

-

Tutorial

R Tutorial (R-Tutorial.html)

ggplot2

ggplot2 Short Tutorial (ggplot2-Tutorial-With-R.html)

ggplot2 Tutorial 1 - Intro (Complete-Ggplot2-Tutorial-Part1-With-R-Code.html)

ggplot2 Tutorial 2 - Theme (Complete-Ggplot2-Tutorial-Part2-Customizing-Theme-With-R-Code.html)

ggplot2 Tutorial 3 - Masterlist (Top50-Ggplot2-Visualizations-MasterList-R-Code.html)

ggplot2 Quickref (ggplot2-cheatsheet.html)

Foundations

Linear Regression (Linear-Regression.html)

Statistical Tests (Statistical-Tests-in-R.html)

Missing Value Treatment (Missing-Value-Treatment-With-R.html)

Outlier Analysis (Outlier-Treatment-With-R.html)

Feature Selection (Variable-Selection-and-Importance-With-R.html)

Model Selection (Model-Selection-in-R.html)

Logistic Regression (Logistic-Regression-With-R.html)

Advanced Linear Regression (Environments.html)

Advanced Regression Models

Advanced Regression Models (adv-regression-models.html)

Time Series

Time Series Analysis (Time-Series-Analysis-With-R.html)

Time Series Forecasting (Time-Series-Forecasting-With-R.html)

More Time Series Forecasting ([Time-Series-Forecasting-With-R-part2.html](#))

High Performance Computing

Parallel computing ([Parallel-Computing-With-R.html](#))

Strategies to Speedup R code ([Strategies-To-Improve-And-Speedup-R-Code.html](#))

Useful Techniques

Association Mining ([Association-Mining-With-R.html](#))

Multi Dimensional Scaling ([Multi-Dimensional-Scaling-With-R.html](#))

Optimization ([Profiling.html](#))

InformationValue package ([Information-Value-With-R.html](#))

Stay up-to-date. Subscribe!

(https://docs.google.com/forms/d/1xkMYkLNFU9U39Dd8S_2JC0p8B5t6_Yq6zUQjanQQJpY/viewform)

Chat! (<https://docs.google.com/forms/d/13GrkCFcNa-TOIIIQghsz2SIEbc-YqY9eJX02B19I5Ow/viewform>)

Contents

Why outliers detection is important?

Detect outliers

Univariate approach

Bivariate approach

Multivariate Model Approach

Outliers Test

outliers package

Treating the outliers

Outlier Treatment

Outliers in data can distort predictions and affect the accuracy, if you don't detect and handle them appropriately especially in regression models.

Why outliers detection is important?

Treating or altering the outlier/extreme values in genuine observations is not a standard operating procedure. However, it is essential to understand their impact on your predictive models. It is left to the best judgement of the investigator to decide whether treating outliers is necessary and how to go about it.

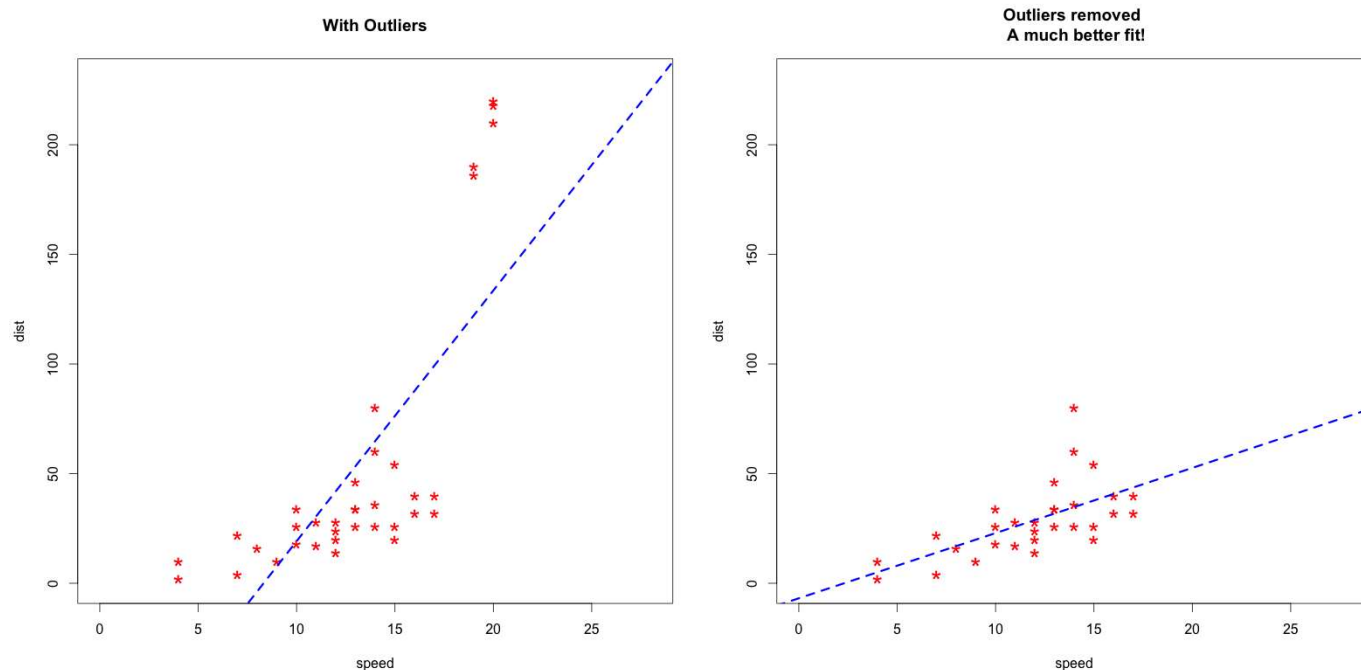
So, why identifying the extreme values is important? Because, it can drastically bias/change the fit estimates and predictions. Let me illustrate this using the cars dataset.

