

Sparse Matrix Computations:

sep 3, 2013

- Sparse: $n \times n$ matrix has n^2 entries
 $O(n)$ non-zeros (Chen's defn).
"approximately"
- Sparse "in spirit": fast matrix-vector products ($O(n)$)
- Sparse matrix computations: based, @ least partially, on matrix-vector products
↳ interesting if they involve $O(n)$ flops
- dense matrix computations: factorizations / decompositions (direct methods).
- "typical" sparse $n \times n$ matrix algorithm: based on solving (iteratively, often) related problems using matrix-vector products with $n \times n$ matrices + decompositions related to smaller matrices.

Problems we are interested in

- linear systems
- eigenvalue problems
- least-squares problems
- problems w/ constraints

arising from

- PDEs
- constrained optimization
- applications (eg. social networks)

Focus: methods + algorithms

- methods: iterative (CG, GMRES, Bi-CG-stab, MINRES) : Krylov Subspace Methods, direct methods
eigenvalue: power method, simultaneous iterations, Arnoldi / Lanczos, Jacobi-Davidson
least-squares: LSQR, LSMR, CGLS
constraints: all kinds of constrained-sparse

course web-page: www.cs.ubc.ca/~greif
↳teaching

Chen away Sept 25+27