



Form ever follows function.

—Louis Sullivan

E pluribus unum.

(One composed of many.)

—Virgil

*O! call back yesterday, bid
time return.*

—William Shakespeare

Call me Ishmael.

—Herman Melville

*When you call me that,
smile.*

—Owen Wister

JavaScript: Functions

OBJECTIVES

In this chapter you will learn:

- To construct programs modularly from small pieces called functions.
- To create new functions.
- How to pass information between functions.
- Simulation techniques that use random number generation.
- How the visibility of identifiers is limited to specific regions of programs.

Self-Review Exercises

9.1 Fill in the blanks in each of the following statements:

a) Program modules in JavaScript are called _____.

ANS: functions.

b) A function is invoked using a(n) _____.

ANS: function call.

c) A variable known only within the function in which it is defined is called a(n) _____.

ANS: local variable.

d) The _____ statement in a called function can be used to pass the value of an expression back to the calling function.

ANS: return.

e) The keyword _____ indicates the beginning of a function definition.

ANS: function.

9.2 For the given program, state the scope (either global scope or function scope) of each of the following elements:

a) The variable x.

ANS: Global scope.

b) The variable y.

ANS: Function scope.

c) The function cube.

ANS: Global scope.

d) The function output.

ANS: Global scope.

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.2: cube.html -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Scoping</title>
9      <script type = "text/javascript">
10         <!--
11           var x;
12
13           function output()
14           {
15             for ( x = 1; x <= 10; x++ )
16               document.writeln( cube( x ) + "<br />" );
17           } // end function output
18
19           function cube( y )
20           {
21             return y * y * y;
22           } // end function cube
23         // -->
24       </script>
25     </head><body onload = "output()"></body>
26 </html>

```

9.3 Fill in the blanks in each of the following statements:

- a) Programmer-defined functions, global variables and JavaScript's global functions are all part of the _____ object.

ANS: Global.

- b) Function _____ determines if its argument is or is not a number.

ANS: isNaN.

- c) Function _____ takes a string argument and returns a string in which all spaces, punctuation, accent characters and any other character that is not in the ASCII character set are encoded in a hexadecimal format.

ANS: escape.

- d) Function _____ takes a string argument representing JavaScript code to execute.

ANS: eval.

- e) Function _____ takes a string as its argument and returns a string in which all characters that were previously encoded with escape are decoded.

ANS: unescape.

9.4 Fill in the blanks in each of the following statements:

- a) The _____ of an identifier is the portion of the program in which the identifier can be used.

ANS: scope.

- b) The three ways to return control from a called function to a caller are _____, _____ and _____.

ANS: return; or return *expression*; or encountering the closing right brace of a function.

- c) The _____ function is used to produce random numbers.

ANS: Math.random.

- d) Variables declared in a block or in a function's parameter list are of _____ scope.

ANS: local.

9.5 Locate the error in each of the following program segments and explain how to correct it:

- a) `method g()`

```
{
    document.writeln( "Inside method g" );
}
```

ANS: Error: method is not the keyword used to begin a function definition.

Correction: Change method to function.

- b) `// This function should return the sum of its arguments`

```
function sum( x, y )
{
    var result;
    result = x + y;
}
```

ANS: Error: The function is supposed to return a value, but does not.

Correction: Delete variable `result`, and either place the statement

`return x + y;`

in the function or add the following statement at the end of the function body:

`return result;`

- c) `function f(a);`

```
{
    document.writeln( a );
}
```

ANS: Error: The semicolon after the right parenthesis that encloses the parameter list.

Correction: Delete the semicolon after the right parenthesis of the parameter list.

9.6 Write a complete JavaScript program to prompt the user for the radius of a sphere, and call function `sphereVolume` to calculate and display the volume of the sphere. Use the statement

```
volume = ( 4.0 / 3.0 ) * Math.PI * Math.pow( radius, 3 );
```

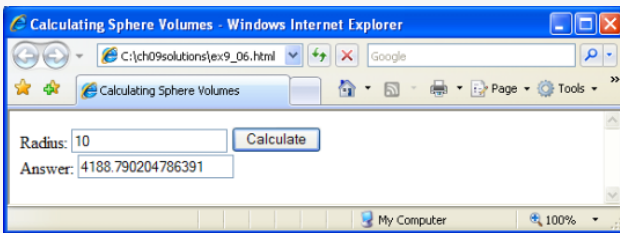
to calculate the volume. The user should input the radius through an XHTML text field in a `<form>` and click an XHTML button to initiate the calculation.

ANS: The following solution calculates the volume of a sphere using the radius entered by the user.

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.6: volume.html -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Calculating Sphere Volumes</title>
9      <script type = "text/javascript">
10        <!--
11          function displayVolume()
12          {
13            var inputField = document.getElementById( "radiusField" );
14            var radius = parseFloat( inputField.value );
15            var answerField = document.getElementById( "answer" );
16            answerField.value = sphereVolume( radius );
17          } // end function displayVolume
18
19          function sphereVolume( radius )
20          {
21            return ( 4.0 / 3.0 ) * Math.PI * Math.pow( radius, 3 );
22          } // end function sphereVolume
23          // -->
24        </script>
25      </head>
26      <body>
27        <form action = "">
28          <div>
29            <label>Radius:
30              <input id = "radiusField" type = "text" /></label>
31              <input type = "button" value = "Calculate"
32                onclick = "displayVolume()" />
33            <br />
34            <label>Answer:
35              <input id = "answer" type = "text" /></label>
36          </div>
37        </form>
38      </body>
39    </html>

```



Exercises

9.7 Write a script that prompts the user for the radius of a circle, uses a function `circleArea` to calculate the area of the circle, and prints the area of the circle.

```

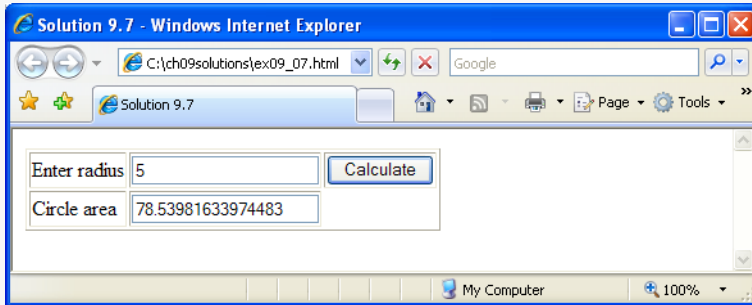
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.7: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.7</title>
9      <script type = "text/javascript">
10         <!--
11         function getArea()
12         {
13             var form = document.getElementById( "myForm" );
14             var input = parseFloat( form.number.value );
15             form.result.value = circleArea( input );
16         } // end function getArea
17
18         function circleArea( radius )
19         {
20             return Math.PI * radius * radius;
21         } // end function circleArea
22         // -->
23     </script>
24 </head>
25 <body>
26     <form id = "myForm" action = "">
27         <table border = "1">
28             <tr><td>Enter radius</td>
29                 <td><input id = "number" type = "text" />
30                 </td>
31                 <td><input type = "button" value = "Calculate"
32                     onclick = "getArea()" /></td>
33             </tr>
34             <tr><td>Circle area</td>
35                 <td><input id = "result" type = "text" />
36                 </td>
37             </tr>
38         </table>

```

```

39     </form>
40 </body>
41 </html>

```



9.8 A parking garage charges a \$2.00 minimum fee to park for up to three hours. The garage charges an additional \$0.50 per hour for each hour *or part thereof* in excess of three hours. The maximum charge for any given 24-hour period is \$10.00. Assume that no car parks for longer than 24 hours at a time. Write a script that calculates and displays the parking charges for each customer who parked a car in this garage yesterday. You should input from the user the hours parked for each customer. The program should display the charge for the current customer and should calculate and display the running total of yesterday's receipts. The program should use the function `calculateCharges` to determine the charge for each customer. Use a text input field to obtain the input from the user.

ANS:

```

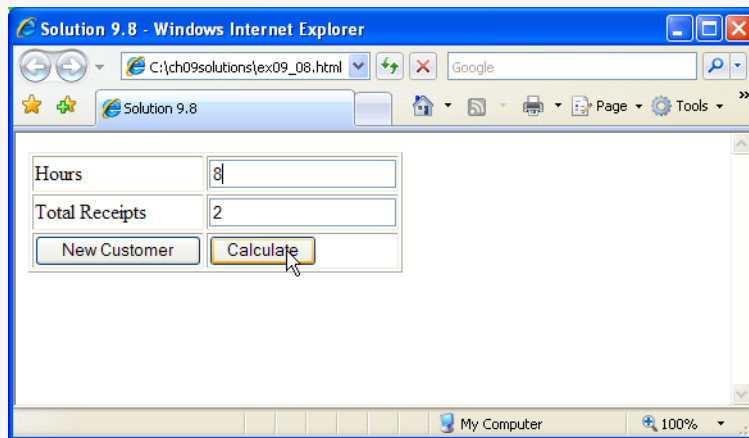
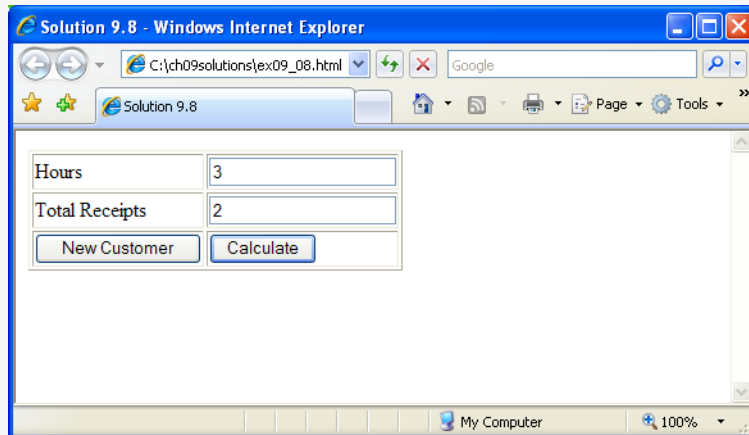
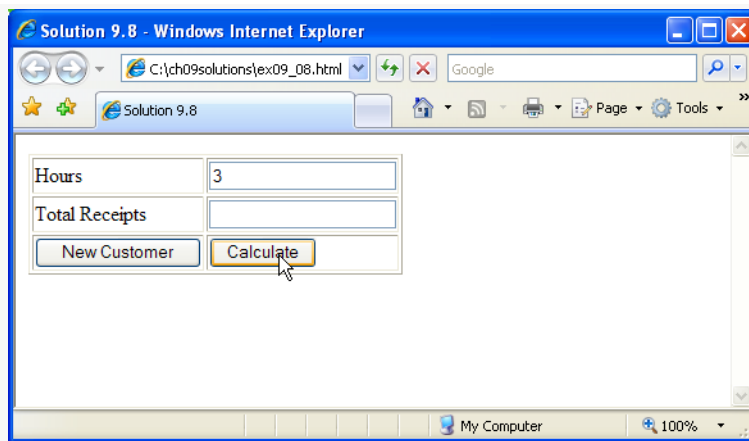
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.8: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.8</title>
9      <script type = "text/javascript">
10         <!--
11         var totalReceipts = 0;
12         var fee;
13
14         function init()
15         {
16             var hoursField = document.getElementById( "hours" );
17             var totalField = document.getElementById( "total" );
18             hoursField.value = 0;
19             totalField.value = "";
20         } // end function init
21
22         function getCharges()
23         {
24             var hoursField = document.getElementById( "hours" );
25             var totalField = document.getElementById( "total" );

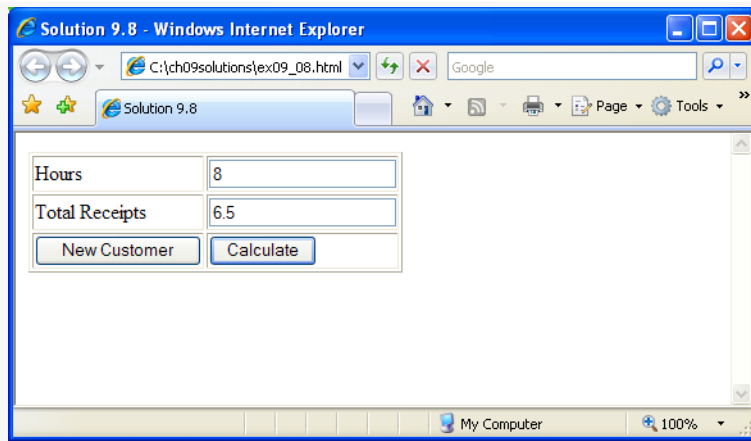
```

```

26     var hours = parseFloat( hoursField.value );
27     fee = calculateCharges( hours );
28     totalReceipts += fee;
29     totalField.value = parseFloat( totalReceipts );
30 } // end function getCharges
31
32 function calculateCharges( hours )
33 {
34     var charge = 0.0;
35
36     if ( hours <= 3.0 && hours > 0.0 )
37         charge = 2.0;
38     else if ( hours > 3.0 && hours <= 19.0 )
39         charge = 2.0 + 0.5 * Math.ceil( hours - 3.0 );
40     else if ( hours > 19.0 )
41         charge = 10.0;
42
43     return charge;
44 } // end function calculateCharges
45 // -->
46 </script>
47 </head>
48 <body>
49     <form action = "">
50         <table border = "1">
51             <tr><td>Hours</td>
52                 <td><input id = "hours" type = "text" /></td>
53             </tr>
54             <tr><td>Total Receipts</td>
55                 <td><input id = "total" type = "text" /></td>
56             </tr>
57             <tr><td>
58                 <input type = "button" value = "New Customer"
59                     onclick = "init()" /></td><td>
60                 <input type = "button" value = "Calculate"
61                     onclick = "getCharges()" />
62             </td>
63             </tr>
64         </table>
65     </form>
66 </body>
67 </html>

```





9.9 Write function `distance` that calculates the distance between two points $(x1, y1)$ and $(x2, y2)$. All numbers and return values should be floating-point values. You'll need the `Math.sqrt` method for calculating square roots. Incorporate this function into a script that enables the user to enter the coordinates of the points through an XHTML form.