To better understand the implications of outliers better, I am going to compare the fit of a simple linear regression model on cars dataset *with* and *without* outliers. In order to distinguish the effect clearly, I manually introduce extreme values to the original cars dataset. Then, I predict on both the datasets.

```
# Inject outliers into data.
cars1 <- cars[1:30, ] # original data
cars_outliers <- data.frame(speed=c(19,19,20,20,20), dist=c(190, 186, 210, 220, 218)) #
introduce outliers.
cars2 <- rbind(cars1, cars_outliers) # data with outliers.
```

```
# Plot of data with outliers.
par(mfrow=c(1, 2))
plot(cars2$speed, cars2$dist, xlim=c(0, 28), ylim=c(0, 230), main="With Outliers", xlab=
"speed", ylab="dist", pch="*", col="red", cex=2)
abline(lm(dist ~ speed, data=cars2), col="blue", lwd=3, lty=2)
```

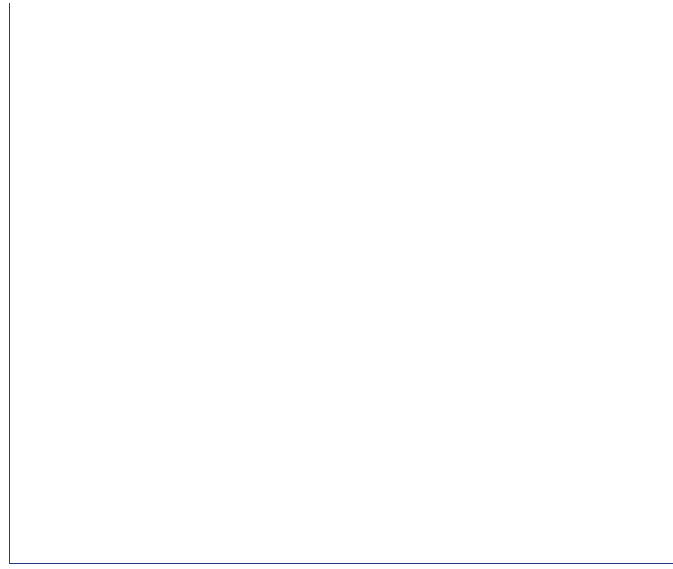
```
# Plot of original data without outliers. Note the change in slope (angle) of best fit l
ine.
plot(cars1$speed, cars1$dist, xlim=c(0, 28), ylim=c(0, 230), main="Outliers removed \n A
much better fit!", xlab="speed", ylab="dist", pch="*", col="red", cex=2)
abline(lm(dist ~ speed, data=cars1), col="blue", lwd=3, lty=2)
```



Notice the change in slope of the best fit line after removing the outliers. Had we used the outliers to train the model(left chart), our predictions would be exaggerated (high error) for larger values of speed because of the larger slope.

