

$$1. \text{ Q) } \int 7 \sin^2(x) \cos^3(x) dx$$

$$\text{A) } I = 7 \int \sin^2(x) \cos^2(x) \cos(x) dx$$

$$\text{Let } u = \sin(x); du = \cos(x) dx. \text{ Also } \cos^2(x) = 1 - \sin^2(x) = 1 - u^2$$

$$\implies I = 7 \int u^2(1 - u^2) du$$

$$= 7 \int (u^2 - u^4) du$$

$$= \frac{7u^3}{3} - \frac{7u^5}{5} + C$$

$$= \frac{7 \sin^3(x)}{3} - \frac{7 \sin^5(x)}{5} + C$$

$$2. \text{ Q) } \int 19 \sin^2(x) \cos^3(x) dx$$

$$3. \text{ Q) } \int_0^{\pi/2} \sin^5(x) \cos^5(x) dx$$

$$\text{A) Let } I = \int \sin^5(x) \cos^5(x) dx$$

$$\text{Let } u = \sin(x); du = \cos(x) dx. \text{ Also } \cos^2(x) = 1 - \sin^2(x) = 1 - u^2$$

$$\implies I = \int u^5(1 - u^2)^2 du$$

$$= \int u^5(1 - 2u^2 + u^4) du$$

$$= \int (u^5 - 2u^7 + u^9) du = u^6/6 - u^8/4 + u^{10}/10 + C$$

$$= \frac{\sin^6(x)}{6} - \frac{\sin^8(x)}{4} + \frac{\sin^{10}(x)}{10} + C$$

$$\implies [I]_0^{\pi/2} = \frac{\sin^6(\pi/2)}{6} - \frac{\sin^8(\pi/2)}{4} + \frac{\sin^{10}(\pi/2)}{10} - 0$$

$$= \frac{1}{6} - \frac{1}{4} + \frac{1}{10} = \frac{10-15+6}{60} = 1/60$$