#### Calibration and Analysis of the GCT Camera for the Cherenkov Telescope Array

Jason J. Watson

Brasenose College University of Oxford

A thesis submitted for the degree of Doctor of Philosophy

Trinity 2018

#### Abstract

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#### Acknowledgements

#### Personal

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#### Abstract

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#### Abbreviations

**AC** Alternating Current.

**ADC** Analogue-to-Digital Converter.

**ASIC** Application-Specific Integrated Circuit.

CHEC Compact High Energy Camera.

**CHEC-M** Compact High Energy Camera (CHEC) using Multi-Anode Photomultiplier Tubes (MAPMTs) as the detector.

**CHEC-S** CHEC using Silicon Photomultiplier Tubes (SiPMTs) as the detector.

CTA Cherenkov Telescope Array.

**DC** Direct Current.

**FEE** Front-End Electronics.

FITS Flexible Image Transport System.

GCT Gamma-ray Cherenkov Telescope.

HV High Voltage.

**IACT** Imaging Atmospheric Cherenkov Telescope.

MAPMT Multi-Anode Photomultiplier Tube.

**NSB** Night-Sky Background.

**p.e.** Photo-Electrons.

**PDE** Photon Detection Efficiency.

**PMT** Photomultiplier Tube.

**RMSE** Root-Mean-Square Error.

**SiPMT** Silicon Photomultiplier Tube.

Abbreviations

**SPE** Single Photo-Electron.

**TARGET** TeV Array Readout with GSa/s sampling and Event Trigger.

**TARGET 5** TARGET (TeV Array Readout with GSa/s sampling and Event Trigger) (version 5).

**TARGET** C TARGET (version C).

**Vped** Pedestal voltage input into the TARGET ASIC.

#### Introduction

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1. Introduction

#### 1.1 Plan

#### **1.1.1** Topics

- High Energy Astrophysics
  - Fermi
  - Fermi Bubbles
  - HAWC
- IACTs
- CTA
- CTA Science
  - Science Cases
  - $-\,$  Use "Science with CTA" paper
- SSTs
- SST Science
  - What do we contribute?
  - What can't be done without us?
- GCT
- CHEC
  - What makes us better?
  - Advantages of Schwarzchild-Couder
    - \* Increased FoV
    - \* Size
    - \* Cost
  - Advantages of full waveform readout
  - Other Advantages?
    - \* Trigger
    - $* \quad {\tt Energy/power/voltage \ Requirements}$
    - \* Commonalities (SCT)

#### 1.1.2 Questions

Shower properties, photons from bottom of shower are received before those at the top as the particle travels faster than light. Good figure in [1]

 ${\rm Gamma/Hadron/Lepton}$ 

### 2

#### Camera Design & Mechanics

2.1 Plan          2.1.1 Topics          2.1.2 Questions          2.2 Introduction	3 3 3 <b>3</b>
2.1 Plan 2.1.1 Topics	
Introduce TARGET architecture & Wilkinson ADC     Different TARGET versions	
• FEE	
• MAPMs	
• SiPMS	
<ul><li>How they work</li><li>Comparison investigations</li><li>Property trade-offs</li></ul>	
• CHEC-M	
Changes for CHEC-S	
Future - MUSIC ASICs	
2.1.2 Questions	

#### 2.2 Introduction

Contents

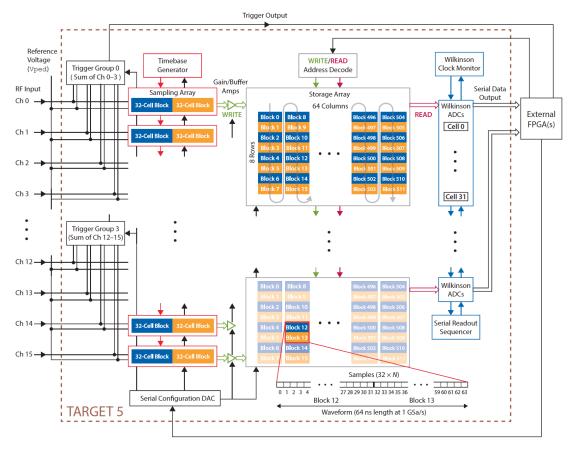


Figure 2.1: Functional block diagram of the TARGET 5 ASIC [2]

Add more details

### 3 CTA Architecture

# 3.1 Plan 5 3.1.1 Topics 5 3.1.2 Questions 5 3.1. Plan 3.1.1 Topics • Requirements • Data Levels 3.1.2 Questions • ?

# Software

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	4.1.2	Questions														6

#### 4.1 Plan

#### **4.1.1** Topics

- TargetIO/TargetDriver
- TargetCalib
- ctapipe
- gammapy/CTOOLS

#### Questions 4.1.2

### 5

#### Calibration

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#### 5.1 Plan

#### **5.1.1** Topics

- Pedestal subtraction
- Transfer functions
- Gain Matching
- SPF
- Flat fielding
- · Time correction
- Future
  - Live calibration

#### 5.1.2 Questions

- TARGET architecture diagram, Wilkinson ADC
- How much detail about all the TF approaches do I go into?

