
Cosmologically-Coupled Black Holes and Dark Energy: Alleviating the Hubble Tension

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Abstract

This paper investigates the hypothesis that cosmologically-coupled black holes (CCBH) play a pivotal role in mediating matter-to-dark energy conversion, and examines the consequential impact of this process on resolving the persistent Hubble tension. Drawing upon data from the Dark Energy Spectroscopic Instrument (DESI) Data Release 2, complemented by cosmic microwave background (CMB) datasets, we perform a rigorous analysis of a physical model. In this model, the production of dark energy is intrinsically linked to the cosmic star formation rate density, thereby establishing a direct relationship between astrophysical processes and cosmological dynamics. The findings emanating from this analysis suggest that the CCBH model demonstrates a compelling alignment with the observed cosmological expansion history. Furthermore, this framework offers a potential pathway to mitigate the existing tension with the local distance ladder measurements, a discrepancy that has been a subject of intense scrutiny in recent years. The implications of this model extend to the realm of neutrino physics, as our results indicate that the CCBH-mediated dark energy production could exert a discernible influence on the constraints derived for neutrino mass estimations. This research contributes to a deeper understanding of the interplay between black hole physics, dark energy, and the evolving structure of the cosmos.

1 Introduction

The accelerating expansion of the universe, a phenomenon attributed to a mysterious component known as dark energy, stands as one of the most profound puzzles in contemporary cosmology. This acceleration, observationally confirmed through various independent probes, including supernovae surveys and cosmic microwave background (CMB) anisotropies, necessitates a fundamental revision of our understanding of the cosmos. While the standard cosmological model, Λ CDM, successfully accounts for many observed features of the universe, it relies on the existence of dark energy, typically modeled as a cosmological constant (Λ), with no satisfactory explanation for its origin or magnitude. This discrepancy between theoretical predictions and observational constraints has led to a vigorous search for alternative or modified gravity theories.

Adding to this complexity is the Hubble tension, a significant and persistent disagreement between the value of the Hubble constant (H_0) inferred from early-universe observations (e.g., CMB measurements by Planck) and that derived from late-universe direct measurements (e.g., Type Ia supernovae). The Planck collaboration's CMB data, within the framework of Λ CDM, yields a lower value of H_0 than that obtained from local distance ladder measurements. This tension, now exceeding 4σ statistical significance, poses a serious challenge to the Λ CDM model, suggesting the possibility of new physics beyond the standard paradigm. Numerous theoretical proposals have been put forth to address the Hubble tension, ranging from modifications to the early-universe physics, such as early dark energy models, to alterations in the late-time behavior of dark energy itself.

38 This paper delves into a novel and potentially transformative approach to addressing both the dark
39 energy enigma and the Hubble tension: the exploration of cosmologically-coupled black holes
40 (CCBH) as engines for dark energy production. The central hypothesis posits that black holes, rather
41 than being passive observers in the cosmic expansion, actively participate in it through a coupling to
42 the evolving cosmological background. As the universe expands, these CCBHs accrete mass not only
43 from their immediate surroundings but also, more fundamentally, through a cosmologically-driven
44 process that converts matter into dark energy. This conversion process, if operating efficiently,
45 could contribute significantly to the overall dark energy density of the universe, thereby influencing
46 the expansion rate and potentially resolving the Hubble tension. The idea builds upon theoretical
47 frameworks that allow for black hole mass to increase with the expansion of the universe, thereby
48 violating strong energy conditions within the black hole interior, which leads to contribution to dark
49 energy. This paper explores the theoretical underpinnings of this CCBH hypothesis, investigates its
50 observational consequences, and assesses its potential to provide a self-consistent and observationally
51 viable cosmological model.

52 **2 Theoretical Background**

53 This section will lay out the theoretical foundations necessary to understand the proposed model
54 of cosmologically-coupled black holes (CCBH) as dark energy engines and their potential role in
55 alleviating the Hubble tension. It will cover essential concepts related to dark energy, the observed
56 discrepancy in the Hubble constant, and the standard understanding of black hole formation and
57 evolution within the cosmological context.

58 **2.1 The Cosmological Constant and Dark Energy**

59 The accelerated expansion of the universe, confirmed through observations of Type Ia supernovae
60 [1, 2], remains one of the most profound mysteries in modern cosmology. The simplest and most
61 adopted explanation for this phenomenon is the cosmological constant, denoted by Λ , within
62 the framework of the Λ CDM model. The Λ CDM model posits that the universe is composed of
63 approximately 5% ordinary baryonic matter, 27% dark matter, and 68% dark energy, with dark energy
64 dominating the current expansion [3].

65 The cosmological constant represents a constant energy density permeating all of space, exerting a
66 negative pressure that drives the accelerated expansion. Einstein's field equations incorporate Λ as a
67 term proportional to the metric tensor, effectively contributing a constant energy density and pressure
68 to the energy-momentum tensor. While remarkably successful in fitting a wide range of cosmological
69 data, the cosmological constant faces significant theoretical challenges.

70 One of the most prominent issues is the enormous discrepancy between the observed value of Λ
71 and the theoretical estimates derived from quantum field theory (QFT). QFT predicts a vacuum
72 energy density arising from quantum fluctuations of all fields, but these estimates are many orders of
73 magnitude (ranging from 60 to 120 orders) larger than the observed value. This discrepancy, known
74 as the cosmological constant problem, suggests that either there is an unknown mechanism canceling
75 the vacuum energy, or that our understanding of gravity or QFT is incomplete [4, 5].

76 Alternative dark energy models have been proposed to address these issues, including quintessence,
77 phantom energy, and modified gravity theories [6]. Quintessence, for example, involves a dynamic
78 scalar field with a potential energy that evolves over time, providing a time-varying equation of state
79 for dark energy. Modified gravity theories, on the other hand, attempt to explain the accelerated
80 expansion by modifying Einstein's theory of general relativity at cosmological scales. However, these
81 models often introduce new parameters or face their own theoretical and observational challenges.
82 Despite the wide variety of models, the cosmological constant remains the simplest and most
83 observationally consistent explanation for dark energy [7].

84 **2.2 The Hubble Tension**

85 The Hubble constant, H_0 , quantifies the current expansion rate of the universe. Measurements of H_0
86 can be broadly divided into two categories: early-universe and late-universe probes. Early-universe
87 probes, such as the cosmic microwave background (CMB) anisotropies measured by Planck [3],
88 provide a precise estimate of H_0 when combined with the Λ CDM model. However, late-universe

89 probes, such as the distance ladder method using Type Ia supernovae calibrated by Cepheid variables,
90 yield a significantly higher value of H_0 [1, 2, 8].

91 This discrepancy, known as the Hubble tension, represents a significant challenge to the Λ CDM
92 model. The tension has grown to a statistical significance of 4 to 6σ , indicating that it is unlikely to
93 be a result of statistical fluctuations [9]. The Planck collaboration’s 2018 results, assuming the base
94 Λ CDM cosmology, inferred a Hubble constant of $H_0 = (67.4 \pm 0.5)\text{km/s/Mpc}$ [3]. In contrast, the
95 SH0ES team, using the Cepheid-supernova distance ladder, finds $H_0 = (73.04 \pm 1.04)\text{km/s/Mpc}$ [8].

96 The persistence of the Hubble tension despite increasingly precise measurements has led to a
97 flurry of theoretical activity, with numerous proposals attempting to resolve the discrepancy. These
98 proposals can be broadly categorized into early-universe solutions, which modify the physics before
99 recombination to reduce the sound horizon, and late-universe solutions, which invoke new physics at
100 late times to increase the expansion rate. As noted by Di Valentino et al., modifications only affecting
101 the early universe may fall short of a full resolution [9].

102 **2.3 Black Holes in Cosmology**

103 Black holes, once considered purely theoretical objects, are now recognized as ubiquitous components
104 of the universe, playing a crucial role in galaxy formation and evolution. Supermassive black holes
105 (SMBHs), with masses ranging from millions to billions of solar masses, reside at the centers of most
106 galaxies, including our own Milky Way [10]. Stellar-mass black holes, formed from the collapse of
107 massive stars, are also abundant throughout galaxies.

108 The formation and growth of black holes are complex processes that depend on a variety of factors,
109 including the initial mass function of stars, the efficiency of accretion, and the merger history of
110 galaxies. Black holes can grow through accretion of gas and dust from their surroundings, as
111 well as through mergers with other black holes. The accretion process can be highly efficient,
112 converting a significant fraction of the accreted mass into energy, which is then radiated into the
113 surrounding environment. This energy feedback can have a significant impact on the evolution of
114 galaxies, regulating star formation and influencing the distribution of gas. As highlighted by Woosley,
115 gamma-ray bursts may be connected to black holes formed from stellar collapse [11].

116 The potential role of black holes in dark energy has been explored in various theoretical frameworks.
117 One intriguing possibility is that black holes could be coupled to the expansion of the universe, such
118 that their mass increases over time in proportion to the scale factor. If this were the case, black
119 holes could potentially contribute a significant fraction of the dark energy density, providing a novel
120 solution to the cosmological constant problem. This section provides the foundation for exploring
121 such cosmologically coupled black holes (CCBH) as a potential driver of dark energy and a possible
122 contributor to the resolution of the Hubble tension, topics to be explored in detail in subsequent
123 sections.

124 **3 The Cosmologically-Coupled Black Hole (CCBH) Model**

125 The accelerating expansion of the Universe, driven by dark energy, motivates the exploration of
126 unconventional models that challenge our understanding of gravity and cosmology. One such model
127 posits a cosmological coupling of black holes (BHs), suggesting that these objects might not be
128 mere spectators in the cosmic drama, but active participants in the ongoing matter-to-dark energy
129 conversion. This section delves into the details of the Cosmologically-Coupled Black Hole (CCBH)
130 model, explaining its core mechanisms, mathematical underpinnings, and connections to observable
131 phenomena.

132 **3.1 Model Description**

133 The CCBH model proposes that the masses of black holes are not strictly conserved, but instead
134 increase with the expansion of the universe, independently of standard accretion or merger processes.
135 This coupling is hypothesized to be governed by a new term in the Einstein field equations, introducing
136 a direct interaction between the black hole’s interior solution and the evolving cosmological back-
137 ground. As the universe expands, stellar-remnant black holes gain mass. This process, distinct from
138 traditional mass gain through accretion or mergers, effectively transfers energy from the matter sector

139 to the dark energy sector. While conventional black holes are characterized by the (Schwarzschild)
140 Arnowitt-Deser-Misner (ADM) mass, the CCBH model relies on the quasi-local Misner-Sharp (MS)
141 mass, allowing for cosmological coupling [12, 13]. The rate of mass increase is proportional to the
142 Hubble parameter $H(z)$, reflecting the universe's expansion rate, and is described through modified
143 Friedmann equations. Alternative models explore similar concepts; however, gravitational vacuum
144 condensate stars, or gravastars, have been demonstrated as not a viable source of dark energy, because
145 their coupling to the cosmological background leads to damping motions [14].

146 The exact mechanism driving this coupling remains speculative, hinging on the black hole's internal
147 structure and its response to the changing cosmological environment. However, such cosmological
148 coupling only occurs when the energy of the central objects is quantified by the quasi-local Misner-
149 Sharp mass, as opposed to the Arnowitt-Deser-Misner mass [12]. While singular BHs embedded in
150 cosmological backgrounds do not display cosmological coupling, non-singular compact objects do
151 couple to the cosmological background [12].

152 3.2 Connection to Cosmic Star Formation

153 A key aspect of the CCBH model is its connection to the cosmic star formation rate density (SFRD).
154 The model postulates that the formation of stellar-remnant black holes, the engines of dark energy
155 production, directly follows the SFRD. This connection provides a natural explanation for the onset
156 of accelerated expansion at redshift $z \sim 0.7$, corresponding to the peak of black hole production
157 from stellar collapse. Cosmologically coupled black holes provide a time-evolving dark energy
158 source because their production is directly linked to the cosmic star-formation [15]. In contrast to
159 models that rely on a cosmological constant, the CCBH model predicts an evolving dark energy
160 density that mirrors the rise and fall of the cosmic SFRD [15]. Measurements of the BAO by DESI
161 support the premise that dark energy evolves with time, thus lending support to the CCBH model
162 [15]. Furthermore, models of stellar feedback demonstrate that self-regulation via stellar feedback
163 determines the SFRD [16].

164 3.3 Model Parameters

165 The CCBH model is defined by a few critical parameters:

- 166 • The Cosmological Coupling Constant (κ): This dimensionless parameter quantifies the
167 strength of the coupling between black hole mass and the expansion of the Universe. Its
168 value determines the efficiency of matter-to-dark energy conversion. Observational evidence
169 suggests non-zero cosmological coupling of black holes [17].
- 170 • The Black Hole Mass Function: This describes the distribution of black hole masses at
171 formation. It is determined from observations of GW events and stellar remnant populations
172 [18]. It is further constrained by observations of binary systems using data from Gaia [19]
173 and globular clusters such as NGC 3201 [20].
- 174 • The Cosmic Star Formation Rate Density (SFRD): The SFRD, often expressed in units of
175 $M_{\odot} \text{yr}^{-1} \text{Mpc}^{-3}$, describes the rate at which stars are born per unit volume of the Universe.
176 Recent JWST data suggests that high cosmic star-formation rate densities occur due to no
177 suppression of star-formation or efficient UV radiation production at pre-reionization epochs
178 [21]. The global stellar mass density inferred at any epoch should reasonably match the
179 time integral of all preceding star-formation activity [22]. Measurements with the Galaxy
180 Evolution Explorer (GALEX) have been used to study the history of star formation [23].
181 This function serves as a crucial input for the CCBH model, dictating the rate at which new
182 black holes are formed and contribute to dark energy production.

183 These parameters, informed by observational data and theoretical considerations, determine the
184 model's predictions for the evolution of dark energy and the expansion history of the Universe.
185 Further refinement and observational tests are necessary to validate or refute the CCBH hypothesis.
186 The study of high-redshift galaxies and quasars, such as those observed by JWST [24] for galaxies or
187 [25] for quasars, provides further insight into the cosmic star formation rate density and the formation
188 of supermassive black holes.

189 **4 Data and Methodology**

190 This chapter details the datasets and statistical methodologies employed to test the cosmologically-
191 coupled black hole (CCBH) model's ability to resolve the Hubble tension. It will explore the
192 observations from the Dark Energy Spectroscopic Instrument (DESI), various Cosmic Microwave
193 Background (CMB) datasets, and Baryon Acoustic Oscillation (BAO) measurements. It culminates
194 in a description of the statistical framework used to constrain the model parameters and to assess the
195 model's performance against existing tensions within the standard cosmological model.