Detect outliers

Univariate approach



For a given continuous variable, outliers are those observations that lie outside $1.5 * IQR$, where IQR, the 'Inter Quartile Range' is the difference between 75th and 25th quartiles. Look at the points outside the whiskers in below box plot.

```
url <- "http://rstatistics.net/wp-content/uploads/2015/09/ozone.csv"
# alternate source: https://raw.githubusercontent.com/selva86/datasets/master/ozone.csv
inputData <- read.csv(url) # import data

outlier_values <- boxplot.stats(inputData$pressure_height)$out # outlier values.
boxplot(inputData$pressure_height, main="Pressure Height", boxwex=0.1)
mtext(paste("Outliers: ", paste(outlier_values, collapse=" ")), cex=0.6)
```

Bivariate approach

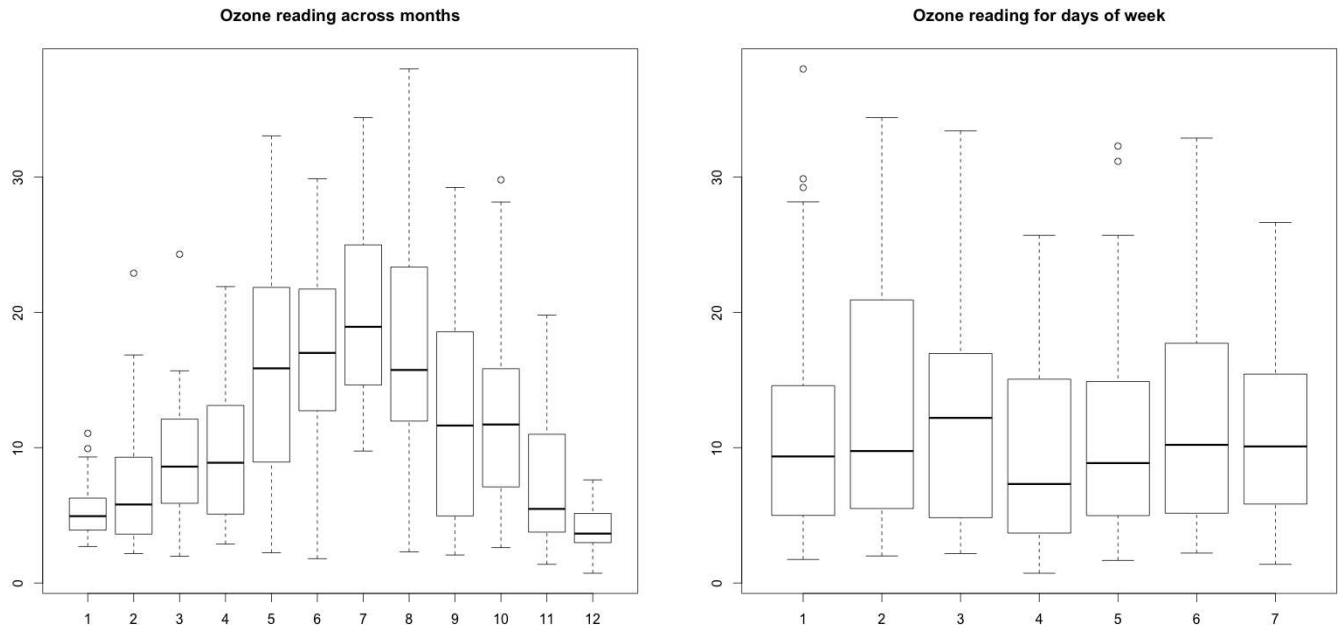
Visualize in box-plot of the X and Y, for categorical X's

```
url <- "http://rstatistics.net/wp-content/uploads/2015/09/ozone.csv"
ozone <- read.csv(url)
```

```
# For categorical variable
```

```
boxplot(ozone_reading ~ Month, data=ozone, main="Ozone reading across months") # clear
pattern is noticeable.
```

```
boxplot(ozone_reading ~ Day_of_week, data=ozone, main="Ozone reading for days of week")
# this may not be significant, as day of week variable is a subset of the month var.
```