ANS:

```

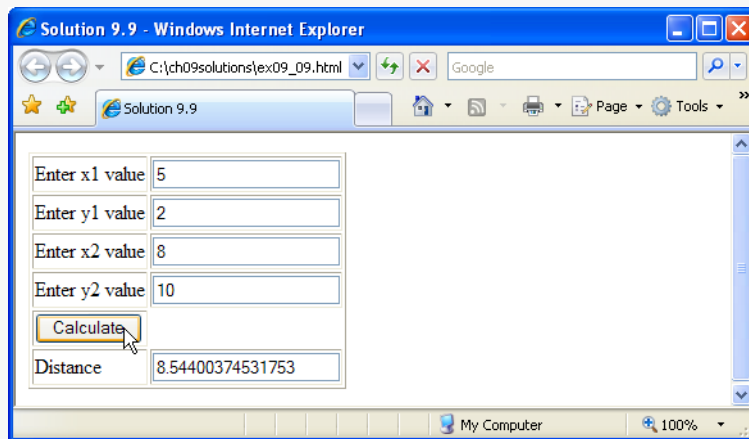
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.9: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.9</title>
9      <script type = "text/javascript">
10        <!--
11        function getDistance()
12        {
13          var form = document.getElementById( "myForm" );
14          var x1 = parseInt( form.x1.value );
15          var y1 = parseInt( form.y1.value );
16          var x2 = parseInt( form.x2.value );
17          var y2 = parseInt( form.y2.value );
18          form.result.value = distance( x1, y1, x2, y2 );
19        } // end function getDistance
20
21        function distance( x1, y1, x2, y2 )
22        {
23          return Math.sqrt( Math.pow( ( x1 - x2 ) , 2 )
24            + Math.pow( ( y1 - y2 ) , 2 ) );
25        } // end function distance
26        <!--
27      </script>
28    </head>
29    <body>
30      <form id = "myForm" action = "">

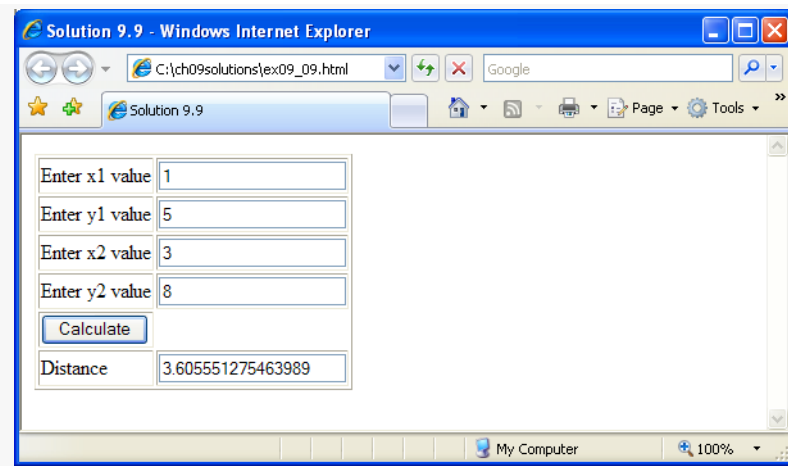
```

```

31     <table border = "1">
32         <tr><td>Enter x1 value</td>
33             <td><input name = "x1" type = "text" />
34         </td>
35     </tr>
36     <tr><td>Enter y1 value</td>
37         <td><input name = "y1" type = "text" />
38     </td>
39 </tr>
40 <tr><td>Enter x2 value</td>
41     <td><input name = "x2" type = "text" />
42 </td>
43 </tr>
44 <tr><td>Enter y2 value</td>
45     <td><input name = "y2" type = "text" />
46 </td>
47 </tr>
48 <tr><td colspan = "2" style = "text-align: right">
49     <input type = "button" value = "Calculate"
50     onclick = "getDistance()" /></td></tr>
51 <tr><td>Distance</td>
52     <td><input name = "result" type = "text" /></td>
53 </tr>
54 </table>
55 </form>
56 </body>
57 </html>

```





9.10 Answer each of the following questions:

a) What does it mean to choose numbers “at random”?

ANS: Every number has an equal chance of being chosen at any time.

b) Why is the `Math.random` function useful for simulating games of chance?

ANS: `Math.random` produces a series of random numbers between 0.1 and 1.0, and randomness is useful in making simulations appear realistic.

c) Why is it often necessary to scale and/or shift the values produced by `Math.random`?

ANS: To produce random numbers in a range other than 0.1 to 1.0.

d) Why is computerized simulation of real-world situations a useful technique?

ANS: It enables more accurate predictions of random events such as cars arriving at toll booths and people arriving in lines at a supermarket. The results of a simulation can help determine how many toll booths to have open or how many cashiers to have open at a specified time.

9.11 Write statements that assign random integers to the variable `n` in the following ranges:

a) $1 \leq n \leq 2$

ANS: `n = Math.floor(1 + Math.random() * 2);`

b) $1 \leq n \leq 100$

ANS: `n = Math.floor(1 + Math.random() * 100);`

c) $0 \leq n \leq 9$

ANS: `n = Math.floor(Math.random() * 10);`

d) $1000 \leq n \leq 112$

ANS: `n = Math.floor(1000 + Math.random() * 113);`

e) $-1 \leq n \leq 1$

ANS: `n = Math.floor(-1 + Math.random() * 3);`

f) $-3 \leq n \leq 1$

ANS: `n = Math.floor(-3 + Math.random() * 15);`

9.12 For each of the following sets of integers, write a single statement that will print a number at random from the set:

a) 2, 4, 6, 8, 10.

ANS: `document.write((parseInt(Math.random() * 5) + 1) * 2);`

b) 3, 5, 7, 9, 11.

ANS: `document.write((parseInt(Math.random() * 5) + 1) * 2 + 1);`

c) 6, 10, 14, 18, 22.

ANS: `document.write(parseInt(Math.random() * 5) * 4 + 6);`

9.13 Write a function `integerPower(base, exponent)` that returns the value of $base^{exponent}$

For example, `integerPower(3, 4) = 3 * 3 * 3 * 3`. Assume that `exponent` and `base` are integers. Function `integerPower` should use a `for` or `while` statement to control the calculation. Do not use any math library functions. Incorporate this function into a script that reads integer values from an XHTML form for `base` and `exponent` and performs the calculation with the `integerPower` function. The XHTML form should consist of two text fields and a button to initiate the calculation. The user should interact with the program by typing numbers in both text fields then clicking the button.

ANS:

```

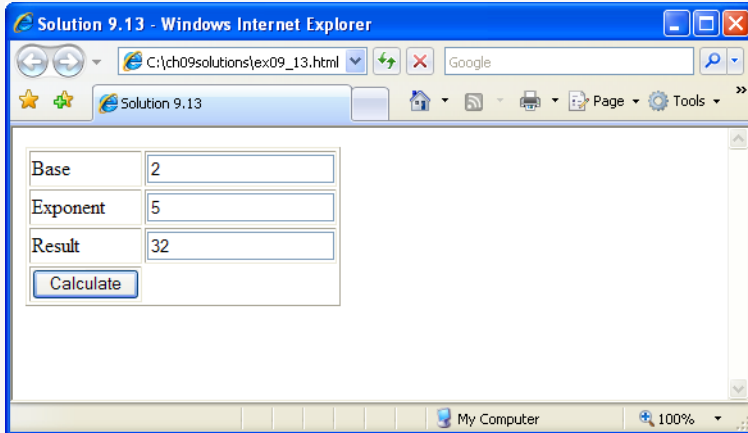
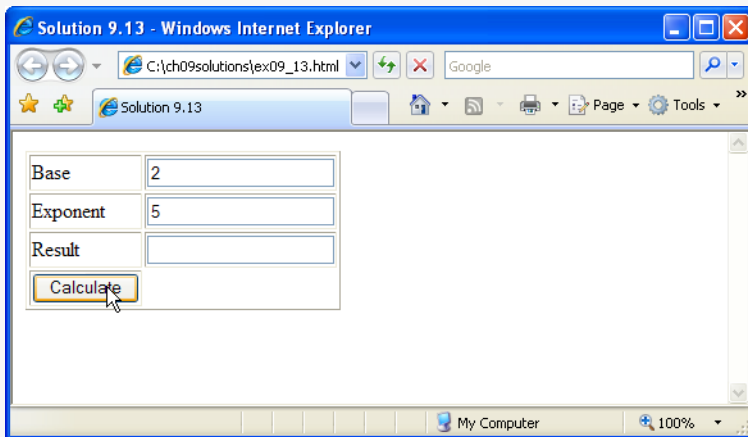
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.13: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.13</title>
9      <script type = "text/javascript">
10        <!--
11          function getExpo()
12          {
13            var form = document.getElementById( "myForm" );
14            var base;
15            var expo;
16            base = parseInt( form.base.value );
17            expo = parseInt( form.expo.value );
18            form.result.value = integerPower( base, expo );
19          } // end function getExpo
20
21          function integerPower( base, expo )
22          {
23            var result = 1;
24
25            for( var i = 0; i < expo; ++i )
26              result *= base;
27
28            return result;
29          } // end function integerPower
30        // -->
31      </script>
32    </head>
33    <body>
34      <form id = "myForm" action = "">
35        <table border = "1">
36          <tr><td>Base</td>
37            <td><input name = "base" type = "text" /></td>
38          </tr>
39          <tr><td>Exponent</td>
40            <td><input name = "expo" type = "text" /></td>
41          </tr>

```

```

42         <tr><td>Result</td>
43             <td><input name = "result" type = "text" />
44             </td>
45         </tr>
46         <tr><td>
47             <input type = "button" value = "Calculate"
48                 onclick = "getExpo()" />
49         </td></tr>
50     </table>
51 </form>
52 </body>
53 </html>

```



9.14 Write a function `multiple` that determines, for a pair of integers, whether the first integer is a multiple of the second. The function should take two integer arguments and return `true` if the first is a multiple of the second, and `false` otherwise. Incorporate this function into a script that inputs a series of pairs of integers (one pair at a time). The XHTML form should consist of two text fields and a button to initiate the calculation. The user should interact with the program by typing numbers in both text fields, then clicking the button.

ANS:

```

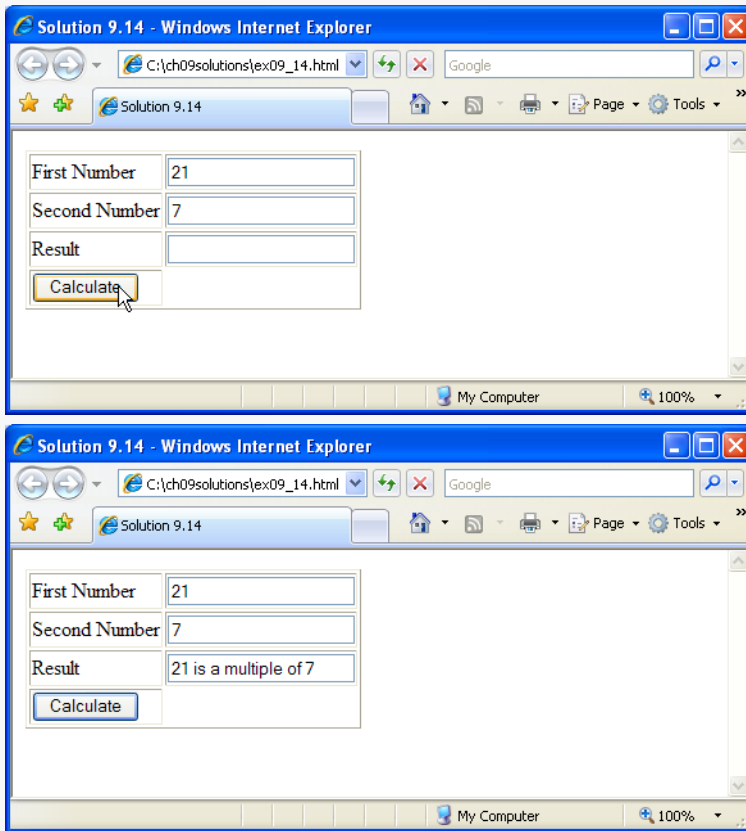
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.14: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.14</title>
9      <script type = "text/javascript">
10        <!--
11          function testMult()
12          {
13            var num1;
14            var num2;
15            var result;
16            var form = document.getElementById( "myForm" );
17            num1 = parseInt( form.num1.value );
18            num2 = parseInt( form.num2.value );
19
20            if ( multiple( num1, num2 ) )
21              form.result.value =
22                num1 + " is a multiple of " + num2;
23            else
24              form.result.value =
25                num1 + " is not a multiple of " + num2;
26          } // end function testMult
27
28          function multiple( num1, num2 )
29          {
30            return ( ( num1 % num2 ) == 0 )
31          } // end function multiple
32          // -->
33        </script>
34      </head>
35      <body>
36        <form id = "myForm" action = "">
37          <table border = "1">
38            <tr><td>First Number</td>
39              <td><input name = "num1" type = "text" /></td>
40            </tr>
41            <tr><td>Second Number</td>
42              <td><input name = "num2" type = "text" /></td>
43            </tr>
44            <tr><td>Result</td>
45              <td><input name = "result" type = "text" />
46            </td>
47            </tr>
48            <tr><td>
49              <input type = "button" value = "Calculate"
50                onclick = "testMult()" /></td>
51            </tr>
52          </table>

```

```

53     </form>
54 </body>
55 </html>

```



9.15 Write a script that inputs integers (one at a time) and passes them one at a time to function `isEven`, which uses the modulus operator to determine whether an integer is even. The function should take an integer argument and return `true` if the integer is even and `false` otherwise. Use sentinel-controlled looping and a prompt dialog.

ANS:

```

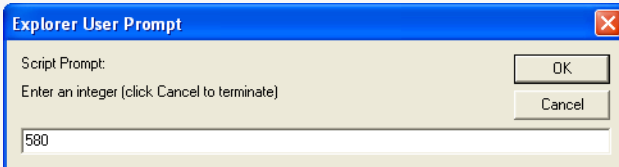
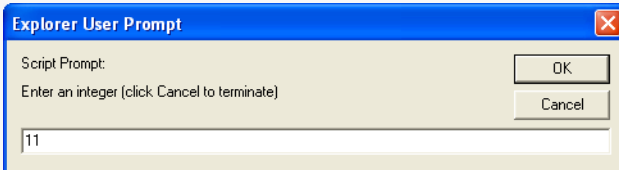
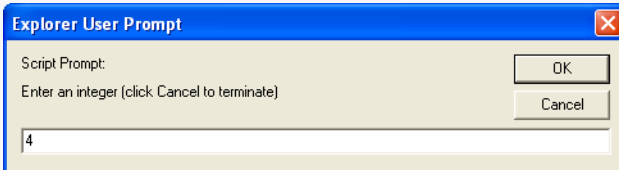
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.15: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.15</title>
9      <script type = "text/javascript">
10        <!--
11          var input;

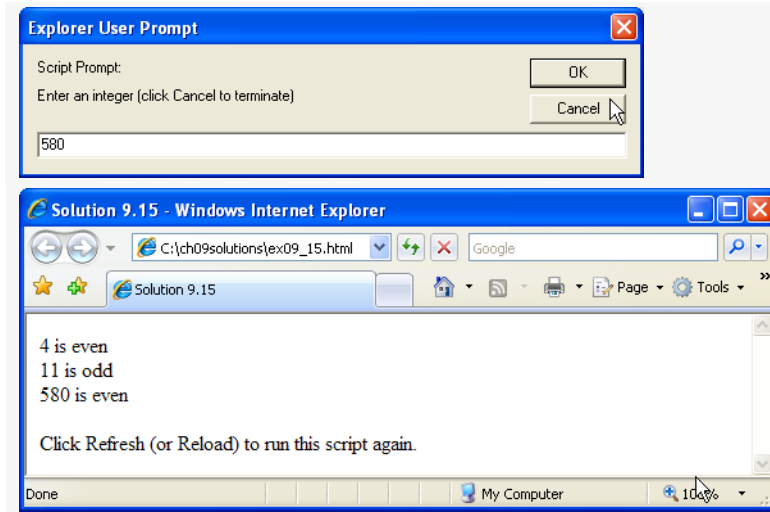
```

```

12     var value;
13
14     input = window.prompt(
15         "Enter an integer (click Cancel to terminate)", "0");
16
17     while ( input )
18     {
19         value = parseInt( input );
20         document.write( value + ( isEven( value ) ?
21             " is even" : " is odd" ) );
22         document.writeln( "<br />" );
23
24         input = window.prompt(
25             "Enter an integer (click Cancel to terminate)",
26             "0" );
27     } // end while
28
29     // this function executes only when called
30     function isEven( num )
31     {
32         return ( num % 2 == 0 );
33     } // end function isEven
34     // -->
35 </script>
36 </head>
37 <body>
38     <p>Click Refresh (or Reload) to run this script again.</p>
39 </body>
40 </html>

```





9.16 Write a function `squareOfAsterisks` that displays a solid square of asterisks whose side is specified in integer parameter `side`. For example, if `side` is 4, the function displays

```
****
****
****
****
```

Incorporate this function into a script that reads an integer value for `side` from the user at the keyboard and performs the drawing with the `squareOfAsterisks` function.

