lab04 master

September 27, 2019

1 Lab 4: Functions and Visualizations

Welcome to Lab 4! This week, we'll learn about functions, table methods such as apply, and how to generate visualizations!

Recommended Reading:

- Applying a Function to a Column
- Visualizations

First, set up the notebook by running the cell below.

```
[]: import numpy as np
     from datascience import *
     # These lines set up graphing capabilities.
     import matplotlib
     %matplotlib inline
     import matplotlib.pyplot as plt
     plt.style.use('fivethirtyeight')
     import warnings
     warnings.simplefilter('ignore', FutureWarning)
     from ipywidgets import interact, interactive, fixed, interact_manual
     import ipywidgets as widgets
     # When you log-in please hit return (not shift + return) after typing in your
     \rightarrow email
     from client.api.notebook import Notebook
     ok = Notebook('lab04.ok')
     _ = ok.submit()
```

Deadline: If you are not attending lab physically, you have to complete this lab and submit by Wednesday, September 18th before 8:59 A.M. in order to receive lab credit. Otherwise, please attend the lab you are enrolled in, get checked off with your (u)GSI or learning assistant **AND** submit this assignment by the end of the lab section (with whatever progress you've made) to receive lab credit.

Submission: Once you're finished, select "Save and Checkpoint" in the File menu and then execute the submit cell at the end. The result will contain a link that you can use to check that your

assignment has been submitted successfully.

1.1 1. Defining functions

Let's write a very simple function that converts a proportion to a percentage by multiplying it by 100. For example, the value of to_percentage(.5) should be the number 50 (no percent sign).

A function definition has a few parts.

```
def It always starts with def (short for define):
def
```

Name Next comes the name of the function. Like other names we've defined, it can't start with a number or contain spaces. Let's call our function to_percentage:

```
def to_percentage
```

Signature Next comes something called the *signature* of the function. This tells Python how many arguments your function should have, and what names you'll use to refer to those arguments in the function's code. A function can have any number of arguments (including 0!).

to_percentage should take one argument, and we'll call that argument proportion since it should be a proportion.

```
def to_percentage(proportion)
```

If we want our function to take more than one argument, we add a comma between each argument name.

We put a colon after the signature to tell Python it's over. If you're getting a syntax error after defining a function, check to make sure you remembered the colon!

```
def to_percentage(proportion):
```

Documentation Functions can do complicated things, so you should write an explanation of what your function does. For small functions, this is less important, but it's a good habit to learn from the start. Conventionally, Python functions are documented by writing an **indented** triple-quoted string:

```
def to_percentage(proportion):
    """Converts a proportion to a percentage."""
```

Body Now we start writing code that runs when the function is called. This is called the *body* of the function and every line **must be indented with a tab**. Any lines that are *not* indented and left-aligned with the def statement is considered outside the function.

Some notes about the body of the function: - We can write code that we would write anywhere else.

- We use the arguments defined in the function signature. We can do this because we assume that when we call the function, values are already assigned to those arguments. - We generally avoid referencing variables defined *outside* the function. If you would like to reference variables outside of the function, pass them through as arguments!

Now, let's give a name to the number we multiply a proportion by to get a percentage:

```
def to_percentage(proportion):
    """Converts a proportion to a percentage."""
    factor = 100
```

return The special instruction return is part of the function's body and tells Python to make the value of the function call equal to whatever comes right after return. We want the value of to percentage (.5) to be the proportion .5 times the factor 100, so we write:

```
def to_percentage(proportion):
    """Converts a proportion to a percentage."""
    factor = 100
    return proportion * factor
```

return only makes sense in the context of a function, and can never be used outside of a function. return is always the last line of the function because Python stops executing the body of a function once it hits a return statement.

Note: return inside a function tells Python what value the function evaluates to. However, there are other functions, like print, that have no return value. For example, print simply prints a certain value out to the console.

return and print are very different.

Question 1.1. Define to_percentage in the cell below. Call your function to convert the proportion .2 to a percentage. Name that percentage twenty_percent.

```
BEGIN QUESTION name: q11
```

[5]: """ # BEGIN PROMPT

def ...
 ''' ... '''
 ... = ...
 return ...
"""; # END PROMPT

BEGIN SOLUTION NO PROMPT

def to_percentage(proportion):
 """Converts a proportion to a percentage."""
 factor = 100
 return proportion * factor
END SOLUTION

twenty_percent = to_percentage(.2) #SOLUTION

twenty_percent

[5]: 20.0

Like you've done with built-in functions in previous labs (max, abs, etc.), you can pass in named values as arguments to your function.