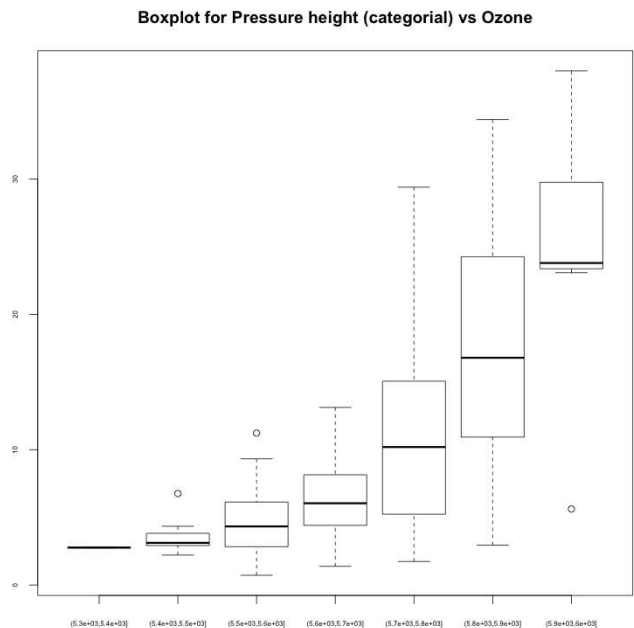
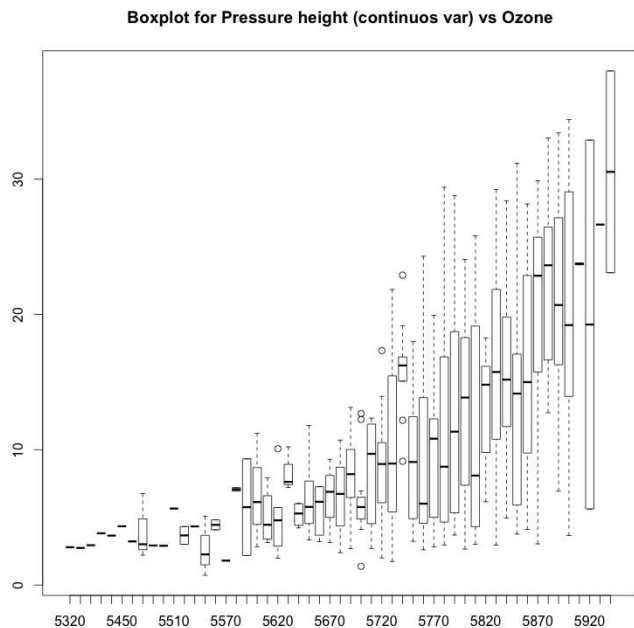


What is the inference? The change in the level of boxes suggests that Month seem to have an impact in ozone_reading while Day_of_week does not. Any outliers in respective categorical level show up as dots outside the whiskers of the boxplot.

```
# For continuous variable (convert to categorical if needed.)
```

```
boxplot(ozone_reading ~ pressure_height, data=ozone, main="Boxplot for Pressure height
(continuos var) vs Ozone")
```

```
boxplot(ozone_reading ~ cut(pressure_height, pretty(inputData$pressure_height)), data=oz
one, main="Boxplot for Pressure height (categorical) vs Ozone", cex.axis=0.5)
```



You can see few outliers in the box plot and how the ozone_reading increases with pressure_height. That's clear.

Multivariate Model Approach

Declaring an observation as an outlier based on a just one (rather unimportant) feature could lead to unrealistic inferences. When you have to decide if an individual entity (represented by row or observation) is an extreme value or not, it's better to collectively consider the features (X's) that matter. Enter Cook's Distance.

Cook's Distance

Cook's distance is a measure computed with respect to a given regression model and therefore is impacted only by the X variables included in the model. But, what does Cook's distance mean? It computes the influence exerted by each data point (row) on the predicted outcome.

The cook's distance for each observation i measures the change in \hat{Y} (fitted Y) for all observations with and without the presence of observation i , so we know how much the observation i impacted the fitted values. Mathematically, cook's distance D_i for observation i is computed as:

$$D_i = \frac{\sum_{j=1}^n \left(\hat{Y}_j - \hat{Y}_{j(i)} \right)^2}{p \times MSE}$$