Flow diagrams? See Cyril talk 18/07/06 camera calibration call

#### 5.2 Introduction

In order to obtain meaningful and reliable results from the camera, a number of calibrations must be applied to the waveforms read. A primary objective of my DPhil is to investigate the most optimal and efficient approaches for these calibrations (in accordance with the Cherenkov Telescope Array (CTA) requirements described in Chapter 3), and to determine if additional calibrations are required.

The calibrations applied have evolved during the course of the prototyping of CHEC; the calibrations applied to CHEC using MAPMTs as the detector (CHEC-M) waveforms are not the same for CHEC using SiPMTs as the detector (CHEC-S). Additionally, the calibration applied for the on-sky pipeline can differ slightly to the calibration used to obtain results such as the charge resolution.

When I joined the CHEC development, the calibration discussion was still in it's infancy. Some approaches had been tested in a laboratory environment [3], but there had been little discussion on how exactly the calibrations will be applied efficiently in an analysis pipeline, where one may not be able to use the same detailed calibration due to limited resources (such as memory and time). A major contribution of my DPhil was to prototype the calibrations procedures, develop an approach for a calibration pipeline, write the software to perform such a pipeline, and finally assess the performance of the pipeline. This was an iterative procedure,

the development of which is still ongoing, however a procedure now exists that allows us to obtain meaningful results from the waveform data, a capability that is of paramount importance in the commissioning of the camera.

In this chapter I will outline the each of the calibration steps that are presently adopted for CHEC camera. They are introduced in the general order that they are applied, and split into the categories of TARGET ASIC (Application-Specific Integrated Circuit), photosensor, and "other" calibrations.

#### 5.3 TARGET Calibration

The calibrations described in this section relate to the TARGET module. As detailed in Chapter 2, the TARGET ASIC is responsible for the sampling, digitisation and readout of the waveform data. As a result there are two calibrations that are solely related to the TARGET ASIC: electronic pedestal subtraction and the linearity correction via the transfer function.

The functional block diagram of the TARGET ASIC in Figure 2.1 outlines the electronics responsible for the need of these calibrations, and should be used as a reference in the following descriptions.

As the calibrations in this section are very low-level, and related to CHEC's specific Front-End Electronics (FEE), they are handled by the TargetCalib library (described in Chapter 4).

#### 5.3.1 Electronic Pedestal Subtraction

The most important, but also the simplest calibration to apply is the subtraction of the electronic pedestal. Each of the cells in the storage array of the ASIC is a unique capacitor. For a specific input input pedestal voltage (Vped), each capacitor has its own resulting electronic pedestal value. As each sample of the waveform corresponds to a single storage cell, each sample therefore has a unique pedestal value to be subtracted. This is apparent in Figure where the variation from sample-to-sample is very large. This variation is large enough that low amplitude pulses are undetectable in the waveform (Figure )) and therefore it is paramount to subtract this per-sample pedestal.

There are  $2^{14} = 16,384$  storage cells per channel (for CHEC-M,  $2^{12} = 4096$  for CHEC-S), therefore there are 32(Modules) \* 64(Channels) \* 16,384(Cells) pedestal values to keep record of. However, there is an additional contribution to the behaviour of the pedestal - discharging a cell to readout its value will slightly discharge adjacent cells. The result of this effect is that the further along in the

Create figure showing the raw waveform and its pedestal subtracted form (no HV)

Figure with low amplitude pulse before and after pedestal subtraction, and high amplitude pulse the same, also mirrored camera image?

DRAFT Printed on July 11, 2018

Figure 5.1

Insert and update

waveform a cell is, the lower its pedestal value will be. An extra dimension of "position in waveform" consequently needs to be considered. This effect is illustrated in Figure , and its affect demonstrated in Figure .

include figures

#### Generation

In order to perform the pedestal subtraction, one must first generate the lookup table of pedestal values. This can be easily obtained with a calibration run where the photosensors are disabled by turning off the High Voltage (HV) , and forcing the camera to trigger (with either an external pulse generator, or internally via software) to obtain a large amount of waveform data. Typically around 30,000 events provide enough samples for every storage cell, in every waveform position, to be hit at least 10 times. The samples are then collected as a running average with the dimensions [ $Module, Channel, StartingBlock, Blockphase + Sample\_i$ ], where the StartingBlock is the storage block that the first sample in the waveform belongs to (see Figure ), Blockphase is the cell index within the storage block that the waveform begins on, and  $Sample\_i$  is the index of each sample in the waveform. This is illustrated in Figure , where for these two readout windows shown, the pedestal running average Pedestal [TM] [CHANNEL] [9] [8:103] and Pedestal [TM] [CHANNEL] [8] [12:107] will be contributed to respectively.

is it HV when considering the sipms?

bp 8 and 12

include

figure, and edit to use

Figure shows a visual representation of the pedestal lookup table for a single channel.