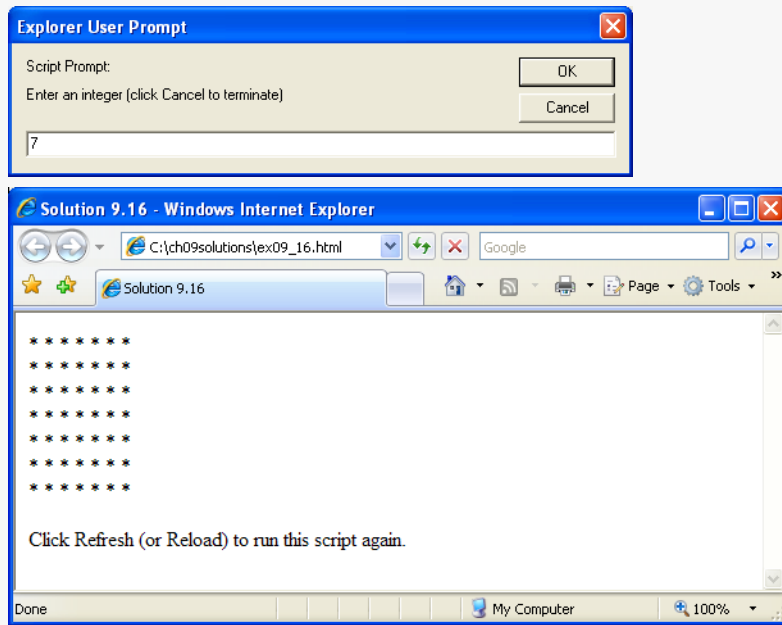
ANS:

```
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.16: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.16</title>
9      <script type = "text/javascript">
10        <!--
11          var input;
12
13          input = window.prompt(
14            "Enter an integer (click Cancel to terminate)", "0");
15
16          squareOfAsterisks( parseInt( input ) );
17
18          // this function executes only when called
19          function squareOfAsterisks( size )
20          {
21            for ( var a = 1; a <= size * size; ++a )
22            {
23              document.write( "* " );
```

```

24         if ( a % size == 0 )
25             document.write( "<br />" );
26     } // end for
27 } // end function squareOfAsterisks
28 // -->
29 </script>
30 </head>
31 <body>
32     <p>Click Refresh (or Reload) to run this script again.</p>
33 </body>
34 </html>

```



9.17 Modify the script created in Exercise 9.16 to also prompt the user for a character which will be used to create the square. Thus, if side is 5 and fillCharacter is #, the function should print

```

#####
#####
#####
#####
#####

```

ANS:

```

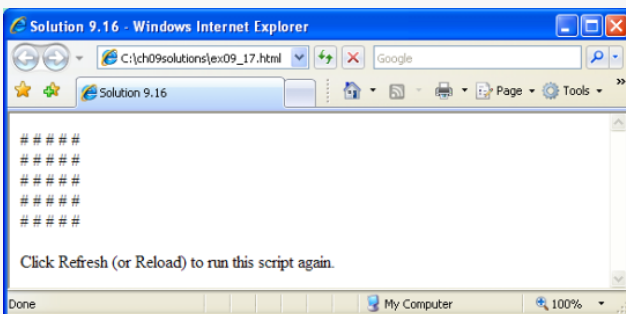
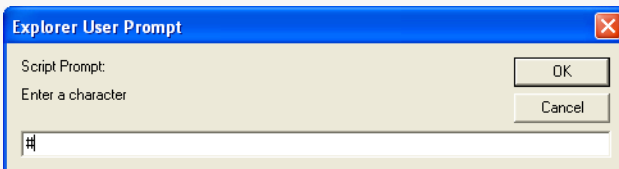
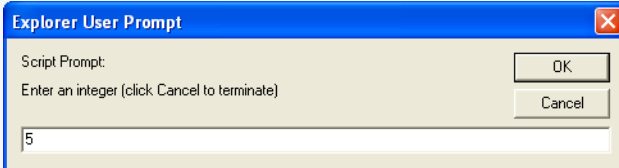
1 <?xml version = "1.0" encoding = "utf-8"?>
2 <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3   "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5 <!-- Exercise 9.16: Solution -->
6 <html xmlns = "http://www.w3.org/1999/xhtml">
7   <head>
8     <title>Solution 9.16</title>

```

```

9      <script type = "text/javascript">
10      <!--
11      var sidelength = window.prompt(
12          "Enter an integer (click Cancel to terminate)", "0");
13      var character = window.prompt( "Enter a character", "*" );
14
15      squareOfCharacters( parseInt( sidelength ), character );
16
17      // this function executes only when called
18      function squareOfCharacters( size, fillCharacter )
19      {
20          for ( var a = 1; a <= size * size; ++a )
21          {
22              document.write( character + " " );
23              if ( a % size == 0 )
24                  document.write( "<br />" );
25          } // end for
26      } // end function squareOfCharacters
27      // -->
28      </script>
29      </head>
30      <body>
31          <p>Click Refresh (or Reload) to run this script again.</p>
32      </body>
33      </html>

```



9.18 Write program segments that accomplish each of the following tasks:

- Calculate the integer part of the quotient when integer a is divided by integer b.
- Calculate the integer remainder when integer a is divided by integer b.
- Use the program pieces developed in parts (a) and (b) to write a function `displayDigits` that receives an integer between 1 and 99999 and prints it as a series of digits, each pair of which is separated by two spaces. For example, the integer 4562 should be printed as
4 5 6 2.
- Incorporate the function developed in part (c) into a script that inputs an integer from a prompt dialog and invokes `displayDigits` by passing to the function the integer entered.

ANS:

```

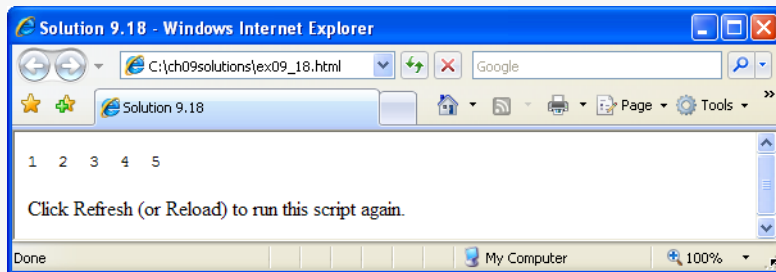
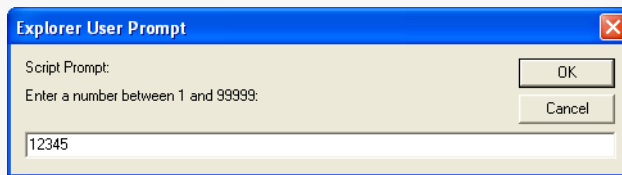
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.18: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.18</title>
9      <script type = "text/javascript">
10        <!--
11          var input;
12
13          input = window.prompt(
14            "Enter a number between 1 and 99999:", "1" );
15          document.writeln( "<pre>" );
16          displayDigits( parseInt( input ) );
17          document.writeln( "</pre>" );
18
19          // the following functions execute only when called
20          // Part A
21          function quotient( a, b )
22          {
23            return Math.floor( a / b );
24          } // end function quotient
25
26          // Part B
27          function remainder( a, b )
28          {
29            return a % b;
30          } // end function remainder
31
32          // Part C
33          function displayDigits( number )
34          {
35            var divisor = 10000, digit;
36
37            // determine the divisor
38            while ( number % divisor == number )
39              divisor = quotient( divisor, 10 );
40
41            while ( divisor >= 1 )
42            {

```

```

43         digit = quotient( number, divisor );
44         document.write( digit + " " );
45         number = remainder( number, divisor );
46         divisor = quotient( divisor, 10 );
47     } // end while
48 } // end function displayDigits
49 // -->
50 </script>
51 </head>
52 <body>
53 <p>Click Refresh (or Reload) to run this script again.</p>
54 </body>
55 </html>

```



9.19 Implement the following functions:

- a) Function `celsius` returns the Celsius equivalent of a Fahrenheit temperature, using the calculation

$$C = 5.0 / 9.0 * (F - 32);$$

- b) Function `fahrenheit` returns the Fahrenheit equivalent of a Celsius temperature, using the calculation

$$F = 9.0 / 5.0 * C + 32;$$

- c) Use these functions to write a script that enables the user to enter either a Fahrenheit or a Celsius temperature and displays the Celsius or Fahrenheit equivalent.

Your XHTML document should contain two buttons—one to initiate the conversion from Fahrenheit to Celsius and one to initiate the conversion from Celsius to Fahrenheit.

ANS:

```

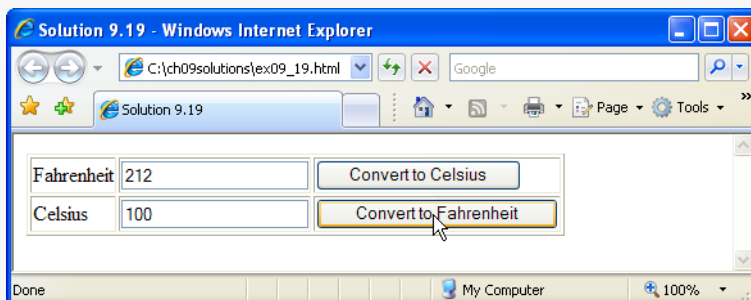
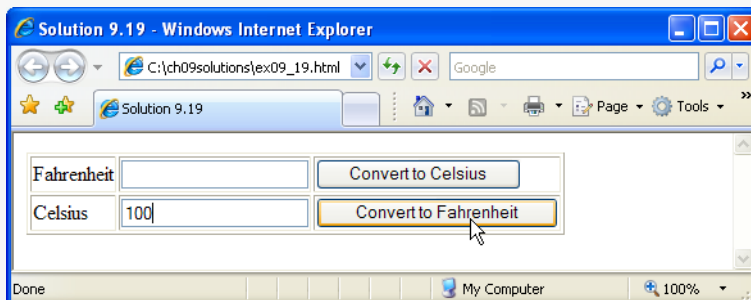
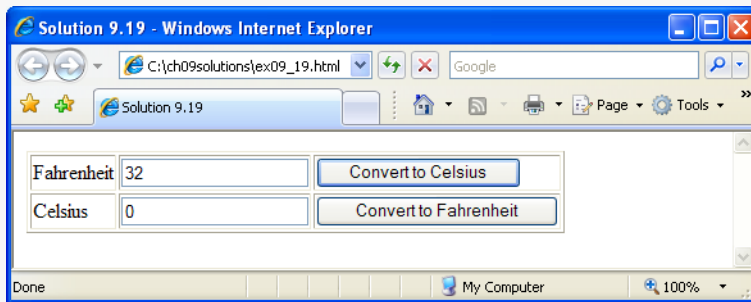
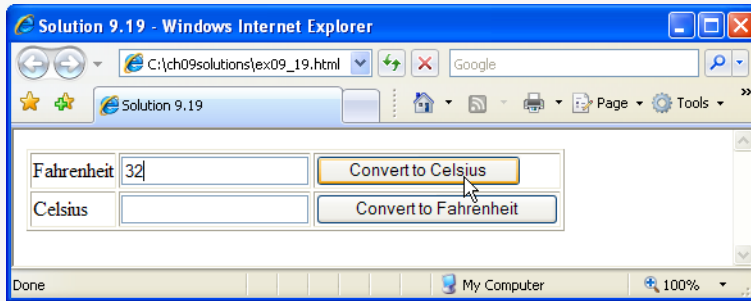
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.19: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.19</title>
9      <script type = "text/javascript">
10        <!--
11          function convertToCelsius()
12          {
13            var form = document.getElementById( "myForm" );
14            var value = parseInt( form.fText.value );
15            form.cText.value = celsius( value );
16          } // convertToCelsius
17
18          function celsius( fTemp )
19          {
20            return ( Math.floor( 5.0 / 9.0 *
21              ( fTemp - 32 ) ) );
22          } // end function celsius
23
24          function convertToFahrenheit()
25          {
26            var form = document.getElementById( "myForm" );
27            var value = parseInt( form.cText.value );
28            form.fText.value = fahrenheit( value );
29          } // end function convertToFahrenheit
30
31          function fahrenheit( cTemp )
32          {
33            return ( Math.floor( 9.0 / 5.0 * cTemp + 32 ) );
34          } // end function fahrenheit
35          // -->
36        </script>
37      </head>
38      <body>
39        <form id = "myForm" action = "">
40          <table border = "1">
41            <tr><td>Fahrenheit</td>
42              <td><input name = "fText" type = "text" /></td>
43              <td><input type = "button" value =
44                "Convert to Celsius" onclick =
45                "convertToCelsius()" /></td>
46            </tr>
47            <tr><td>Celsius</td>
48              <td><input name = "cText" type = "text" /></td>
49              <td><input type = "button" value =
50                "Convert to Fahrenheit" onclick =
51                "convertToFahrenheit()" /></td>
52            </tr>
53          </table>

```

```

54     </form>
55 </body>
56 </html>

```



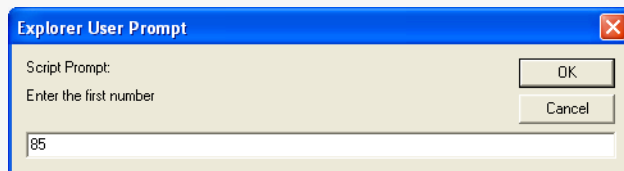
9.20 Write a function `minimum3` that returns the smallest of three floating-point numbers. Use the `Math.min` function to implement `minimum3`. Incorporate the function into a script that reads three values from the user and determines the smallest value.