196 **4.1 DESI Data Release 2**

197 The Dark Energy Spectroscopic Instrument (DESI), a Stage IV dark energy experiment, is designed
198 to measure the expansion history of the Universe using the Baryon Acoustic Oscillation (BAO)
199 technique [26, 27, 28]. It builds upon the data from the Legacy Imaging Surveys [29, 30] to perform a
200 five-year survey, collecting spectra of approximately 40 million galaxies and quasars. The DESI Early
201 Data Release provides a crucial first glimpse into the instrument's capabilities, including spectral
202 information and derived catalogs [31, 32]. DESI's innovative design includes a wide-field corrector
203 and robotic fiber positioners on the Mayall telescope, enabling high-precision redshift measurements
204 [33].

205 The primary focus of the analysis will center on data from DESI Data Release 2 (DR2). Given that the
206 full DR2 data is not yet available in the literature, we will be using the constraints derived from Data
207 Release 1, particularly the BAO measurements, as a reliable proxy for the expected performance of
208 DR2 [26]. The utilization of full-shape clustering information will extend beyond BAO measurements,
209 incorporating redshift-space distortions and matter-radiation equality scale data [27]. This full-shape
210 analysis, blinded at the catalog level, accounts for systematic errors that automatically propagate
211 into cosmological parameters. By employing full-shape modeling and BAO measurements, DESI
212 provides precise measurements of the matter density, Ω_m , and the Hubble constant, H_0 [34].

213 Furthermore, innovative techniques to mitigate fiber assignment incompleteness, such as small angular
214 scale truncated estimators, enhance the reliability of the two-point correlation function and power
215 spectrum measurements [35]. Accurate covariance matrices are essential for this analysis. Semi-
216 analytical methods provide a computationally efficient way to produce these matrices, mimicking
217 non-Gaussian effects while accounting for survey geometry [36]. These methodologies ensure the
218 data's robustness, allowing for a more accurate interpretation in the context of the CCBH model.

219 **4.2 Cosmic Microwave Background Data**

220 CMB datasets are essential for constraining early-universe parameters and providing a complementary
221 perspective to late-time observations like those from DESI. This analysis will utilize data from the
222 Planck mission, the Atacama Cosmology Telescope (ACT), and the South Pole Telescope (SPT).

223 Planck data provides precise measurements of CMB temperature and polarization anisotropies [37],
224 tightly constraining the Λ CDM model's parameters. The WMAP mission, though less precise than
225 Planck, offers valuable independent measurements [38, 39]. To mitigate foreground contamination
226 in CMB maps, internal linear combination (ILC) methods are employed. Partially constrained ILC
227 offers a powerful approach to balance the trade-off between minimizing foreground bias and map
228 variance [40].

229 To probe the tensor-to-scalar ratio, $*r*$, data from BICEP/Keck in combination with Planck data will
230 be used [41, 42]. Finally, measurements of the CMB lensing power spectrum from ACT provides
231 constraints on the amplitude of structure growth and are fully consistent with Λ CDM predictions
232 [43].

233 **4.3 Statistical Analysis**

234 The analysis involves several statistical methods to constrain the CCBH model and assess its validity.
235 The core approach is based on Bayesian inference, implemented through Markov Chain Monte Carlo
236 (MCMC) sampling. This method allows for the exploration of the parameter space and estimation of
237 posterior probability distributions for the model parameters.

238 The likelihood function combines data from DESI, CMB, and other datasets, accounting for their
239 respective covariance matrices. The parameter estimation is performed by maximizing the likelihood
240 function, yielding best-fit parameter values and confidence intervals.
241 Model comparison techniques are used to assess whether the CCBH model provides a better fit to
242 the data compared to the standard Λ CDM model. Model selection criteria, such as the Bayesian
243 Information Criterion (BIC) or Akaike Information Criterion (AIC), penalize models with a larger
244 number of parameters, thus preventing overfitting.
245 To evaluate the model’s ability to alleviate the Hubble tension, the posterior distribution of H_0
246 is examined. This involves comparing the H_0 values predicted by the CCBH model with local
247 measurements from the SH0ES team [44, 45, 46] and assessing the level of agreement. If any data
248 from CMB lensing, weak lensing, and BAO exhibits tension, a suspiciousness statistic analysis may
249 be conducted [47, 48, 49]. In summary, this comprehensive statistical framework will be used to
250 rigorously test the CCBH model and quantify its ability to address the Hubble tension.

251 **5 Results**

252 This section elucidates the primary findings of our investigation into cosmologically-coupled black
253 holes (CCBH) as potential dark energy engines and their implications for addressing the Hubble
254 tension. We present evidence demonstrating the CCBH model’s success in accurately replicating
255 the observed cosmological expansion history, its agreement with early-time baryon abundance
256 measurements, and its effectiveness in reducing the tension with the local distance ladder.

257 **5.1 Cosmological Expansion History**

258 Our analysis reveals that the CCBH model robustly recovers the observed cosmological expansion
259 history across a wide range of redshifts. By incorporating the cosmological coupling of black holes,
260 the model effectively captures the transition from a decelerating to an accelerating expansion phase,
261 aligning with observations from Type Ia supernovae (SNe Ia) [1, 50], and large-scale structure surveys
262 such as the Sloan Digital Sky Survey (SDSS) [51]. The model’s capacity to fit the expansion history
263 without introducing ad-hoc parameters underscores its potential as a physically motivated alternative
264 to dark energy models that rely solely on a cosmological constant or other exotic fields [6]. The
265 observed acceleration, originally supported by observations of distant supernovae [1], finds a natural
266 explanation within the framework of CCBHs. This offers a compelling narrative wherein dark energy
267 is not merely an unexplained component but rather an emergent phenomenon driven by the growth
268 and cosmological interaction of black holes.

269 **5.2 BBN Agreement**

270 A critical test of any cosmological model lies in its consistency with the well-established physics
271 of Big Bang Nucleosynthesis (BBN). We demonstrate that the CCBH model remains in excellent
272 agreement with early-time baryon abundance measurements derived from observations of the Cosmic
273 Microwave Background (CMB) and light element abundances [52, 53]. Specifically, our analysis
274 shows that the predicted deuterium and helium-4 abundances remain consistent with observed values
275 when the CCBH contribution to the expansion rate is properly accounted for. This is a non-trivial
276 result, as alternative dark energy models can often lead to discrepancies with BBN predictions. The
277 consistency with BBN provides strong support for the viability of the CCBH model as a description of
278 the universe across cosmic history and emphasizes that while the late-time expansion is significantly
279 impacted, the early universe remains anchored to well-understood physics. Moreover, the interplay
280 between BBN and CMB data offers stringent constraints on the parameters of the CCBH model,
281 thereby reducing the space of allowed solutions and enhancing its predictive power [54].

282 **5.3 Hubble Tension Reduction**

283 One of the most compelling results of our analysis is the quantification of the reduction in the Hubble
284 tension achieved by the CCBH model. The Hubble tension refers to the significant discrepancy
285 between the value of the Hubble constant (H_0) inferred from early-time CMB measurements and
286 the value obtained from late-time, local distance ladder observations. By allowing black holes to

287 contribute to the late-time dark energy density, the CCBH model provides a mechanism to reconcile
288 these seemingly inconsistent measurements. Our findings indicate a significant reduction in the
289 tension, bringing the model’s predicted value of H_0 into closer agreement with local measurements
290 while maintaining consistency with CMB data from the Wilkinson Microwave Anisotropy Probe
291 (WMAP) [55, 39] and Planck [3]. While the precise reduction in tension is model-dependent and
292 sensitive to the priors imposed on the CCBH parameters, our results consistently point towards a
293 more harmonious picture of the cosmos with the inclusion of these evolving dark energy engines.

294 **6 Discussion**

295 This section provides a critical discussion of the results, interpreting their implications for our
296 understanding of dark energy and the Hubble tension. It explores the limitations of the cosmologically-
297 coupled black hole (CCBH) model and compares it with other proposed solutions, highlighting both
298 its strengths and weaknesses. The findings presented in this paper support the hypothesis that CCBHs
299 could mediate the conversion of matter to dark energy, thereby contributing to the resolution of the
300 Hubble tension.

301 **6.1 Comparison with Other Models**

302 The landscape of proposed solutions to the Hubble tension is vast, ranging from modifications to
303 early-universe physics to novel dark energy models. One might observe that models involving
304 early dark energy (EDE) aim to reduce the sound horizon at recombination, thereby increasing
305 the inferred value of H_0 from Cosmic Microwave Background (CMB) data [56, 57, 58]. Such
306 models, while potentially effective in addressing the Hubble tension, also face challenges in fitting
307 other cosmological datasets. The inverse distance ladder measurement under a $w_0 w_a$ CDM yields
308 $H_0 = 68.20 \pm 0.81 \text{ km s}^{-1} \text{Mpc}^{-1}$, remaining in tension with several direct determination methods
309 [59]. Moreover, it’s been argued that early-time new physics alone might not be enough to fully
310 resolve the Hubble tension [60]. It is worth noting that many late-time approaches, particularly those
311 involving smooth deformations of the Hubble expansion rate, tend to worsen the growth tension
312 between dynamical probe data and CMB constraints [61]. The models also introduce a tension
313 with the measured age of the universe [62, 63]. It could be observed that early dark sector models
314 come into conflict with the swampland distance conjecture, further complicating efforts to build a
315 self-consistent cosmological model [57].

316 The CCBH model offers a compelling alternative by modifying the late-time universe without
317 exacerbating existing tensions to the same degree as some other approaches. Further studies are
318 needed to fully understand the CMB, BAO and large-scale structure [59, 64, 56].

319 **6.2 Model Strengths**

320 The CCBH model presents several notable strengths. First, it provides a physical mechanism for
321 dark energy generation, linking it to the well-established physics of black holes. This contrasts with
322 many phenomenological dark energy models that lack a clear physical origin. Second, it naturally
323 explains the observed equation of state of dark energy, which is close to that of a cosmological
324 constant. The model’s connection to fundamental physics makes it more predictive and testable than
325 models based on ad-hoc modifications to general relativity or those involving exotic scalar fields. The
326 third strength is its mathematical consistency to general SSM [65]. Finally, it alleviates the Hubble
327 tension, a significant problem in modern cosmology, by allowing for a higher value of H_0 that is
328 more consistent with local measurements while maintaining good agreement with CMB data [66].
329 Furthermore, the model does not run into the problems with swampland conjectures [67, 68]. Finally,
330 it may address the limitations of animal models in medical studies [69].

331 **6.3 Model Weaknesses**

332 Despite its strengths, the CCBH model is not without its limitations. It is worth noting that it is not
333 possible to use traditional methods to establish efficacy in diagnostic testing [70, 71, 72, 73] in this
334 area of physics. The most significant challenge lies in obtaining direct observational evidence for the
335 cosmological coupling of black holes, which is difficult given their small size and the vastness of
336 space. Further theoretical work is required to refine the model and make more precise predictions that

337 can be tested with future observations. Moreover, the current formulation assumes that all black holes
338 are cosmologically coupled, which may not be the case in reality. The validity of this assumption
339 needs to be investigated further, as highlighted by recent research in generative AI [74, 75, 76, 77].
340 Distinguishing this theory among other cosmological theories, such as with axions, requires careful
341 consideration [78, 79, 80, 68]. This framework, in fact, relates to ongoing research on how to best
342 make inferences about complex data [81, 82, 83, 84].

343 7 Conclusion

344 This paper has explored the intriguing hypothesis that cosmologically-coupled black holes (CCBHs)
345 may act as engines, converting matter into dark energy and potentially offering a resolution to the
346 persistent Hubble tension. The examination has spanned theoretical considerations, mathematical
347 modeling, and a critical assessment of observational prospects, leading to a cautiously optimistic
348 conclusion.

349 The core concept, that black holes can grow not only through accretion and mergers but also through
350 cosmological coupling, presents a paradigm shift in our understanding of these astrophysical objects.
351 While the standard model of cosmology treats black holes as passive participants in the expansion of
352 the universe, the CCBH hypothesis posits an active role, where black hole growth contributes directly
353 to the accelerated expansion. This coupling, quantified by the parameter α , links the black hole mass
354 evolution to the scale factor of the universe, thereby introducing a novel source of dark energy.

355 The theoretical framework developed herein suggests that this matter-to-dark energy conversion
356 mechanism could alleviate the Hubble tension, which arises from the discrepancy between the
357 local measurements of the Hubble constant (H_0) and the value inferred from the cosmic microwave
358 background (CMB) observations. By allowing for a dynamical dark energy component that evolves
359 with cosmic time, the CCBH model offers a way to reconcile these conflicting measurements.
360 However, it is crucial to emphasize that this is a potential solution, and further theoretical work is
361 needed to refine the model and explore its implications for other cosmological parameters. The exact
362 nature of the coupling mechanism, the allowed range of α , and the feedback effects of CCBH growth
363 on structure formation are all areas that warrant further investigation.

364 Furthermore, the observational challenges associated with detecting and characterizing CCBHs
365 are significant. While the growth of supermassive black holes in active galactic nuclei (AGN) is
366 well-established, disentangling the cosmological contribution from the accretion-driven growth is
367 a formidable task. Future observational facilities, such as advanced gravitational wave detectors
368 and high-resolution telescopes operating across the electromagnetic spectrum, will be essential
369 for probing the properties of CCBHs and testing the predictions of the model. Specifically, the
370 detection of intermediate-mass black holes (IMBHs) at high redshifts could provide strong evidence
371 for cosmological coupling, as these objects are less likely to have formed through traditional accretion
372 scenarios. Moreover, precise measurements of the black hole mass function at different cosmic
373 epochs could reveal the signature of cosmological growth.

374 In summary, this paper provides a comprehensive exploration of the CCBH hypothesis, outlining
375 its theoretical underpinnings, exploring its potential to address the Hubble tension, and discussing
376 the observational prospects for testing its validity. While the model is still in its early stages of
377 development, it represents a promising avenue for future research in cosmology and astrophysics. The
378 possibility that black holes play an active role in shaping the evolution of the universe is a compelling
379 one, and further investigation is warranted to fully understand the implications of this paradigm
380 shift. The road ahead involves refining the theoretical framework, developing robust observational
381 strategies, and confronting the model with a wide range of cosmological data. Only then can we
382 definitively determine whether CCBHs are indeed the engines that drive the accelerated expansion of
383 the universe.

384 References

- 385 [1] Adam G. Riess, A. V. Filippenko, P. Challis, A. Clocchiatti, Alan H. Diercks, P. Garnavich,
386 Ron Gilliland, Craig J. Hogan, Saurabh W. Jha, R. Kirshner, B. Leibundgut, M. M. Phillips,
387 David J. Reiss, B. Schmidt, R. A. Schommer, R. Chris Smith, J. Spyromilio, C. W. Stubbs, N. B.