The TargetCalib library handles this generation, and stores the pedestal look-up table into a FITS (Flexible Image Transport System). A new pedestal file is typically generated at the start of each new dataset, as its dependencies on temperature and evolution with time are still being investigated.

A figure showing the lookup table of the pedestal, for checm due to the storage block ordering. Annotate a single repeated

block

#### Application

To apply the pedestal, the entry within the lookup table that corresponds to each sample is subtracted from the waveform. The result of the calibration can be seen in Figures .

talk about the variation in pedestal values, and mean? Talk bout the pattern seen between blocks

Figure 5.2

Insert and update, Also include extra plot versus event

#### Performance

One quantification of this calibration's performance is the standard deviation per sample of the residual waveform from applying the pedestal subtraction to the data used to produce it. Figure 5.1 shows the spread in these values .

This quantity informs about the intrinsic spread of the pedestal values about their mean, and can also indicate at some changes in pedestal value with time. Figure 5.2 demonstrates an occurrence of the pedestal value changing with time, and is investigated further in Section 5.5.2.

quote conversion into photo-electrons, and write actual resulting performance, and talk about if its good enough

#### 5.3.2 Transfer Function

The other calibration related to the digitisation and readout inside the TARGET ASIC is caused by the non-linearities in the storing and reading of charge to and from the storage cells. The components responsible for the need for this calibration are the sampling array, gain/buffer amps, and the Wilkinson Analogue-to-Digital Converters (ADCs), seen in Figure 2.1. As a result of the non-linearity of these components, the sample value readout does not scale linearly - a sample with twice the amplitude input into TARGET will have less than twice the amplitude when readout.

To correct for this non-linearity, a look-up table is generated to convert from the sample amplitude read-out (in ADC counts), to the input sample amplitude (in mV). This look-up table is known as the Transfer Function. As one might expect, each sampling cell has its own linear response to correct for, and therefore a look-up table is typically required at-least per channel and per sampling cell, however a noticeably improved performance is observed by considering a Transfer Function per storage cell .

There are two forms of Transfer Function that have been considered for CHEC, distinguished by the type of input used to generate them. A Direct Current (DC) Transfer Function is created by applying a constant DC input of known voltage into the module, and iterating over the full dynamic range by varying the voltage. An Alternating Current (AC) Transfer Function is generated by inputting an AC signal (such as a pulse with the expected shape from the photosensor plus shaper) of known amplitude, and iterating as with the DC approach. During previous investigations of the TARGET module, where sinusoidal signals were input into the module, a dependence on the signal frequency and input amplitude was observed that acts

need to show this, maybe in TF Investigations appendix?

to further reduce the output amplitude [3][2]. The source of this dependence was deemed to be due to the amplifiers, which cannot slew fast enough to keep up with the input signal if the frequency and amplitude are large.

#### Generation (DC Transfer Function)

During the commissioning of CHEC-M, a DC Transfer Function was used with no AC corrections. To generate this Transfer Function the internal input pedestal voltage (Vped) setting is used to apply a DC voltage offset of known amplitude. The full dynamic range of the module is explored by repeating the process for amplitudes between . The waveforms produced by these runs are read-out, and the running average range is grouped and monitored according to [Module, Channel, SamplingCell, InputAmplitude], utilising every sample in the waveform. Around 1,000 events are required to provide sufficient statistics. This produces a lookup table like the one shown in Figure . figure

The second step in the generation is to flip the axes of this lookup table, and linearly interpolate at the ADC points defined by the user. This provides a second lookup table that can be more efficiently used to provide a calibrated mV value for the measured ADC value (Figure ). This table is saved to a FITS fall figure file, ready for application.

#### Generation (AC Transfer Function)

As the ability to internally set a DC voltage with a known amplitude via the Vped was made more difficult in TARGET (version C) (TARGET C) (see 2) , and the ability to input a DC voltage externally is prohibited by the AC coupling of the module , the decision was made to transition to an AC Transfer Function that uses the expected pulse shape as an input. This approach therefore corrects for the AC effect with the appropriate frequency.

