Introduction to Deep Learning Lecture 6 Convolutional Filters

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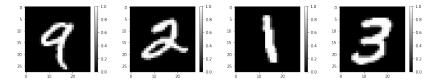




Housekeeping

- Some references for today
 - Official pytorch tutorials
 - Pytorch tutorials by yunjey, from beginning to advanced
 - Deep Learning Book on ConvNets
 - MIT Intro to Deep Learning Lecture on ConvNets
- Today's url
 - https://git.io/2020deep06
- Email if you need help with any of this!

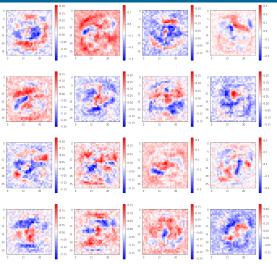
What do we want a neural network to do?



- Thinking of our mnist dataset from last week and a 2 layer hidden network, we might expect/want the network to piece together a structure like this
 - In the first layer, find loops and lines in the various parts of the image
 - In the second layer, see if they combine together (fire at the same time), in certain combinations
- In the example, theres a "loop" a the top connected to a "line" for 9, a similar "loop" at the bottom but connect to a "hook", a "line" similar to that in 9 for the 1, and some "hooks" for the 3
- Is the network structured this way? I.e. are there "loop", "hook", "line" finders

idea from 3blue1brown on neural nets

What does it really do?



- Plot of the weights from each pixel connection in the first layer of a 2 hidden layer model from MNIST (red means this pixel should be fired to fire this node, blue means that if the pixel is fired the node is suppressed)
- Maybe recognizable structures, but lots of fairly random swirls
- One issue with the network is that structures like loops and lines need to be fit, but these can appear in different places on the image
- So, we don't have a "loop finder" node, we need to find loops in any
 of many different points on the image, leading to a jumble of weights

• Can we change our network so "loop finder" structures are possible?

Lan J. Watson (UoS)

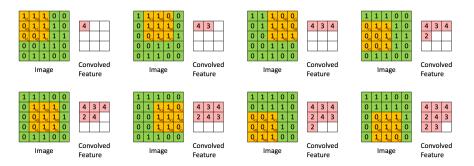
Convolutional Filters

Intro to Deep Learning

Convolutional Layers

- A convolution layer is a connection between one layer and the next in a NN with a very specific structure:
 - Typically, it works with a 3d input like an image: channels (red, green, blue), width, height
 - It contains a kernel or filter, which is a 3d block sized channel × n × m, n and m are user-specified, with each element of the block a weight to be set in training
 - The outputs consists of all $n \times m$ convolutions of the filter with the image, creating a new one-channel image
 - Discrete convolution, meaning each element of the kernel is multiplied with a pixel in (one channel of) the image, and all are summed together
 - The output of the filter is passed through an activation function, the same as the usual fully-connected layer
- A single convolutional layer generally consists of many convolutional filters, each filter giving one layer in the output
- Networks with convolutional layers are Convolutional Neural Networks: CNN

Convolutional Filters In Pictures



 1
 1
 1
 0
 0

 0
 1
 1
 1
 0
 4
 3
 4

 0
 0
 12
 12
 2
 4
 3
 4

 0
 0
 12
 12
 0
 2
 3
 4

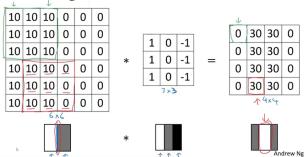
 0
 1
 12
 0
 0
 0

Image

- Convolved Feature
- A filter sliding over the image builds up the output layer, each output is sum of filter elements multiplied by image pixels
- The same filter is used for each pixel, the weights are learnt during training (as well as an output bias)

Example Filter

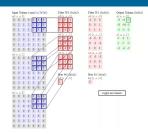
Vertical edge detection



- As an example, here is a 3x3 filter for detecting vertical edges
- The opposing plus and minus sides cancel in a block of color
- At an edge, the filter is either highly positive (white to left of edge), or negative (white to right of edge)
- What would a horizontal edge detector look like?

Andrew Ng lecture by way of https://kharshit.github.io/blog/

Multiple Filter Outputs

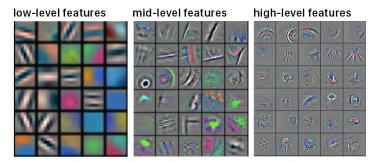


- When multiple filters are used in a single layer, they have the same width and height, so they can be put together in a single output as channels × width × height
- This is exactly the image structure which was the input to the network
- This means this convolutional structure can be used several times in series
 - Each successive layer effectively sees a larger part of the image, since each pixel in the output of one layer is from several pixels

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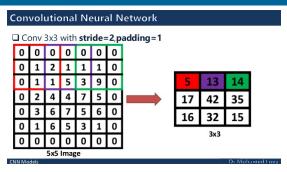
• The image shows that a 3-channel input needs filters with a 3x3x3 block, and 2 filters produce a 2 channel output