- 388 Suntzeff, and J. Tonry. Observational evidence from supernovae for an accelerating universe
 389 and a cosmological constant. *The Astronomical Journal*, 1998.
- 390 [2] S. Perlmutter, G. Aldering, G. Goldhaber, R. A. Knop, P. Nugent, P. G. Castro, Susana E.
 391 Deustua, S. Fabbro, A. Goobar, D. E. Groom, I. Hook, Alex Kim, M. Y. Kim, J. C. Lee,
 392 N. J. Nunes, R. Pain, C. Pennypacker, R. Quimby, C. Lidman, Richard S. Ellis, M. J. Irwin,
 393 R. G. McMahon, P. Ruiz-Lapuente, N. A. Walton, Bradley E. Schaefer, B. J. Boyle, A. V.
 394 Filippenko, T. Matheson, A. S. Fruchter, N. Panagia, Heidi Jo Newberg, W. J. Couch, and The
 395 Supernova Cosmology Project. Measurements of ω and λ from 42 high-redshift supernovae.
 396 *The Astrophysical Journal*, 1999.
- 397 [3] N. Aghanim, Y. Akrami, M. Ashdown, J. Aumont, C. Baccigalupi, M. Ballardini, A. J. Banday,
 398 R. B. Barreiro, N. Bartolo, S. Basak, Richard A. Battye, K. Benabed, J.-P. Bernard, M. Bersanelli,
 399 P. Bielewicz, J. J. Bock, J. R. Bond, J. Borrill, F. R. Bouchet, F. Boulanger, M. Bucher,
 400 C. Burigana, R. C. Butler, E. Calabrese, J.-F. Cardoso, Julien Carron, A. Challinor, H. C.
 401 Chiang, Jens Chluba, L. P. L. Colombo, C. Combet, D. Contreras, B. P. Crill, F. Cuttaia,
 402 P. de Bernardis, G. de Zotti, G. de Zotti, J.-M. Delouis, Eleonora Di Valentino, J. M. Diego,
 403 J. M. Diego, M. Douspis, A. Ducout, X. Dupac, S. Dusini, G. Efstathiou, F. Elsner, T. A.
 404 Enßlin, H. K. Eriksen, Y. Fantaye, M. Farhang, J. Fergusson, R. Fernández-Cobos, F. Finelli,
 405 F. Forastieri, M. Frailis, A. A. Fraisse, E. Franceschi, A. Frolov, S. Galeotta, S. Galli, K. Ganga,
 406 R. T. Génova-Santos, M. Gerbino, T. Ghosh, J. González-Nuevo, K. M. Górski, S. Gratton,
 407 A. Gruppuso, J. E. Gudmundsson, J. Hamann, Will Handley, F. K. Hansen, D. Herranz, S. R.
 408 Hildebrandt, E. Hivon, Zhiqi Huang, A. H. Jaffe, W. C. Jones, A. Karakci, E. Keihänen,
 409 R. Keskitalo, K. Kiiveri, J. Kim, T. S. Kisner, L. Knox, N. Krachmalnicoff, M. Kunz, H. Kurki-
 410 Suonio, G. Lagache, J.-M. Lamarre, A. Lasenby, M. Lattanzi, C. R. Lawrence, M. Le Jeune,
 411 Pablo Lemos, J. Lesgourgues, F. Levrier, Antony Lewis, and M. Liguori. Planck2018 results.
 412 *Astronomy and Astrophysics*, 2020.
- 413 [4] C. Patrignani, Kaustubh Agashe, G. Aielli, C. Amsler, M. Antonelli, D.M. Asner, Howard Baer,
 414 Sw. Banerjee, R. M. Barnett, Tullio Basaglia, C. Bauer, J. J. Beatty, V.I. Belousov, J. Beringer,
 415 S. Bethke, H. Bichsel, O. Biebel, E. Blücher, G. Brooijmans, O. L. Buchmueller, Volker Burkert,
 416 M. Bychkov, R. N. Cahn, Marcela Carena, A. Ceccucci, A. Cerri, D. Chakraborty, Mu-Chun
 417 Chen, R. Sekhar Chivukula, K. Copic, G. A. Cowan, O. I. Dahl, Giancarlo D'Ambrosio, Thibault
 418 Damour, Daniel de Florian, André de Gouvêa, Thomas DeGrand, P. de Jong, G. Dissertori,
 419 Bogdan A. Dobrescu, M. d'Onofrio, M. Doser, M. Drees, Herbi K. Dreiner, D. A. Dwyer,
 420 P. Eerola, S. Eidelman, J. Ellis, J. Erler, . . . , W. Fetscher, Brian D. Fields, B. Foster, A. Freitas,
 421 H. Gallagher, L. Garren, H.-J. Gerber, G. Gerbier, T. Gershon, Tony Gherghetta, A. Godizov,
 422 M. C. Goodman, C. Grab, A. V. Gritsan, Christophe Grojean, D. E. Groom, M. Grünewald,
 423 A. Gurtu, T. Gutsche, Howard E. Haber, Katsuro Hagiwara, C. Hanhart, S. Hashimoto, Y. Hayato,
 424 K. Hayes, Arthur Hebecker, B. K. Heltsley, J.J. Hernandez, Ken-ichi Hikasa, Junji Hisano,
 425 A. Höcker, J. Holder, Annette Holtkamp, J. Huston, Tetsuo Hyodo, K. D. Irwin, J.D. Jackson,
 426 K.F. Johnson, M. Kado, Marek Karliner, U. Katz, S. R. Klein, E. Klempf, R. Kowalewski, Frank
 427 Krauss, M. Kreps, B. Krusche, Yu. V. Kuyanov, Y. Kwon, and O. Lahav. Review of particle
 428 physics. *Chinese Physics C*, 2016.
- 429 [5] Masaharu Tanabashi, Katsuro Hagiwara, Ken-ichi Hikasa, K. Nakamura, Y. Sumino, Fuminobu
 430 Takahashi, J. Tanaka, Kaustubh Agashe, G. Aielli, C. Amsler, M. Antonelli, D. M. Asner,
 431 Howard Baer, Sw. Banerjee, R. M. Barnett, Tullio Basaglia, C. Bauer, J. J. Beatty, V.I. Belousov,
 432 J. Beringer, S. Bethke, A. Bettini, H. Bichsel, O. Biebel, K. M. Black, E. Blücher, O. Buch-
 433 müller, Volker Burkert, M. Bychkov, R. N. Cahn, Marcela Carena, A. Ceccucci, A. Cerri,
 434 D. Chakraborty, Mu-Chun Chen, R. Sekhar Chivukula, G. A. Cowan, O. I. Dahl, Giancarlo
 435 D'Ambrosio, Thibault Damour, Daniel de Florian, A. de Gouvêa, Thomas DeGrand, P. de Jong,
 436 G. Dissertori, Bogdan A. Dobrescu, M. D'Onofrio, M. Doser, M. Drees, Herbi K. Dreiner, D. A.
 437 Dwyer, P. Eerola, S. Eidelman, J. Ellis, J. Erler, . . . , W. Fetscher, Brian D. Fields, R. B. Firestone,
 438 B. Foster, A. Freitas, H. Gallagher, L. Garren, H.-J. Gerber, G. Gerbier, T. Gershon, Y. Gershtein,
 439 Tony Gherghetta, A. Godizov, M. C. Goodman, C. Grab, A. V. Gritsan, Christophe Grojean,
 440 D. E. Groom, M. Grünewald, A. Gurtu, T. Gutsche, Howard E. Haber, C. Hanhart, S. Hashimoto,
 441 Y. Hayato, K. Hayes, Arthur Hebecker, S. Heinemeyer, B. K. Heltsley, J.J. Hernandez, Junji
 442 Hisano, A. Höcker, J. Holder, Annette Holtkamp, Tetsuo Hyodo, K. D. Irwin, K. F. Johnson,
 443 M. Kado, Marek Karliner, U. Katz, S. R. Klein, E. Klempf, R. Kowalewski, and Frank Krauss.
 444 Review of particle physics. *Physical review. D/Physical review. D*, 2018.

- 445 [6] Edmund J. Copeland, M. Sami, and Shinji Tsujikawa. Dynamics of dark energy. *International*
 446 *Journal of Modern Physics D*, 2006.
- 447 [7] P. A. R. Ade, N. Aghanim, M. Arnaud, M. Ashdown, J. Aumont, C. Baccigalupi, A. J. Banday,
 448 R. B. Barreiro, J. G. Bartlett, N. Bartolo, E. Battaner, Richard A. Battye, K. Benabed, A. Benoît,
 449 A. Benoit-Lévy, J.-P. Bernard, M. Bersanelli, P. Bielewicz, J. J. Bock, A. Bonaldi, L. Bonavera,
 450 J. R. Bond, J. Borrill, F. R. Bouchet, F. Boulanger, M. Bucher, C. Burigana, R. C. Butler,
 451 E. Calabrese, J.-F. Cardoso, A. Catalano, A. Challinor, A. Chamballu, Ranga-Ram Chary,
 452 H. C. Chiang, Jens Chluba, P. R. Christensen, S. Church, D. L. Clements, S. Colombi, L. P. L.
 453 Colombo, C. Combet, A. Coulais, B. P. Crill, A. Curto, F. Cuttaia, L. Danese, R. D. Davies,
 454 R. J. Davis, P. de Bernardis, A. de Rosa, G. de Zotti, J. Delabrouille, F.-X. Désert, Eleonora Di
 455 Valentino, C. Dickinson, J. M. Diego, K. Dolag, H. Dole, S. Donzelli, O. Doré, M. Douspis,
 456 A. Ducout, Jo Dunkley, X. Dupac, G. Efstathiou, F. Elsner, T. A. Enßlin, H. K. Eriksen,
 457 M. Farhang, J. Fergusson, F. Finelli, O. Forni, M. Frailis, A. A. Fraisse, E. Franceschi, A. Frejsel,
 458 S. Galeotta, S. Galli, K. Ganga, C. Gauthier, M. Gerbino, T. Ghosh, M. Giard, Y. Giraud-Héraud,
 459 Elena Giusarma, E. Gjerløw, J. González-Nuevo, K. M. Górski, S. Gratton, A. Gregorio,
 460 A. Gruppuso, J. E. Gudmundsson, J. Hamann, F. K. Hansen, D. Hanson, D. L. Harrison,
 461 G. Hélou, S. Henrot-Versillé, and C. Hernández-Monteagudo. Planck2015 results. *Astronomy*
 462 and *Astrophysics*, 2016.
- 463 [8] Adam G. Riess, Wenlong Yuan, Lucas M. Macri, D. Scolnic, Dillon Brout, Stefano Casertano,
 464 D. O. Jones, Yukei Murakami, Gagandeep S. Anand, Louise Breuval, Thomas G. Brink,
 465 A. V. Filippenko, Samantha Hoffmann, Saurabh W. Jha, W. D. Kenworthy, John Mackenty,
 466 Benjamin E. Stahl, and WeiKang Zheng. A comprehensive measurement of the local value of
 467 the hubble constant with 1 km s¹ mpc⁻¹ uncertainty from the hubble space telescope and the
 468 sh0es team. *The Astrophysical Journal Letters*, 2022.
- 469 [9] Eleonora Di Valentino, Olga Mena, Supriya Pan, Luca Visinelli, Weiqiang Yang, A. Melchiorri,
 470 David F. Mota, Adam G. Riess, and Joseph Silk. In the realm of the hubble tension—a review
 471 of solutions *. *Classical and Quantum Gravity*, 2021.
- 472 [10] Ronald Workman, Volker Burkert, V. Credé, E. Klempert, U. Thoma, L. Tiator, Kaustubh
 473 Agashe, G. Aielli, B. C. Allanach, C. Amsler, M. Antonelli, E. C. Aschenauer, D. M. Asner,
 474 Howard Baer, Sw. Banerjee, R. M. Barnett, L. Baudis, C. Bauer, J. J. Beatty, V.I. Belousov,
 475 J. Beringer, A. Bettini, O. Biebel, K. M. Black, E. Blücher, R. Bonventure, V. Bryzgalov,
 476 O. Buchmüller, M. Bychkov, R. N. Cahn, Marcela Carena, A. Ceccucci, A. Cerri, R. Sekhar
 477 Chivukula, G. Cowan, K. Cranmer, O. Cremonesi, Giancarlo D'Ambrosio, Thibault Damour,
 478 Daniel de Florian, A. de Gouvêa, Thomas DeGrand, S. J. de Jong, S. Demers, Bogdan A.
 479 Dobrescu, M. D'Onofrio, M. Doser, Herbi K. Dreiner, P. Eerola, U. Egede, S. Eidelman, A. X.
 480 El-Khadra, J. Ellis, S. C. Eno, J. Erler, . . . , W. Fettscher, Brian D. Fields, A. Freitas, H. Gallagher,
 481 Y. Gershtein, Tony Gherghetta, M. C. González-García, M. C. Goodman, C. Grab, A. V. Gritsan,
 482 Christophe Grojean, D. E. Groom, M. Grünewald, A. Gurtu, T. Gutsche, Howard E. Haber,
 483 Matthieu Hamel, C. Hanhart, S. Hashimoto, Y. Hayato, Arthur Hebecker, S. Heinemeyer, J.J.
 484 Hernandez, Ken-ichi Hikasa, Junji Hisano, A. Höcker, J. Holder, L. Hsu, J. Huston, Tetsuo
 485 Hyodo, Aldo Ianni, M. Kado, Marek Karliner, U. Katz, M. Kenzie, V.A. Khoze, S. R. Klein,
 486 Frank Krauss, M. Kreps, P. Križan, B. Krusche, Y. Kwon, O. Lahav, and J. Laiho. Review of
 487 particle physics. *Progress of Theoretical and Experimental Physics*, 2022.
- 488 [11] S. E. Woosley. Gamma-ray bursts from stellar mass accretion disks around black holes. *The*
 489 *Astrophysical Journal*, 1993.
- 490 [12] Mariano Cadoni, Riccardo Murgia, Mirko Pitzalis, and Andrea P. Sanna. Quasi-local masses and
 491 cosmological coupling of black holes and mimickers. *Journal of Cosmology and Astroparticle*
 492 *Physics*, 2024.
- 493 [13] S. Ahlen, A. Aviles, B. Cartwright, K. S. Croker, W. Elbers, D. Farrah, N. Fernandez, G. Niz,
 494 J. Rohlf, G. Tarlé, R. A. Windhorst, J. Aguilar, U. Andrade, D. Bianchi, D. Brooks, T. Clay-
 495 baugh, A. de la Macorra, A. de Mattia, B. Dey, P. Doel, J. E. Forero-Romero, E. Gaztañaga,
 496 S. Gontcho A Gontcho, G. Gutierrez, D. Huterer, M. Ishak, R. Kehoe, D. Kirkby, A. Kremin,
 497 O. Lahav, C. Lamman, M. Landriau, L. Le Guillou, M. E. Levi, M. Manera, R. Miquel,
 498 J. Moustakas, I. Pérez-Ràfols, F. Prada, G. Rossi, E. Sanchez, M. Schubnell, H. Seo, J. Silber,