Question 1.2. Use to_percentage again to convert the proportion named a_proportion (defined below) to a percentage called a_percentage.

Note: You don't need to define to_percentage again! Like other named values, functions stick around after you define them.

BEGIN QUESTION name: q12

```
[30]: a_proportion = 2**(.5) / 2
a_percentage = to_percentage(a_proportion) #SOLUTION
a_percentage
```

[30]: 70.71067811865476

Here's something important about functions: the names assigned within a function body are only accessible within the function body. Once the function has returned, those names are gone. So even if you created a variable called factor and defined factor = 100 inside of the body of the to_percentage function and then called to_percentage, factor would not have a value assigned to it outside of the body of to_percentage:

```
[29]: # You should see an error when you run this. (If you don't, you might # have defined factor somewhere above.) factor
```

As we've seen with built-in functions, functions can also take strings (or arrays, or tables) as arguments, and they can return those things, too.

Question 1.3. Define a function called disemvowel. It should take a single string as its argument. (You can call that argument whatever you want.) It should return a copy of that string, but with all the characters that are vowels removed. (In English, the vowels are the characters "a", "e", "i", "o", and "u".) You can use as many lines inside of the function to do this as you'd like.

Hint: To remove all the "a"s from a string, you can use that_string.replace("a", ""). The .replace method for strings returns a new string, so you can call replace multiple times, one after the other.

BEGIN QUESTION name: q13

```
[31]: def disemvowel(a_string):
    """Removes all vowels from a string.""" #SOLUTION
    return a_string.replace("a", "").replace("e", "").replace("i", "").
    →replace("o", "").replace("u", "") #SOLUTION

# An example call to your function. (It's often helpful to run
    # an example call from time to time while you're writing a function,
    # to see how it currently works.)
    disemvowel("Can you read this without vowels?")
```

[31]: 'Cn y rd ths wtht vwls?'

Calls on calls O use a series of lines to build up a complex computation, it's useful to define a series of small functions that build on each other. Since you can write any code inside a function's body, you can call other functions you've written.

If a function is a like a recipe, defining a function in terms of other functions is like having a recipe for cake telling you to follow another recipe to make the frosting, and another to make the jam filling. This makes the cake recipe shorter and clearer, and it avoids having a bunch of duplicated frosting recipes. It's a foundation of productive programming.

For example, suppose you want to count the number of characters that aren't vowels in a piece of text. One way to do that is this to remove all the vowels and count the size of the remaining string.

Question 1.4. Write a function called num_non_vowels. It should take a string as its argument and return a number. That number should be the number of characters in the argument string that aren't vowels. You should use the disemvowel function you wrote above inside of the num_non_vowels function.

Hint: The function len takes a string as its argument and returns the number of characters in it.

BEGIN QUESTION name: q14

```
[37]: def num_non_vowels(a_string):
    """The number of characters in a string, minus the vowels."""
    return len(disemvowel(a_string)) #SOLUTION

# Try calling your function yourself to make sure the output is what
    # you expect. You can also use the interact function in the next cell if you'd
    → like.
```

Functions can also encapsulate code that *displays output* instead of computing a value. For example, if you call **print** inside a function, and then call that function, something will get printed.

The movies_by_year dataset in the textbook has information about movie sales in recent years. Suppose you'd like to display the year with the 5th-highest total gross movie sales, printed in a human-readable way. You might do this:

```
[40]: movies_by_year = Table.read_table("movies_by_year.csv")
rank = 5
fifth_from_top_movie_year = movies_by_year.sort("Total Gross", descending=True).

→column("Year").item(rank-1)
print("Year number", rank, "for total gross movie sales was:",

→fifth_from_top_movie_year)
```

Year number 5 for total gross movie sales was: 2010

After writing this, you realize you also wanted to print out the 2nd and 3rd-highest years. Instead of copying your code, you decide to put it in a function. Since the rank varies, you make that an argument to your function.

Question 1.5. Write a function called print_kth_top_movie_year. It should take a single argument, the rank of the year (like 2, 3, or 5 in the above examples). It should print out a message like the one above.

Note: Your function shouldn't have a return statement.