The full dynamic range is once again explored, by injecting pulses of a variety of amplitudes. In order to extract the values that correspond to negative amplitudes in this method, the amplitude of the input undershoot is also monitored. Only the samples that corresponds to the maximum of the input pulse (and minimum of the undershoot) has a "true" amplitude of the input amplitude. Therefore to extract the correct samples, each waveform is fitted with two Landau functions, a fair approximation to the pulse shape (Figure ). Consequently, only two samples are extracted per waveform, requiring a much larger population of events (200,000) in order to generate a reliable running average grouped according to [Module, Channel, StorageCell, InputAmplitude]. It is important to note that a

more
precise
ref, and
remember
to mention this
change

remember to introduce ac coupling

figure showing

Transfer Function per storage cell was adopted for TARGET C, as it was found to significantly improve the residuals (see <u>for further discussion</u>).

appendix tf investigations

The second step in the generation is identical to the DC Transfer Function. The resulting lookup tables can be seen in Figures & .

add figures

#### Application

Irrespective of the Transfer Function type, they are stored in a format which enables them to be applied identically. When calibrating a waveform, the relevant lookup table is obtained according to the channel and cell of the sample, and is linearly interpolated to provide the calibrated value in mV.

#### Performance

Due to its complexity and variety of approaches, the Transfer Function is still one of the most actively discussed aspects of the CHEC calibration, and is most certainly the area where the majority of improvements can be made. Some possibilities for improvement include:

- An improved sample extraction method for the AC Transfer Function Waveform
- Possibilities for a DC approach for TARGET C
- Returning to the approach described in [2] where the pedestal is included inside the Transfer Function
- Alternatives to linear interpolation, such as Piecewise Cubic Hermite Interpolating Polynomial (PCHIP)
- Exchanging the lookup table for a parametrised regression characterisation of the Transfer Function
- Decision between "per storage cell" or "per sampling cell"
- Inclusion of temperature corrections

Appendix provides some insight into the current progression in these active investigations.

 $\begin{array}{c} {\rm tf~investi-} \\ {\rm gations} \end{array}$ 

Assessing the performance of the Transfer Functions is a more complicated task than for the pedestals. This is largely because instead of a comparison to a null signal, you are instead comparing to an input amplitude which contains its own uncertainty,

and could potentially be incorrect. So while the residuals of the Transfer Function may be small, it does not necessarily mean the calibration is accurate. Therefore the most decisive performance indicator should be one that provides an independent measurement on the "correct" amplitude. The most obvious scheme fitting this requirement is the charge resolution, covered in detail by 7. However, while it does hold the drawbacks just mentioned, investigating the residuals through the Root-Mean-Square Error (RMSE) can provide insights on the Transfer Function calibrated unhindered by other components in the detector chain. Figure demonstrates the RMSE for the presently adopted Transfer Functions for TARGET C, compared to a simple calibration with a fixed conversion value  $X \ mv/ADC$ .

For ch7: Remember to talk about how the MC charge resolution provides us insight into performance with perfect Transfer

figure

obtain sensible value, and talk about the result a bit, nonlinearity, show equation for RMSE

#### 5.4 Photosensor Calibration

The other primary component in the detector chain that requires calibration is the photosensor itself. As photosensors are a much more common instrument used in a variety of experiments, the calibration procedures typically already exist, and it is a simple case of adapting them to fit our needs.

However, unlike with the TARGET modules, where the procedures are very similar between CHEC-M and CHEC-S, an MAPMT is very different to a SiPMT. Therefore it is logical to deal with the calibration procedure for each of these photosensors separately.

#### 5.4.1 CHEC-M

Photomultiplier tubes have been widely used in Gamma-ray Astronomy since the first Imaging Atmospheric Cherenkov Telescopes (IACTs) , therefore the characterisation of these devices is very well understood. However, MAPMTs are a more recent evolution of the devices, and although they have the same underlying concept, they do suffer from some limitations, such as the inability to tweak the HV on a pixel level, and the electrical crosstalk across the tightly packed pixels .

get source

check checm paper for other limitations

A common method to characterize MAPMTs, and the one we also adopted, is the use of the Single Photo-Electron (SPE) spectrum. The primary result this spectrum provides is the per pixel value to calibrate from the measured signal in mV (or mV\*ns for integrated charge) to Photo-Electrons (p.e.). This conversion value is hereafter referred to as the SPE value. In order to investigate this parameter, the photosensor is illuminated with a very low light level (average illumination

<1 p.e. per pixel). As the photosensor is essentially a photon counting device, the individual peaks of the photoelectrons that are produced by the photocathode can be identified in the histogram of charge amplitudes. The SPE value is therefore the average charge of the first photoelectron peak. However, the resolution of these peaks can be quite poor, especially for MAPMTs, therefore the resulting distribution is fit with a function that characterises the photosensor:</p>

add equation for mapm spe fit, and reference its origin

SPE fit plots

This SPE value is proportional to the gain of the photomultiplier, and therefore also proportional to the HV applied across the photomultiplier. In order to extract a clear SPE spectrum, the voltage across the MAPMTs are set to the maximum value of 1100 V, thereby maximising the separation between the photoelectron and pedestal peaks.