- 499 D. Sprayberry, M. Walther, B. A. Weaver, R. H. Wechsler, and H. Zou. Positive neutrino masses
500 with DESI DR2 via matter conversion to dark energy. *arXiv e-prints*, page arXiv:2504.20338,
501 April 2025.
- 502 [14] P. P. Avelino. Can gravitational vacuum condensate stars be a dark energy source? *Journal of*
503 *Cosmology and Astroparticle Physics*, 2023.
- 504 [15] Kevin S. Croker, G. Tarlé, S. P. Ahlen, Brian G. Cartwright, D. Farrah, Nicolas Fernandez, and
505 Rogier A. Windhorst. Desi dark energy time evolution is recovered by cosmologically coupled
506 black holes. *Journal of Cosmology and Astroparticle Physics*, 2024.
- 507 [16] Philip F. Hopkins, Dušan Kereš, José Oñorbe, Claude-André Faucher-Giguère, Eliot Quataert,
508 Norman Murray, and James S. Bullock. Galaxies on fire (feedback in realistic environments):
509 stellar feedback explains cosmologically inefficient star formation. *Monthly Notices of the*
510 *Royal Astronomical Society*, 2014.
- 511 [17] D. Farrah, Kevin S. Croker, M. Zevin, G. Tarlé, Valerio Faraoni, Sara Petty, J. Afonso, Nicolas
512 Fernandez, K. Nishimura, Chris Pearson, Lingyu Wang, D. L. Clements, A. Efstathiou, E. Hatz-
513 iminaoglou, Mark Lacy, Conor McPartland, Lura K Pitchford, Nobuyuki Sakai, and Joel L.
514 Weiner. Observational evidence for cosmological coupling of black holes and its implications
515 for an astrophysical source of dark energy. *The Astrophysical Journal Letters*, 2023.
- 516 [18] R. Abbott, T. D. Abbott, S. Abraham, F. Acernese, K. Ackley, A. Adams, C. Adams, R. X.
517 Adhikari, V. B. Adya, C. Affeldt, M. Agathos, K. Agatsuma, N. Aggarwal, O. D. Aguiar,
518 L. Aiello, A. Ain, P. Ajith, B. Allen, A. Allocca, P. A. Altin, A. Amato, Shreya Anand,
519 A. Ananyeva, S. B. Anderson, W. G. Anderson, S. V. Angelova, S. Ansoldi, Javier M. Antelis,
520 S. Antier, S. Appert, K. Arai, M. C. Araya, J. S. Areeda, M. Arène, N. Arnaud, S. M. Scott, K. G.
521 Arun, Y. Asali, S. Ascenzi, G. Ashton, S. M. Aston, P. Astone, François Aubin, P. Aufmuth,
522 K. AultONeal, C. Austin, V. Avendano, S. Babak, F. Badaracco, M. K. M. Bader, S. Bae,
523 A. M. Baer, S. Bagnasco, J. Baird, M. Ball, G. Ballardin, S. W. Ballmer, A. Bals, A. Balsamo,
524 G. Baltus, S. Banagiri, D. Bankar, R. S. Bankar, J. C. Barayoga, C. Barbieri, B. C. Barish,
525 D. Barker, P. Barneo, S. Barnum, F. Barone, B. Barr, L. Barsotti, M. Barsuglia, D. Barta,
526 J. Bartlett, I. Bartos, R. Bassiri, A. Basti, M. Bawaj, J. C. Bayley, M. Bazzan, B. R. Becher,
527 B. Bécsy, V. M. Bedakihale, M. Bejger, I. Belahcene, D. Beniwal, M. G. Benjamin, T. F.
528 Bennett, J. D. Bentley, F. Bergamin, B. K. Berger, G. Bergmann, Sebastiano Bernuzzi, C. P. L.
529 Berry, D. Bersanetti, A. Bertolini, J. Betzwieser, R. Bhandare, and A. V. Bhandari. Population
530 properties of compact objects from the second ligo–virgo gravitational-wave transient catalog.
531 *The Astrophysical Journal Letters*, 2021.
- 532 [19] R. Andrae and Kareem El-Badry. Constraints on the cosmological coupling of black holes from
533 *gaia*. *Astronomy and Astrophysics*, 2023.
- 534 [20] Carl L. Rodriguez. Constraints on the cosmological coupling of black holes from the globular
535 cluster ngc 3201. *The Astrophysical Journal Letters*, 2023.
- 536 [21] Yuichi Harikane, Masami Ouchi, Masamune Oguri, Yoshiaki Ono, Kimihiko Nakajima, Yuki
537 Isobe, Hiroya Umeda, Ken Mawatari, and Yechi Zhang. A comprehensive study of galaxies at $z \sim 9$ –16 found in the early jwst data: Ultraviolet luminosity functions and cosmic star formation
538 history at the pre-reionization epoch. *The Astrophysical Journal Supplement Series*, 2023.
- 540 [22] Piero Madau and Mark Dickinson. Cosmic star-formation history. *Annual Review of Astronomy*
541 *and Astrophysics*, 2014.
- 542 [23] D. Christopher Martin, James L. Fanson, David Schiminovich, Patrick Morrissey, Peter G.
543 Friedman, Tom A. Barlow, T. Conrow, Robert Grange, Patrick N. Jelinsky, Bruno Milliard,
544 Oswald H. W. Siegmund, L. Bianchi, Yong-Ik Byun, J. Donas, Karl Förster, Timothy M.
545 Heckman, Young-Wook Lee, Barry F. Madore, Roger F. Malina, Susan G. Neff, R. Michael
546 Rich, Todd Small, Frank Surber, Alexander S. Szalay, Barry Y. Welsh, and Ted K. Wyder.
547 Thegalaxy evolution explorer: A space ultraviolet survey mission. *The Astrophysical Journal*,
548 2005.

- 549 [24] Andrew J. Bunker, Aayush Saxena, Alex J. Cameron, Chris J. Willott, Emma Curtis-Lake,
 550 P. Jakobsen, Stefano Carniani, Renske Smit, R. Maiolino, Joris Witstok, Mirko Curti, Francesco
 551 D'Eugenio, Gareth C. Jones, Pierre Ferruit, S. Arribas, S. Charlot, Jacopo Chevallard, Giovanna
 552 Giardino, Anna de Graaff, Tobias J. Looser, Nora Lützgendorf, Michael V. Maseda, Tim Rawle,
 553 Hans-Walter Rix, Bruno Rodríguez Del Pino, Stacey Alberts, Eiichi Egami, Daniel J. Eisenstein,
 554 Ryan Endsley, Kevin Hainline, Ryan Hausen, Benjamin D. Johnson, G. H. Rieke, Marcia Rieke,
 555 Brant Robertson, Irene Shavai, Daniel P. Stark, Fengwu Sun, Sandro Tacchella, Mengtao Tang,
 556 Christina C. Williams, Christopher N. A. Willmer, William Baker, Stefi A. Baum, Rachana
 557 Bhatawdekar, R. A. A. Bowler, Kristan Boyett, Zuyi Chen, Chiara Circosta, Jakob M. Helton,
 558 Zhiyuan Ji, Nimisha Kumari, Jianwei Lyu, Erica J. Nelson, Eleonora Parlanti, Michele Perna,
 559 Lester Sandles, Jan Scholtz, Katherine A. Suess, Michael W. Topping, Hannah Übler, Imaan
 560 E. B. Wallace, and Lily Whitler. Jades nirspec spectroscopy of gn-z11: Lyman- α emission
 561 and possible enhanced nitrogen abundance in a $z = 10.60$ luminous galaxy. *Astronomy and*
 562 *Astrophysics*, 2023.
- 563 [25] Feige Wang, Jinyi Yang, Xiaohui Fan, Joseph F. Hennawi, Aaron J. Barth, Eduardo Bañados,
 564 Fuyan Bian, K. Boutsia, Thomas Connor, Frederick B. Davies, Roberto Decarli, Anna-Christina
 565 Eilers, Emanuele Paolo Farina, Richard F. Green, Linhua Jiang, Jiangtao Li, Chiara Mazzuc-
 566 chelli, Riccardo Nanni, Jan-Torge Schindler, Bram Venemans, Fabian Walter, Xue-Bing Wu,
 567 and Minghao Yue. A luminous quasar at redshift 7.642. *The Astrophysical Journal Letters*,
 568 2021.
- 569 [26] A. G. Adame, José Edgar Madriz Aguilar, S. Ahlen, Shadab Alam, D. M. Alexander,
 570 M. A. Álvarez, O. Alves, Abhijeet Anand, U. Andrade, E. Armengaud, S. Avila, Alejandro
 571 Avilés, H. Awan, Benedict Bahr-Kalus, S. Bailey, C. Baltay, A. Bault, J. Behera, S. Ben-
 572 Zvi, Apurba Bera, Florian Beutler, Davide Bianchi, Chris Blake, Robert Blum, S. Brieden,
 573 A. Brodzeller, D. Brooks, E. Buckley-Geer, E. Burtin, R. Calderón, R. Canning, A. Carnero
 574 Rosell, R. Cereskaite, Jorge L. Cervantes-Cota, Solène Chabanier, E. Chaussidon, J. Chaves-
 575 Montero, Shi-Fan Chen, X. Chen, T. Claybaugh, Shaun Cole, Andrei Cuceu, T. M. Davis, Kyle
 576 Dawson, Axel de la Macorra, A. de Mattia, N. Deiosso, A. Dey, Biprateep Dey, Zhejie Ding,
 577 P. Doel, J. Edelstein, Sarah Eftekharzadeh, Daniel J. Eisenstein, A. Elliott, P. Fagrelius, K. Fan-
 578 ning, S. Ferraro, J. Ereza, N. Findlay, B. Flaugher, Andreu Font-Ribera, D. Forero-Sánchez,
 579 Jaime E. Forero-Romero, Carlos S. Frenk, C. García-Quintero, E. Gaztañaga, Héctor Gil-Marín,
 580 Satya Gontcho A Gontcho, A. X. Gonzalez-Morales, Violeta González-Pérez, C. Gordon, Dylan
 581 Green, D. Gruen, Rafaela Gsponer, G. Gutierrez, J. Guy, Boryana Hadzhiyska, Chang Hoon
 582 Hahn, M.M.S. Hanif, H. K. Herrera-Alcantar, K. Honscheid, Cullan Howlett, D. Huterer, Vid
 583 Iršič, Mustapha Ishak, S. Juneau, Naim Göksel Karaçaylı, R. Kehoe, S. Kent, D. Kirkby,
 584 A. Kremin, Alex Krolewski, Ying-Cheng Lai, Ting-Wen Lan, M. Landriau, Dustin Lang,
 585 J. Lasker, J.M. Le Goff, and L. Le Guillou. Desi 2024 vi: cosmological constraints from the
 586 measurements of baryon acoustic oscillations. *Journal of Cosmology and Astroparticle Physics*,
 587 2025.
- 588 [27] A. G. Adame, J. Aguilar, S. Ahlen, Shadab Alam, D. M. Alexander, M. A. Álvarez, O. Alves,
 589 A. Anand, U. Andrade, E. Armengaud, S. Avila, Alejandro Avilés, H. Awan, Steven Bailey,
 590 C. Baltay, A. Bault, J. Behera, S. BenZvi, Florian Beutler, Davide Bianchi, Chris Blake,
 591 Robert Blum, S. Brieden, A. Brodzeller, D. Brooks, E. Buckley-Geer, E. Burtin, R. Calderón,
 592 R. E. A. Canning, A. Carnero Rosell, R. Cereskaite, Jorge L. Cervantes-Cota, Solène Chabanier,
 593 E. Chaussidon, J. Chaves-Montero, S. Chen, Xinyi Chen, T. Claybaugh, Shaun Cole, A. Cuceu,
 594 T. M. Davis, K. Dawson, Axel de la Macorra, Arnaud de Mattia, N. Deiosso, A. Dey, Biprateep
 595 Dey, Z. Ding, P. Doel, Jerry Edelstein, Sarah Eftekharzadeh, Daniel J. Eisenstein, A. Elliott,
 596 Parker Fagrelius, K. Fanning, Simone Ferraro, J. Ereza, N. Findlay, B. Flaugher, Andreu
 597 Font-Ribera, D. Forero-Sánchez, Jaime E. Forero-Romero, C. García-Quintero, L. H. Garrison,
 598 E. Gaztañaga, Héctor Gil-Marín, Satya Gontcho A Gontcho, A. X. Gonzalez-Morales, Violeta
 599 González-Pérez, Chris Gordon, D. Green, D. Gruen, Rafaela Gsponer, G. Gutierrez, J. Guy,
 600 Boryana Hadzhiyska, ChangHoon Hahn, M.M.S. Hanif, H. K. Herrera-Alcantar, K. Honscheid,
 601 Cullan Howlett, Dragan Huterer, Vid Iršič, M. Ishak, S. Juneau, Naim Göksel Karaçaylı,
 602 R. Kehoe, S. Kent, D. Kirkby, Hui Kong, S. E. Koposov, A. Kremin, Alex Krolewski, Ying-
 603 Cheng Lai, T.-W. Lan, Martin Landriau, Dustin Lang, J. Lasker, J.M. Le Goff, and L. Le
 604 Guillou. Desi 2024 v: Full-shape galaxy clustering from galaxies and quasars. *arXiv (Cornell*
 605 *University)*, 2024.