where,

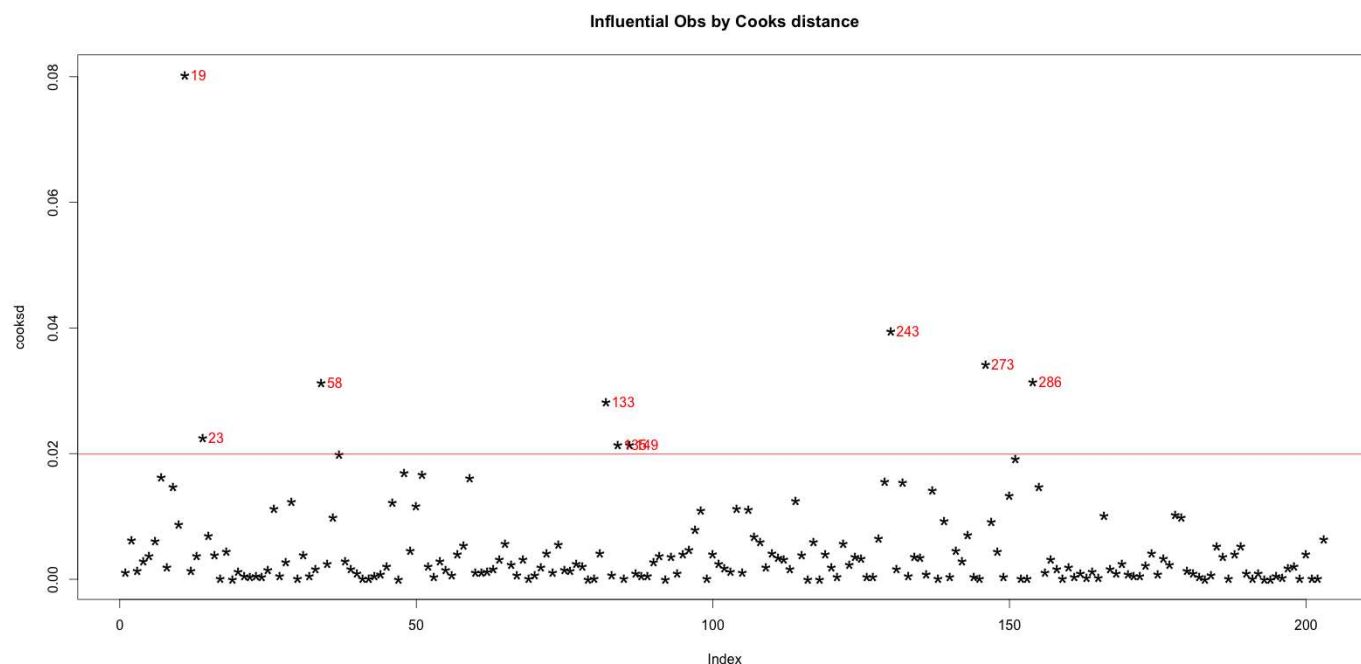
- \hat{Y}_j is the value of j_{th} fitted response when all the observations are included.
- $\hat{Y}_{j(i)}$ is the value of j_{th} fitted response, where the fit does not include observation i .
- MSE is the mean squared error.
- p is the number of coefficients in the regression model.

```
mod <- lm(ozone_reading ~ ., data=ozone)
cooks_d <- cooks.distance(mod)
```

Influence measures

In general use, those observations that have a cook's distance greater than 4 times the mean may be classified as influential. This is not a hard boundary.

```
plot(cooks_d, pch="*", cex=2, main="Influential Obs by Cooks distance") # plot cook's distance
abline(h = 4*mean(cooks_d, na.rm=T), col="red") # add cutoff line
text(x=1:length(cooks_d)+1, y=cooks_d, labels=ifelse(cooks_d>4*mean(cooks_d, na.rm=T), names
(cooks_d), ""), col="red") # add labels
```



Now let's find out the influential rows from the original data. If you extract and examine each influential row 1-by-1 (from below output), you will be able to reason out why that row turned out influential. It is likely that one of the X variables included in the model had extreme values.

```
influential <- as.numeric(names(cooksd)[(cooksd > 4*mean(cooksd, na.rm=T))]) # influential row numbers
head(ozone[influential, ]) # influential observations.
```

#>	Month	Day_of_month	Day_of_week	ozone_reading	pressure_height	Wind_speed	Humidity
#> 19	1	19	1	4.07	5680	5	73
#> 23	1	23	5	4.90	5700	5	59
#> 58	2	27	5	22.89	5740	3	47
#> 133	5	12	3	33.04	5880	3	80
#> 135	5	14	5	31.15	5850	4	76
#> 149	5	28	5	4.82	5750	3	76

#>	Temperature_Sandburg	Temperature_ElMonte	Inversion_base_height	Pressure_gradient
#> 19		52	56.48	393
#> 23		69	51.08	3044
#> 58		53	58.82	885
#> 133		80	73.04	436
#> 135		78	71.24	1181
#> 149		65	51.08	3644

#>	Inversion_temperature	Visibility
#> 19	69.80	10
#> 23	52.88	150
#> 58	67.10	80
#> 133	86.36	40
#> 135	79.88	17
#> 149	59.36	70

Lets examine the first 6 rows from above output to find out why these rows could be tagged as *influential observations*.