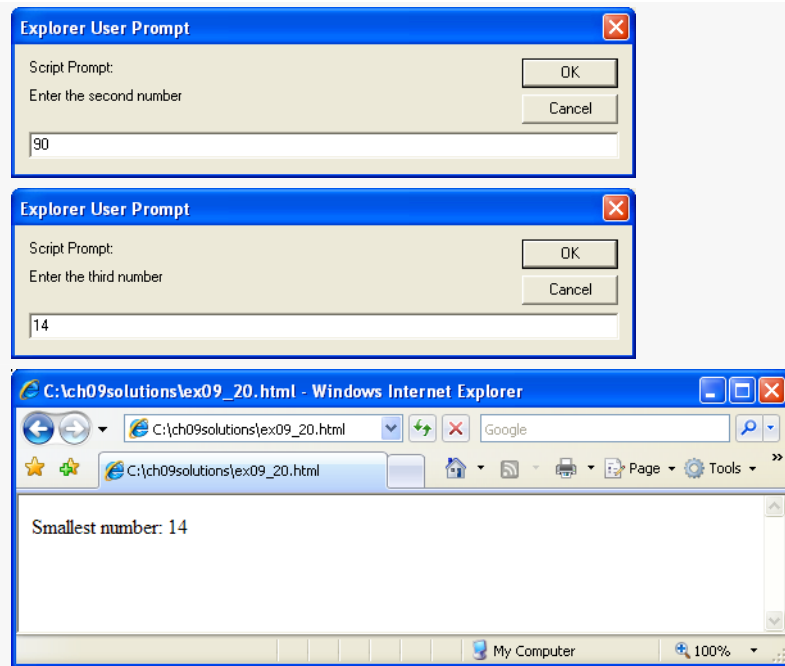
ANS:

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.20: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.20</title>
9      <script type = "text/javascript">
10         <!--
11           var number1;
12           var number2;
13           var number3;
14           var min;
15
16           function run()
17           {
18             number1 = window.prompt( "Enter the first number", "0" );
19             number2 = window.prompt( "Enter the second number", "0" );
20             number3 = window.prompt( "Enter the third number", "0" );
21
22             min = minimum3( number1, number2, number3 );
23
24             document.write( "Smallest number: " + min );
25           } // end function run
26
27           function minimum3( a, b, c )
28           {
29             var smallest;
30
31             smallest = Math.min( a, b );
32             smallest = Math.min( smallest, c );
33             return smallest;
34           } // end function minimum3
35         // -->
36       </script>
37     </head>
38     <body onload = "run()"></body>
39 </html>

```





9.21 An integer number is said to be a **perfect number** if its factors, including 1 (but not the number itself), sum to the number. For example, 6 is a perfect number, because $6 = 1 + 2 + 3$. Write a function `perfect` that determines whether parameter `number` is a perfect number. Use this function in a script that determines and displays all the perfect numbers between 1 and 1000. Print the factors of each perfect number to confirm that the number is indeed perfect. Challenge the computing power of your computer by testing numbers much larger than 1000. Display the results in a `<textarea>`.

ANS:

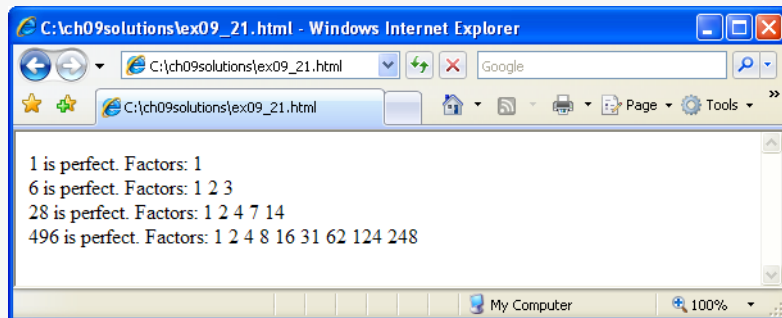
```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.21: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.21</title>
9      <script type = "text/javascript">
10        <!--
11          var factors;
12
13          function start()
14          {
15            for ( var i = 1; i <= 1000; ++i )
16              if ( perfect( i ) == true )
17
```

```

18         document.write( i + " is perfect. Factors: "
19             + factors + "<br />");
20     } // end function start
21
22     function perfect( value )
23     {
24         var factorSum = 1;
25         factors = "1";
26
27         for ( var b = 2; b <= Math.floor( value / 2 ); b++ )
28
29             if ( value % b == 0 )
30             {
31                 factorSum += b;
32                 factors += " " + b;
33             } // end if
34
35             if ( factorSum == value )
36                 return true;
37
38             return false;
39         } // end function perfect
40     // -->
41 </script>
42 </head>
43 <body onload = "start()">
44 <h1>Perfect numbers from 1 to 1000</h1>
45 </body>
46 </html>

```



9.22 An integer is said to be prime if it is greater than 1 and divisible only by 1 and itself. For example, 2, 3, 5 and 7 are prime, but 4, 6, 8 and 9 are not.

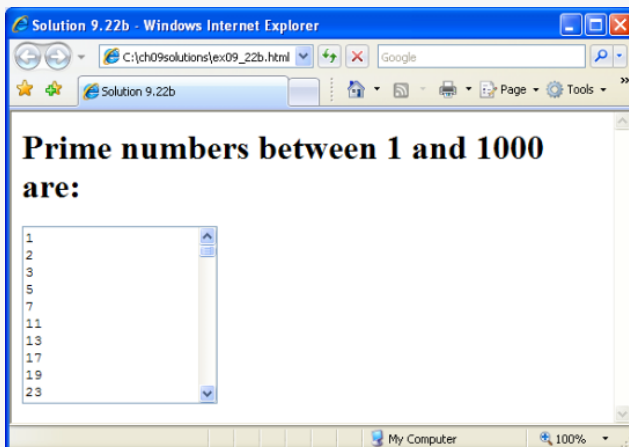
- Write a function that determines whether a number is prime.
- Use this function in a script that determines and prints all the prime numbers between 1 and 10,000. How many of these 10,000 numbers do you really have to test before being sure that you have found all the primes? Display the results in a <textarea>.

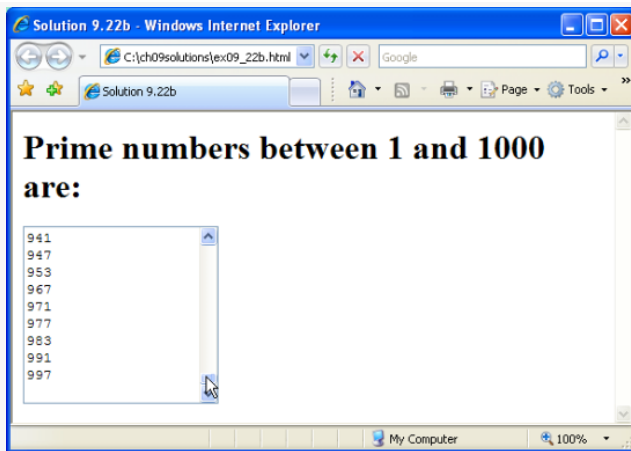
ANS:

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.22b: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.22b</title>
9      <script type = "text/javascript">
10        <!--
11        document.writeln( "<h1>Prime numbers between 1 and"
12          + " 1000 are: <br /></h1>" );
13        document.writeln( "<textarea rows = '10'>" );
14
15        for ( var m = 1; m <= 1000; m++ )
16          if ( prime( m ) )
17          {
18            document.writeln( m );
19          } // end if
20        document.writeln( "</textarea>" );
21
22        function prime( n )
23        {
24          for ( var v = 2; v <= n / 2; v++ )
25            if ( n % v == 0 )
26              return false;
27
28          return true;
29        } // end function prime
30        // -->
31      </script>
32    </head>
33    <body></body>
34  </html>

```





- c) Initially, you might think that $n/2$ is the upper limit for which you must test to see whether a number is prime, but you only need go as high as the square root of n . Why? Rewrite the program, and run it both ways. Estimate the performance improvement.

ANS:

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.22c: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.22c</title>
9      <script type = "text/javascript">
10        <!--
11
12        var count = 0;
13
14        document.writeln( "<h1>Prime numbers between 1 and"
15          + " 1000 are: <br /></h1>" );
16        document.writeln( "<textarea rows = '10'>" );
17
18        for ( var m = 1; m <= 1000; m++ )
19
20          if ( prime( m ) == true )
21          {
22            ++count;
23            document.writeln( m );
24          } // end if
25
26        document.writeln("</textarea>");
27
28        function prime( n )
29        {

```

```

30         for ( var v = 2; v <= Math.sqrt( n ); v++ )
31
32             if ( n % v == 0 )
33                 return false;
34
35             return true;
36         } // end function prime
37         // -->
38     </script>
39 </head>
40 <body></body>
41 </html>

```

The performance is significantly enhanced. The browsers can now handle larger upper limits of numbers to test, such as 10,000, without having to prompt the user for permission to continue.

9.23 Write a function that takes an integer value and returns the number with its digits reversed. For example, given the number 7631, the function should return 1367. Incorporate the function into a script that reads a value from the user.

ANS:

```

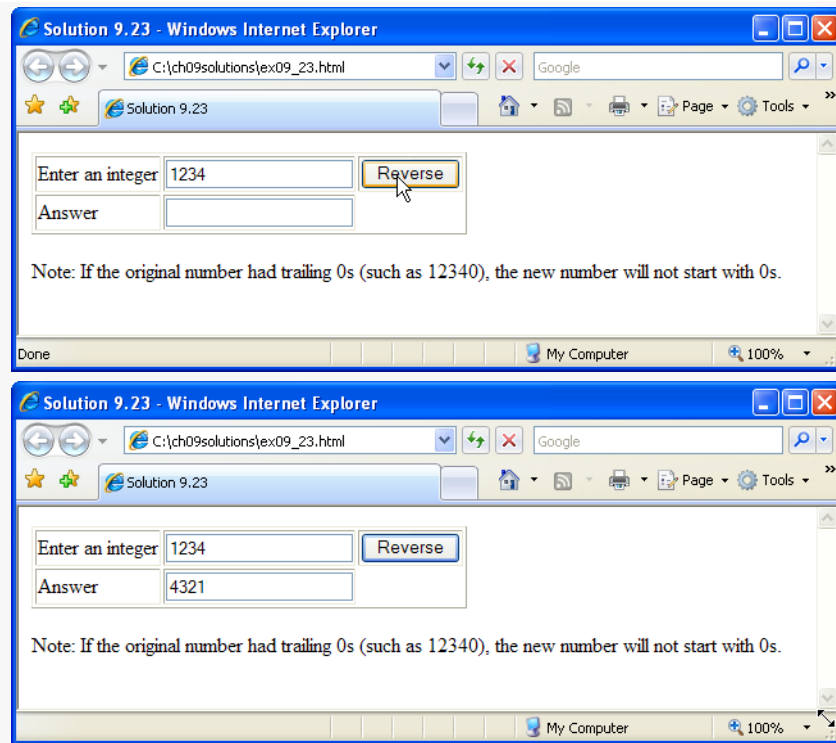
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3      "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.23: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7      <head>
8          <title>Solution 9.23</title>
9          <script type = "text/javascript">
10              <!--
11              function reverseNumber()
12              {
13                  var form = document.getElementById( "myForm" );
14                  var input = parseInt( form.number.value );
15                  form.answer.value = reverseInt( input );
16              } // end function reverseNumber()
17
18              // the following functions execute only when called
19              function reverseInt( number )
20              {
21                  var digit;
22                  var newNumber = 0;
23                  var multiplier = 1;
24                  var divisor = determineDivisor( number );
25
26                  while ( divisor >= 1 )
27                  {
28                      digit = quotient( number, divisor );
29                      newNumber += digit * multiplier
30                      number = remainder( number, divisor );
31                      divisor = quotient( divisor, 10 );

```

```

32         multiplier *= 10;
33     } // end while
34     return newNumber;
35 } // end function reverseInt
36
37 function determineDivisor( number )
38 {
39     var divisor = 1;
40
41     while ( quotient( number / 10, divisor ) != 0 )
42         divisor *= 10;
43
44     return divisor;
45 } // end function determineDivisor
46
47 function quotient( a, b )
48 {
49     return Math.floor( a / b );
50 } // end function quotient
51
52 function remainder( a, b )
53 {
54     return a % b;
55 } // end function remainder
56 // -->
57 </script>
58 </head>
59
60 <body>
61 <form id = "myForm" action = "">
62     <table border = "1">
63         <tr><td>Enter an integer</td>
64             <td><input name = "number" type = "text" /></td>
65             <td><input type = "button" value = "Reverse"
66                 onclick = "reverseNumber()" /></td>
67         </tr>
68         <tr><td>Answer</td>
69             <td><input name = "answer" type = "text" /></td>
70         </tr>
71     </table>
72 </form>
73 <p>Note: If the original number had trailing 0s (such as
74     12340), the new number will not start with 0s.</p>
75 </body>
76 </html>

```



9.24 The **greatest common divisor** (GCD) of two integers is the largest integer that evenly divides each of the two numbers. Write a function `gcd` that returns the greatest common divisor of two integers. Incorporate the function into a script that reads two values from the user.

ANS:

```

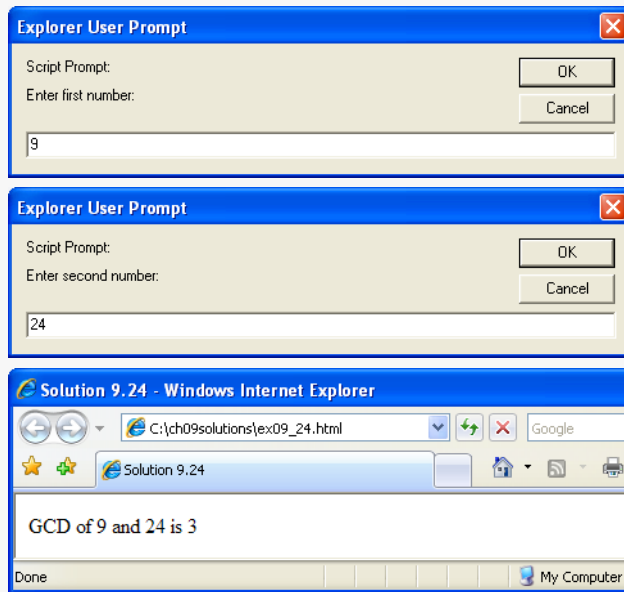
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.24: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.24</title>
9      <script type = "text/javascript">
10        <!--
11          var num1 = window.prompt( "Enter first number:", "1" );
12          var num2 = window.prompt( "Enter second number:", "1" );
13          var result = gcd( num1, num2 );
14          document.write( "GCD of " + num1 + " and " + num2 +
15                        " is " + result );
16
17          function gcd( x, y )
18          {
19            var greatest = 1;

```

```

20
21         for ( var z = 2; z <= Math.min( x, y ); z++ )
22             if ( ( x % z == 0 ) && ( y % z == 0 ) )
23                 greatest = z;
24
25         return greatest;
26     } // function gcd
27     // -->
28 </script>
29 </head>
30 <body></body>
31 </html>

```



9.25 Write a function `qualityPoints` that inputs a student's average and returns 4 if the student's average is 90–100, 3 if the average is 80–89, 2 if the average is 70–79, 1 if the average is 60–69 and 0 if the average is lower than 60. Incorporate the function into a script that reads a value from the user.

ANS:

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3      "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.25: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7      <head>
8          <title>Solution 9.25</title>
9          <script type = "text/javascript">
10              <!--

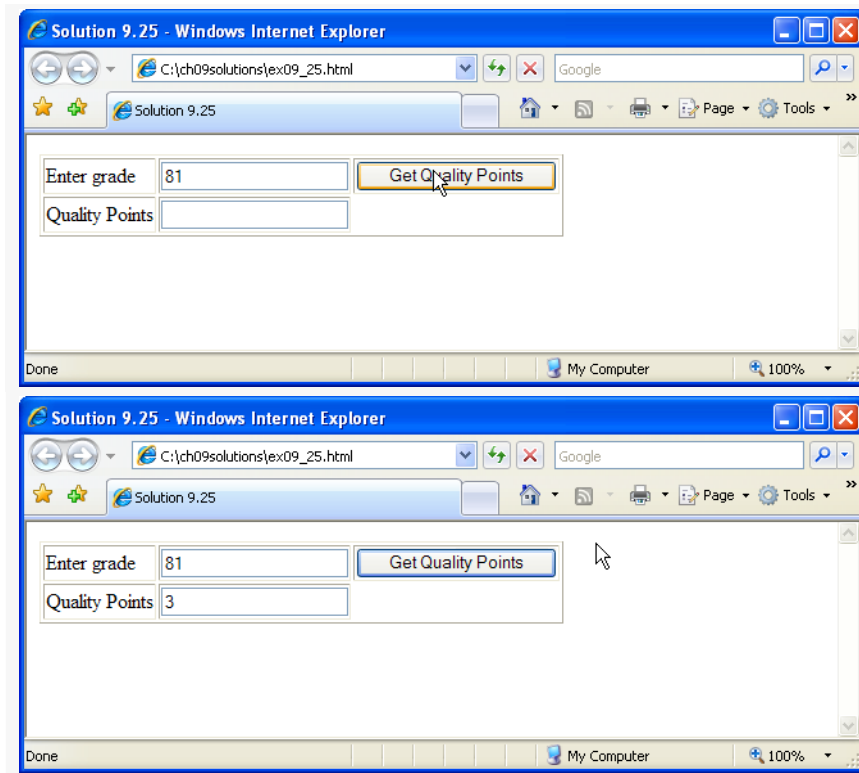
```



```

11     function determineQualityPoints()
12     {
13         var form = document.getElementById( "myForm" );
14         var input = parseInt( form.number.value );
15
16         form.points.value =
17             ( input >= 0 && input <= 100 ) ?
18             qualityPoints( input ) : "Invalid input.";
19     } // end function determineQualityPoints
20
21     function qualityPoints( grade )
22     {
23         if ( grade >= 90 )
24             return 4;
25         else if ( grade >= 80 )
26             return 3;
27         else if ( grade >= 70 )
28             return 2;
29         else if ( grade >= 60 )
30             return 1;
31         else
32             return 0;
33     } // end function qualityPoints
34     // -->
35 </script>
36 </head>
37
38 <body>
39     <form id = "myForm" action = "">
40         <table border = "1">
41             <tr><td>Enter grade</td>
42                 <td><input name = "number" type = "text" />
43                 </td>
44                 <td><input type = "button" value =
45                     "Get Quality Points" onclick =
46                     "determineQualityPoints()" /></td>
47             </tr><tr>
48                 <td>Quality Points</td>
49                 <td><input type = "text" name =
50                     "points" /></td>
51             </tr>
52         </table>
53     </form>
54 </body>
55 </html>

```



9.26 Write a script that simulates coin tossing. Let the program toss the coin each time the user clicks the **Toss** button. Count the number of times each side of the coin appears. Display the results. The program should call a separate function `flip` that takes no arguments and returns `false` for tails and `true` for heads. [Note: If the program realistically simulates the coin tossing, each side of the coin should appear approximately half the time.]