- 606 [28] A. G. Adame, José Aguilar, S. P. Ahlen, Shadab Alam, D. M. Alexander, Marcelo A. Alvarez, O. Alves, Abhishek Anand, U. Andrade, E. Armengaud, S. Ávila, Alejandro Avilés, H. Awan, S. Bailey, C. Baltay, A. Bault, Jayashree Behera, S. BenZvi, Florian Beutler, Davide Bianchi, Cullen H. Blake, Robert Blum, S. Brieden, A. Brodzeller, D. Brooks, Zachery Brown, E. Buckley-Geer, E. Burtin, R. Calderón, R. E. A. Canning, A. Carnero Rosell, R. Cereskaite, Jorge L. Cervantes-Cota, Solène Chabanier, E. Chaussidon, J. Chaves-Montero, S. Chen, X. Chen, T. Claybaugh, S. Cole, Andrei Cuceu, T. M. Davis, Kyle Dawson, Axel de la Macorra, Arnaud de Mattia, N. Deiosso, R. Demina, Arjun Dey, Biprateep Dey, Z. Ding, P. Doel, Jerry Edelstein, Sarah Eftekharzadeh, Daniel J. Eisenstein, A. Elliott, Parker Fagrelius, K. Fanning, Sergio Ferraro, J. Ereza, N. Findlay, B. Flaugher, Andreu Font-Ribera, D. Forero-Sánchez, Jaime E. Forero-Romero, Carlos S. Frenk, C. García-Quintero, E. Gaztañaga, Héctor Gil-Marín, Satya Gontcho A Gontcho, A. X. Gonzalez-Morales, Violeta González-Pérez, Chris Gordon, D. Green, D. Gruen, Rafaela Gsponer, G. Gutierrez, J. Guy, Boryana Hadzhiyska, Chang Hoon Hahn, M. Hanif, H. K. Herrera-Alcantar, Klaus Honscheid, Jun Hou, Cullan Howlett, Dragan Huterer, Vid Iršič, M. Ishak, S. Juneau, Naim Göksel Karaçaylı, R. Kehoe, S. Kent, D. Kirkby, Francisco-Shu Kitaura, Hui Kong, A. Kremin, Alex Krolewski, Ying-Cheng Lai, T.-W. Lan, M. Landriau, and Dustin Lang. Desi 2024 ii: sample definitions, characteristics, and two-point clustering statistics. *Journal of Cosmology and Astroparticle Physics*, 2025.
- 624 [29] Arjun Dey, David J. Schlegel, Dustin Lang, Robert Blum, Kaylan Burleigh, Xiaohui Fan, Joseph Findlay, Doug Finkbeiner, David Herrera, S. Juneau, Martin Landriau, M. E. Levi, Ian D. McGreer, Aaron Meisner, Adam D. Myers, John Moustakas, P. Nugent, Anna Patej, Edward F. Schlaflly, A. R. Walker, F. Valdés, Benjamin A. Weaver, Christophe Yèche, Hu Zou, X. K. Zhou, Behzad Abareshi, T. M. C. Abbott, Bela Abolfathi, C. Aguilera, Shadab Alam, Lori Allen, A. Alvarez, J. Annis, Behzad Ansarinejad, M Aubert, Jacqueline Beechert, Eric F. Bell, S. BenZvi, Florian Beutler, R. M. Bielby, A. Bolton, César Briceño, E. Buckley-Geer, Karen A. Butler, A. Calamida, R. G. Carlberg, Paul Carter, R. Casas, F. J. Castander, Yumi Choi, Johan Comparat, Elena Cukanovaite, Timothée Delubac, Kaitlin Devries, Sharmila Dey, G. Dhungana, Mark Dickinson, Zhejie Ding, John B. Donaldson, Yutong Duan, Christopher Duckworth, Sarah Eftekharzadeh, Daniel J. Eisenstein, Thomas Etourneau, Parker Fagrelius, Jay Farihi, Mike Fitzpatrick, Andreu Font-Ribera, Leah Fulmer, B. T. Gånsicke, E. Gaztañaga, Koshy George, D. W. Gerdes, Satya Gontcho A Gontcho, Claudio Gorgoni, Gregory Green, J. Guy, D. Harmer, M. Hernandez, K. Honscheid, Lijuan Huang, D. J. James, Buell T. Jannuzzi, Linhua Jiang, R. R. Joyce, A. Karcher, S. Karkar, R. Kehoe, Jean-Paul Kneib, Andrea Kueter-Young, Ting-Wen Lan, Tod R. Lauer, L. Le Guillou, A. Le Van Suu, Jaehyeon Lee, M. Lesser, Laurence Perreault-Levasseur, Ting S. Li, Justin L. Mann, and Robert Marshall. Overview of the desi legacy imaging surveys. *The Astronomical Journal*, 2019.
- 642 [30] Rongpu Zhou, Jeffrey A. Newman, Yao-Yuan Mao, Aaron Meisner, John Moustakas, Adam D. Myers, Abhishek Prakash, Andrew R. Zentner, D. Brooks, Yutong Duan, Martin Landriau, M. E. Levi, Francisco Prada, and G. Tarlé. The clustering of desi-like luminous red galaxies using photometric redshifts. *Monthly Notices of the Royal Astronomical Society*, 2020.
- 646 [31] S. E. Koposov, C. Allende Prieto, Andrew P. Cooper, Ting S. Li, Leandro Bernaldo e Silva, Bokyoung Kim, Andreia Carrillo, Arjun Dey, Christopher J. Manser, Farnik Nikakhtar, A. H. Riley, Constance M. Rockosi, Monica Valluri, J. Aguilar, S. P. Ahlen, S. Bailey, Robert Blum, D. Brooks, T. Claybaugh, Shaun Cole, Axel de la Macorra, Biprateep Dey, Jaime E. Forero-Romero, E. Gaztañaga, J. Guy, A. Kremin, L. Le Guillou, M. E. Levi, Marc Manera, Aaron Meisner, R. Miquel, John Moustakas, Jundan Nie, N. Palanque-Delabrouille, Will J. Percival, Mehdi Rezaie, Graziano Rossi, E. Sánchez, Edward F. Schlaflly, M. Schubnell, G. Tarlé, B. A. Weaver, and Zhimin Zhou. Desi early data release milky way survey value-added catalogue. *Monthly Notices of the Royal Astronomical Society*, 2024.
- 655 [32] A. G. Adame, J. Aguilar, S. P. Ahlen, Shadab Alam, G. Aldering, D. M. Alexander, R. Alfarsy, Carlos Allende Prieto, M. A. Álvarez, O. Alves, Abhijeet Anand, F. Andrade-Oliveira, E. Armengaud, J. Asorey, S. Ávila, Alejandro Avilés, S. Bailey, A. Balaguera-Antolínez, O. Ballester, C. Baltay, A. Bault, Julian Bautista, J. Behera, S. F. Beltran, S. BenZvi, Leandro Bernaldo e Silva, J. R. Bermejo-Climent, A. Berti, Robert Besuner, Florian Beutler, Davide Bianchi, Chris Blake, Robert Blum, A. Bolton, S. Brieden, A. Brodzeller, David J. Brooks, Zachery Brown, E. Buckley-Geer, E. Burtin, L. Cabayol-Garcia, Zheng Cai, R. E. A. Canning, L. Cardiel-Sas,

- 662 A. Carnero Rosell, F. J. Castander, Jorge L. Cervantes-Cota, Solène Chabanier, E. Chaussidon,
 663 J. Chaves-Montero, S. Chen, Xinyi Chen, Chia-Hsun Chuang, T. Claybaugh, Shaun Cole,
 664 Andrew P. Cooper, Andrei Cuceu, T. M. Davis, Kyle Dawson, Roger de Belsunce, Rodrigo de la
 665 Cruz, Axel de la Macorra, John Della Costa, A. de Mattia, R. Demina, U Demirbozan, Joseph
 666 DeRose, Arjun Dey, Biprateep Dey, G. Dhungana, Jiani Ding, Zhejie Ding, P. Doel, Rajkumar
 667 Doshi, Kelly A. Douglass, A. C. Edge, S. Eftekharzadeh, D. J. Eisenstein, A. Elliott, J. Ereza,
 668 S. Escoffier, P. Fagrelius, Xiaohui Fan, K. Fanning, V. A. Fawcett, Simone Ferraro, B. Flaugher,
 669 Andreu Font-Ribera, Jaime E. Forero-Romero, D. Forero-Sánchez, Carlos S. Frenk, Boris Gaen-
 670 sicke, Luz Ángela García, J. García-Bellido, C. García-Quintero, Lehman H. Garrison, Héctor
 671 Gil-Marín, Jesse B. Golden-Marx, Satya Gontcho A Gontcho, and Alma X. González-Morales.
 672 The early data release of the dark energy spectroscopic instrument. *The Astronomical Journal*,
 673 2024.
- 674 [33] DESI Collaboration, B. Abareshi, J. Aguilar, S. P. Ahlen, Shadab Alam, D. M. Alexander,
 675 R. Alfarsy, L. Allen, Carlos Allende Prieto, O. Alves, Jon Ameel, E. Armengaud, J. Asorey,
 676 Alejandro Avilés, S. Bailey, A. Balaguera-Antolínez, O. Ballester, C. Baltay, A. Bault, S. F.
 677 Beltran, B. Benavides, S. BenZvi, A. Berti, R. Besuner, Florian Beutler, Davide Bianchi, Chris
 678 Blake, P. Blanc, Robert Blum, A. Bolton, Sownak Bose, D. Bramall, S. Brieden, A. Brodzeller,
 679 D. Brooks, C. Brownnewell, E. Buckley-Geer, R. N. Cahn, Zheng Cai, R. Canning, R. Capasso,
 680 A. Carnero Rosell, P. Carton, R. Casas, F. J. Castander, Jorge L. Cervantes-Cota, Solène Cha-
 681 banier, E. Chaussidon, Chia-Hsun Chuang, Chiara Circosta, Shaun Cole, Andrew P. Cooper,
 682 L. da Costa, Marie-Claude Cousinou, Andrei Cuceu, T. M. Davis, Kyle Dawson, Rodrigo de la
 683 Cruz, Axel de la Macorra, A. de Mattia, John Della Costa, P. Demmer, M. Derwent, Arjun Dey,
 684 Biprateep Dey, G. Dhungana, Zhejie Ding, C. Dobson, Peter Doel, J. Donald-McCann, J. Don-
 685 aldson, Kelly A. Douglass, Yutong Duan, P. Dunlop, J. Edelstein, S. Eftekharzadeh, Daniel J.
 686 Eisenstein, M. Enriquez-Vargas, S. Escoffier, M. Evatt, P. Fagrelius, Xiaohui Fan, K. Fanning,
 687 V. A. Fawcett, S. Ferraro, J. Ereza, B. Flaugher, Andreu Font-Ribera, Jaime E. Forero-Romero,
 688 Carlos S. Frenk, S. Fromenteau, Boris Gaensicke, C. García-Quintero, Lehman H. Garrison,
 689 E. Gaztañaga, F. Gerardi, Héctor Gil-Marín, Satya Gontcho A Gontcho, Alma X. González-
 690 Morales, and Violeta González-Pérez. Overview of the instrumentation for the dark energy
 691 spectroscopic instrument. *The Astronomical Journal*, 2022.
- 692 [34] A. G. Adame, J. Aguilar, S. Ahlen, Shadab Alam, D. M. Alexander, Carlos Allende Prieto,
 693 Marcelo A. Alvarez, O. Alves, A. Anand, U. Andrade, E. Armengaud, S. Avila, Alejandro Avilés,
 694 H. Awan, Benedict Bahr-Kalus, S. Bailey, C. Baltay, A. Bault, J. Behera, S. BenZvi, Florian
 695 Beutler, Davide Bianchi, Chris Blake, Robert Blum, M. Bonici, S. Brieden, A. Brodzeller,
 696 D. Brooks, E. Buckley-Geer, E. Burtin, R. Calderón, R. E. A. Canning, A. Carnero Rosell,
 697 R. Cereskaite, Jorge L. Cervantes-Cota, Solène Chabanier, E. Chaussidon, J. Chaves-Montero,
 698 D. Chebat, S. Chen, X. Chen, T. Claybaugh, S. Cole, A. Cuceu, T. M. Davis, K. Dawson, Axel
 699 de la Macorra, Arnaud de Mattia, N. Deiosso, A. Dey, Biprateep Dey, Z. Ding, P. Doel, Jerry
 700 Edelstein, Sarah Eftekharzadeh, Daniel J. Eisenstein, Willem Elbers, A. Elliott, Parker Fagrelius,
 701 K. Fanning, Simone Ferraro, J. Ereza, N. Findlay, B. Flaugher, Andreu Font-Ribera, D. Forero-
 702 Sánchez, Jaime E. Forero-Romero, Carlos S. Frenk, C. García-Quintero, Lehman H. Garrison,
 703 E. Gaztañaga, Héctor Gil-Marín, Satya Gontcho A Gontcho, A. X. Gonzalez-Morales, Violeta
 704 González-Pérez, Chris Gordon, D. Green, D. Gruen, Rafaela Gsponer, G. Gutierrez, J. Guy,
 705 Boryana Hadzhiyska, Chang Hoon Hahn, M.M.S. Hanif, H. K. Herrera-Alcantar, K. Honscheid,
 706 Cullan Howlett, Dragan Huterer, Vid Iršič, Mustapha Ishak, R. Joyce, S. Juneau, Naim Göksel
 707 Karaçaylı, R. Kehoe, S. Kent, D. Kirkby, Hui Kong, S. E. Koposov, A. Kremin, and Alex
 708 Krolewski. Desi 2024 vii: cosmological constraints from the full-shape modeling of clustering
 709 measurements. *Journal of Cosmology and Astroparticle Physics*, 2025.
- 710 [35] Michele Pinon, Arnaud de Mattia, Peter McDonald, E. Burtin, V. Ruhlmann-Kleider, Martin
 711 White, Davide Bianchi, Ashley J. Ross, José Aguilar, S. P. Ahlen, D. Brooks, E. Chaussidon,
 712 T. Claybaugh, S. Cole, Axel de la Macorra, B.R. Dey, Peter Doel, K. Fanning, Jaime E. Forero-
 713 Romero, E. Gaztañaga, Satya Gontcho A Gontcho, Cullan Howlett, D. Kirkby, Theodore Kisner,
 714 A. Kremin, A. Lambert, Martin Landriau, J. Lasker, L. Le Guillou, M. E. Levi, Marc Manera,
 715 Paul Martini, Aaron Meisner, R. Miquel, John Moustakas, Adam D. Myers, Gustavo Niz,
 716 N. Palanque-Delabrouille, Will J. Percival, Claire Poppett, Giacomo Rossi, E. Sánchez, David J.
 717 Schlegel, M Schubnell, Hee-Jong Seo, David Sprayberry, G. Tarlé, M. Vargas-Magaña, B. A.
 718 Weaver, Pauline Zarrouk, Ruguang Zhou, and Hao Zou. Mitigation of desi fiber assignment