- Row 58, 133, 135 have very high ozone_reading.
- Rows 23, 135 and 149 have very high Inversion_base_height.
- Row 19 has very low Pressure_gradient.

Outliers Test

The function `outlierTest` from `car` package gives the most extreme observation based on the given model. Here's an example based on the `mod` linear model object we'd just created.

```
car::outlierTest(mod)
#> No Studentized residuals with Bonferonni  $p < 0.05$ 
#> Largest  $|rstudent|$ :
#>       $rstudent$  unadjusted  $p$ -value Bonferonni  $p$ 
#> 243 3.045756      0.0026525      0.53845
```

This output suggests that observation in row 243 is most extreme.

outliers package

The outliers package (<https://cran.r-project.org/web/packages/outliers/index.html>) provides a number of useful functions to systematically extract outliers. Some of these are convenient and come handy, especially the `outlier()` and `scores()` functions.

outliers

`outliers` gets the extreme most observation from the mean. If you set the argument `opposite=TRUE`, it fetches from the other side.

```

set.seed(1234)
y=rnorm(100)
outlier(y)
#> [1] 2.548991
outlier(y,opposite=TRUE)
#> [1] -2.345698
dim(y) <- c(20,5) # convert it to a matrix
outlier(y)
#> [1] 2.415835 1.102298 1.647817 2.548991 2.121117
outlier(y,opposite=TRUE)
#> [1] -2.345698 -2.180040 -1.806031 -1.390701 -1.372302

```

scores

There are two aspects to the `scores()` function.

1. Compute the normalised scores based on “z”, “t”, “chisq” etc
2. Find out observations that lie beyond a given percentile based on a given score.

```

set.seed(1234)
x = rnorm(10)
scores(x) # z-scores => (x-mean)/sd
scores(x, type="chisq") # chi-sq scores => (x - mean(x))^2/var(x)
#> [1] 0.68458034 0.44007451 2.17210689 3.88421971 0.66539631 . . .
scores(x, type="t") # t scores

```

```

scores(x, type="chisq", prob=0.9) # beyond 90th %ile based on chi-sq
#> [1] FALSE FALSE FALSE TRUE FALSE FALSE FALSE FALSE FALSE
scores(x, type="chisq", prob=0.95) # beyond 95th %ile
scores(x, type="z", prob=0.95) # beyond 95th %ile based on z-scores
scores(x, type="t", prob=0.95) # beyond 95th %ile based on t-scores

```

Treating the outliers

Once the outliers are identified and you have decided to make amends as per the nature of the problem, you may consider one of the following approaches.

1. Imputation

Imputation with mean / median / mode. This method has been dealt with in detail in the discussion about treating missing values (<http://r-statistics.co/Missing-Value-Treatment-With-R.html#3.%20Imputation%20with%20mean%20/%20median%20/%20mode>).

2. Capping

For missing values that lie outside the $1.5 * IQR$ limits, we could cap it by replacing those observations outside the lower limit with the value of 5th %ile and those that lie above the upper limit, with the value of 95th %ile. Below is a sample code that achieves this.

```
x <- ozone$pressure_height
qnt <- quantile(x, probs=c(.25, .75), na.rm = T)
caps <- quantile(x, probs=c(.05, .95), na.rm = T)
H <- 1.5 * IQR(x, na.rm = T)
x[x < (qnt[1] - H)] <- caps[1]
x[x > (qnt[2] + H)] <- caps[2]
```

3. Prediction

In yet another approach, the outliers can be replaced with missing values (NA) and then can be predicted by considering them as a response variable. We already discussed how to predict missing values (<http://r-statistics.co/Missing-Value-Treatment-With-R.html#4.%20Prediction>).

Have a suggestion or found a bug? Notify here.

(<https://docs.google.com/forms/d/e/1FAIpQLSeIJmlvwe562R7JVpi5J2ydLyhk5-7OrGRMFGYrMJvjPal8eA/viewform>)

 **ezoic** (<https://www.ezoic.com/what-is-ezoic/>)
report this ad

© 2016-17 Selva Prabhakaran. Powered by jekyll (<http://jekyllrb.com/>), knitr (<http://yihui.name/knitr/>), and pandoc (<http://johnmacfarlane.net/pandoc/>). This work is licensed under the Creative Commons License. (<http://creativecommons.org/licenses/by-nc/3.0/>)