ANS:

```

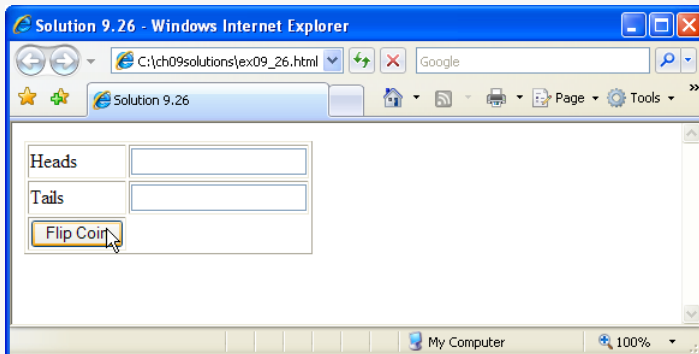
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.26: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.26</title>
9      <script type = "text/javascript">
10         <!--
11         var heads = 0;
12         var tails = 0;
13
14         function toss()
15         {
16             var headsField = document.getElementById( "heads" );

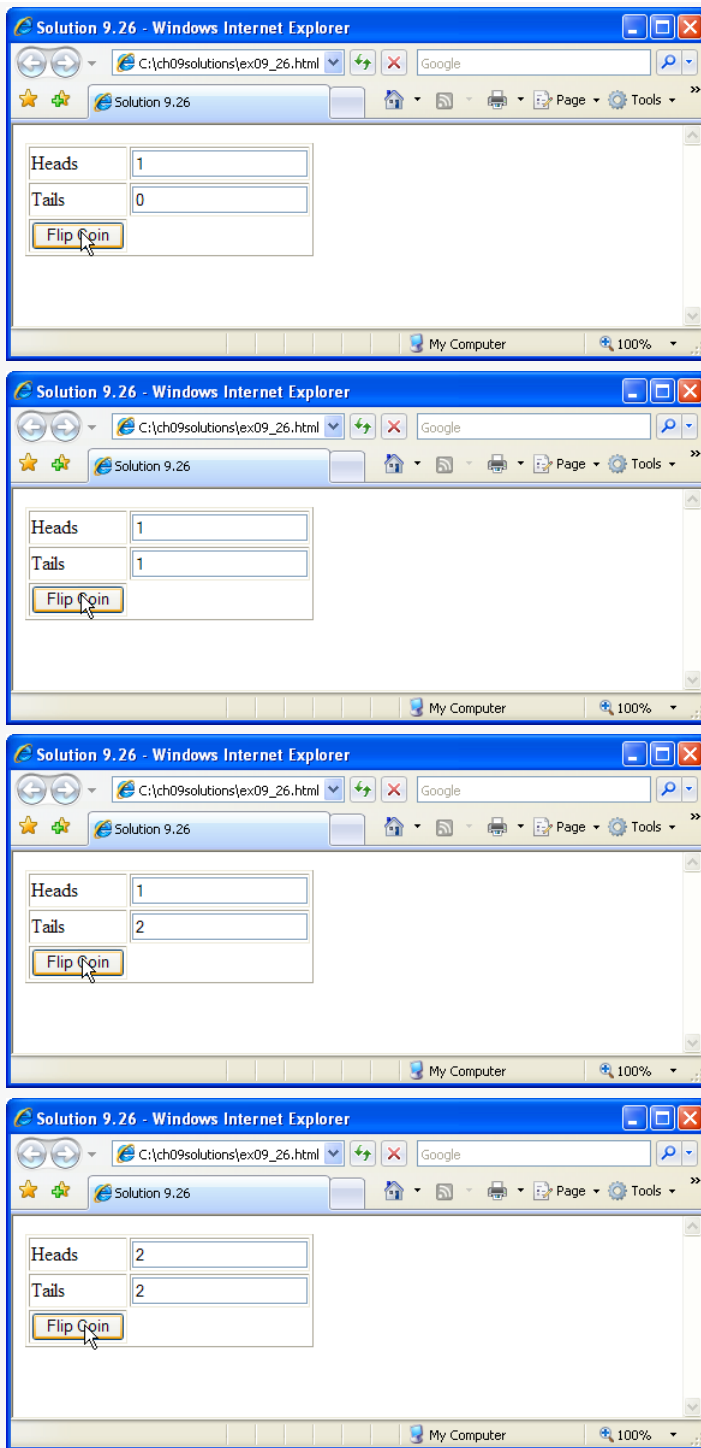
```

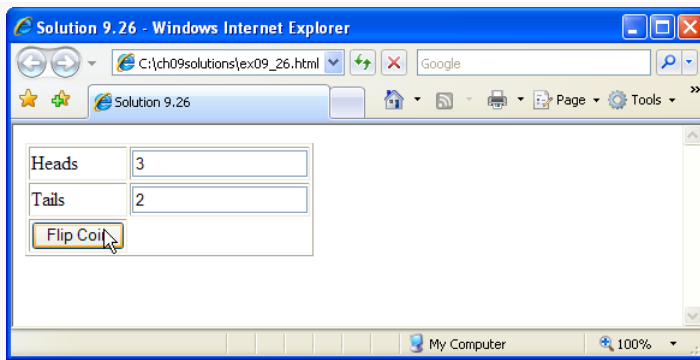
```

17     var tailsField = document.getElementById( "tails" );
18
19     if ( flip() )
20     {
21         ++heads;
22         headsField.value = heads;
23     }
24     else
25     {
26         ++tails;
27         tailsField.value = tails;
28     }
29 } // end function toss
30
31 function flip()
32 {
33     return Math.floor( Math.random() * 2 ) == 1
34 } // end function flip
35 // -->
36 </script>
37 </head>
38
39 <body>
40     <form action = "">
41         <table border = "1">
42             <tr><td>Heads</td>
43                 <td><input id = "heads" type = "text" />
44             </td>
45         </tr>
46         <tr><td>Tails</td>
47             <td><input id = "tails" type = "text" />
48         </td>
49         </tr>
50         <tr><td><input type = "button" value = "Flip Coin"
51             onclick = "toss()" /></td>
52         </tr>
53         </table>
54     </form>
55 </body>
56 </html>

```







9.27 Computers are playing an increasing role in education. Write a program that will help an elementary-school student learn multiplication. Use `Math.random` to produce two positive one-digit integers. It should then display a question such as

How much is 6 times 7?

The student then types the answer into a text field. Your program checks the student's answer. If it is correct, display the string "Very good!" and generate a new question. If the answer is wrong, display the string "No. Please try again." and let the student try the same question again repeatedly until the student finally gets it right. A separate function should be used to generate each new question. This function should be called once when the script begins execution and each time the user answers the question correctly.

ANS:

```

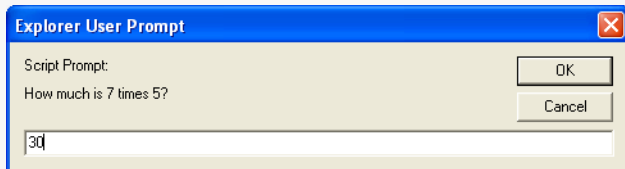
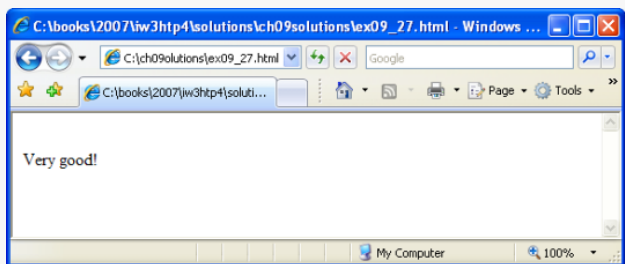
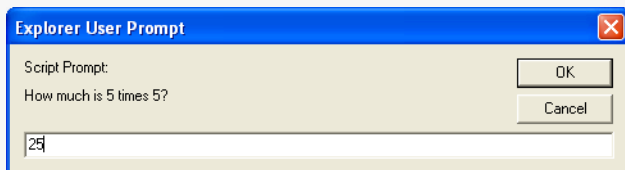
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.27: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.27</title>
9      <script type = "text/javascript">
10         <!--
11         var number1;
12         var number2;
13         var answer;
14
15         function run()
16         {
17             ask();
18
19             while( window.prompt(
20                 "Would you like to answer another question?" +
21                 " ( yes or no ) ", "yes" ) == "yes" )
22             {
23                 ask();
24             } // end while
25         } // end function run

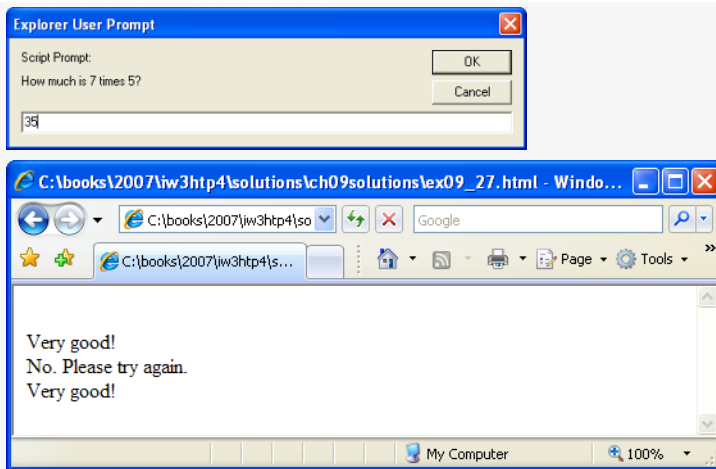
```

```

26
27     function ask()
28     {
29         number1 = Math.floor( 1 + Math.random() * 9 );
30         number2 = Math.floor( 1 + Math.random() * 9 );
31
32         while( true )
33         {
34             answer = window.prompt( "How much is " +
35                                     number1 + " times " + number2 + "?" );
36
37             if ( parseInt( answer ) != number1 * number2 )
38                 document.write( "<br />No. Please try again." );
39             else
40             {
41                 document.write( "<br />Very good!" );
42                 return;
43             } // end else
44         } // end while
45     } // end function ask
46     // -->
47 </script>
48 </head>
49 <body onload = "run()">
50 </body>
51 </html>

```





9.28 The use of computers in education is referred to as **computer-assisted instruction** (CAI). One problem that develops in CAI environments is student fatigue. This problem can be eliminated by varying the computer's dialogue to hold the student's attention. Modify the program in Exercise 9.27 to print one of a variety of comments for each correct answer and each incorrect answer. The set of responses for correct answers is as follows:

Very good!
 Excellent!
 Nice work!
 Keep up the good work!

The set of responses for incorrect answers is as follows:

No. Please try again.
 Wrong. Try once more.
 Don't give up!
 No. Keep trying.

Use random number generation to choose a number from 1 to 4 that will be used to select an appropriate response to each answer. Use a switch statement to issue the responses.

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.28: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.28</title>
9      <script type = "text/javascript">
10         <!--
11             var number1;
12             var number2;
13             var answer;
14

```

```

15     function run()
16     {
17         ask();
18
19         while( window.prompt(
20             "Would you like to answer another question?" +
21             " ( yes or no ) ", "yes" ) == "yes" )
22         {
23             ask();
24         } // end while
25     } // end function run
26
27     function ask()
28     {
29         number1 = Math.floor( 1 + Math.random() * 9 );
30         number2 = Math.floor( 1 + Math.random() * 9 );
31
32         while( true )
33         {
34             answer = window.prompt( "How much is " +
35                                     number1 + " times " + number2 + "?" );
36
37             if ( parseInt( answer ) != number1 * number2 )
38             {
39                 response = Math.floor( 1 + Math.random() * 4 );
40
41                 switch ( response )
42                 {
43                     case 1:
44                         document.write( "No. Please try again." );
45                         break;
46                     case 2:
47                         document.write( "Wrong. Try once more." );
48                         break;
49                     case 3:
50                         document.write( "Don't give up!" );
51                         break;
52                     case 4:
53                         document.write( "No. Keep trying." );
54                         break;
55                 } // end switch
56                 document.write( "<br />" );
57
58             } // end if
59             else
60             {
61                 response = Math.floor( 1 + Math.random() * 4 );
62
63                 switch ( response )
64                 {
65                     case 1:
66                         document.write( "Very good!" );
67                         break;

```



```

68         case 2:
69             document.write( "Excellent!");
70             break;
71         case 3:
72             document.write( "Nice work!");
73             break;
74         case 4:
75             document.write( "Keep up the good work!" );
76             break;
77     } // end switch
78     document.write( "<br />" );
79     return;
80 } // end else
81 } // end while
82 } // end function ask
83 // -->
84 </script>
85 </head>
86 <body onload = "run()">
87 </body>
88 </html>

```

Explorer User Prompt

Script Prompt:
How much is 1 times 3?

5

OK Cancel

Explorer User Prompt

Script Prompt:
How much is 1 times 3?

13

OK Cancel

Explorer User Prompt

Script Prompt:
How much is 1 times 3?

3

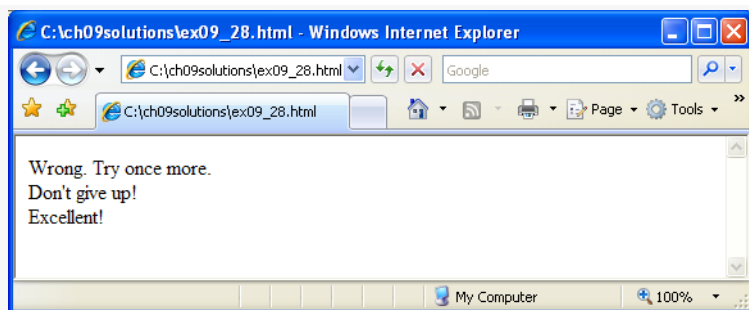
OK Cancel

Explorer User Prompt

Script Prompt:
Would you like to answer another question? (yes or no)

no

OK Cancel



9.29 More sophisticated computer-assisted instruction systems monitor the student's performance over a period of time. The decision to begin a new topic is often based on the student's success with previous topics. Modify the program in Exercise 9.28 to count the number of correct and incorrect responses typed by the student. After the student answers 10 questions, your program should calculate the percentage of correct responses. If the percentage is lower than 75 percent, print Please ask your instructor for extra help, and reset the program so another student can try it.

ANS:

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.29: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.29</title>
9      <script type = "text/javascript">
10         <!--
11             var number1;
12             var number2;
13             var answer;
14
15             function run()
16             {
17                 while ( true )
18                 {
19                     var correct = 0;
20
21                     for (var i = 0; i < 10; i++ )
22                         correct += ask();
23
24                     var getHelp = "";
25
26                     if ( correct <= 7 )
27                         getHelp = "Please see your instructor for extra help"
28
29                     alert( "Total correct: " + correct + " " + getHelp );
30                     var tenMore = window.prompt(
31                         "Would you like to answer ten more? (yes or no)",
32                         "yes");

