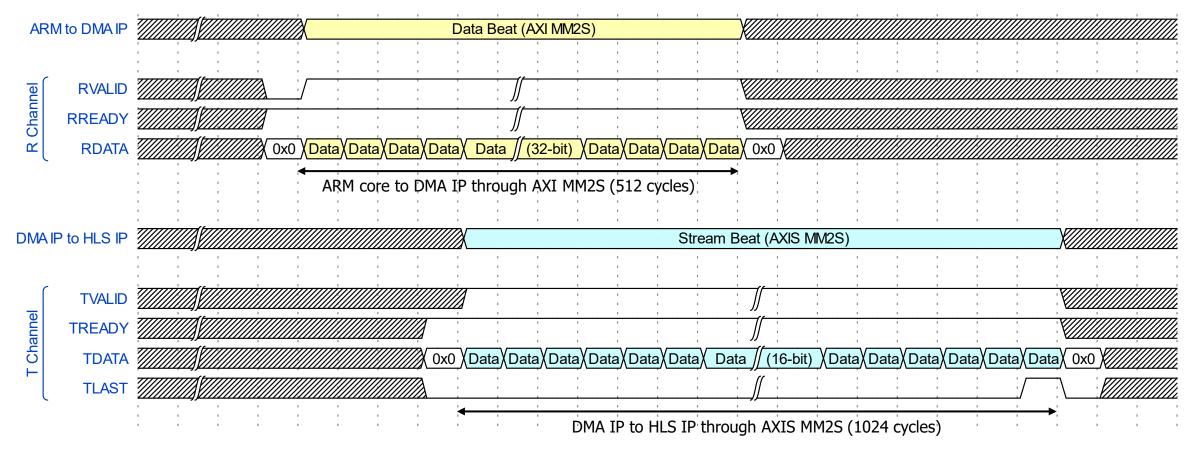
- Waveform in dmaInit() part obtained through Integrated Logic Analyzer (ILA).
- Read and write DMA IP config.
- ARM Core ascertain that read channel is open by reading and writing MM2S control register.
- ARM Core ascertain that write channel is not open by reading and writing S2MM control register.



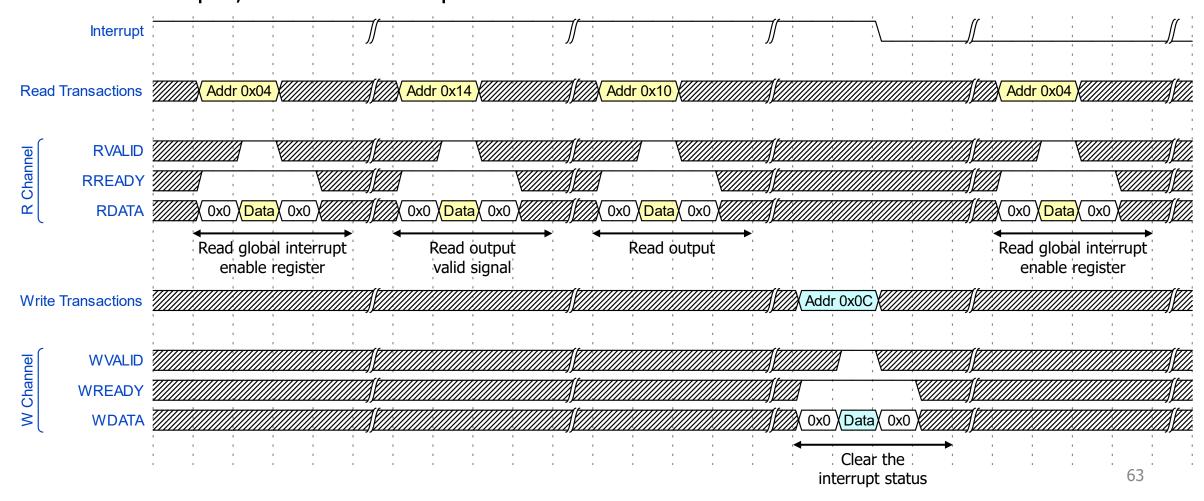
- Waveform in predictInit() part obtained through Integrated Logic Analyzer (ILA).
- Read and write predict IP config.
- Set the interrupt signal to be HIGH when the application done.
- Enable predict IP automatically restart and start.