BEGIN QUESTION name: q15

```
[41]: def print_kth_top_movie_year(k):
    # BEGIN SOLUTION
    year = movies_by_year.sort("Total Gross", descending=True).column("Year").
    →item(k-1)
    print("Year number", k, "for total gross movie sales was:", year)
    # END SOLUTION
    """ # BEGIN PROMPT
    print(...)
    """; # END PROMPT

# Example calls to your function:
print_kth_top_movie_year(2)
print_kth_top_movie_year(3)
```

```
Year number 2 for total gross movie sales was: 2013
Year number 3 for total gross movie sales was: 2012
```

```
[43]: # interact also allows you to pass in an array for a function argument. It will # then present a dropdown menu of options.
_ = interact(print_kth_top_movie_year, k=np.arange(1, 10))
```

interactive(children=(Dropdown(description='k', options=(1, 2, 3, 4, 5, 6, 7, 8, 9), value=1),

1.1.1 print is not the same as return

The print_kth_top_movie_year(k) function prints the total gross movie sales for the year that was provided! However, since we did not return any value in this function, we can not use it after we call it. Let's look at an example of another function that prints a value but does not return it.

```
[44]: def print_number_five(): print(5)
```

```
[45]: print_number_five()
```

5

However, if we try to use the output of print_number_five(), we see that the value 5 is printed but we get a TypeError when we try to add the number 2 to it!

```
[47]: print_number_five_output = print_number_five()
print_number_five_output + 2
```

5

TypeError: unsupported operand type(s) for +: 'NoneType' and 'int'

It may seem that print_number_five() is returning a value, 5. In reality, it just displays the number 5 to you without giving you the actual value! If your function prints out a value without returning it and you try to use that value, you will run into errors, so be careful!

Explain to your neighbor how you might add a line of code to the print_number_five function (after print(5)) so that the code print_number_five_output + 5 would result in the value 10, rather than an error.

1.2 2. Functions and CEO Incomes

In this question, we'll look at the 2015 compensation of CEOs at the 100 largest companies in California. The data was compiled from a Los Angeles Times analysis, and ultimately came from filings mandated by the SEC from all publicly-traded companies. Two companies have two CEOs, so there are 102 CEOs in the dataset.

We've copied the raw data from the LA Times page into a file called raw_compensation.csv. (The page notes that all dollar amounts are in millions of dollars.)

```
[3]: raw_compensation = Table.read_table('raw_compensation.csv')
raw_compensation
```

```
[3]: Rank | Name
                                 | Company (Headquarters)
                                                                    | Total Pay | %
                       | Cash Pay | Equity Pay | Other Pay | Ratio of CEO pay to
     Change
     average industry worker pay
          | Mark V. Hurd*
                                  Oracle (Redwood City)
                                                                    | $53.25
                                                                                | (No
     previous year) | $0.95
                                | $52.27
                                              | $0.02
                                                           1 362
          | Safra A. Catz*
                                | Oracle (Redwood City)
                                                                    | $53.24
                                                                                | (No
     previous year) | $0.95
                                              1 $0.02
                                | $52.27
                                                           362
                                                                                I -3%
     3
          | Robert A. Iger
                                | Walt Disney (Burbank)
                                                                    | $44.91
       $24.89
                 | $17.28
                               | $2.74
                                           | 477
          | Marissa A. Mayer
                                | Yahoo! (Sunnyvale)
                                                                    | $35.98
                                                                                | -15%
       $1.00
                | $34.43
                              1 $0.55
                                           | 342
          | Marc Benioff
                                 | salesforce.com (San Francisco) | $33.36
                                                                                | -16%
       $4.65
                 | $27.26
                              | $1.45
                                           1 338
          | John H. Hammergren | McKesson (San Francisco)
                                                                    1 $24.84
                                                                                | -4%
                              1 $0.37
       $12.10
                 I $12.37
                                           1 222
     7
          | John S. Watson
                                | Chevron (San Ramon)
                                                                    | $22.04
                                                                                | -15%
       $4.31
                 | $14.68
                              | $3.05
                                           I 183
          | Jeffrey Weiner
                                | LinkedIn (Mountain View)
                                                                    | $19.86
                                                                                | 27%
       $2.47
                 | $17.26
                              | $0.13
                                           | 182
          | John T. Chambers** | Cisco Systems (San Jose)
                                                                                1 19%
                                                                    | $19.62
     | $5.10
                | $14.51
                              | $0.01
                                           | 170
                                                                   | $19.32
          | John G. Stumpf
                                 | Wells Fargo
                                                (San Francisco)
                                                                                I -10%
     | $6.80
                 | $12.50
                              | $0.02
                                           | 256
     ... (92 rows omitted)
```