In order to extrapolate the correct SPE value for other HV settings, the following relation:

Can be used in combination with a logarithmic fit of a dataset where the amplitude is measured as a function of HV to obtain  $\alpha$  per pixel.

In order to apply this calibration, the SPE value (with units of  $mV * ns * p.e.^{-1}$ ) per pixel is multiplied by the charge extracted per pixel.

show a waveform with this factor applied, maybe also the spectrum

5.4.2 CHEC-S

In the transition to SiPMTs, the calibration procedure for the photosensors was revised to better utilise the upgraded functionality of CHEC-S.

#### Gain Matching

Firstly, the voltage across the photosensors are now configurable per superpixel (group of 4 pixels) as opposed to per module. This allows the voltage to be fine-tuned to produce an identical gain response on a per superpixel level.

The procedure for this is illustrated in Figure:

- The camera is illuminated with approximately 50 p.e.

• The waveforms are readout and averaged per superpixel (excluding any dead pixels)

double check, maybe linear regression in log space?

include plot of relation

plots of the SPE values at different hv sets

superpixels in ch3

• The next voltage settings are calculated such that they will reduce the spread in the pulse height of the averaged waveforms

• The new voltage setting are applied, and the process is repeated

This iterating approach reduces the gain spread between pixels from (Figure )

need a note here or in ch2 about how other parameters of an sipmt change with hv

add final compari-

values

The additional benefit of this calibration is that changes in temperature, which would normally affect the gain, can be accounted for by changing the HV, therefore maintaining a constant gain response across the camera. This particular in situ calibration has not yet been implemented, but is intended for the future.

plot with gain vs temperature?

#### **SPE** Calibration

The second step in the CHEC-S photosensor calibration differs according to the purpose of the dataset being calibrated. In order to completely characterise the camera, and produce the Charge Resolution results, the per pixel SPE value must be obtained, and used to produce the absolute charge in a waveform (the complete Charge Resolution procedure can be found in Chapter ??).

The function that characterises the SPE distribution of an SiPMT is not wildly different to that of an MAPMT, but does include the significant contribution of the optical crosstalk:

write function

The other significant difference in the SPE distribution of an SiPMT is the improved resolution of the peaks. Typically when an SiPMT is illuminated at peaks from can be identified. Figure shows the SPE spectrum for the model of SiPMT we have installed into the camera. However, due to the inclusion of the other electronics in the camera, this incredible resolution is mostly suppressed, but is still significantly better than what was observed with CHEC-M.

Figure shows the SPE spectrum and fit for a pixel in our camera. The resulting parameters are

talk about the spe fit parameters, and show some histograms

reference chec-m figure

obtain spe figure of

sipm on its own

illumination

figure

#### Flat-Fielding

Alternatively, in the default data-taking mode of on-sky Cherenkov images, the flat-fielding approach is used. This exists as a software extension to the gain-matching to further unify the response across the camera. With an illumination of approximately 50 p.e. (as with the gain matching), the coefficients are extracted such that the charge measured in each pixel is the same (after accounting for the difference in illumination between pixels due to the beam profile and curved geometry of the focal plane). These coefficients differ in those obtained via the SPE method as they include the relative Photon Detection Efficiency (PDE) between pixels in the correction.

The argument between flat-fielding according to gain response (SPE fitting) or according to illumination response (method we are adopting) is a common one among IACTs, and is also a current topic among the different CTA telescopes. The reason we have chosen to adopt the latter is it reduces the pixel-to-pixel variations in their response to being illuminated, which is important for Cherenkov shower images. The measured charge in each pixel will not be exactly representative of the number of photoelectrons, but instead it will be representative of the number of photons. However, in order to keep the charge extracted in relatable units, a single nominal  $mV * ns * p.e.^{-1}$  conversion value will be applied to the entire camera.

find
references
where
HESS/MAGIC
differ
in their
approach

needs some demonstration of its impact, some plots for example, that continue on from the gain matching plots

#### 5.5 Other

In addition to the calibrations mentioned thus far, there are a few less important calibrations that could improve the performance further.

#### 5.5.1 Timing Corrections

Due to the routing of the electronics in the front-end, the electrical signal path is slightly different per channel, causing a small difference in apparent arrival of the pulse in the waveform. The relative arrival time per pixel can be seen in Figure .

Not only does this need to be taken into consideration when investigating the timing performance, it also can have a significant impact on the charge extraction, which typically relies on other pixels (neighbouring or entire camera, see Chapter 6) sharing an compatible pulse time. The effect of a 1 ns incorrectly extracted charge (when the peak finding is done using the waveforms from all pixels) can have the impact on the charge resolution shown in Figure \_\_\_\_\_

The first approach in correcting for this affect is to shift the charge extraction by the timing correction. However, current charge extraction methods do not operate camera image showing relative time

show impact of an incorrect time extraction on charge resolution maybe of just TM?

on time scales smaller than the waveform binning, therefore approaches on how to adapt those methods for corrections below that scale are being discussed.