- Waveform in dataTx() part obtained through Integrated Logic Analyzer (ILA).
- Data transfer from ARM Core to HLS IP through DMA IP.
- ARM to DMA IP reads data in 32-bit units, while DMA IP to HLS IP reads data in 16-bit units.



- Waveform in interruptRx() part obtained through Integrated Logic Analyzer (ILA).
- Read predict IP output valid signal and output data when interrupt signal asserted.
- After read output, clear the interrupt status.

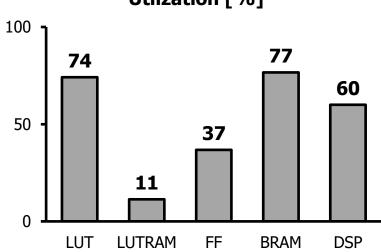


Summary of HW utilization, timing, on-chip power and implemented design.

[Utilization Summary]

| Resource | Utilization | Available | |
|----------|-------------|-----------|--|
| LUT | 13057 | 17600 | |
| LUTRAM | 683 | 6000 | |
| FF | 12961 | 35200 | |
| BRAM | 46 | 60 | |
| DSP | 48 | 80 | |

Utilzation [%]



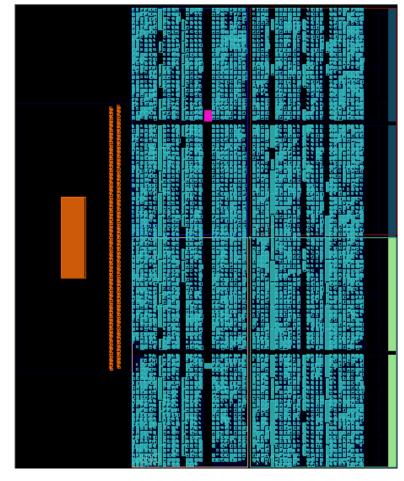
[Timing Summary]

| | Setup | Hold |
|-----|----------|----------|
| WNS | 0.043 ns | 0.018 ns |
| TNS | 0.000 ns | 0.000 ns |

[On-chip Power Summary]

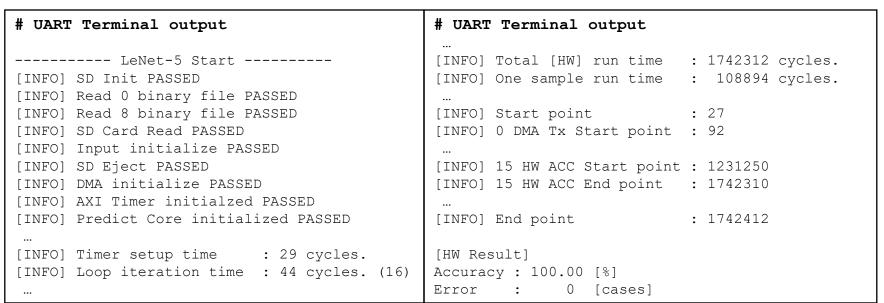
| | | Dynamic | |
|--------------------------|-----------|---------------|--|
| | Clocks | 0.050 W (3%) | |
| | Signals | 0.128 W (7%) | |
| 93% 1.82 <i>W</i> | Logic | 0.084 W (5%) | |
| | BRAM | 0.102 W (6%) | |
| | DSP | 0.069 W (4%) | |
| | PS7 | 1.395 W (75%) | |
| 7% | | Static | |
| 0.13 <i>W</i> | PL Static | 0.128 W(100%) | |
| | | | |