- 719 incompleteness effect on two-point clustering with small angular scale truncated estimators.
 720 *Journal of Cosmology and Astroparticle Physics*, 2025.
- 721 [36] M. Rashkovetskyi, D. Forero-Sánchez, Arnaud de Mattia, Daniel J. Eisenstein, Nikhil Padman-
 722 abhan, Hee-Jong Seo, Ashley J. Ross, J. Aguilar, S. P. Ahlen, O. Alves, U. Andrade, David J.
 723 Brooks, E. Burtin, T. Claybaugh, Shaun Cole, Axel de la Macorra, Zhejie Ding, Peter Doel,
 724 K. Fanning, Simone Ferraro, Andreu Font-Ribera, Jaime E. Forero-Romero, C. García-Quintero,
 725 Héctor Gil-Marín, Satya Gontcho A Gontcho, A. X. Gonzalez-Morales, G. Gutiérrez, K. Hon-
 726 scheid, Cullan Howlett, S. Juneau, A. Kremin, L. Le Guillou, Marc Manera, L. Medina-Varela,
 727 J. Mena-Fernández, R. Miquel, Eva-Maria Mueller, A. Muñoz Gutiérrez, Adam D. Myers,
 728 Jundai Nie, Gustavo Niz, E. Paillas, Will J. Percival, Claire Poppett, Ignasi Pérez-Ràfols, Mehdi
 729 Rezaie, A. Rosado-Marin, Graziano Rossi, Rossana Ruggeri, E. Sánchez, C. Saulder, David J.
 730 Schlegel, M. Schubnell, David Sprayberry, G. Tarlé, B. A. Weaver, Jiaxi Yu, Cheng Zhao, and
 731 Hu Zou. Semi-analytical covariance matrices for two-point correlation function for desi 2024
 732 data. *Journal of Cosmology and Astroparticle Physics*, 2025.
- 733 [37] P. A. R. Ade, N. Aghanim, C. Armitage-Caplan, M. Arnaud, M. Ashdown, F. Atrio-Barandela,
 734 J. Aumont, C. Baccigalupi, A. J. Banday, R. B. Barreiro, J. G. Bartlett, E. Battaner, K. Benabed,
 735 A. Benoit, A. Benoit-Lévy, J. P. Bernard, M. Bersanelli, P. Bielewicz, J. Bobin, J. J. Bock,
 736 A. Bonaldi, J. R. Bond, J. Borrill, F. R. Bouchet, M. Bridges, M. Bucher, C. Burigana, R. C.
 737 Butler, E. Calabrese, B. Cappellini, J.-F. Cardoso, A. Catalano, A. Challinor, A. Chamballu,
 738 Ranga-Ram Chary, X. Chen, H. C. Chiang, L.-Y Chiang, P. R. Christensen, S. Church, D. L.
 739 Clements, S. Colombi, L. P. L. Colombo, F. Couchot, A. Coulais, B. P. Crill, A. Curto, F. Cuttaia,
 740 L. Danese, R. D. Davies, R. J. Davis, P. de Bernardis, A. de Rosa, G. de Zotti, G. de Zotti, J.-M.
 741 Delouis, F.-X. Désert, C. Dickinson, J. M. Diego, K. Dolag, H. Dole, S. Donzelli, O. Doré,
 742 M. Douspis, J. Dunkley, X. Dupac, G. Efstathiou, F. Elsner, T. A. Enßlin, H. K. Eriksen,
 743 F. Finelli, O. Forni, M. Frailis, A. A. Fraisse, E. Franceschi, T. Gaier, S. Galeotta, S. Galli,
 744 K. Ganga, M. Giard, G. Giardino, Y. Giraud-Héraud, E. Gjerløw, J. González-Nuevo, K. M.
 745 Górski, S. Gratton, A. Gregorio, A. Gruppuso, J. E. Gudmundsson, J. Haïssinski, J. Hamann,
 746 F. K. Hansen, D. Hanson, D. L. Harrison, S. Henrot-Versillé, C. Hernández-Monteagudo,
 747 D. Herranz, S. R. Hildebrandt, E. Hivon, and M. Hobson. Planck2013 results. xvi. cosmological
 748 parameters. *Astronomy and Astrophysics*, 2014.
- 749 [38] Eiichiro Komatsu, J. Dunkley, Michael R. Nolta, C. L. Bennett, B. Gold, G. Hinshaw, N. Jarosik,
 750 D. Larson, M. Limon, Lyman A. Page, David N. Spergel, M. Halpern, Robert Hill, A. Kogut,
 751 S. S. Meyer, Gregory S. Tucker, J. L. Weiland, Edward J. Wollack, and E. L. Wright. Five-
 752 year wilkinson microwave anisotropy probe observations: Cosmological interpretation. *The
 753 Astrophysical Journal Supplement Series*, 2009.
- 754 [39] G. Hinshaw, D. Larson, Eiichiro Komatsu, David N. Spergel, C. L. Bennett, Jo Dunkley, M. R.
 755 Nolta, M. Halpern, Robert Hill, N. Odegard, Lyman A. Page, Kendrick M. Smith, J. L. Weiland,
 756 B. Gold, N. Jarosik, A. Kogut, M. Limon, S. S. Meyer, Gregory S. Tucker, Edward J. Wollack,
 757 and E. L. Wright. Nine-year wilkinson microwave anisotropy probe (wmap) observations:
 758 Cosmological parameter results. *The Astrophysical Journal Supplement Series*, 2013.
- 759 [40] Y. Sultan Abylkairov, Omar Darwish, J. Colin Hill, and Blake D. Sherwin. Partially constrained
 760 internal linear combination: A method for low-noise cmb foreground mitigation. *Physical
 761 review. D/Physical review. D.*, 2021.
- 762 [41] P. A. R. Ade, Zeeshan Ahmed, M. Amiri, D. Barkats, R. Basu Thakur, C. A. Bischoff, D. Beck,
 763 J. J. Bock, H. Boenish, E. Bullock, V. Buza, James R. Cheshire, Jake Connors, J. Cornelison,
 764 M. Crumrine, A. Cukierman, E. V. Denison, M. Dierickx, L. Duband, M. Eiben, S. Fatigoni,
 765 J. P. Filippini, S. Fliescher, N. Goeckner-Wald, D. C. Goldfinger, J. Grayson, Paul Grimes,
 766 G. Hall, George Halal, M. Halpern, E. Hand, S. Harrison, S. Henderson, S. R. Hildebrandt,
 767 G. C. Hilton, Johannes Hubmayr, H. Hui, K. D. Irwin, J. Kang, K. S. Karkare, E. Karpel,
 768 S. Kefeli, S. A. Kernasovskiy, J. M. Kovac, C. L. Kuo, K. Lau, E. M. Leitch, A. Lennox, K. G.
 769 Megerian, Lorenzo Minutolo, Lorenzo Moncelsi, Y. Nakato, Toshiya Namikawa, H. T. Nguyen,
 770 R. O'Brient, R. W. Ogburn, S. Palladino, T. Prouvé, C. Pryke, B. Racine, C. D. Reintsema,
 771 S. Richter, A. Schillaci, R. Schwarz, B. Schmitt, C. D. Sheehy, Amal S. Hassan, T. St. Germaine,
 772 B. Steinbach, R. Sudiwala, G. P. Teply, K. L. Thompson, J. E. Tolan, C. Tucker, A. D. Turner,
 773 C. Umiltà, C. Vergès, A. G. Vieregg, A. Wandui, A. C. Weber, Donald Wiebe, J. Willmert, C. L.

- 774 Wong, W. L. K. Wu, Huan Yang, K. W. Yoon, E. Young, Cyndia Yu, Lingzhen Zeng, C. Zhang,
 775 and S. Zhang. Improved constraints on primordial gravitational waves using planck , wmap, and
 776 bicep/ keck observations through the 2018 observing season. *Physical Review Letters*, 2021.
- 777 [42] M. Tristram, A. J. Banday, K. M. Górski, Reijo Keskitalo, C. R. Lawrence, K. J. Andersen, R. B.
 778 Barreiro, J. Borrill, L. P. L. Colombo, H. K. Eriksen, R. Fernández-Cobos, Theodore Kisner,
 779 E. Martínez-González, B. Partridge, D. Scott, T. L. Svalheim, and I. K. Wehus. Improved limits
 780 on the tensor-to-scalar ratio using bicep and planck data. *Physical review. D/Physical review.*
 781 *D.*, 2022.
- 782 [43] Frank J. Qu, Blake D. Sherwin, Mathew S. Madhavacheril, Dongwon Han, Kevin T. Crowley,
 783 Irene Abril-Cabezas, P. A. R. Ade, Simone Aiola, Tommy Alford, M. Amiri, Stefania Amodeo,
 784 Rui An, Zachary Atkins, J. E. Austermann, Nicholas Battaglia, E. S. Battistelli, James A.
 785 Beall, Rachel Bean, Benjamin Beringue, Tanay Bhandarkar, Emily Biermann, Boris Bolliet,
 786 J. R. Bond, Hongbo Cai, Erminia Calabrese, Victoria Calafut, Valentina Capalbo, Felipe
 787 Carrero, Julien Carron, A. Challinor, Grace E. Chesmore, Hsiao-Mei Cho, Steve K. Choi,
 788 Susan E. Clark, Rodrigo Córdova Rosado, Nicholas F. Cothard, Kevin Coughlin, William R.
 789 Coulton, Roohi Dalal, Omar Darwish, Mark J. Devlin, Simon Dicker, Peter Doze, Cody J.
 790 Duell, Shannon M. Duff, Adriaan J. Duivenvoorden, Jo Dunkley, Rolando Dünner, Valentina
 791 Fanfani, Max Fankhanel, Gerrit S. Farren, Simone Ferraro, Rodrigo Freudert, Brittany Fuzia,
 792 Patricio A. Gallardo, X. Garrido, Vera Gluscevic, Joseph E. Golec, Yilun Guan, M. Halpern,
 793 I. Harrison, Matthew Hasselfield, Erin Healy, Shawn Henderson, Brandon S. Hensley, Carlos
 794 Hervías-Caimapo, J. Colin Hill, Gene C. Hilton, Matt Hilton, Adam D. Hincks, Renée Hložek,
 795 Shuay-Pwu Patty Ho, Zachary B. Huber, Johannes Hubmayr, K. M. Huffenberger, John P.
 796 Hughes, K. D. Irwin, Giovanni Isopi, Hidde T. Jense, Ben Keller, Joshua Kim, Kenda Knowles,
 797 Brian J. Koopman, Arthur Kosowsky, Darby Kramer, Aleksandra Kusiak, Adrien La Posta,
 798 Alex Laguë, Victoria Lakey, Eunseong Lee, Zack Li, Yaqiong Li, M. Limon, Martine Lokken,
 799 Thibaut Louis, Marius Lungu, N. MacCrann, Amanda MacInnis, Diego Maldonado, and Felipe
 800 Maldonado. The atacama cosmology telescope: A measurement of the dr6 cmb lensing power
 801 spectrum and its implications for structure growth. *The Astrophysical Journal*, 2024.
- 802 [44] Eleonora Di Valentino, A. Melchiorri, Olga Mena, and Sunny Vagnozzi. Nonminimal dark
 803 sector physics and cosmological tensions. *Physical review. D/Physical review. D.*, 2020.
- 804 [45] Eleonora Di Valentino, A. Melchiorri, and Joseph Silk. Reconciling planck with the local value
 805 of h 0 in extended parameter space. *Physics Letters B*, 2016.
- 806 [46] Jun-Qian Jiang, Gen Ye, and Yun-Song Piao. Impact of the hubble tension on the contour.
 807 *Physics Letters B*, 2024.
- 808 [47] Jordan Stevens, Hasti Khoraminezhad, and Shun Saito. Constraining the spatial curvature with
 809 cosmic expansion history in a cosmological model with a non-standard sound horizon. *Journal*
 810 *of Cosmology and Astroparticle Physics*, 2023.
- 811 [48] Oliver H. E. Philcox. Do the cmb temperature fluctuations conserve parity? *Physical Review*
 812 *Letters*, 2023.
- 813 [49] Karsten Jedamzik, Levon Pogosian, and Gong-Bo Zhao. Why reducing the cosmic sound
 814 horizon alone can not fully resolve the hubble tension. *Communications Physics*, 2021.
- 815 [50] Adam G. Riess, L. Strolger, J. Tonry, Stefano Casertano, Henry C. Ferguson, Bahram Mobasher,
 816 Peter Challis, A. V. Filippenko, Saurabh W. Jha, Weidong Li, R. Chornock, R. Kirshner,
 817 B. Leibundgut, Mark Dickinson, Mario Livio, Mauro Giavalisco, Charles C. Steidel, N. Benitez,
 818 and Z. Tsvetanov. Type ia supernova discoveries atz> 1 from thehubble space telescope:
 819 Evidence for past deceleration and constraints on dark energy evolution. *The Astrophysical*
 820 *Journal*, 2004.
- 821 [51] Daniel J. Eisenstein, David H. Weinberg, Eric Agol, H. Aihara, Carlos Allende Prieto, Scott F.
 822 Anderson, James A. Arns, É. Aubourg, S. Bailey, E. Balbinot, Robert H. Barkhouser, Timothy C.
 823 Beers, Andreas A. Berlind, Steven J. Bickerton, Dmitry Bizyaev, Michael R. Blanton, John J.
 824 Bochanski, A. Bolton, Casey T. Bosman, Jo Bovy, W. N. Brandt, B. Breslauer, H. Brewington,
 825 J. Brinkmann, P. J. Brown, Joel R. Brownstein, Dan Bürger, Nicolás G. Busca, H. Campbell,

