1. Q) Find f_{ave}, where $f(x) = 3x^2 + 4x$, on $[-1, 3]$

A) $\int f(x)dx = \int (3x^2 + 4x)dx$

$= x^3 + 2x^2 + C$

$\implies f_{ave} = \frac{\left[x^3+2x^2\right]_{-1}^{3}}{3+1}$

$= \frac{(3^3+2.3^2)-((-1)^3+2(-1)^2)}{4}$

$= \frac{(27+18)-(-1+2)}{4}$

$= \frac{45-1}{4} = 11$

2. Q) Find f_{ave}, where $f(x) = 5\cos(x)$, on $[-\pi/2, \pi/2]$

A) $\int f(x)dx = \int 5\cos(x)dx$

$= 5\sin(x) + C$

$\implies f_{ave} = \frac{[5\sin(x)]_{\pi/2}^{-\pi/2}}{-\pi/2-\pi/2}$

$= \frac{(-5)-(5)}{-\pi}$

$= \frac{10}{\pi}$

3. Q) Find f_{ave}, where $f(t) = \frac{t}{\sqrt{3+t^2}}$, on $[1, 3]$

A) $\int f(t)dt = \int \frac{t}{\sqrt{3+t^2}}dt$

$= \int \frac{t}{\sqrt{3+t^2}}dt = \frac{1}{2}\int \frac{1}{\sqrt{u}}du$, for $u = 3 + t^2$

$= \sqrt{u} + C = \sqrt{(3+t^2)} + C$

$\implies f_{ave} = \frac{\left[\sqrt{(3+t^2)}\right]_1^3}{3-1}$

$= \frac{(\sqrt{3+9})-(\sqrt{3+1})}{2} = \frac{\sqrt{12}-2}{2} = \sqrt{3} - 1$

4. Q) Find f_{ave}, where $f(t) = e^{\sin(t)}\cos(t)$, on $[0, \pi/2]$

A) $\int f(t)dt = \int e^{\sin(t)}\cos(t)dt$

$= \int e^u du$, for $u = \sin(t)$

$= e^u = e^{\sin(t)} + C$

$\implies f_{ave} = \frac{\left[e^{\sin(t)}\right]_0^{\pi/2}}{\pi/2-0}$

$= \frac{e^1-e^0}{\pi/2} = \frac{e-1}{\pi/2} = \frac{2(e-1)}{\pi}$

5. Q) Find f_{ave}, where $f(x) = 6\cos^4(x)\sin(x)$, on $[0, \pi]$

A) $\int f(x)dx = \int 6\cos^4(x)\sin(x)dx$

$= -6\int u^4 du$, for $u = \cos(x)$

$= -\frac{6}{5}u^5 + C = -\frac{6}{5}\cos^5(x) + C$

$\implies f_{ave} = -\frac{6}{5}\frac{\left[\cos^5(x)\right]_0^{\pi}}{\pi-0}$

$= -\frac{6}{5}\frac{\cos^5(\pi)-\cos^5(0)}{\pi}$

$= -\frac{6}{5}\frac{-1-1}{\pi} = \frac{12}{5\pi}$