```

```

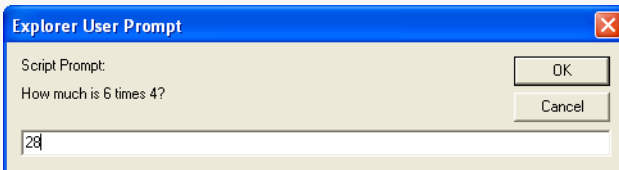
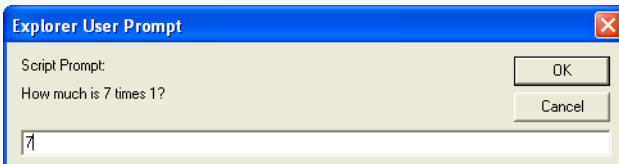
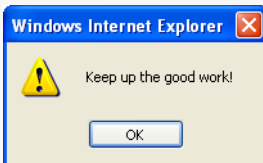
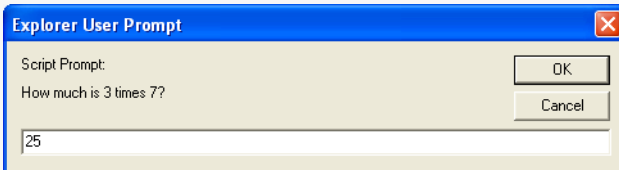
33         if ( tenMore == "no" )
34             return;
35     } // end while
36 } // end function run
37
38 function ask()
39 {
40     number1 = Math.floor( 1 + Math.random() * 9 );
41     number2 = Math.floor( 1 + Math.random() * 9 );
42
43     while ( true )
44     {
45         answer = window.prompt( "How much is " +
46             number1 + " times " + number2 + "?" );
47
48         if ( parseInt( answer ) != number1 * number2 )
49         {
50             response = Math.floor( 1 + Math.random() * 4 );
51
52             switch ( response )
53             {
54                 case 1:
55                     alert( "No." );
56                     break;
57                 case 2:
58                     alert( "Wrong. Try another one." );
59                     break;
60                 case 3:
61                     alert( "Don't give up!" );
62                     break;
63                 case 4:
64                     alert( "No. Keep trying." );
65                     break;
66             } // end switch
67             return 0;
68         } // end if
69     else
70     {
71         response = Math.floor( 1 + Math.random() * 4 );
72
73         switch ( response )
74         {
75             case 1:
76                 alert( "Very good!" );
77                 break;
78             case 2:
79                 alert( "Excellent!" );
80                 break;
81             case 3:
82                 alert( "Fantastic!" );
83                 break;
84             case 4:
85                 alert( "Keep up the good work!" );
86                 break;
87         } // end switch

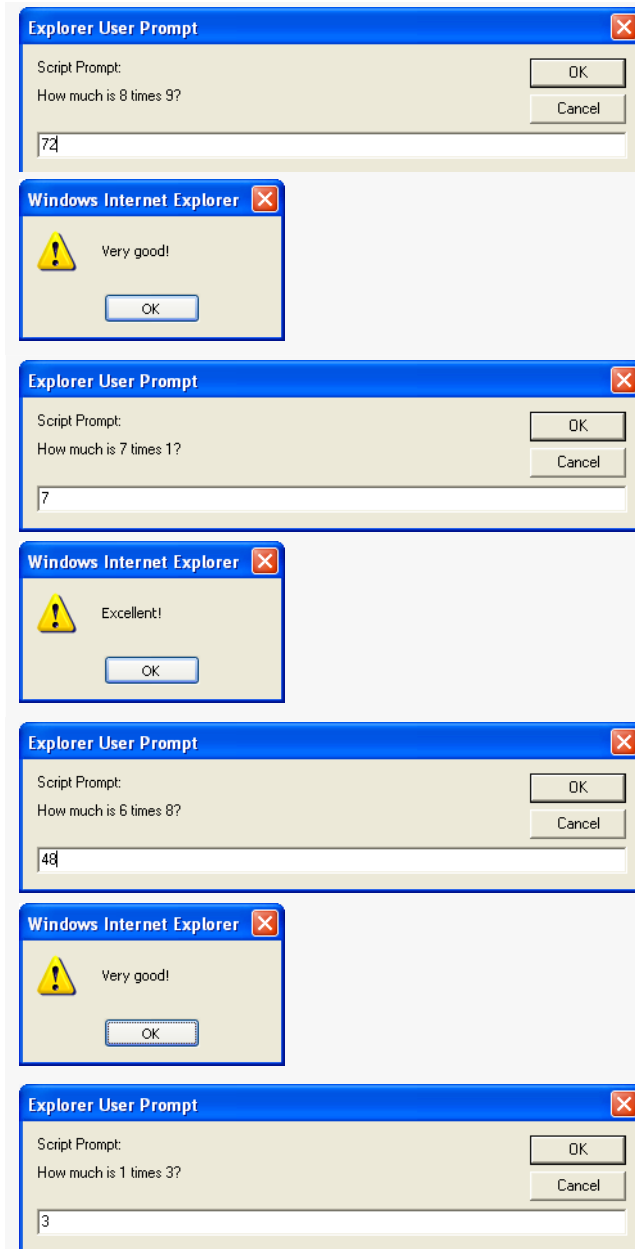
```

```

88         return 1;
89     } // end else
90 } // end while
91 } // end function ask
92 // -->
93 </script>
94 </head>
95 <body onload = "run()">
96 </body>
97 </html>

```





9.30 Write a script that plays a “guess the number” game as follows: Your program chooses the number to be guessed by selecting a random integer in the range 1 to 1000. The script displays the prompt `Guess a number between 1 and 1000` next to a text field. The player types a first guess into the text field and clicks a button to submit the guess to the script. If the player's guess is incorrect, your program should display `Too high. Try again.` or `Too low. Try again.` to help the player “zero in” on the correct answer and should clear the text field so the user can enter the next guess. When

the user enters the correct answer, display Congratulations. You guessed the number! and clear the text field so the user can play again. [Note: The guessing technique employed in this problem is similar to a **binary search**, which we discuss in Chapter 10, JavaScript: Arrays.]

ANS:

```

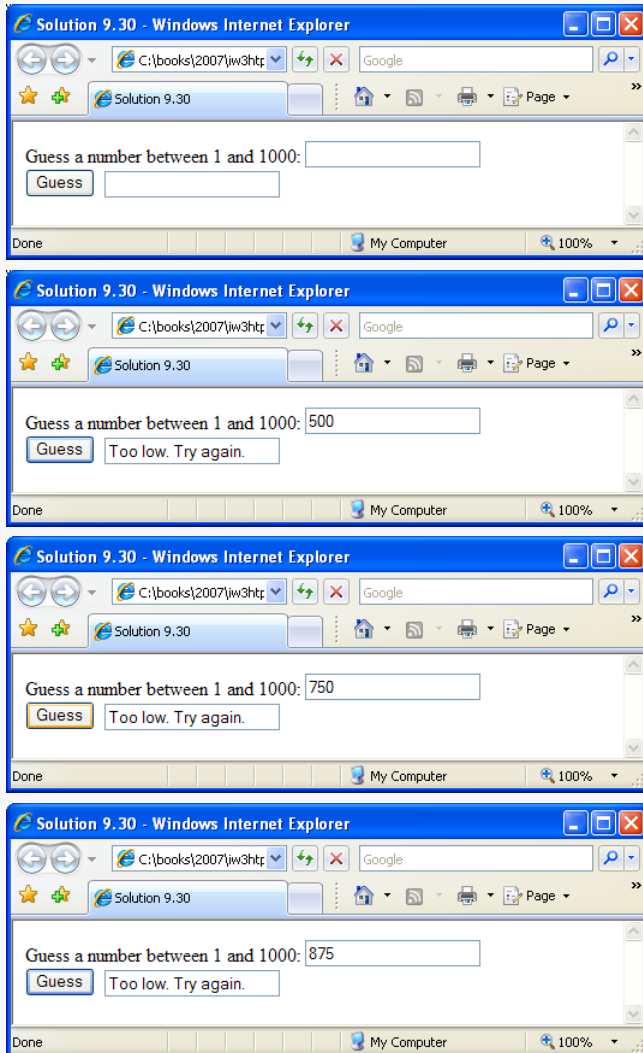
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.30: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.30</title>
9      <script type = "text/javascript">
10        <!--
11          function check()
12          {
13            var hintField = document.getElementById( "hint" );
14            var targetField = document.getElementById( "target" );
15            var guessField = document.getElementById( "userguess" );
16
17            if ( parseInt( guessField.value ) > targetField.value )
18              hintField.value = "Too high. Try again.";
19            else if ( parseInt( guessField.value ) < targetField.value )
20              hintField.value = "Too low. Try again.";
21            else
22            {
23              hintField.value = "You guessed it!";
24              changevalue();
25            } // end else
26          } // end function check
27
28          function changevalue()
29          {
30            document.getElementById( "target" ).value =
31              Math.floor( 1 + Math.random() * 1000 );
32          } // end function changevalue
33          // -->
34        </script>
35      </head>
36
37      <body onload = "changevalue()">
38        <form id = "guess" action = "">
39          <div>
40            Guess a number between 1 and 1000:
41            <input type = "text" id = "userguess" /><br />
42            <input type = "button" value = "Guess"
43              onclick = "check()" />
44            <input type = "hidden" id = "target" value = "0" />
45            <label>
46              <input id = "hint" type = "text" />
47            </label>
48          </div>
49        </form>

```

```

50     </body>
51 </html>

```



9.31 Modify the program of Exercise 9.30 to count the number of guesses the player makes. If the number is 10 or fewer, display Either you know the secret or you got lucky! If the player guesses the number in 10 tries, display Ahah! You know the secret! If the player makes more than 10 guesses, display You should be able to do better! Why should it take no more than 10 guesses? Well, with each good guess, the player should be able to eliminate half of the numbers. Now show why any number 1 to 1000 can be guessed in 10 or fewer tries.

ANS:

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.31: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.31</title>
9      <script type = "text/javascript">
10        <!--
11          var numGuesses = 0;
12
13          function check()
14          {
15            var form = document.getElementById( "guess" );
16            if ( parseInt( form.userguess.value ) >
17                form.target.value )
18              form.hint.value = "Too high. Try again.";
19            else if ( parseInt( form.userguess.value ) <
20                      form.target.value )
21              form.hint.value = "Too low. Try again.";
22            else {
23              form.hint.value =
24                "You guessed it!";
25              if ( parseInt( numGuesses ) < 10 )
26                window.alert( "Either you know the secret or"
27                               + " you got lucky!" );
28              if ( parseInt( numGuesses ) == 10 )
29                window.alert( "Ahah! You know the secret!" );
30              if ( parseInt( numGuesses ) > 10 )
31                window.alert(
32                  "You should be able to do better!" );
33
34              guess.userguess.value = "";
35              window.status = "Done";
36              changevalue();
37            } // end else
38            numGuesses++;
39          } // end function check
40
41          function changevalue()
42          {
43            document.getElementById( "guess" ).target.value =
44              Math.floor( 1 + Math.random() * 1000 );
45          } // end function changevalue
46          // -->
47        </script>
48      </head>
49
50      <body onload = "changevalue()">
51        <form id = "guess" action = "">
52          <div>