We want to compute the average of the CEOs' pay. Try running the cell below.

```
[4]: np.average(raw_compensation.column("Total Pay"))
```

```
TypeError
                                                   Traceback (most recent call_{\sqcup}
→last)
       <ipython-input-4-f97fab5a8083> in <module>
   ---> 1 np.average(raw_compensation.column("Total Pay"))
       c:
\rightarrow\users\anna\appdata\local\programs\python\python36\lib\site-packages\numpy\lib\function_base
→py in average(a, axis, weights, returned)
       354
       355
               if weights is None:
   --> 356
                   avg = a.mean(axis)
                   scl = avg.dtype.type(a.size/avg.size)
       357
       358
               else:
→\users\anna\appdata\local\programs\python\python36\lib\site-packages\numpy\core\_methods.
→py in _mean(a, axis, dtype, out, keepdims)
        73
                       is_float16_result = True
        74
   ---> 75
               ret = umr_sum(arr, axis, dtype, out, keepdims)
               if isinstance(ret, mu.ndarray):
        76
        77
                   ret = um.true_divide(
```

TypeError: cannot perform reduce with flexible type

You should see a TypeError. Let's examine why this error occurred by looking at the values in the Total Pay column.

Question 2.1. Use the type function and set total_pay_type to the type of the first value in the "Total Pay" column.

```
BEGIN QUESTION
  name: q21

[9]: total_pay_type = type(raw_compensation.column("Total Pay").item(0)) #SOLUTION
  total_pay_type

[9]: str
```

Question 2.2. You should have found that the values in the Total Pay column are strings. It doesn't make sense to take the average of string values, so we need to convert them to numbers if

we want to do this. Extract the first value in Total Pay. It's Mark Hurd's pay in 2015, in *millions* of dollars. Call it mark_hurd_pay_string.

```
BEGIN QUESTION

name: q22

[13]: mark hurd nav string = r
```

```
[13]: mark_hurd_pay_string = raw_compensation.column("Total Pay").item(0) #SOLUTION mark_hurd_pay_string
```

[13]: '\$53.25 '

Question 2.3. Convert mark_hurd_pay_string to a number of dollars.

Some hints, as this question requires multiple steps: - The string method strip will be useful for removing the dollar sign; it removes a specified character from the start or end of a string. For example, the value of "100%".strip("%") is the string "100".

- You'll also need the function float, which converts a string that looks like a number to an actual number.
- Finally, remember that the answer should be in dollars, not millions of dollars.

```
BEGIN QUESTION name: q23
```

```
[15]: mark_hurd_pay = 10**6 * float(mark_hurd_pay_string.strip("$")) #SOLUTION
mark_hurd_pay
```

[15]: 53250000.0

To compute the average pay, we need to do this for every CEO. But that looks like it would involve copying this code 102 times.

This is where functions come in. First, we'll define a new function, giving a name to the expression that converts "total pay" strings to numeric values. Later in this lab, we'll see the payoff: we can call that function on every pay string in the dataset at once.

The next section of this lab explains how to define a function For now, just fill in the ellipses in the cell below.

Question 2.4. Copy the expression you used to compute mark_hurd_pay, and use it as the return expression of the function below. But make sure you replace the specific mark_hurd_pay_string with the generic pay_string name specified in the first line in the def statement.

Hint: When dealing with functions, you should generally not be referencing any variable outside of the function. Usually, you want to be working with the arguments that are passed into it, such as pay_string for this function. If you're using mark_hurd_pay_string within your function, you're referencing an outside variable!

```
BEGIN QUESTION name: q24
```

```
[21]: def convert_pay_string_to_number(pay_string):
```

```
"""Converts a pay string like '$100' (in millions) to a number of dollars.

"""

return 10**6 * float(pay_string.strip("$")) #SOLUTION
```

Running that cell doesn't convert any particular pay string. Instead, it creates a function called convert_pay_string_to_number that can convert *any* string with the right format to a number representing millions of dollars.

We can call our function just like we call the built-in functions we've seen. It takes one argument -- a string -- and it returns a float.

[26]: 53240000.0

So, what have we gained by defining the convert_pay_string_to_number function? Well, without it, we'd have to copy the code 10**6 * float(some_pay_string.strip("\$")) each time we wanted to convert a pay string. Now we just call a function whose name says exactly what it's doing.

1.3 3. applying functions

Defining a function is a lot like giving a name to a value with =. In fact, a function is a value just like the number 1 or the text "data"!