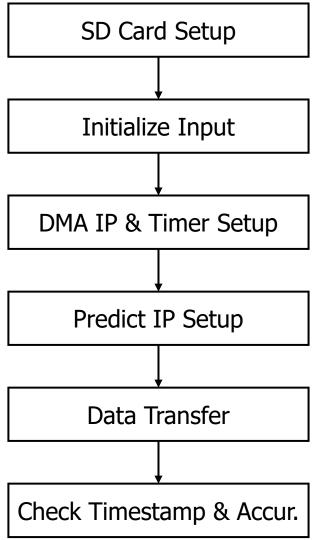
[Implemented Design]



SW Driver of LeNet-5 (Processing System)

- Read the input binary file stored in SD card and initialize.
- Input is initialized through the data read from the SD card.
- Configure to use DMA IP, AXI Timer IP, and predict IP.
- Before transferring data, cache flush the data to be transferred.
- Data is transferred using XAxiDma SimpleTransfer() Xilinx API.
- Measure DMA transfer latency, predict IP operataion latency, etc...
- Check the accuracy to make sure predict IP implemented correctly.





Result of running the Original model and the Lite model with different compile options on ARM core.

[Original LeNet-5 on ARM core]

| _ | | | | _ |
|--------------|------------------------|----------------|----------------|----------------|
| No. of input | -00 | -01 | -02 | -03 |
| 1 | 33.10 ms | 6.13 ms | 6.12 ms | 6.61 ms |
| 4 | 132.36 ms | 24.69 ms | 24.25 ms | 26.00 ms |
| 16 | 529.41 ms | 96.84 ms | 96.86 ms | 103.59 ms |
| 64 | 2116.83 ms | 393.79 ms | 386.63 ms | 414.97 ms |
| 256 | 8465.10 ms | 1576.09 ms | 1544.76 ms | 1659.93 ms |
| Average | 33.08 <i>ms</i> | 6.15 ms | 6.05 ms | 6.50 ms |

[Light LeNet-5 on ARM core]

| No. of input | -00 | -01 | -02 | -03 | |
|--------------|------------------------|------------------------------|----------|----------------|--|
| 1 | 13.15 ms | 3.15 ms 2.31 ms 1.43 ms | | 1.30 ms | |
| 4 | 52.56 <i>ms</i> | 9.20 ms | 5.71 ms | 5.18 ms | |
| 16 | 210.33 ms | 36.76 ms | 22.85 ms | 20.68 ms | |
| 64 | 839.48 ms | 147.09 ms | 91.39 ms | 82.66 ms | |
| 256 | 3355.89 ms | 587.93 ms 364.92 ms 330.59 a | | 330.59 ms | |
| Average | 13.13 ms | ns 2.30 ms 1.43 ms 1.3 | | 1.30 ms | |