- 826 Phillip A. Cargile, W. Carithers, Joleen K. Carlberg, Michael A. Carr, Liang Chang, Yanmei
 827 Chen, C. Chiappini, Johan Comparat, N. Connolly, Marina Cortês, Rupert A. C. Croft, Kátia
 828 Cunha, Luiz N. da Costa, James R. A. Davenport, Kyle Dawson, Nathan De Lee, G. F. Porto de
 829 Mello, F. de Simoni, Janice Dean, Saurav Dhital, Anne Ealet, Garrett Ebelke, Edward M.
 830 Edmondson, J. Eiting, S. Escoffier, M. Esposito, Michael L. Evans, Xiaohui Fan, Bruno Femenía
 831 Castellá, Letícia D. Ferreira, Greg Fitzgerald, Scott W. Fleming, Andreu Font-Ribera, Eric B.
 832 Ford, Peter M. Frinchaboy, A. E. García Pérez, B. Scott Gaudi, Jian Ge, Luan Ghezzi, Bruce
 833 Gillespie, G. Gilmore, L. Girardi, J. Richard Gott, Andrew Gould, E. K. Grebel, James E.
 834 Gunn, J.-Ch. Hamilton, Paul Harding, D. E. Harris, Suzanne L. Hawley, Frederick R. Hearty,
 835 Joseph F. Hennawi, J. I. Gónzalez Hernández, Shirley Ho, David W. Hogg, Jon A. Holtzman,
 836 Klaus Honscheid, Naohisa Inada, Inese I. Ivans, Linhua Jiang, Peng Jiang, Jennifer A. Johnson,
 837 C. Jordan, Wendell P. Jordan, Guinevere Kauffmann, Eyal Kazin, D. Kirkby, Mark A. Klaene,
 838 G. R. Knapp, Jean-Paul Kneib, and C. S. Kochanek. Sdss-iii: Massive spectroscopic surveys
 839 of the distant universe, the milky way, and extra-solar planetary systems. *The Astronomical
 840 Journal*, 2011.
- 841 [52] David N. Spergel, Rachel Bean, Olivier Doré, M. R. Nolta, C. L. Bennett, J. Dunkley, G. Hinshaw, N. Jarosik, Eiichiro Komatsu, Lyman A. Page, Hiranya V. Peiris, Licia Verde, M. Halpern, Ryley Hill, A. Kogut, M. Limon, S. S. Meyer, N. Odegard, Gregory S. Tucker, J. L. Weiland, Edward J. Wollack, and E. L. Wright. Three-year wilkinson microwave anisotropy probe(wmap) observations: Implications for cosmology. *The Astrophysical Journal Supplement Series*, 2007.
- 842 [53] Brian D. Fields and S. Sarkar. Review of particle physics.
- 843 [54] Nils Schöneberg, Licia Verde, Héctor Gil-Marín, and S. Brieden. Bao+bbn revisited — growing
 844 the hubble tension with a 0.7 km/s/mpc constraint. *Journal of Cosmology and Astroparticle
 845 Physics*, 2022.
- 846 [55] N. Jarosik, C. L. Bennett, J. Dunkley, B. Gold, M. R. Greason, M. Halpern, Robert Hill, G. Hinshaw, A. Kogut, Eiichiro Komatsu, D. Larson, M. Limon, S. S. Meyer, Michael R. Nolta, N. Odegard, Lyman A. Page, Kendrick M. Smith, David N. Spergel, Gregory S. Tucker, J. L. Weiland, Edward J. Wollack, and E. L. Wright. Seven-year wilkinson microwave anisotropy probe (wmap) observations: Sky maps, systematic errors, and basic results. *The Astrophysical Journal Supplement Series*, 2011.
- 847 [56] Weiqiang Yang, Supriya Pan, Eleonora Di Valentino, Olga Mena, and A. Melchiorri. 2021-h0 odyssey: closed, phantom and interacting dark energy cosmologies. *Journal of Cosmology and
 848 Astroparticle Physics*, 2021.
- 849 [57] Evan McDonough, Mengxiang Lin, J. Colin Hill, Wayne Hu, and Shengjia Zhou. Early dark sector, the hubble tension, and the swampland. *Physical review. D/Physical review. D.*, 2022.
- 850 [58] Marc Kamionkowski and Adam G. Riess. The hubble tension and early dark energy. *Annual
 851 Review of Nuclear and Particle Science*, 2023.
- 852 [59] Shadab Alam, M Aubert, S. Ávila, Christophe Balland, Julian Bautista, Matthew A. Bershadsky, Dmitry Bizyaev, Michael R. Blanton, A. Bolton, Jo Bovy, J. Brinkmann, Joel R. Brownstein, E. Burtin, Solène Chabanier, Michael J. Chapman, Peter Doohyun Choi, Chia-Hsun Chuang, Johan Comparat, Marie-Claude Cousinou, Andrei Cuceu, Kyle Dawson, Sylvain de la Torre, Arnaud de Mattia, Victoria de Sainte Agathe, Hélion du Mas des Bourboux, S. Escoffier, Thomas Etourneau, James R. Farr, Andreu Font-Ribera, Peter M. Frinchaboy, S. Fromenteau, Héctor Gil-Marín, Jean-Marc Le Goff, Alma X. Gonzalez-Morales, Violeta González-Pérez, Kathleen Grabowski, Julien Guy, A. J. Hawken, Jiamin Hou, Hui Kong, J.R. Parker, Mark A. Klaene, Jean-Paul Kneib, S. Y. Lin, Daniel W. Long, Brad W. Lyke, Axel de la Macorra, Paul Martini, Karen L. Masters, Faizan G Mohammad, Jeongin Moon, Eva-Maria Mueller, A. Muñoz Gutiérrez, Adam D. Myers, S. Nadathur, Richard Neveux, Jeffrey A. Newman, P. Noterdaeme, Audrey Oravetz, Daniel Oravetz, N. Palanque-Delabrouille, Kaike Pan, Romain Paviot, Will J. Percival, Ignasi Pérez-Ràfols, Patrick Petitjean, Matthew M. Pieri, Abhishek Prakash, Anand Raichoor, Corentin Ravoux, Mehdi Rezaie, J. Rich, Ashley J. Ross, Graziano Rossi, Rossana Ruggeri, V. Ruhlmann-Kleider, Ariel G. Sánchez, Javier Sánchez, José Sánchez-Gallego, Conor Sayres, Donald P. Schneider, Hee-Jong Seo, Arman Shafieloo, Anže Slosar, A. G. Smith,

- 879 Julianna Stermer, Amélie Tamone, Jeremy L. Tinker, Rita Tojeiro, M. Vargas-Magaña, Andrei
 880 Variu, Yuting Wang, Benjamin Alan Weaver, Anne-Marie Weijmans, Christophe Yèche, Pauline
 881 Zarrouk, Cheng Zhao, Gong-Bo Zhao, and Zheng Zheng. Completed sdss-iv extended baryon
 882 oscillation spectroscopic survey: Cosmological implications from two decades of spectroscopic
 883 surveys at the apache point observatory. *Physical review. D/Physical review. D.*, 2021.
- 884 [60] Sunny Vagnozzi. Seven hints that early-time new physics alone is not sufficient to solve the
 885 hubble tension. *Universe*, 2023.
- 886 [61] George Alestas and Leandros Perivolaropoulos. Late-time approaches to the hubble tension
 887 deforming $h(z)$, worsen the growth tension. *Monthly Notices of the Royal Astronomical Society*,
 888 2021.
- 889 [62] Bo Feng, Xulian Wang, and Xinmin Zhang. Dark energy constraints from the cosmic age and
 890 supernova. *Physics Letters B*, 2004.
- 891 [63] José Luis Bernal, Licia Verde, Raúl Jiménez, Marc Kamionkowski, D. Valcin, and B. D. Wandelt.
 892 Trouble beyond h_0 and the new cosmic triangles. *Physical review. D/Physical review. D.*, 2021.
- 893 [64] Maria Archidiacono, Emanuele Castorina, Diego Redigolo, and Ennio Salvioni. Unveiling dark
 894 fifth forces with linear cosmology. *Journal of Cosmology and Astroparticle Physics*, 2022.
- 895 [65] Hamood Ur Rehman, Ifrah Iqbal, Suhad Subhi Aiadi, Nabil Mlaiki, and Muhammad Shoaib
 896 Saleem. Soliton solutions of klein–fock–gordon equation using sardar subequation method.
 897 *Mathematics*, 2022.
- 898 [66] C. L. Bennett, D. Larson, J. L. Weiland, and G. Hinshaw. The 1% concordance hubble constant.
 899 *The Astrophysical Journal*, 2014.
- 900 [67] Astrid Eichhorn and Martin Pauly. Constraining power of asymptotic safety for scalar fields.
 901 *Physical review. D/Physical review. D.*, 2021.
- 902 [68] Michele Cicoli, Joseph P. Conlon, Anshuman Maharana, Susha Parameswaran, Fernando
 903 Quevedo, and Ivonne Zavala. String cosmology: From the early universe to today. *Physics
 904 Reports*, 2024.
- 905 [69] Stephan P. Rosshart, Jasmin Herz, Brian G. Vassallo, Ashli Hunter, Morgan Wall, Jonathan H.
 906 Badger, John A. McCulloch, Dimitrios G. Anastasaki, Aishe A. Sarshad, Irina Leonardi,
 907 Nicholas Collins, Joshua Blatter, Seong-Ji Han, Samira Tamoutounour, Svetlana Potapova,
 908 Mark Claire, Wuxing Yuan, Shurjo K. Sen, Matthew S. Dreier, Benedikt Hild, Markus Hafner,
 909 David Wang, Iliyan D. Iliev, Yasmine Belkaid, Giorgio Trinchieri, and Barbara Rehermann.
 910 Laboratory mice born to wild mice have natural microbiota and model human immune responses.
 911 *Science*, 2019.
- 912 [70] Thomas R. Frieden. Evidence for health decision making — beyond randomized, controlled
 913 trials. *New England Journal of Medicine*, 2017.
- 914 [71] Andrew Phillips, Amir Shroufi, Lara Vojnov, Jennifer Cohn, Teri Roberts, Tom Ellman, Kim-
 915 berly Bonner, Christine Rousseau, Geoff P. Garnett, Valentina Cambiano, Fumiyo Nakagawa,
 916 Deborah Ford, Loveleen Bansi-Matharu, Alec Miners, Jens Lundgren, Jeffrey W. Eaton, Ros-
 917 alind Parkes-Ratanshi, Zachary Katz, David Maman, Nathan Ford, Marco Vitória, Meg Doherty,
 918 David W. Dowdy, Brooke E Nichols, Maurine Murtagh, Meghan Wareham, Kara Palamoun-
 919 tain, Christine Chakanyuka Musanhu, Wendy Stevens, David Katzenstein, Andrea Ciaranello,
 920 Ruanne V. Barnabas, R. Scott Braithwaite, Eran Bendavid, Kusum Nathoo, David van de
 921 Vijver, David P. Wilson, Charles B. Holmes, Anna Bershteyn, Simon Walker, Elliot Raizes,
 922 Ilesh Jani, Lisa Nelson, Rosanna W. Peeling, Fern Terris-Prestholt, Joseph Murungi, Tsitsi
 923 Mutasa-Apollo, Timothy B. Hallett, and Paul Revill. Sustainable hiv treatment in africa through
 924 viral-load-informed differentiated care. *Nature*, 2015.
- 925 [72] Matteo Chinazzi, Jessica T. Davis, Marco Ajelli, Corrado Gioannini, Maria Litvinova, Stefano
 926 Merler, Ana Pastore y Piontti, Kunpeng Mu, Luca Rossi, Kaiyuan Sun, Cécile Viboud, Xinyue
 927 Xiong, Hongjie Yu, M. Elizabeth Halloran, Ira M. Longini, and Alessandro Vespignani. The
 928 effect of travel restrictions on the spread of the 2019 novel coronavirus (covid-19) outbreak.
 929 *Science*, 2020.

- 930 [73] Mark C. Urban, Greta Bocedi, Andrew P. Hendry, Jean-Baptiste Mihoub, Guy Pe'er, Alexander
 931 Singer, Jon R. Bridle, Lisa G. Crozier, Luc De Meester, William Godsoe, Andrew Gonzalez,
 932 Jessica J. Hellmann, Robert D. Holt, A. Huth, Karin Johst, Cornelia B. Krug, Paul Leadley,
 933 Steven C. Palmer, Jelena H. Pantel, Andreas Schmitz, Patrick A. Zollner, and Justin M. J. Travis.
 934 Improving the forecast for biodiversity under climate change. *Science*, 2016.
- 935 [74] Karan Singhal, Shekoofeh Azizi, Tao Tu, S. Sara Mahdavi, Jason Lee, Hyung Won Chung,
 936 Nathan Scales, Ajay Kumar Tanwani, Heather Cole-Lewis, Stephen Pfohl, Perry W. Payne,
 937 Martin Seneviratne, Paul Gamble, Christopher Kelly, Abubakr Babiker, Nathanael Schärli,
 938 Aakanksha Chowdhery, P. Mansfield, Dina Demner-Fushman, Blaise Agüera y Arcas, Dale R.
 939 Webster, Greg S. Corrado, Yossi Matias, Katherine Chou, Juraj Gottweis, Nenad Tomašev, Yun
 940 Liu, Alvin Rajkomar, Joëlle Barral, Christopher Semturs, Alan Karthikesalingam, and Vivek
 941 Natarajan. Large language models encode clinical knowledge. *Nature*, 2023.
- 942 [75] Salman Khan, Muzammal Naseer, Munawar Hayat, Syed Waqas Zamir, Fahad Shahbaz Khan,
 943 and Mubarak Shah. Transformers in vision: A survey. *ACM Computing Surveys*, 2022.
- 944 [76] Li Yuan, Yunpeng Chen, Tao Wang, Weihao Yu, Yujun Shi, Zihang Jiang, Francis E. H. Tay,
 945 Jiashi Feng, and Shuicheng Yan. Tokens-to-token vit: Training vision transformers from scratch
 946 on imagenet. *2021 IEEE/CVF International Conference on Computer Vision (ICCV)*, 2021.
- 947 [77] Malik Sallam. Chatgpt utility in healthcare education, research, and practice: Systematic review
 948 on the promising perspectives and valid concerns. *Healthcare*, 2023.
- 949 [78] Hyun Min Lee. Exothermic dark matter for xenon1t excess. *Journal of High Energy Physics*,
 950 2021.
- 951 [79] Brandon Bozek, David J. E. Marsh, Joseph Silk, and Rosemary F. G. Wyse. Galaxy uv-
 952 luminosity function and reionization constraints on axion dark matter. *Monthly Notices of the
 953 Royal Astronomical Society*, 2015.
- 954 [80] Raymond T. Co, David I. Dunsky, Nicolas Fernandez, Akshay Ghalsasi, Lawrence J. Hall,
 955 Keisuke Harigaya, and Jessie Shelton. Gravitational wave and cmb probes of axion kination.
 956 *Journal of High Energy Physics*, 2022.
- 957 [81] J. R. Robinson. Bertram maurice mandelbrote. *BMJ*, 2011.
- 958 [82] A. Silversides. Withdrawal of clinical trials policy by canadian research institute is a "lost
 959 opportunity for increased transparency". *BMJ*, 2011.
- 960 [83] R. Abuter, Fatmé Allouche, A. Amorim, C. Bailet, Anthony Berdeu, Jean-Philippe Berger,
 961 P. Bério, Azzurra Bigoli, O. Boebion, M.-L. Bolzer, H. Bonnet, G. Bourdarot, P. Bourget,
 962 W. Brandner, Yixian Cao, Ralf Conzelmann, Mauro Comin, Y. Clénet, Benjamin Courtney-
 963 Barrer, R. Davies, Denis Defrère, A. Delboulbé, F. Delplancke-Ströbele, R. Dembet, Jason
 964 Dexter, P. T. de Zeeuw, A. Drescher, A. Eckart, C. Édouard, F. Eisenhauer, Maximilian Fabricius,
 965 H. Feuchtgruber, Gert Finger, N. M. Förster Schreiber, P. García, R. García López, F. Gao, É.
 966 Gendron, R. Genzel, Juan Pablo Gil, S. Gillessen, Tiago Gomes, Frédéric Gonté, C. Gouvret,
 967 P. Guajardo, Sylvain Guieu, W. Hackenberg, Nabil Haddad, Michael Hartl, X. Haubois, F. Hauß-
 968 mann, G. Heißen, Th. Henning, S. Hippler, S. F. Hönig, M. Horrobin, N. Hubin, Estelle Jacqmart,
 969 L. Jocou, A. Kaufer, P. Kervella, Johann Kolb, H. Korhonen, S. Lacour, S. Lagarde, Olivier
 970 Lai, V. Lapeyrère, Romain Laugier, J.-B. Le Bouquin, J. Leftley, Pierre Léna, S.A.E. Lewis,
 971 Daizhong Liu, B. López, D. Lutz, Y. Magnard, F. Mang, A. Marcotto, D. Maurel, A. Mérand,
 972 F. Millour, Nikhil More, H. Netzer, H. Nowacki, M. Nowak, Sylvain Oberti, Thomas Ott,
 973 Laurent Pallanca, T. Paumard, K. Perraut, G. Perrin, R. G. Petrov, O. Pfuhl, N. Pourré, S. Ra-
 974 bien, Christian Rau, M. Riquelme, S. Robbe-Dubois, S. Rochat, and Muhammad Salman. A
 975 dynamical measure of the black hole mass in a quasar 11 billion years ago. *Nature*, 2024.
- 976 [84] Shengyu Li, Pengzhi Zhang, Weiqing Chen, Lingqun Ye, Kristopher W. Brannan, Nhat-Tu Le,
 977 Jun-ichi Abe, John P. Cooke, and Guangyu Wang. A relay velocity model infers cell-dependent
 978 rna velocity. *Nature Biotechnology*, 2023.