For example, we can make a new name for the built-in function max if we want:

```
[48]: our_name_for_max = max
our_name_for_max(2, 6)
```

[48]: 6

The old name for max is still around:

```
[49]: max(2, 6)
```

[49]: 6

Try just writing max or our_name_for_max (or the name of any other function) in a cell, and run that cell. Python will print out a (very brief) description of the function.

```
[52]: max
```

Now try writing <code>?max</code> or <code>?our_name_for_max</code> (or the name of any other function) in a cell, and run that cell. A information box should show up at the bottom of your screen a longer description of the function

```
[53]: ?our_name_for_max
```

Let's look at what happens when we set maxto a non-function value. You'll notice that a TypeError will occur when you try calling max. Things like integers and strings are not callable. Look out for any fungions that might have been renamed when you encounter this type of error

```
[4]: \max = 6 \max(2, 6)
```

```
[5]: # This cell resets max to the built-in function. Just run this cell, don't

→ change its contents

import builtins

max = builtins.max
```

Why is this useful? Since functions are just values, it's possible to pass them as arguments to other functions. Here's a simple but not-so-practical example: we can make an array of functions.

```
[51]: make_array(max, np.average, are.equal_to)
```

[51]: array([<built-in function max>, <function average at 0x000002971FFCEEA0>, <function are.equal_to at 0x000002972936BF28>], dtype=object)

TypeError: 'int' object is not callable

Question 3.1. Make an array containing any 3 other functions you've seen. Call it some_functions.

BEGIN QUESTION name: q31

```
[54]: some_functions = make_array(min, np.arange, print) #SOLUTION some_functions
```

Working with functions as values can lead to some funny-looking code. For example, see if you can figure out why the following code works. Check your explanation with a neighbor or a staff member.

```
[59]: make_array(max, np.average, are.equal_to).item(0)(4, -2, 7)
```

[59]: 7

A more useful example of passing functions to other functions as arguments is the table method apply.

apply calls a function many times, once on *each* element in a column of a table. It produces an *array* of the results. Here we use apply to convert every CEO's pay to a number, using the function you defined:

```
[60]: raw_compensation.apply(convert_pay_string_to_number, "Total Pay")

[60]: array([5.325e+07, 5.324e+07, 4.491e+07, 3.598e+07, 3.336e+07, 2.484e+07,
```

```
2.204e+07, 1.986e+07, 1.962e+07, 1.932e+07, 1.876e+07, 1.861e+07,
1.836e+07, 1.809e+07, 1.710e+07, 1.663e+07, 1.633e+07, 1.614e+07,
1.610e+07, 1.602e+07, 1.510e+07, 1.498e+07, 1.463e+07, 1.451e+07,
1.444e+07, 1.436e+07, 1.431e+07, 1.409e+07, 1.400e+07, 1.367e+07,
1.234e+07, 1.220e+07, 1.218e+07, 1.213e+07, 1.205e+07, 1.184e+07,
1.171e+07, 1.163e+07, 1.116e+07, 1.111e+07, 1.111e+07, 1.073e+07,
1.050e+07, 1.043e+07, 1.037e+07, 1.028e+07, 1.027e+07, 1.018e+07,
1.016e+07, 9.970e+06, 9.960e+06, 9.860e+06, 9.740e+06, 9.420e+06,
9.390e+06, 9.220e+06, 9.060e+06, 9.030e+06, 8.860e+06, 8.760e+06,
8.570e+06, 8.380e+06, 8.360e+06, 8.350e+06, 8.230e+06, 7.860e+06,
7.700e+06, 7.580e+06, 7.510e+06, 7.230e+06, 7.210e+06, 7.120e+06,
6.880e+06, 6.770e+06, 6.640e+06, 6.560e+06, 6.140e+06, 5.920e+06,
5.900e+06, 5.890e+06, 5.730e+06, 5.420e+06, 5.040e+06, 4.920e+06,
4.920e+06, 4.470e+06, 4.250e+06, 4.080e+06, 3.930e+06, 3.720e+06,
2.880e+06, 2.830e+06, 2.820e+06, 2.450e+06, 1.790e+06, 1.680e+06,
1.530e+06, 9.400e+05, 8.100e+05, 7.000e+04, 4.000e+04, 0.000e+00])
```

Here's an illustration of what that did:

Note that we didn't write raw_compensation.apply(convert_pay_string_to_number(), "Total Pay") or raw_compensation.apply(convert_pay_string_to_number("Total Pay")). We just passed the name of the function, with no parentheses, to apply, because all we want to do is let apply know the name of the function we'd like to use and the name of the column we'd

like to use it on. apply will then call the function convert_pay_string_to_number on each value in the column for us!

Question 3.2. Using apply, make a table that's a copy of raw_compensation with one additional column called Total Pay (\$). That column should contain the result of applying convert_pay_string_to_number to the Total Pay column (as we did above). Call the new table compensation.