➡ 81%↓ ➡ 1%↓ ➡ 7%↑

⇒ 82%↓ **⇒** 38%↓ **⇒** 9%↓

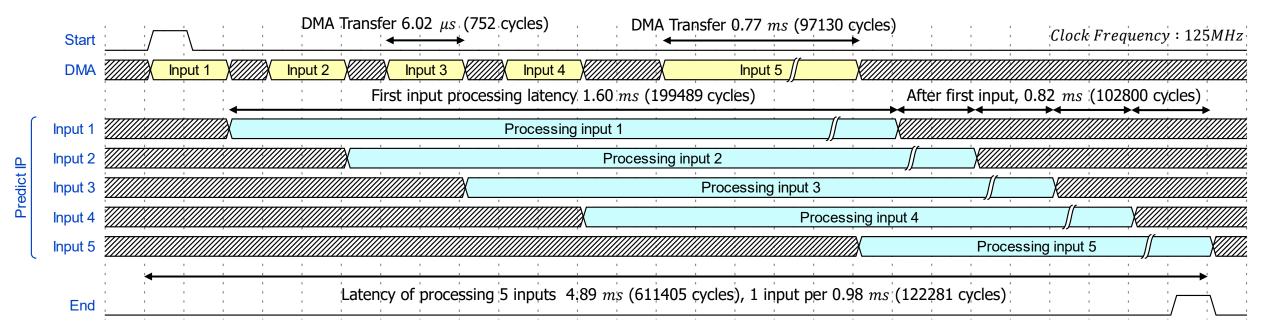
```
# UART Terminal output
----- LeNet-5 Start -----
...

[ORG Result]
Accuracy : 94.55 [%]
Error : 545 [cases]
----- LeNet-5 End -----
```

```
# UART Terminal output
----- LeNet-5 Start -----
...

[Lite Result]
Accuracy: 97.47 [%]
Error: 253 [cases]
----- LeNet-5 End ------
```

- Start and end points are checked through AXI Timer IP.
- For the first input, the latency is high, but it decreases from the second input onwards.
- Predict IP is taking high latency to receive the 5th input as it has not yet consumed the data.
- Because ap ctrl chin block level protocol is applied to predict IP, the 5th input is back pressured.
- As the number of inputs increases, the latency per one input will decrease.



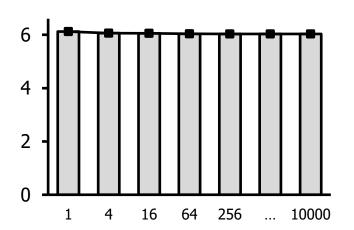
- Although the ARM core operates at 667MHz and predict IP operates at 125MHz,
- Predict IP on programmable logic has the best performance. (36% faster than Lite on ARM core)

| No. of input | -02 (Org) | Average | | |
|--------------|-------------|---------|--|--|
| 1 | 6.12 ms | 6.12 ms | | |
| 4 | 24.25 ms | 6.06 ms | | |
| 16 | 96.86 ms | 6.05 ms | | |
| 64 | 386.63 ms | 6.04 ms | | |
| 256 | 1544.76 ms | 6.03 ms | | |
| | 24699.98 ms | 6.03 ms | | |
| 10000 | 60323.51 ms | 6.03 ms | | |

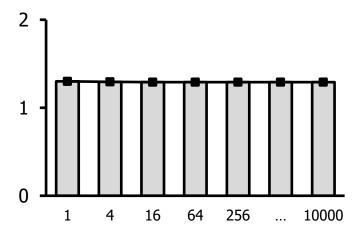
| No. of input | -03 (Lite) | Average | | |
|--------------|-------------|---------|--|--|
| 1 | 1.30 ms | 1.30 ms | | |
| 4 | 5.18 ms | 1.30 ms | | |
| 16 | 20.68 ms | 1.29 ms | | |
| 64 | 82.66 ms | 1.29 ms | | |
| 256 | 330.59 ms | 1.29 ms | | |
| | 5290.26 ms | 1.29 ms | | |
| 10000 | 12915.67 ms | 1.29 ms | | |

| No. of input | -00 (predict) | Average | | |
|--------------|---------------|---------|--|--|
| 1 | 1.60 ms | 1.60 ms | | |
| 4 | 4.06 ms | 1.01 ms | | |
| 16 | 13.93 ms | 0.87 ms | | |
| 64 | 53.41 ms | 0.83 ms | | |
| 256 | 211.31 ms | 0.83 ms | | |
| | 3369.31 ms | 0.82 ms | | |
| 10000 | 8224.70 ms | 0.82 ms | | |
| | | • | | |

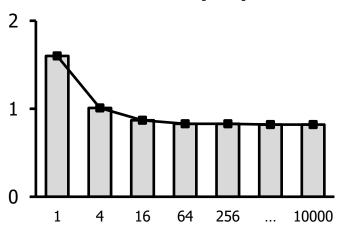
Original Average (-02)



