

1. Q) Surface area of revolution:

$$y = \sqrt{1 + e^x}, 0 \leq x \leq 3$$

$$\text{A) } \boxed{S = \int_a^b 2\pi f(x) \sqrt{1 + [f'(x)^2]} dx}$$

$$f = (1 + e^x)^{1/2}$$

$$f' = \frac{e^x}{2\sqrt{1 + e^x}}$$

$$S = \int_0^3 2\pi (1 + e^x)^{1/2} \sqrt{1 + \left(\frac{e^x}{2\sqrt{1 + e^x}}\right)^2} dx$$

$$= 2\pi \int_0^3 (1 + e^x)^{1/2} \sqrt{1 + \frac{e^{2x}}{4(1 + e^x)}} dx$$

$$= \pi \int_0^3 \sqrt{4(1 + e^x) + e^{2x}} dx$$

$$= \pi \int_0^3 \sqrt{2^2 + 2 \cdot 2 \cdot e^x + e^{x^2}} dx = \pi \int_0^3 (2 + e^x) dx$$

$$= \pi [2x + e^x]_0^3$$

$$= \pi [6 + e^3 - 0 - e^0]$$

$$= \pi [5 + e^3]$$