BEGIN QUESTION name: q32

```
[61]: compensation = raw_compensation.with_column(
    "Total Pay ($)",
    raw_compensation.apply(convert_pay_string_to_number, "Total Pay") #SOLUTION
    )
    compensation
```

```
[61]: Rank | Name
                                 | Company (Headquarters)
                                                                  | Total Pay | %
                       | Cash Pay | Equity Pay | Other Pay | Ratio of CEO pay to
      Change
      average industry worker pay | Total Pay ($)
           | Mark V. Hurd*
                              | Oracle (Redwood City)
                                                                   | $53.25
                                                                               | (No
      previous year) | $0.95
                                 | $52.27
                                              1 $0.02
                                                          | 362
      | 5.325e+07
          | Safra A. Catz*
                                | Oracle (Redwood City)
                                                                   | $53.24
                                                                               | (No
      previous year) | $0.95
                                 | $52.27
                                              1 $0.02
                                                          362
      1 5.324e+07
           | Robert A. Iger
                                | Walt Disney (Burbank)
                                                                  | $44.91
                                                                               I -3%
      1 $24.89
                I $17.28
                              1 $2.74
                                           1 477
      | 4.491e+07
           | Marissa A. Mayer
                                | Yahoo! (Sunnyvale)
                                                                  I $35.98
                                                                               | -15%
      I $1.00
                 1 $34.43
                              I $0.55
                                           1 342
      1 3.598e+07
           | Marc Benioff
                                 | salesforce.com (San Francisco) | $33.36
                                                                               | -16%
      l $4.65
                 1 $27.26
                              I $1.45
                                           1 338
      | 3.336e+07
           | John H. Hammergren | McKesson (San Francisco)
                                                                               | -4%
                                                                  | $24.84
      | $12.10
                | $12.37
                              | $0.37
                                           | 222
      1 2.484e+07
           | John S. Watson
                                 | Chevron (San Ramon)
                                                                  | $22.04
                                                                               I -15%
      | $4.31
                 | $14.68
                              | $3.05
                                           I 183
      | 2.204e+07
                                 | LinkedIn (Mountain View)
           | Jeffrey Weiner
                                                                  | $19.86
                                                                               | 27%
      1 $2.47
                 I $17.26
                              I $0.13
                                           I 182
      | 1.986e+07
           | John T. Chambers** | Cisco Systems (San Jose)
                                                                  | $19.62
                                                                               1 19%
                              | $0.01
      | $5.10
                l $14.51
                                           l 170
      l 1.962e+07
           | John G. Stumpf
                                | Wells Fargo (San Francisco)
                                                                 | $19.32
                                                                               | -10%
```

```
| $6.80 | $12.50 | $0.02 | 256
| 1.932e+07
... (92 rows omitted)
```

Now that we have all the pays as numbers, we can learn more about them through computation.

Question 3.3. Compute the average total pay of the CEOs in the dataset.

```
BEGIN QUESTION name: q33
```

```
[64]: average_total_pay = np.average(compensation.column("Total Pay ($)")) #SOLUTION average_total_pay
```

[64]: 11445294.11764706

Question 3.4. Companies pay executives in a variety of ways: in cash, by granting stock or other equity in the company, or with ancillary benefits (like private jets). Compute the proportion of each CEO's pay that was cash. (Your answer should be an array of numbers, one for each CEO in the dataset.)

Note: When you answer this question, you'll encounter a red box appearing below your code cell that says something like RuntimeWarning: invalid value encountered in true_divide. Don't worry too much about the message. Warnings are raised by Python when it encounters an unusual condition in your code, but the condition is not severe enough to warrant throwing an error.

The warning below is Python's cryptic way of telling you that you're dividing a number by zero. If you extract the values in Total Pay (\$) as an array, you'll see that the last element is 0.

```
BEGIN QUESTION name: q34
```

c:\users\anna\appdata\local\programs\python\python36\lib\sitepackages\ipykernel_launcher.py:1: RuntimeWarning: invalid value encountered in
true_divide