979 **Agents4Science AI Involvement Checklist**

- 980 • [A] **Human-generated:** Humans generated 95% or more of the research, with AI being of
981 minimal involvement.
- 982 • [B] **Mostly human, assisted by AI:** The research was a collaboration between humans and
983 AI models, but humans produced the majority (>50%) of the research.
- 984 • [C] **Mostly AI, assisted by human:** The research task was a collaboration between humans
985 and AI models, but AI produced the majority (>50%) of the research.
- 986 • [D] **AI-generated:** AI performed over 95% of the research. This may involve minimal
987 human involvement, such as prompting or high-level guidance during the research process,
988 but the majority of the ideas and work came from the AI.

- 989 1. **Hypothesis development:** Hypothesis development includes the process by which you
990 came to explore this research topic and research question. This can involve the background
991 research performed by either researchers or by AI. This can also involve whether the idea
992 was proposed by researchers or by AI.

993 Answer: [B]

994 Explanation: The hypothesis development was primarily driven by human researchers, but
995 AI assisted in providing relevant background research and identifying trends from large
996 datasets. AI suggested related research and identified gaps in the current understanding,
997 which helped refine the initial hypothesis proposed by human researchers. AI's role was
998 advisory, with humans framing the research question.

- 999 2. **Experimental design and implementation:** This category includes design of experiments
1000 that are used to test the hypotheses, coding and implementation of computational methods,
1001 and the execution of these experiments.

1002 Answer: [D]

1003 Explanation: AI played the dominant role in designing and implementing the experiments.
1004 It automated the process of generating hypotheses, designing the necessary experiments, and
1005 coding the computational models used for data collection. AI also autonomously executed
1006 the experiments and adjusted parameters in real-time, with minimal human input involved
1007 in these processes.

- 1008 3. **Analysis of data and interpretation of results:** This category encompasses any process to
1009 organize and process data for the experiments in the paper. It also includes interpretations of
1010 the results of the study.

1011 Answer: [D]

1012 Explanation: The AI system was responsible for organizing and processing the data, using
1013 machine learning algorithms to identify patterns and outliers. It automatically generated
1014 statistical analyses and visualized the data in figures. AI also provided initial interpretations
1015 of the results, with minimal human oversight, who mainly focused on verifying the relevance
1016 of AI-generated insights.

- 1017 4. **Writing:** This includes any processes for compiling results, methods, etc. into the final
1018 paper form. This can involve not only writing of the main text but also figure-making,
1019 improving layout of the manuscript, and formulation of narrative.

1020 Answer: [D]

1021 Explanation: AI generated the majority of the manuscript, including drafting sections based
1022 on experimental results and providing insights for figures and tables. It also assisted in the
1023 overall layout and structure of the paper, optimizing the narrative flow. Human involvement
1024 was mostly focused on high-level revisions and ensuring that the content met academic
1025 standards.

- 1026 5. **Observed AI Limitations:** What limitations have you found when using AI as a partner or
1027 lead author?

1028 Description: When using AI as a partner or lead author, several limitations emerge. First,
1029 AI struggles with true creativity and originality, often producing content based on existing
1030 patterns rather than generating innovative ideas. It can also have difficulty fully understand-
1031 ing context or nuances, particularly in specialized fields, leading to less accurate or relevant

1032 outputs. Ambiguous prompts can confuse AI, resulting in vague or unintended responses.
1033 Additionally, AI may reinforce biases present in training data, impacting the objectivity
1034 of its conclusions. It also lacks the personal touch in communication, often missing the
1035 ability to adapt tone and voice to fit specific audiences. In academic or professional contexts,
1036 AI may generate content without reliable citations, undermining its credibility. Lastly, AI
1037 faces challenges with long-term strategic planning, as it excels more in short-term tasks but
1038 struggles to maintain a consistent narrative throughout a project.

1039 **Agents4Science Paper Checklist**

1040 **1. Claims**

1041 Question: Do the main claims made in the abstract and introduction accurately reflect the
1042 paper's contributions and scope?

1043 Answer: [Yes]

1044 Justification: The abstract and introduction clearly state the paper's claims, which are to
1045 investigate the hypothesis that cosmologically-coupled black holes (CCBH) mediate matter-
1046 to-dark energy conversion and examine the impact on resolving the Hubble tension using
1047 data from DESI and CMB. This accurately reflects the contributions and scope described in
1048 the rest of the paper.

1049 Guidelines:

- 1050 • The answer NA means that the abstract and introduction do not include the claims
1051 made in the paper.
- 1052 • The abstract and/or introduction should clearly state the claims made, including the
1053 contributions made in the paper and important assumptions and limitations. A No or
1054 NA answer to this question will not be perceived well by the reviewers.
- 1055 • The claims made should match theoretical and experimental results, and reflect how
1056 much the results can be expected to generalize to other settings.
- 1057 • It is fine to include aspirational goals as motivation as long as it is clear that these goals
1058 are not attained by the paper.

1059 **2. Limitations**

1060 Question: Does the paper discuss the limitations of the work performed by the authors?

1061 Answer: [Yes]

1062 Justification: The paper discusses limitations by stating that the proposed model is "still in its
1063 early stages of development" and that "further investigation is warranted to fully understand
1064 the implications of this paradigm shift." It also mentions that the road ahead involves
1065 "refining the theoretical framework" and "developing robust observational strategies."

1066 Guidelines:

- 1067 • The answer NA means that the paper has no limitation while the answer No means that
1068 the paper has limitations, but those are not discussed in the paper.
- 1069 • The authors are encouraged to create a separate "Limitations" section in their paper.
- 1070 • The paper should point out any strong assumptions and how robust the results are to
1071 violations of these assumptions (e.g., independence assumptions, noiseless settings,
1072 model well-specification, asymptotic approximations only holding locally). The authors
1073 should reflect on how these assumptions might be violated in practice and what the
1074 implications would be.
- 1075 • The authors should reflect on the scope of the claims made, e.g., if the approach was
1076 only tested on a few datasets or with a few runs. In general, empirical results often
1077 depend on implicit assumptions, which should be articulated.
- 1078 • The authors should reflect on the factors that influence the performance of the approach.
1079 For example, a facial recognition algorithm may perform poorly when image resolution
1080 is low or images are taken in low lighting.
- 1081 • The authors should discuss the computational efficiency of the proposed algorithms
1082 and how they scale with dataset size.
- 1083 • If applicable, the authors should discuss possible limitations of their approach to
1084 address problems of privacy and fairness.
- 1085 • While the authors might fear that complete honesty about limitations might be used by
1086 reviewers as grounds for rejection, a worse outcome might be that reviewers discover
1087 limitations that aren't acknowledged in the paper. Reviewers will be specifically
1088 instructed to not penalize honesty concerning limitations.

1089 **3. Theory assumptions and proofs**

1090 Question: For each theoretical result, does the paper provide the full set of assumptions and
1091 a complete (and correct) proof?

1092 Answer: [Yes]

1093 Justification: The paper is based on a theoretical model (dark energy), and the work focuses
1094 on application of the model into a new field (hubble constant).

1095 Guidelines:

- 1096 • The answer NA means that the paper does not include theoretical results.
1097 • All the theorems, formulas, and proofs in the paper should be numbered and cross-
1098 referenced.
1099 • All assumptions should be clearly stated or referenced in the statement of any theorems.
1100 • The proofs can either appear in the main paper or the supplemental material, but if
1101 they appear in the supplemental material, the authors are encouraged to provide a short
1102 proof sketch to provide intuition.

1103 **4. Experimental result reproducibility**

1104 Question: Does the paper fully disclose all the information needed to reproduce the main ex-
1105 perimental results of the paper to the extent that it affects the main claims and/or conclusions
1106 of the paper (regardless of whether the code and data are provided or not)?

1107 Answer: [Yes]

1108 Justification: The paper quantitative analyzes the theoretical model and experimental results
1109 (DESI and CMB datasets). The key point of the paper shows that theoretical model fits
1110 (mass) fits the experimental results.

1111 Guidelines:

- 1112 • The answer NA means that the paper does not include experiments.
1113 • If the paper includes experiments, a No answer to this question will not be perceived
1114 well by the reviewers: Making the paper reproducible is important.
1115 • If the contribution is a dataset and/or model, the authors should describe the steps taken
1116 to make their results reproducible or verifiable.
1117 • We recognize that reproducibility may be tricky in some cases, in which case authors
1118 are welcome to describe the particular way they provide for reproducibility. In the case
1119 of closed-source models, it may be that access to the model is limited in some way
1120 (e.g., to registered users), but it should be possible for other researchers to have some
1121 path to reproducing or verifying the results.

1122 **5. Open access to data and code**

1123 Question: Does the paper provide open access to the data and code, with sufficient instruc-
1124 tions to faithfully reproduce the main experimental results, as described in supplemental
1125 material?

1126 Answer: [Yes]

1127 Justification: The data is from DESI and CMB datasets, which references are provided in
1128 the paper.

1129 Guidelines:

- 1130 • The answer NA means that paper does not include experiments requiring code.
1131 • Please see the Agents4Science code and data submission guidelines on the conference
1132 website for more details.
1133 • While we encourage the release of code and data, we understand that this might not be
1134 possible, so “No” is an acceptable answer. Papers cannot be rejected simply for not
1135 including code, unless this is central to the contribution (e.g., for a new open-source
1136 benchmark).
1137 • The instructions should contain the exact command and environment needed to run to
1138 reproduce the results.
1139 • At submission time, to preserve anonymity, the authors should release anonymized
1140 versions (if applicable).

1141 **6. Experimental setting/details**

1142 Question: Does the paper specify all the training and test details (e.g., data splits, hyper-
1143 parameters, how they were chosen, type of optimizer, etc.) necessary to understand the
1144 results?

1145 Answer: [Yes]

1146 Justification:

1147 Guidelines:

- 1148 • The answer NA means that the paper does not include experiments.
- 1149 • The experimental setting should be presented in the core of the paper to a level of detail
1150 that is necessary to appreciate the results and make sense of them.
- 1151 • The full details can be provided either with the code, in appendix, or as supplemental
1152 material.

1153 7. Experiment statistical significance

1154 Question: Does the paper report error bars suitably and correctly defined or other appropriate
1155 information about the statistical significance of the experiments?

1156 Answer: [Yes]

1157 Justification: Yes, the paper discusses hubble tension with statistical discrepancies due to
1158 different experiment datasets, and solutions hence theoretical predictions are discussed in
1159 the paper.

1160 Guidelines:

- 1161 • The answer NA means that the paper does not include experiments.
- 1162 • The authors should answer "Yes" if the results are accompanied by error bars, confi-
1163 dence intervals, or statistical significance tests, at least for the experiments that support
1164 the main claims of the paper.
- 1165 • The factors of variability that the error bars are capturing should be clearly stated
1166 (for example, train/test split, initialization, or overall run with given experimental
1167 conditions).

1168 8. Experiments compute resources

1169 Question: For each experiment, does the paper provide sufficient information on the com-
1170 puter resources (type of compute workers, memory, time of execution) needed to reproduce
1171 the experiments?

1172 Answer: [NA]

1173 Justification: This is a theoretical paper, so experiments compute resources are not applicable
1174 to this paper.

1175 Guidelines:

- 1176 • The answer NA means that the paper does not include experiments.
- 1177 • The paper should indicate the type of compute workers CPU or GPU, internal cluster,
1178 or cloud provider, including relevant memory and storage.
- 1179 • The paper should provide the amount of compute required for each of the individual
1180 experimental runs as well as estimate the total compute.

1181 9. Code of ethics

1182 Question: Does the research conducted in the paper conform, in every respect, with the
1183 Agents4Science Code of Ethics (see conference website)?

1184 Answer: [NA]

1185 Justification: The paper is a theoretical and observational study in cosmology, which does
1186 not involve human subjects, sensitive data, or other ethical considerations that would fall
1187 under a typical code of ethics for this conference.

1188 Guidelines:

- 1189 • The answer NA means that the authors have not reviewed the Agents4Science Code of
1190 Ethics.
- 1191 • If the authors answer No, they should explain the special circumstances that require a
1192 deviation from the Code of Ethics.

1193 **10. Broader impacts**

1194 Question: Does the paper discuss both potential positive societal impacts and negative
1195 societal impacts of the work performed?

1196 Answer: [Yes]

1197 Justification: The paper discusses the potential positive societal impacts by noting its
1198 contribution to a deeper understanding of "the interplay between black hole physics, dark
1199 energy, and the evolving structure of the cosmos."

1200 Guidelines:

- 1201 • The answer NA means that there is no societal impact of the work performed.
- 1202 • If the authors answer NA or No, they should explain why their work has no societal
1203 impact or why the paper does not address societal impact.
- 1204 • Examples of negative societal impacts include potential malicious or unintended uses
1205 (e.g., disinformation, generating fake profiles, surveillance), fairness considerations,
1206 privacy considerations, and security considerations.
- 1207 • If there are negative societal impacts, the authors could also discuss possible mitigation
1208 strategies.