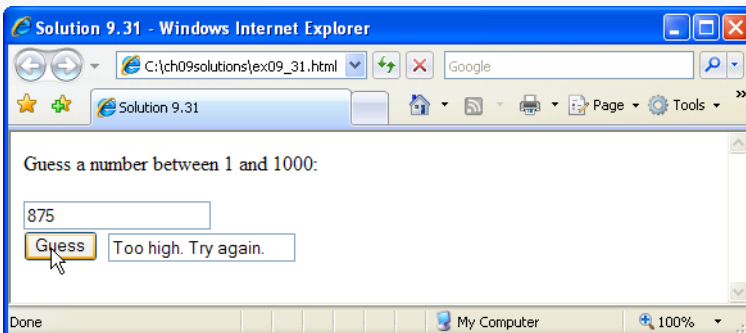
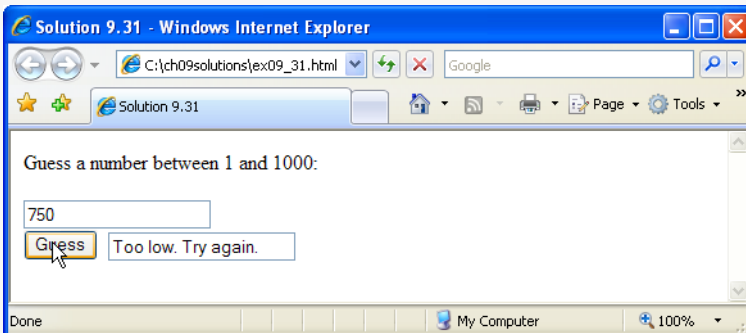
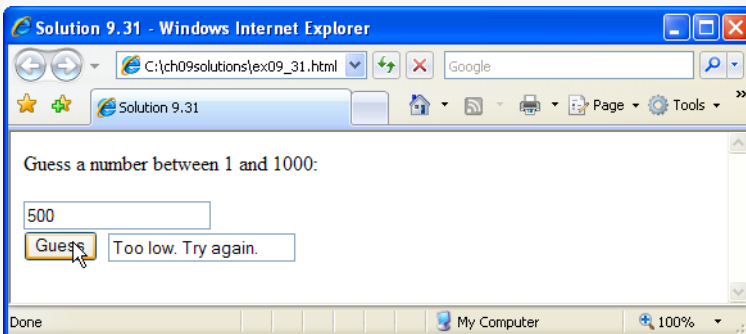
```

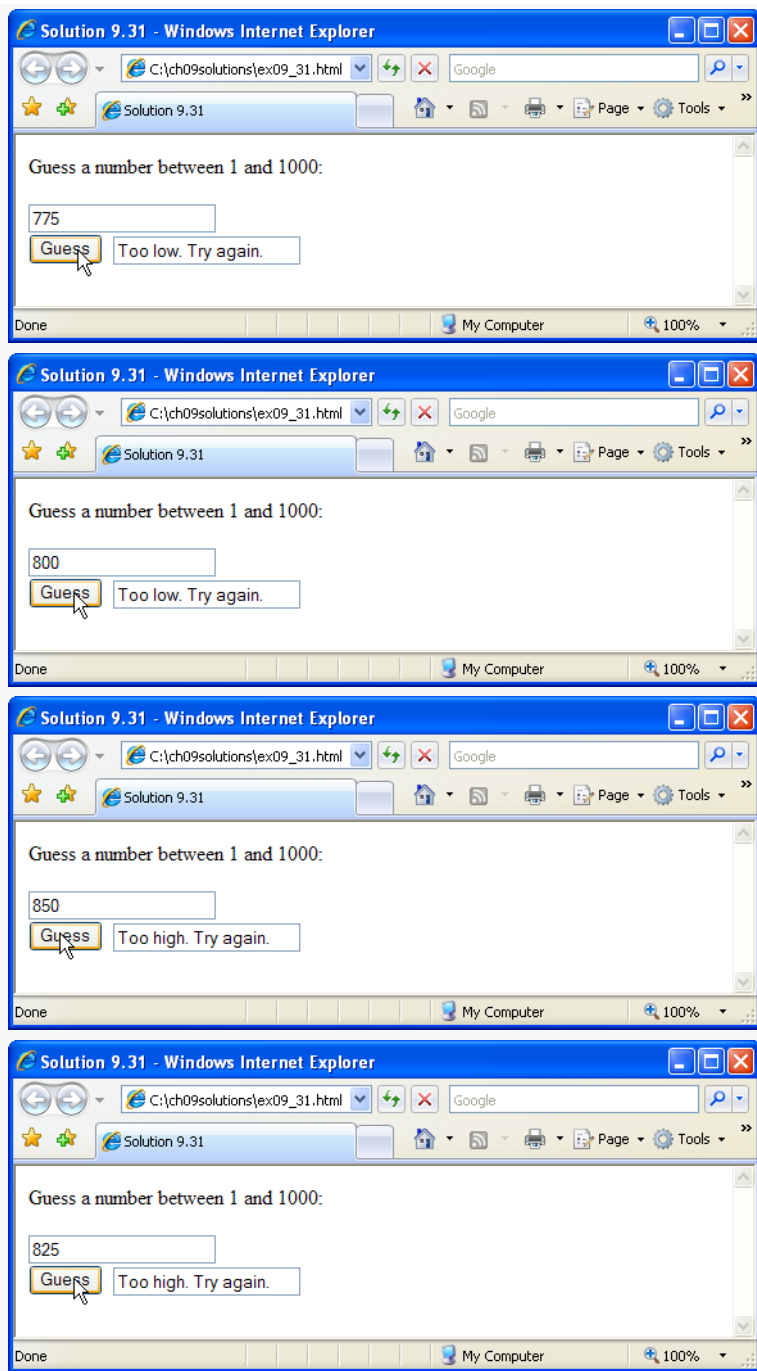


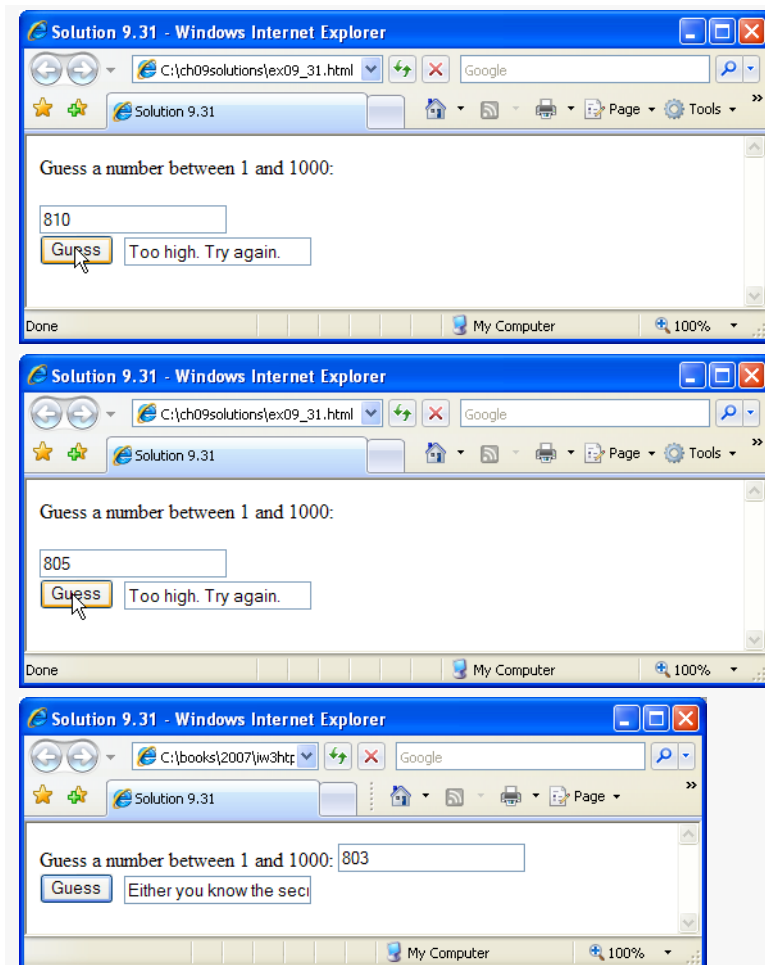
```

53         <p>Guess a number between 1 and 1000:</p>
54         <input type = "text" name = "userguess" /><br />
55         <input type = "button" value = "Guess"
56             onclick = "check()" />
57         <input type = "hidden" name = "target" value = "0" />
58         <label>
59             <input name = "hint" type = "text" />
60         </label>
61     </div>
62 </form>
63 </body>
64 </html>

```







With each guess, we can eliminate one-half of the possible guessing pool if we guess the number exactly halfway into the current guessing range. So after the first guess, there are still 500 possibilities; after the second, there are 250, etc. The number of remaining possibilities can be generalized with the expression $1000 * (1/2)^{(\text{number of guesses completed})}$. So after 9 guesses, there are fewer than 2 possible answers. This can be rounded down to 1, so by using this binary guessing technique, the answer can always be obtained in 10 or fewer guesses.

9.32 Exercises 9.27 through 9.29 developed a computer-assisted instruction program to teach an elementary-school student multiplication. This exercise suggests enhancements to that program.

- a) Modify the program to allow the user to enter a grade-level capability. A grade level of 1 means to use only single-digit numbers in the problems, a grade level of 2 means to use numbers as large as two digits, and so on.

ANS:

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.32a: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.32a</title>
9      <script type = "text/javascript">
10        <!--
11          var number1;
12          var number2;
13          var answer;
14          var scaleFactor;
15
16          function run()
17          {
18            var gradeLevel = window.prompt( "Enter grade level" );
19            scaleFactor = Math.pow( 10, gradeLevel ) - 1;
20
21            ask();
22
23            while ( window.prompt(
24              "Would you like to answer another question?" +
25                " ( yes or no ) ", "yes" ) == "yes" )
26            {
27              ask();
28            } // end while
29          } // end function run
30
31          function ask()
32          {
33            number1 = Math.floor( 1 + Math.random() * scaleFactor );
34            number2 = Math.floor( 1 + Math.random() * scaleFactor );
35
36            while( true )
37            {
38              answer = window.prompt( "How much is " +
39                number1 + " times " + number2 + "?" );
40
41              if ( parseInt( answer ) != number1 * number2 )
42                document.write( "<br />No. Please try again." );
43              else
44              {
45                document.write( "<br />Very good!" );
46                return;
47              } // end else
48            } // end while
49          } // end function ask
50          // -->
51        </script>
52      </head>

```

```
53 <body onload = "run()">
54 </body>
55 </html>
```

Explorer User Prompt

Script Prompt:
Enter grade level

1

OK Cancel

Explorer User Prompt

Script Prompt:
How much is 7 times 2?

14

OK Cancel

Explorer User Prompt

Script Prompt:
Would you like to answer another question? (yes or no)

no

OK Cancel

Explorer User Prompt

Script Prompt:
Enter grade level

2

OK Cancel

Explorer User Prompt

Script Prompt:
How much is 27 times 72?

1944

OK Cancel

Explorer User Prompt

Script Prompt:
Would you like to answer another question? (yes or no)

no

OK Cancel

- b) Modify the program to allow the user to pick the type of arithmetic problems he or she wishes to study. An option of 1 means addition problems only, 2 means subtraction problems only, 3 means multiplication problems only, 4 means division problems only and 5 means to intermix randomly problems of all these types.

ANS:

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.32b: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.32b</title>
9      <script type = "text/javascript">
10        <!--
11          var number1;
12          var number2;
13          var answer;
14          var operation;
15          var operationWord;
16          var correctAnswer;
17          var randomOperator = false;
18
19          function run()
20          {
21            operation = parseInt( window.prompt(
22                                  "Enter problem type: \n" +
23                                  "1 - Addition, " +
24                                  "2 - Subtraction, " +
25                                  "3 - Multiplication, " +
26                                  "4 - Division, " +
27                                  "5 - Mixed" ) );
28
29            ask();
30
31            while ( window.prompt(
32                      "Would you like to answer another question?" +
33                      " ( yes or no ) ", "yes" ) == "yes" )
34            {
35              ask();
36            } // end while
37          } // end function run
38
39          function ask()
40          {
41            number1 = Math.floor( 1 + Math.random() * 9 );
42            number2 = Math.floor( 1 + Math.random() * 9 );
43
44            if ( !setOperation( operation ) )
45              return;
46
47            while( true )
48            {
49              if ( randomOperator )
50                setOperation( 5 ); // set a random operation
51
52            answer = window.prompt( "How much is " +

```

```

53
54         if ( parseInt( answer ) !== correctAnswer )
55             document.write( "<br />No. Please try again." );
56         else
57         {
58             document.write( "<br />Very good!" );
59             return;
60         } // end else
61     } // end while
62 } // end function ask
63
64 function setOperation( op )
65 {
66     switch ( op )
67     {
68     case 1:
69         correctAnswer = number1 + number2;
70         operationWord = " plus ";
71         break;
72     case 2:
73         correctAnswer = number1 - number2;
74         operationWord = " minus ";
75         break;
76     case 3:
77         correctAnswer = number1 * number2;
78         operationWord = " times ";
79         break;
80     case 4:
81         correctAnswer = number1;
82         number1 = number1 * number2;
83         operationWord = " divided by ";
84         break;
85     case 5:
86         randomOperator = true;
87         setOperation( Math.floor( 1 + Math.random() * 4 ) );
88         break;
89     default:
90         alert( "Operation type must be 1-5." );
91         return false;
92     } // end switch
93     return true;
94 } // end function setOperation
95 // -->
96 </script>
97 </head>
98 <body onload = "run()">
99 </body>
100 </html>

```

Explorer User Prompt

Script Prompt:

Enter problem type:
1 - Addition, 2 - Subtraction, 3 - Multiplication, 4 - Division, 5 - Mixed

OK Cancel

1

Explorer User Prompt

Script Prompt:

How much is 5 plus 5?

OK Cancel

10

Explorer User Prompt

Script Prompt:

Would you like to answer another question? (yes or no)

OK Cancel

no

Explorer User Prompt

Script Prompt:

Enter problem type:
1 - Addition, 2 - Subtraction, 3 - Multiplication, 4 - Division, 5 - Mixed

OK Cancel

5

Explorer User Prompt

Script Prompt:

How much is 9 minus 1?

OK Cancel

8

Explorer User Prompt

Script Prompt:

Would you like to answer another question? (yes or no)

OK Cancel

yes

Explorer User Prompt

Script Prompt:

How much is 8 times 7?

OK Cancel

56

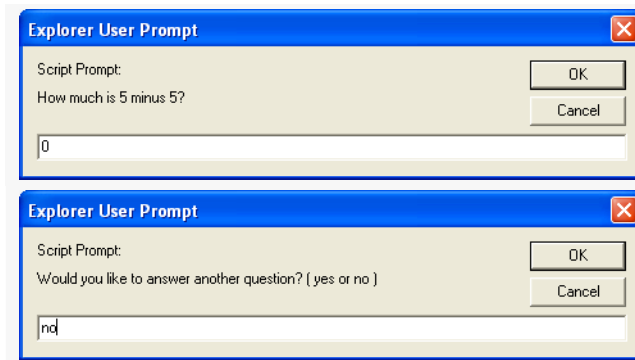
Explorer User Prompt

Script Prompt:

Would you like to answer another question? (yes or no)

OK Cancel

yes



9.33 Modify the craps program in Fig. 9.6 to allow wagering. Initialize variable `bankBalance` to 1000 dollars. Prompt the player to enter a wager. Check that the wager is less than or equal to `bankBalance` and, if not, have the user reenter wager until a valid wager is entered. After a valid wager is entered, run one game of craps. If the player wins, increase `bankBalance` by wager, and print the new `bankBalance`. If the player loses, decrease `bankBalance` by wager, print the new `bankBalance`, check whether `bankBalance` has become zero and, if so, print the message Sorry. You busted! As the game progresses, print various messages to create some chatter, such as Oh, you're going for broke, huh? or Aw c'mon, take a chance! or You're up big. Now's the time to cash in your chips!. Implement the chatter as a separate function that randomly chooses the string to display.

ANS:

```

1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.33: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.33</title>
9      <style type = "text/css">
10         table { text-align: right }
11         body { font-family: arial, sans-serif }
12         div.red { color: red }
13      </style>
14      <script type = "text/javascript">
15        <!--
16        // variables used to test the state of the game
17        var WON = 0;
18        var LOST = 1;
19        var CONTINUE_ROLLING = 2;
20
21        // other variables used in program
22        var firstRoll = true; // true if current roll is first
23        var sumOfDice = 0; // sum of the dice
24        var myPoint = 0; // point if no win/loss on first roll
25        var gameStatus = CONTINUE_ROLLING; // game not over yet
26        var balance = 1000; // the current balance
27        var wager; // the player's wager

```

```

28
29 // process one roll of the dice
30 function play()
31 {
32     chatter();
33
34     // get the point field on the page
35     var point = document.getElementById( "pointfield" );
36
37     // get the status div on the page
38     var statusDiv = document.getElementById( "status" );
39     if ( firstRoll ) // first roll of the dice
40     {
41         do
42         {
43             wager = parseInt( window.prompt( "Enter a wager:" ) );
44         }
45         while ( wager > balance );
46
47         balance -= wager;
48         document.getElementById( "wager" ).innerHTML = "Wager: "
49             + wager;
50         document.getElementById( "balance" ).innerHTML =
51             "Balance: " + balance;
52         sumOfDice = rollDice();
53
54         switch ( sumOfDice )
55         {
56             case 7: case 11: // win on first roll
57                 gameStatus = WON;
58                 // clear point field
59                 point.value = "";
60                 break;
61             case 2: case 3: case 12: // lose on first roll
62                 gameStatus = LOST;
63                 // clear point field
64                 point.value = "";
65                 break;
66             default: // remember point
67                 gameStatus = CONTINUE_ROLLING;
68                 myPoint = sumOfDice;
69                 point.value = myPoint;
70                 firstRoll = false;
71         } // end switch
72     } // end if
73     else
74     {
75         sumOfDice = rollDice();
76
77         if ( sumOfDice == myPoint ) // win by making point
78             gameStatus = WON;
79         else
80             if ( sumOfDice == 7 ) // lose by rolling 7
81                 gameStatus = LOST;
82     } // end else

```

```

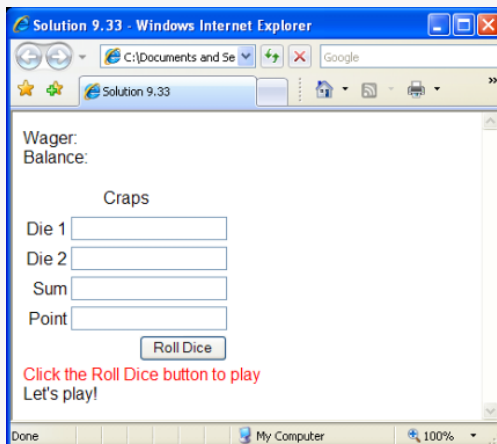
83
84     if ( gameStatus == CONTINUE_ROLLING )
85         statusDiv.innerHTML = "Roll again";
86     else
87     {
88         if ( gameStatus == WON )
89         {
90             statusDiv.innerHTML = "Player wins. " +
91                 "Click Roll Dice to play again.";
92             balance += 2 * wager;
93             document.getElementById( "balance" ).innerHTML =
94                 "Balance: " + balance;
95         }
96     else
97     {
98         statusDiv.innerHTML = "Player loses. " +
99             "Click Roll Dice to play again.";
100
101         if ( balance <= 0 )
102         {
103             alert( "You busted! Play again." );
104             balance = 1000;
105             document.getElementById( "balance" ).innerHTML =
106                 "Balance: " + balance;
107         }
108     }
109     firstRoll = true;
110 } // end else
111 } // end function play
112
113 // roll the dice
114 function rollDice()
115 {
116     var die1;
117     var die2;
118     var workSum;
119
120     die1 = Math.floor( 1 + Math.random() * 6 );
121     die2 = Math.floor( 1 + Math.random() * 6 );
122     workSum = die1 + die2;
123
124     document.getElementById( "die1field" ).value = die1;
125     document.getElementById( "die2field" ).value = die2;
126     document.getElementById( "sumfield" ).value = workSum;
127
128     return workSum;
129 } // end function rollDice
130
131 function chatter()
132 {
133     var chatterBox = document.getElementById( "chatter" )
134
135     if ( balance < 500 )
136         chatterBox.innerHTML = "You're going broke!";

```