"""Entry point for launching an IPython kernel.

```
[67]: array([0.01784038, 0.01784373, 0.55421955, 0.02779322, 0.13938849, 0.48711755, 0.19555354, 0.12437059, 0.25993884, 0.35196687, 0.3075693, 0.22138635, 0.13126362, 0.1708126, 0.23099415, 0.06734817, 0.13043478, 0.28004957, 0.33229814, 0.15355805, 0.29337748, 0.21829105, 0.31100478, 0.25086147, 0.2299169, 0.16991643, 0.31795947, 0.26188786, 0.28357143, 0.15654718, 0.38168558, 0.28934426, 0.20361248, 0.47650453, 0.45643154, 0.36402027, 0.2177626, 0.24763543, 0.42562724, 0.2610261,
```

```
0.18361836, 0.1444548, 0.33333333, 0.10834132, 0.20925747,
0.97276265, 0.22979552, 0.22789784, 0.37893701, 0.25175527,
0.73895582, 0.37018256, 0.2412731, 0.2133758, 0.20553781,
0.23318872, 0.33664459, 0.3875969, 0.56094808, 0.11757991,
0.35239207, 0.24463007, 0.25
                               , 0.23712575, 0.43377886,
0.31424936, 0.46363636, 0.32585752, 0.24766977, 0.98755187,
0.27184466, 0.96207865, 0.31831395, 0.81979321, 0.23795181,
0.17530488, 0.21172638, 0.37162162, 0.27288136, 0.26994907,
0.55148342, 0.3597786, 0.
                                 , 0.47154472, 0.47154472,
0.29753915, 0.16235294, 0.48529412, 0.46819338, 0.32526882,
0.98958333, 0.61130742, 0.67021277, 0.75510204, 0.50837989,
0.98809524, 0.98039216, 0.9893617, 0.87654321, 0.
1.
                  nanl)
```

Check out the % Change column in compensation. It shows the percentage increase in the CEO's pay from the previous year. For CEOs with no previous year on record, it instead says "(No previous year)". The values in this column are *strings*, not numbers, so like the Total Pay column, it's not usable without a bit of extra work.

Given your current pay and the percentage increase from the previous year, you can compute your previous year's pay. For example, if your pay is \$120 this year, and that's an increase of 50% from the previous year, then your previous year's pay was $\frac{\$120}{1+\frac{50}{100}}$, or \$80.

Question 3.5. Create a new table called with_previous_compensation. It should be a copy of compensation, but with the "(No previous year)" CEOs filtered out, and with an extra column called 2014 Total Pay (\$). That column should have each CEO's pay in 2014.

Hint 1: You can print out your results after each step to make sure you're on the right track.

Hint 2: We've provided a structure that you can use to get to the answer. However, if it's confusing, feel free to delete the current structure and approach the problem your own way!

```
BEGIN QUESTION name: q35
```

```
percent_changes = having_previous_year.apply(percent_string_to_num, "% Change")__
#SOLUTION

# Calculate the previous year's pay
# We're still working off the table having_previous_year
previous_pay = having_previous_year.column("Total Pay ($)") / (1 +__
percent_changes / 100) #SOLUTION

# Put the previous pay column into the having_previous_year table
with_previous_compensation = having_previous_year.with_column("2014 Total Pay__
($)", previous_pay) #SOLUTION

with_previous_compensation
```

```
[70]: Rank | Name
                             | Company (Headquarters)
                                                          | Total Pay | %
     Change | Cash Pay | Equity Pay | Other Pay | Ratio of CEO pay to average
     industry worker pay | Total Pay ($) | 2014 Total Pay ($)
          | Robert A. Iger | Walt Disney (Burbank)
                                                          | $44.91
                                                                      I -3%
                           | $2.74
     | $24.89 | $17.28
     4.491e+07
                   1 4.6299e+07
          | Marissa A. Mayer | Yahoo! (Sunnyvale)
                                                 | $35.98
                                                                      I -15%
     | $1.00 | $34.43 | $0.55
                                     | 342
     1 3.598e+07
                   1 4.23294e+07
          | Marc Benioff
                             | salesforce.com (San Francisco) | $33.36
                                                                     l -16%
     | $4.65
             | $27.26
                           | $1.45
                                     | 338
     l 3.336e+07
                   | 3.97143e+07
          | John H. Hammergren | McKesson (San Francisco)
                                                         l $24.84
                                                                      I -4%
     l $12.10
              | $12.37 | $0.37
     l 2.484e+07
                   1 2.5875e+07
         | John S. Watson
                           | Chevron (San Ramon)
                                                          1 $22.04
                                                                      I -15%
     | $4.31
             | $14.68
                                     l 183
                          | $3.05
     l 2.204e+07
                   l 2.59294e+07
          | Jeffrey Weiner
                           | LinkedIn (Mountain View)
                                                          | $19.86
                                                                      | 27%
                                      l 182
     1 $2.47
             l $17.26
                           I $0.13
     | 1.986e+07
                   | 1.56378e+07
          | John T. Chambers** | Cisco Systems (San Jose)
                                                          | $19.62
                                                                      1 19%
     | $5.10
               | $14.51
                           I $0.01
                                      | 170
     | 1.962e+07
                   | 1.64874e+07
                           | Wells Fargo (San Francisco)
     10 | John G. Stumpf
                                                          | $19.32
                                                                      1 -10%
     | $6.80
              | $12.50
                           1 $0.02
                                      | 256
     1.932e+07
                   2.14667e+07
     11 | John C. Martin** | Gilead Sciences (Foster City) | $18.76
                                                                      | -1%
     | $5.77 | $12.98
                          l $0.01
                                     l 117
                   | 1.89495e+07
     | 1.876e+07
     13 | Shantanu Narayen | Adobe Systems (San Jose) | $18.36
                                                                    I 3%
                         | $0.09
                                    l 125
     | $2.41
              | $15.85
                  l 1.78252e+07
     l 1.836e+07
```