Lite Average (-03)



Predict IP (-00)

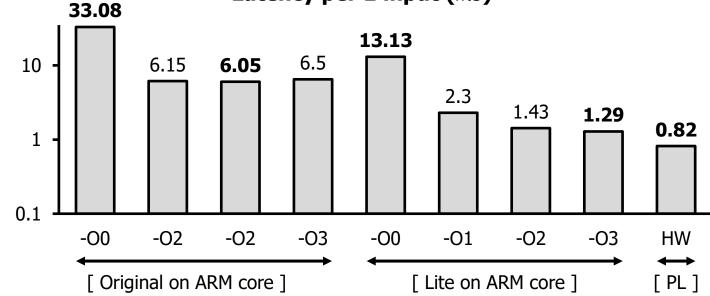


- Predict IP on PL is 40.34x faster than Original with -O0 compile option on PS.
- Predict IP on PL is 7.38x faster than Original with -O2 compile option on PS.
- Predict IP on PL is 16.01x faster than Lite with -O0 compile option on PS.
- Predict IP on PL is 1.57x faster than Lite with -O3 compile option on PS.

| Model | vs. HW |
|----------------|--------|
| Original (-O0) | 98 % ↓ |
| Original (-O1) | 87 % ↓ |
| Original (-O2) | 86 % ↓ |
| Original (-O3) | 87 % ↓ |
| Lite (-00) | 94 % ↓ |
| Lite (-01) | 64 % ↓ |
| Lite (-O2) | 42 % ↓ |
| Lite (-03) | 36 % ↓ |

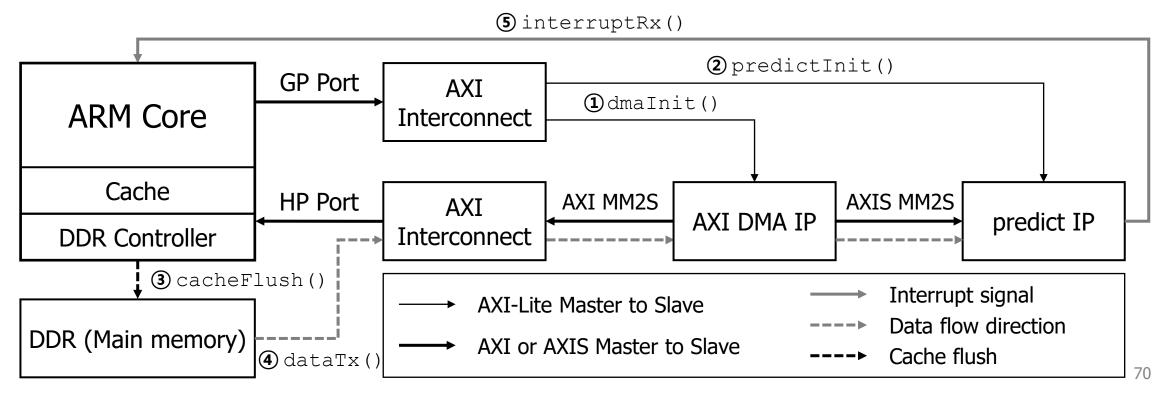
| | -00 | -01 | -02 | -03 | -00 | -01 | -02 | -03 | HW |
|---------|-----------------|---------|----------------|---------|-----------------|---------|---------|----------------|----------------|
| Average | 33.08 ms | 6.15 ms | 6.05 ms | 6.50 ms | 13.13 ms | 2.30 ms | 1.43 ms | 1.29 ms | 0.82 ms |

Latency per 1 input (ms)