#### 5.5.2 Temperature Corrections

Temperature is most likely the most prominent factor in changing the calibration values on short scales, and has been mentioned in almost every approach. Investigations into exactly how these parameters change with temperature are ongoing, but examples can be seen in:

Figure
Figure
TF Variation with temp
Figure
Gain variation with temp

In the future we intend to have a calibration pipeline that is independent of these temperature effects. For the photosensors this is very simple, as the voltage across them can be altered to account for the temperature changes. For the TARGET modules, this may require an additional lookup table, or an extra dimension to the existing tables.

#### 5.5.3 LED Flashers

Although not technically a part of the waveform processing chain, the LED flashers have an important role in the calibration pipeline, especially for the final operation of the CHEC cameras in CTA. Their purpose is to allow us to perform in situ calibration, by uniformly illuminating the camera via reflection in the secondary mirror. However to achieve this, we must characterize and calibrate the LEDs such that we accurately know the illumination they are providing.

include some results on the LED calibration, and also mention their temperature dependence

#### 5.6 Future

During the long development of CHEC, the calibration procedure has evolved a lot, and multiple iterations have occurred to either:

- accommodate the changes required in the upgrades of hardware (such as from TARGET (version 5) (TARGET 5) to TARGET C)
- simplify the calibration to save on resources
- or account for additional factors, thereby improving the calibration (such as the AC contribution to the Transfer Functions)

Therefore, while each iteration improves in one aspect, it may be at the expense of the others. As a result, the TARGET calibration procedure described in this chapter appears quite complicated compared to the approaches detailed in [3] and [2]. The primary next step in the calibration development for CHEC is therefore to review the procedure used, with the aim to produce an approach that is simpler, includes aspects such as temperature dependence, and meets the requirements and processing rates required by CTA.

### 6

#### Pipeline Reduction

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#### 

#### 6.2 Introduction

Following the low-level calibration detailed in 5, the waveforms should no longer require any further corrections unique to the electronics they were produced with. The waveforms from CHEC should now be in such a state that they can be processed in the same way as the waveforms from other cameras. This chapter describes the reduction performed on the waveforms in order to extract the Cherenkov shower information. With regards to the CTA data levels (Figure ), this concerns the steps from DL0 to DL2 .

figure with data levels in ch3

These reduction methods have been a primary component of IACT analysis since the beginning of the field, therefore much thought and development has previously been performed on these techniques. As CTA is a large consortium that essentially consists of the worldwide IACT community, the developers of the reduction approaches for previous IACTs have brought them forward to CTA. However, due to:

double

- (a) CTA is to consist of the most advanced IACTs to date, with higher shower imaging resolution and multiplicity than has previously been available
- (b) the capabilities of digital signal processing has significantly increased in the past decade

The opportunity for more advanced and more successful algorithms exist within CTA. Some effort has already been made in this direction, but it is an aspect that is expected to constantly evolve and improve during the lifetime of CTA. In this chapter I will attempt to provide a broad overview of the existing and in-development reduction techniques.

#### 6.3 Charge Extraction Methods

The most low-level reduction stage is the extraction of information from the calibrated waveforms provided by each camera individually. This procedure is very generic, allowing for the utilisation of common signal processing techniques that are not unique to Cherenkov shower analysis. The goal is to extract as much information from the pulse created by the Cherenkov shower light, while simultaneously limiting the amount of noise introduced from factors such as Night-Sky Background (NSB) . Two quantities are extracted in this stage: the signal charge in each pixel (the sums of which is a measure of the energy within the shower), and the signal arrival time per pixel.

talk about all the contributing factors (noise etc.) to waveforms in ch2

The total signal charge in a pixel, i.e. the total number of photo-electrons released from the Photomultiplier Tube (PMT)'s photocathode, is proportional to the total area below the pulse corresponding to the Cherenkov photons. If the waveforms were completely free of noise, and the readout window was large enough to capture the full Cherenkov signal, a simple integration of the entire readout would be a satisfactory approach for obtaining the signal charge. However, as we do not have the luxury of perfect waveforms, more complex methods are designed. Charge extraction algorithms typically consist of two aspects: how the signal pulse is found, and how the pulse is integrated.