```

137         else if ( balance > 1500 )
138             chatterBox.innerHTML = "You're doing well!";
139         else if ( balance > 3000 )
140             chatterBox.innerHTML = "You'd better cash in!";
141         else
142             chatterBox.innerHTML = "You haven't lost big yet...";
143     }
144     // -->
145 </script>
146 </head>
147 <body>
148     <div id = "wager">Wager: </div><div id = "balance">Balance: </div>
149     <form action = "">
150         <table>
151             <caption>Craps</caption>
152             <tr><td>Die 1</td>
153                 <td><input id = "die1field" type = "text" />
154                 </td></tr>
155             <tr><td>Die 2</td>
156                 <td><input id = "die2field" type = "text" />
157                 </td></tr>
158             <tr><td>Sum</td>
159                 <td><input id = "sumfield" type = "text" />
160                 </td></tr>
161             <tr><td>Point</td>
162                 <td><input id = "pointfield" type = "text" />
163                 </td></tr>
164             <tr><td /><td><input type = "button" value = "Roll Dice"
165                 onclick = "play()" /></td></tr>
166         </table>
167         <div id = "status" class = "red">
168             Click the Roll Dice button to play</div>
169         <div id = "chatter">Let's play!</div>
170     </form>
171 </body>
172 </html>

```



Explorer User Prompt

Script Prompt:
Enter your wager:

100

OK
Cancel

Solution 9.33 - Windows Internet Explorer

C:\Documents and Se Google

Solution 9.33

Wager: 100
Balance: 1100

Craps

Die 1 1
Die 2 6
Sum 7
Point

Roll Dice

Player wins. Click Roll Dice to play again.
You haven't lost big yet...

Done My Computer 100%

Explorer User Prompt

Script Prompt:
Enter your wager:

500

OK
Cancel

Solution 9.33 - Windows Internet Explorer

C:\Documents and Se Google

Solution 9.33

Wager: 500
Balance: 600

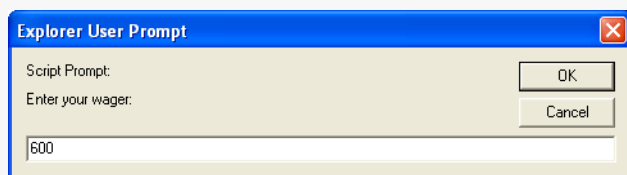
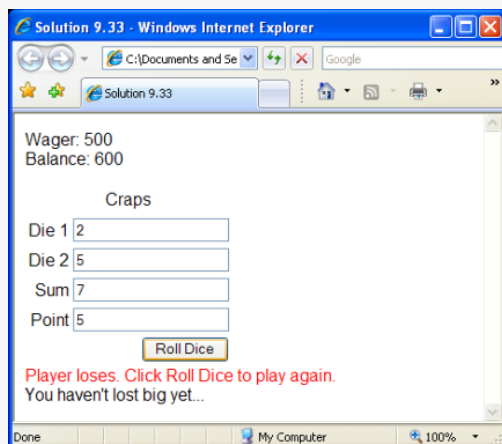
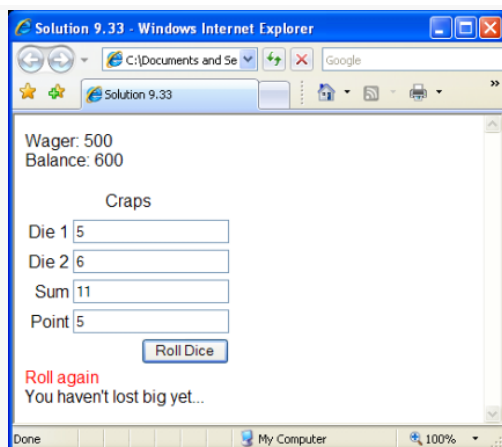
Craps

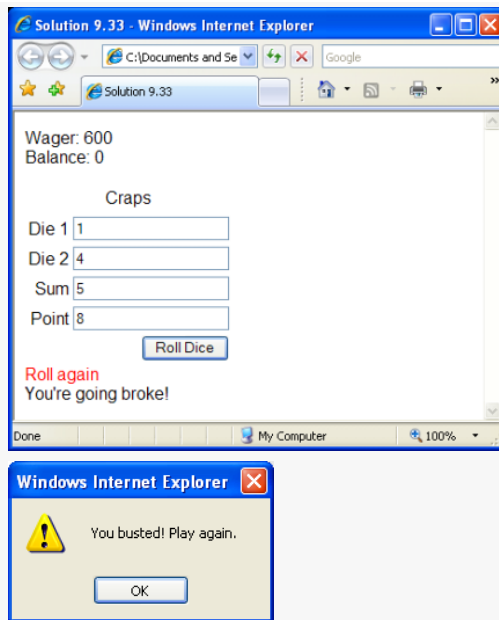
Die 1 2
Die 2 3
Sum 5
Point 5

Roll Dice

Roll again
You haven't lost big yet...

Done My Computer 100%





9.34 Write a recursive function `power(base, exponent)` that, when invoked, returns $base^{exponent}$

for example, `power(3, 4) = 3 * 3 * 3 * 3`. Assume that `exponent` is an integer greater than or equal to 0. The recursion step would use the relationship

$$base^{exponent} = base \cdot base^{exponent - 1}$$

and the terminating condition occurs when `exponent` is equal to 0, because

$$base^0 = 1$$

Incorporate this function into a script that enables the user to enter the base and exponent.

ANS:

```

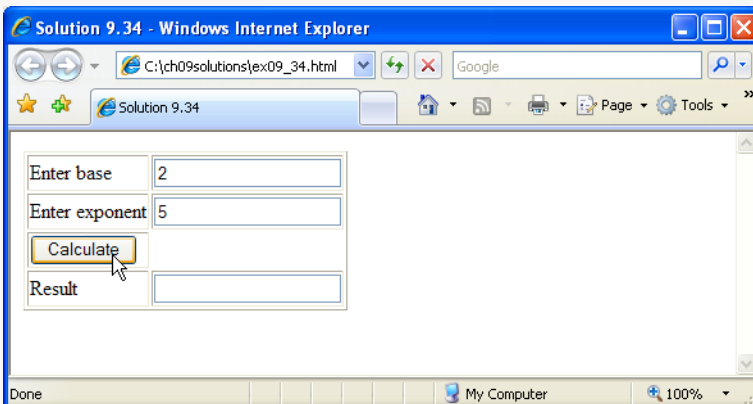
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.34: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.34</title>
9      <script type = "text/javascript">
10         <!--
11         function getPower()
12         {
13             var form = document.getElementById( "myForm" );
14             var base = parseInt( form.base.value );
15             var exponent = parseInt(form.exponent.value );
16             form.result.value = power( base, exponent );
17         } // end function getPower

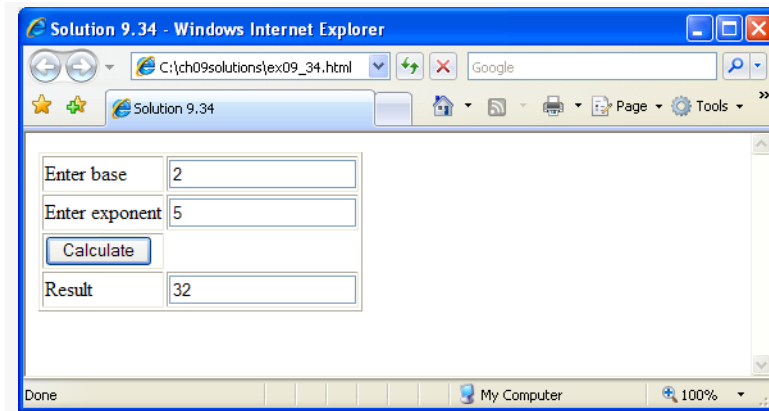
```

```

18
19     function power( b, exp )
20     {
21         if ( exp == 0 )
22             return 1;
23         else
24             return b * power( b, exp - 1 );
25     } // end function power
26     // -->
27 </script>
28 </head>
29
30 <body>
31     <form id = "myForm" action = "">
32         <table border = "1">
33             <tr><td>Enter base</td>
34                 <td><input name = "base" type = "text" />
35             </td>
36         </tr>
37         <tr><td>Enter exponent</td>
38             <td><input name = "exponent" type = "text" />
39         </td>
40     </tr>
41     <tr><td><input type = "button" value = "Calculate"
42         onclick = "getPower()" /></td>
43     </tr>
44     <tr><td>Result</td>
45         <td><input name = "result" type = "text" />
46     </td>
47 </tr>
48 </table>
49 </form>
50 </body>
51 </html>

```





9.35 (*Visualizing Recursion*) It is interesting to watch recursion in action. Modify the factorial function in Fig. 9.11 to display its local variable and recursive-call parameter. For each recursive call, display the outputs on a separate line and add a level of indentation. Do your utmost to make the outputs clear, interesting and meaningful. Your goal here is to design and implement an output format that helps a person understand recursion better. You may want to add such display capabilities to the many other recursion examples and exercises throughout the text.

ANS:

```

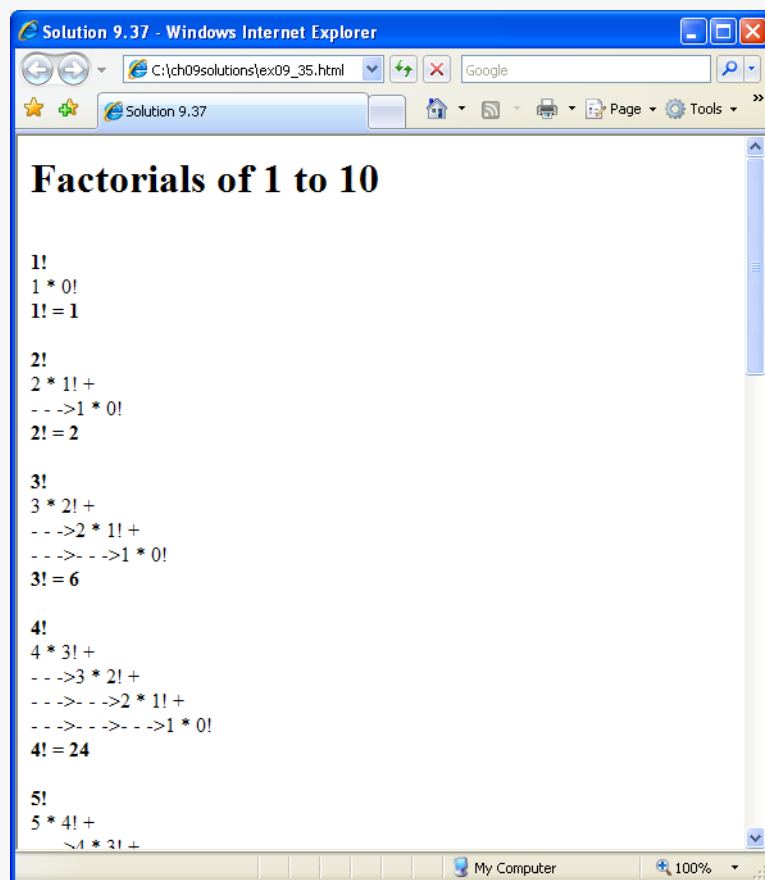
1  <?xml version = "1.0" encoding = "utf-8"?>
2  <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Strict//EN"
3    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-strict.dtd">
4
5  <!-- Exercise 9.35: Solution -->
6  <html xmlns = "http://www.w3.org/1999/xhtml">
7    <head>
8      <title>Solution 9.35</title>
9      <script type = "text/javascript">
10         <!--
11         var indent = "";
12
13         document.writeln( "<h1>Factorials of 1 to 10</h1>" );
14
15         for ( var i = 1; i <= 10; i++ )
16         {
17             document.writeln( "<br /><strong>" + i +
18                               "!</strong><br />" );
19             var fact = factorial(i);
20             document.writeln( "<strong>" + i + "! = " +
21                               parseInt(fact) + "</strong><br />" );
22             indent = "";
23         } // end for
24         //recursive definition of function factorial
25         function factorial( number )
26         {
27             if ( number <= 1 ) // base case
28             {

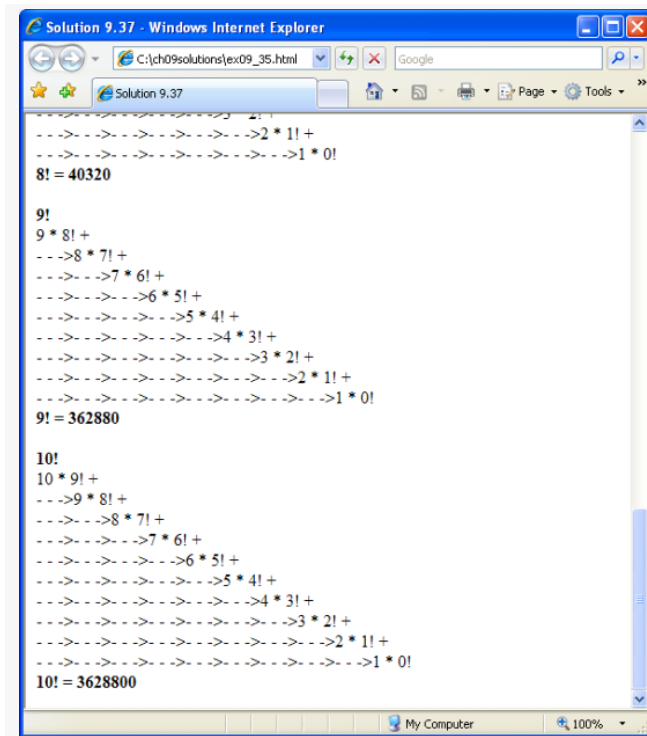
```

```

29         document.writeln( indent + parseInt(number) +
30             " * " + parseInt( number - 1 ) +
31             "! <br />" );
32         return "1";
33     } // end if
34 else
35 {
36     document.writeln( indent + parseInt(number) +
37         " * " + parseInt( number - 1 ) +
38         "! + <br />" );
39     indent += " - - ->";
40     return number * factorial( number - 1 );
41 } // end else
42 } // end function factorial
43 //-->
44 </script>
45 </head>
46 <body></body>
47 </html>

```





9.36 What does the following function do?

```
// Parameter b must be a positive
// integer to prevent infinite recursion
function mystery( a, b )
{
    if ( b == 1 )
        return a;
    else
        return a + mystery( a, b - 1 );
}
```

ANS: The function performs the multiplication of a and b, where b must be greater than or equal to 1.

9.37 Find the error in the following recursive function, and explain how to correct it:

```
function sum( n )
{
    if ( n == 0 )
        return 0;
    else
        return n + sum( n );
}
```

ANS: The value n does not decrement toward the (n == 0) base case, creating an infinite loop. Fix this problem by calling return n + sum(n - 1) instead.