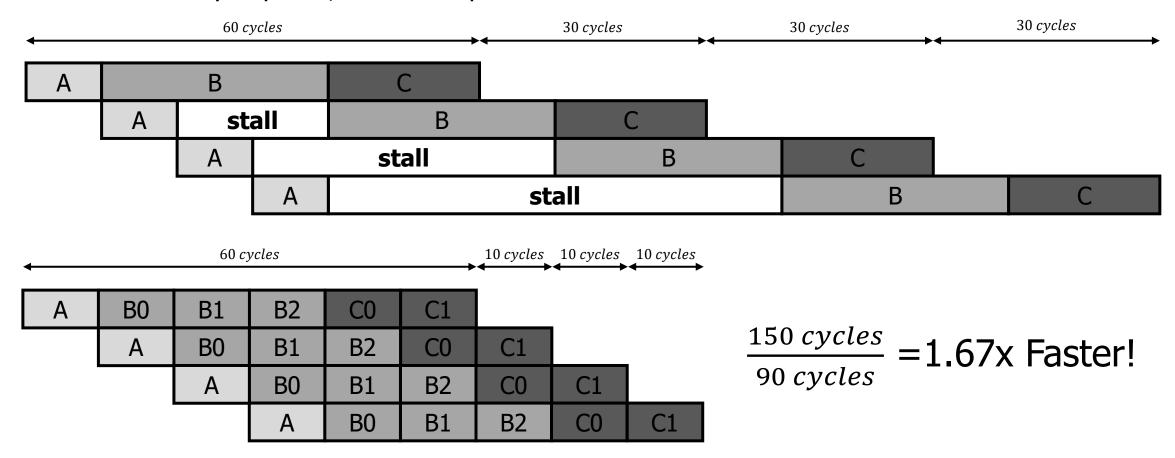
Overview of HW Design & SW Driver & Performance

- HW Design
 - Predict IP based on AXI Stream is connected to main memory (DDR) through DMA IP.
- SW Driver
 - When the interrupt signal becomes active HIGH, read the result and measure the latency.
- Performance Analysis
 - Comparing the result of different compile options in PS and the results through predict IP in PL.



Future Work

- Currently, performance is limited to the pipeline stage that takes the longest latency.
- Ideally, if all pipeline stages decomposed equally, performance would be better.
- Performance may improve, but it is expected to consume more resources.



References (Xilinx documents)

- Vitis High-Level Synthesis User Guide, UG1399 (v2022.2)
- Vivado Design Suite User Guide (High-Level Synthesis), UG902 (v2020.1)
- Vivado Design Suite Tutorial (High-Level Synthesis), UG871 (v2015.4)
- Vivado Design Suite AXI Reference Guide, UG1037 (v4.0)
- Vivado Design Suite User Guide (Programming and Debugging) UG908 (v2022.2)
- AXI DMA (v7.1) LogiCORE IP Product Guide, PG021
- AXI Timer (v2.0) LogiCORE IP Product Guide, PG079
- Zynq-7000 SoC Technical Reference Manual, UG585 (v1.13)
- Zynq-7000 All Programmable SoC Software Developers Guide, UG812 (v12.0)
- A Zynq Accelerator for Floating Point Matrix Multiplication Designed with Vivado HLS, XAPP1170 (v2.0)

References (etc.)

- The Zynq Book (Embedded Processing with the ARM Cortex-A9 on the Xilinx Zynq-7000 All Programmable SoC)
- Parallel Programming for FPGAs (The HLS Book)
- (1998) "Gradient-based learning applied to document recognition", *Proceedings of the IEEE*, vol. 86, no. 11, pp. 2278-2324
- (2016) "Eyeriss: A Spatial Architecture for Energy-Efficient Dataflow for Convolutional Neural Networks", ACM/IEEE 43rd Annual International Symposium on Computer Architecture (ISCA)
- (2015) "Deep Learning with Limited Numerical Precision", *Proceedings of the 32nd International Conference on Machine Learning (ICML)*
- Wavedrom (https://wavedrom.com/)
- Github (<u>https://github.com/wasinsangdam/LeNet-5</u>)

THANK YOU!