#### 6.3.1 Peak Finding

Two factors must be considered when finding the signal pulse of a Cherenkov shower. Firstly, the majority of camera pixels will not contain any Cherenkov signal while still containing noise. Secondly, due to the nature of Cherenkov showers (Chapter ), those pixels with Cherenkov signal will have different arrival times due to the time evolution of the Cherenkov image . This time gradient across the image is especially apparent for bright showers at a large core distance from the telescope. The most successful peak finding technique is the one that best accounts for those two factors. Some simple techniques used to define a peak time from a waveform include:

reference where the time gradient of Cherenkov showers are described

figure of peak time?

- Local Peak Finding: Each waveform is treated independently from the other. The maximum point in the waveform is treated as the peak/arrival time. This approach is intrinsically biased to assume every waveform contains a signal; therefore, in the absence of a Cherenkov signal, the largest noise pulse will be extracted, resulting in a higher total charge than should be obtained.
- Global Peak Finding: The waveform from every pixel is combined into an average, from which the maximum point is treated as the peak time for every pixel. This technique is only useful if a large portion of the camera is simultaneously illuminated, such as by a laser in the case of lab commissioning and calibration runs.
- Neighbour Peak Finding: The waveforms from the neighbouring pixels are combined into an average, from which the maximum point is treated as the peak time for the pixel-of-interest. This technique is often preferred for Cherenkov images as it has a reduced charge bias (especially if the pixel-of-interest's waveform is not included in the average); pixels with Cherenkov signal typically have neighbours that also contain Cherenkov signal at a correlated time, while the neighbours of empty pixels only contain noise, and therefore a random peak time is extracted.
- Fixed Peak Value: Due to a reliable definition of the camera trigger and subsequent electronic chain, the position of the pulse in the waveform could consistently be known a-priori, allowing for a fixed peak time. However, this method requires a larger integration window size in order to capture the full pulse in the tail of the Cherenkov shower, which occur at a later time than the initial photons which trigger the camera, therefore resulting in a larger noise included in the signal. However, this technique usually contains the least bias, as no signal is assumed to exist.

A more complex peak finding technique is the *Gradient Peak Finding* approach. This approach was designed for the VERITAS telescope [4][1][5], but is applicable to any IACT telescope with the ability of a dynamically choosing an integration window. *Gradient Peak Finding* is a two-pass approach where the time-gradient of the Cherenkov signal across the camera's focal plane is obtained by first extracting the signal using one of the other methods, and then cleaning and parameterising the image using simple techniques described later in this chapter. This time-gradient can then be used to assume a peak time based on camera pixel position. This

method provides a more unbiased estimation of the peak time of the signal at the expense of simplicity.

verbose descrip-tion from [1]

These peak finding methods have been described in relation to the maximum of the signal pulse, however they may instead use other characteristic positions of the pulse, such as the half-maximum time on the rising edge, or the centre of gravity of the pulse. Additionally, more advanced peak finding techniques may up-sample (possibly by zero-padding in the frequency domain via a Fourier transform) or interpolate the signal to obtain a more precise peak time [1][5], or even apply low-pass filters in order to remove low frequency baseline noise. The peak finding should be done in conjunction with any timing corrections () that may be required.

reference timing calibration section

maybe derive gradient

here, and cross correlation

next, then each

subsection has the full de-

scription of at least one

complex algorithm

update

#### Integration 6.3.2

Once the peak time has been obtained, the simplest approach to extract the signal is to define an integration window centred about this time. The size of the window needs to be large enough to capture sufficient signal from the pulse, but small enough that not too much noise (NSB, dark counts, afterpulsing) is included within the window, thereby maximising the signal-to-noise. Additionally, the camera's pulse shape may not be symmetric, so a better signal-to-noise may be achieved by shifting the window a few samples with respect to the peak time. Typically, an integration window size on the order of  $\tilde{1}0$  ns is used, with a shift of  $\tilde{3}$  ns. .

values based on results figures demonstrating the different peak finding

Beyond the simple "boxcar" integrator method (where every sample integrated has a weight of 1), other more advanced strategies may define their own alternative approach to extract the charge. One example is the fitting of the signal pulse, wither with an analytical description of the expected pulse, or with a more unconstrained description such as a cubic spline. A second complex approach is the use of digital filters, which can be used in combination with knowledge of the pulse shape to robustly extract the signal even in the presence of high noise. Such a technique has been designed and adopted for Gamma-ray Cherenkov Telescope (GCT), referred to as the Cross-Correlation method. Due to its adoption and sophistication, it is described here in more detail.

Cross-correlation is a common signal processing technique used as a measure of the similarity between two signals as a function of the displacement in time applied to one of the signals. Given a function f(t) defined between  $0 \le t \le T$  and a second function q(t), the cross-correlation between the two functions  $(f \star q)$  is defined as [6]

$$f \star g = \overline{f}(-t) * g(t), \tag{6.3.2.1}$$

where \* indicates the convolution and  $\overline{f}(-t)$  is the complex conjugate of f(t). Since the convolution of these functions at a time displacement (also referred to as "lag")  $\tau$  is defined by

$$(f * g)(\tau) = \int_0^T f(t)g(\tau - t)dt$$
 (6.3.2.2)

#### 6.3.3 Adopted approaches

Some examples of approaches adopted by other telescopes are outlined below.