... (71 rows omitted)

Question 3.6. What was the average pay of these CEOs in 2014?

BEGIN QUESTION name: q36

[74]: average_pay_2014 = np.average(with_previous_compensation.column("2014 Total Pay

→(\$)")) #SOLUTION

average_pay_2014

[74]: 11649176.115603436

Why is apply useful?

For operations like arithmetic, or the functions in the NumPy library, you don't need to use apply, because they automatically work on each element of an array. But there are many things that don't. The string manipulation we did in today's lab is one example. Since you can write any code you want in a function, apply gives you total control over how you operate on data.

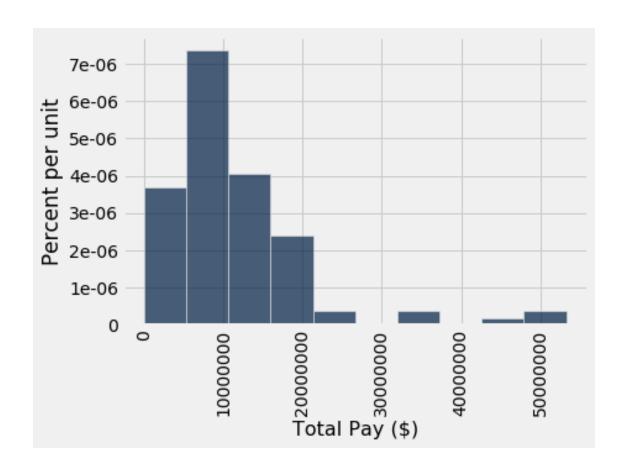
1.4 4. Histograms

Earlier, we computed the average pay among the CEOs in our 102-CEO dataset. The average doesn't tell us everything about the amounts CEOs are paid, though. Maybe just a few CEOs make the bulk of the money, even among these 102.

We can use a *histogram* method to display the *distribution* of a set of numbers. The table method **hist** takes a single argument, the name of a column of numbers. It produces a histogram of the numbers in that column.

Question 4.1. Make a histogram of the total pay of the CEOs in compensation. Check with your neighbor or a staff member to make sure you have the right plot.

[76]: compensation.hist("Total Pay (\$)") #SOLUTION



Question 4.2. How many CEOs made more than \$30 million in total pay? Find the value using code, then check that the value you found is consistent with what you see in the histogram.

Hint: Use the table method where and the property num_rows.

```
BEGIN QUESTION name: q42
```

```
[77]: num_ceos_more_than_30_million_2 = compensation.where("Total Pay ($)", are.

above(30*10**6)).num_rows #SOLUTION

num_ceos_more_than_30_million_2
```

[77]: 5

1.5 5. Project 1 Partner Form

Project 1 will be released this Friday! You have the option of working with a partner that is enrolled in your lab. Your GSI will be sending out a form to match you up with a partner for this project. You may also indicate if you're working alone or have already found a partner and do not need to be paired up. This form is **mandatory** - please fill it out before submitting your lab. Set **submitted** to **True** once you've submitted the form.

Note: If you are completing this lab before the early submission deadline, the form may not have been sent out yet. Set submitted to True for now, and keep an eye out for an email from your GSI later this week.

BEGIN QUESTION name: q5

```
[6]: submitted = True #SOLUTION
```

Great job! You're finished with lab 4! Be sure to...

- run all the tests (the next cell has a shortcut for that),
- Save and Checkpoint from the File menu,
- run the last cell to submit your work,
- and ask one of the staff members to check you off.

```
[]: # For your convenience, you can run this cell to run all the tests at once!
import os
_ = [ok.grade(q[:-3]) for q in os.listdir("tests") if q.startswith('q')]

[]: _ = ok.submit()
```