

1. Q — Use the **Euclidean Algorithm** to find integers a and b such that $70a + 182b = 28$. Are the integers c and d such that $70c + 182d = 30$?

A —

Original Pair	Division Expression	GCD
(182, 70)	$182 = 2 \cdot 70 + \mathbf{42}$	(70, 42)
(70, 42)	$70 = 1 \cdot 42 + \mathbf{28}$	(42, 28)
(42, 28)	$42 = 1 \cdot 28 + \mathbf{14}$	(28, 14)
(28, 14)	$28 = 2 \cdot 14 + \mathbf{0}$	14

Substituting the GCD (**14**) into the penultimate Division Expression:

$$\begin{aligned}
 14 &= 42 - (\mathbf{1})(28) \\
 &= 42 - (\mathbf{1})(70 - (\mathbf{1})(42)) \\
 &= (\mathbf{-1})(70) + (\mathbf{2})(42) \\
 &= (\mathbf{-1})(70) + (\mathbf{2})(182 - (\mathbf{2})(70)) \\
 &= (\mathbf{-1})(70) + (\mathbf{2})(182) - (\mathbf{4})(70) \\
 &= (\mathbf{2})(182) - (\mathbf{5})(70) \\
 \therefore 28 &= (\mathbf{4})(182) - (\mathbf{10})(70)
 \end{aligned}$$

Since **30** does not appear in the remainders in the table above, it is **not** possible to attain $70c + 182d = 30$ with integers, c and d .