#### **MAGIC**

Members of the MAGIC telescope performed a study comparing the techniques proposed for their signal reconstruction. In [7] they compare four approaches: fixed-window, sliding-window with amplitude-weighted time, cubic spline fit with integral or amplitude extraction, and digital filter. It is concluded the digital filter, which relies on knowledge of the signal shape to minimise the noise contributions, provides a charge reconstruction with acceptable bias and minimal variance, while remaining stable in the occurrence of small variations in pulse shape and position.

#### VERITAS

Similar to the aforementioned study for the MAGIC telescope, a comparison of charge extraction approaches was performed for VERITAS [4][1][5]. Specifically, the extraction methods compared include a *simple-window* using a-priori knowledge of the Cherenkov pulse time in the trace, a *dynamic-window* which slides across the trace to find the Cherenkov pulse, a *trace-fit* evaluator with fits the trace with two exponential functions which respectively describe the rise and fall time of the pulse, a *matched-filter* which "uses a digital filter based on the assumed shape of the FADC pulse to integrate the charge" [5], and finally an implementation of the "Gradient Peak Finding" approach described earlier in the chapter . At first glance, some of these approaches bear resemblance to those used by MAGIC, however there are slight differences:

- in the VERITAS pulse fitting technique, an attempt to describe the pulse analytically was made whereas the MAGIC approach used a more loosely defined spline
- the filter used by VERITAS is a cross-correlation in Fourier space, whereas
  the filter used by MAGIC is generated using their knowledge of the noise
  auto-correlation matrix

should I move gradient peak finding to later, alongside the cross correlation method, as it has a nice analytical section from [1]

6. Pipeline Reduction

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Either as a result of these differences, or due to the difference in the instruments themselves, the *matched-filter* appears to result in a worse reconstruction than one would expect from the conclusion reached by MAGIC. One might justify that this degradation of signal extraction with the *matched-filter* for higher amplitudes is due to a change in pulse shape at higher amplitudes, thereby requiring a different "assumed FADC pulse shape", but it is not clear if that is what is occurring here. These studies conclude that the *matched-filter* "holds promise" for reconstructing low charges, whereas while the *trace-fit* performs extremely poor for the low charges (as expected), it performs the best for amplitudes > 4 photoelectrons [5].

**HESS** 

FlashCam

**ASTRI** 

#### 6.3.4 Performance Assessment

Deciding on which charge extraction method to use is not trivial - as shown in the above discussion, different cameras may perform better with different algorithms. This is anticipated in *ctapipe* (4), where different ChargeExtractors can easily be selected at runtime depending on the camera source.

- 6.4 Image Cleaning
- 6.4.1 Tailcut Cleaning
- 6.4.2 Wavelets
- 6.5 Shower Parameterisation
- 6.5.1 Hillas
- 6.5.2 Model and Model++
- 6.5.3 ImPACT
- 6.5.4 Neural Nets
- 6.6  $\gamma$ -Hadron Separation
- 6.7 Energy Reconstruction
- 6.8 Direction Reconstruction

advanced techniques that don't fit into these categories, machine learning, photon counting

# Camera Performance

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#### 7.1 Plan

#### **7.1.1** Topics

- Charge Resolution
- TF Investigations
- Different NSBMC Validation
- MC Performance

#### 7.1.2 Questions

- What other criteria?
  - Trigger performance even though I haven't contributed

# On-Sky Pipeline

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#### 8.1 Plan

#### **8.1.1** Topics

- Decided upon reduction methods
- Potentially different than for performance chapter
- CHEC-M campaign
- MC CHEC-S
- Future observations
- $\bullet \quad \text{Jupiter observations (Beyond cherenkov?)}$

#### 8.1.2 Questions

•

# Summary

#### Appendices



#### Transfer Function Investigations

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• AC vs	ge resolution of different approaches
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#### Charge Extractor Investigations

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#### B.1 Plan

#### B.1.1 Topics

- $\bullet$  RMS extracted charge with varying integration window size and shift with different NSBs and amplitudes (and combination of amplitudes)
- $\bullet \quad \text{Charge resolution of different methods with different NSB (including full integration method)}\\$
- in the absence of the need for peak finding (laser illumination), and when peak finding is important (Cherenkov) split into two, best integration technique (different NSBs, different integration window sizes), and best peak finding (different NSBs, need Cherenkov data)
- window size might actually change for Cherenkov got to capture entire signal, and signal might not be centred at "calculated peak time".

#### **B.1.2** Questions

•

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