Filters Over Several Input Layers



- Convolutional layers are typically built up one after the other
- The idea is that features get built up, at low levels, you might have edge detectors, later layers use these edges to build up structure, and by high levels recognizable objects are being searched for
 - These images are made by doing reverse gradient descent on the network, i.e. updating the image pixels themselves, trying to make the image "light up" (set node output high) a particular node
- Networks these days can contain *hundreds* of these layers
 - This is the meaning of *deep* in deep learning

Strides and Padding



- When sliding across the image, you can move the filter more than 1 pixel at a time, this is the stride
 - By default its just 1, ie sliding the image
- The filter will reduce the size of the image (can only fit in so many 3x3 blocks), you can *pad* the image (with zeros, or copying the outer variables) to keep the outputs the same size
- Can also use different strides or pads in the vertical and horizontal directions

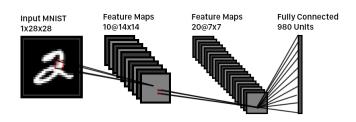
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Pooling Layers

$$\begin{pmatrix} 1 & 2 & 3 & 4 \\ 2 & 3 & 4 & 5 \\ 4 & 3 & 2 & 1 \\ 5 & 4 & 3 & 2 \end{pmatrix} \rightarrow_{max}^{2x2} \begin{pmatrix} 3 & 5 \\ 5 & 3 \end{pmatrix}$$

- We may want to reduce the size of the images flowing through the network for computational and conceptual efficiency reasons
 - As we add filters, we should be building up higher level features, which are less localized on the image
 - Another way to say this is we want to downsample the image
- We can reduce the image through *pooling*, applying an operation on each $n \times n$ patch of the image (leaping not sliding)
- A typical use is max pooling, we could find the maximum of each patch of the image
- \bullet Here, we apply a 2 \times 2 max pooling to reduce a 4 \times 4 matrix to 2 \times 2
- Another typical operation is to take the average of each patch

Structuring a Network with Convolutional Layers



- The basic CNN consists of several convolutional layers, followed by "squashing" the output of the last convolution into a regular 1d node structure, after which the fully connected layers of a normal NN can be used
- So the idea is, the convolutional layers search for particular high level "features", then the output is decided by which features do or do not exist in the network

Image from https://twopointseven.github.io/2017-10-29/cnn/

Some Benefits of The Convolutional Neural Network

- Fewer parameters than a fully connected network
 - Parameters for a cxhxw image fully connected to n nodes: cxhxwxn + n
 - Parameters for a cxhxw image convolutional to n mxm filters (no padding/stride 1): cxmxmxn + n
 - If our filter size is smaller than the image, much, much fewer parameters, and independent of input height, width
 - Fewer parameters is better for overtraining
- The sliding connections mean the network can learn features independent of position
 - A fully connected layer would need to learn what a 'hand' or an 'eye' looks like independently everywhere it could be in the image
 - This parameter sharing between parts of the image means that the network can learn more robust features
- We have developed a structure which could possibly be our "loop finder"

Convolutional Filters in pytorch

- torch.nn.Conv2d provides a convolutional filter, you tell it:
 - The number of input channels
 - The number of output channels
 - The size of the filter (can be a number for nxn or a 2-tuple for nxm)
 - Optionally, you can change the stride and the padding
- The filters take in tensors of rank 4, with shape: (number of images, number of channels, height of image, width of image) (pytorch always assumes you're processing multiple images)
- The output is also a rank 4 tensor, with the number of output channels changed, and the height and width can be expanded or contracted by changing the stride and padding

Pooling Layers in pytorch

- Similar to Conv2d, there is torch.nn.MaxPool2d and torch.nn.AvgPool2d to max and average pooling respectively,
- They only need to be given the filter size, and have similar input/output shapes (rank-4 tensors everywhere)

```
pool = torch.nn.MaxPool2d(2)
pool(torch.tensor([ [[[1,2,3,4],[1,1,1,1],
                       [1,1,1,1],[4,5,6,7]]]
tensor([[[[2., 4.],
         [5., 7.]]])
pool = torch.nn.AvgPool2d(2)
pool(torch.tensor([ [ [[1,2,3,4],[1,1,1,1],
                       [1.1.1..1], [4.5.6.7]]
tensor([[[[1.2500, 2.2500],
          [2.7500, 3.7500]]]])
```

Building a Network

- Networks will at some point need to go from processing 2d images with multiple channels, to a discrete probability distribution (if we are making a classifier)
- You can insert a view into the forward function to adjust the output nodes into a 1d line (-1 at the front so it automatically sizes to any number of images in the input)
- Here is a simple CNN for MNIST with 1 convolutional layer, which is reshaped and then connected to the 10 category output layer

```
class SimpleCNN(torch.nn.Module):
    def __init__(self):
        super(SimpleCNN, self).__init__()
        self.conv = torch.nn.Conv2d(1,6,5) # 5x5 filter, no padding
        self.fc = torch.nn.Linear(6*24*24,10)
    def forward(self, x):
        x = torch.tanh(self.conv(x))
        x = self.fc(x.view(-1, 6*24*24))
        return x
```

Exercises

We will train a few convolutional networks in pytorch.