

1. Q — $\int x e^{6x} dx$

A —

Let $u = x; v' = e^{6x}$. Therefore $v = \frac{1}{6}e^{6x}$

According to integration by parts:

$$\int uv' = uv - \int vu'$$

$$\text{Therefore } \int x e^{6x} dx = x \frac{1}{6} e^{6x} - \int \frac{1}{6} e^{6x} dx$$

$$= x \frac{1}{6} e^{6x} - \frac{1}{6} \int e^{6x} dx$$

$$= x \frac{1}{6} e^{6x} - \frac{1}{36} e^{6x} + C.$$