→ Homework 3-P. Perceptron

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Do this homework on anaconda

Homework Purpose: Learn SGD and Perceptron

Perceptron model

image-3.png

▼ The net input of the perceptron including the bias

image-2.png

Remark:

$$\sum_{i=1}^{m} w_i x_i + b = b + w_1 x_1 + \dots + w_m x_m = (w_0, w_1, \dots, w_m) \cdot (1, x_1, \dots, x_m)$$

where $w_0 = b$

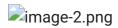
Vector form of the net input

image.png

▼ The perceptron fires if and only if the net input is non-negative

image.png

- A linear classifier uses lines to classify data points—any object on one side of the line is part of one class and any object on the other side is part of the other class.
- A successful linear classifier could use H_1 or H_2 to discriminate between the two classes, whereas H_3 would be a poor decision boundary.
- H_1 or H_2 are called a separating hyperplane



Geometric Interpretation of a separating hyperplane

```
image-3.png
```

- ▼ When a data is miclassified, we move w to a certain direction
 - · Which direction? How much should we move? Figure it out

```
image-2.png
```

Remark: gradient_descent.py, linear_algebra.py must be in the folder having this notebook file

```
# run this cell
from gradient_descent import *
from linear_algebra import *
```

- ▼ Problem 1 (30 pts)
 - We want to implement a simple neural network called Perceptron.
 - We will use minimize_stochastic to optimize the network

The code of SGD

```
def in_random_order(data):
    """generator that returns the elements of data in random order"""
    indexes = [i for i, _ in enumerate(data)] # create a list of indexes
    random.shuffle(indexes) # shuffle them
    for i in indexes: # return the data in that order
        yield data[i]
```

```
def minimize_stochastic(target_fn, gradient_fn, x, y, theta_0, alpha_0=0.01):
   data = list(zip(x, y))
   theta = theta 0
   data = list(zip(x, y))
   theta = theta 0
                                                # initial guess
   alpha = alpha_0
                                                # initial step size
   min theta, min value = None, float("inf") # the minimum so far
   iterations_with_no_improvement = 0
   # if we ever go 100 iterations with no improvement, stop
   while iterations_with_no_improvement < 100:</pre>
       count += 1
       value = sum( target_fn(x_i, y_i, theta) for x_i, y_i in data )
        if value < min value:
            # if we've found a new minimum, remember it
            # and go back to the original step size
            min_theta, min_value = theta, value
            iterations_with_no_improvement = 0
            alpha = alpha 0
       else:
            # otherwise we're not improving, so try shrinking the step size
            iterations_with_no_improvement += 1
            alpha *= 0.9
        # and take a gradient step for each of the data points
        for x_i, y_i in in_random_order(data):
            gradient_i = gradient_fn(x_i, y_i, theta)
            theta = vector_subtract(theta, scalar_multiply(alpha, gradient_i))
   min theta = theta
   return min theta
```

You should define an error function and a gradient function for perceptron: Remark: ONE or TWO lines for an error function and a gradient function are

enough. If the number of lines > 2, you get a penalty

▼ Define your error function here:

```
# YOUR CODE MUST BE HERE

def perceptron_error(x_i, y_i, w):
    return max(0, -y_i * dot(x_i, w))
```

▼ Define your gradient function here:

```
# YOUR CODE MUST BE HERE def perceptron_error_gradient(x_i, y_i, w): return [(-y_i * x) \text{ if perceptron_error}(x_i, y_i, w) \neq 0 \text{ else } 0 \text{ for } x \text{ in } x_i]
```

Double-click (or enter) to edit

Define a function to shade a decision boundary

- The region of $w_1 \cdot x_1 + w_2 \cdot x_2 + w_0 \ge 0$ are shaded as red; otherwise shaded as blue
- x_min, x_max, y_min, y_max defines a shading area
- The resulting shading and plotting must be very similar as shown in the given answer images

```
# YOUR CODE MUST BE HERE
import numpy as np
import matplotlib.pyplot as plt

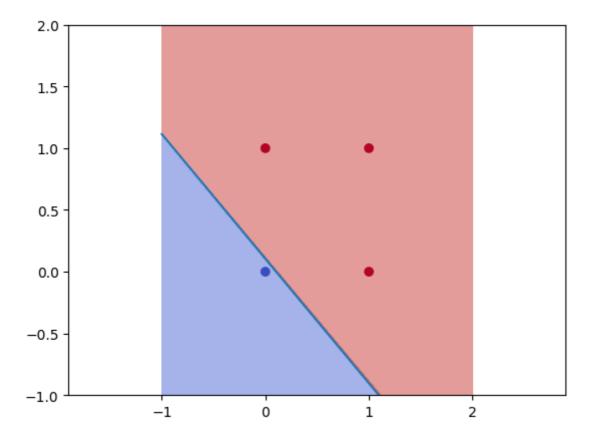
def shade_decision_region(X, y, w, x_min, x_max, y_min, y_max):
    if not isinstance(X, np.ndarray):
        X = np.array(X)

    xx, yy = np.meshgrid(np.linspace(x_min, x_max, 100), np.linspace(y_min, y_max,
    Z = np.sign(w[0] + w[1]*xx + w[2]*yy)  # Get predicted value for each point in

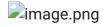
    plt.contourf(xx, yy, Z, cmap="coolwarm", alpha=0.5)
    plt.scatter(X[:, 1], X[:, 2], c=y, cmap="coolwarm")
    plt.plot([x_min, x_max], [(-w[0] - w[1] * x_min) / w[2], (-w[0] - w[1] * x_max)
    plt.xlim(x_min - 0.3*(x_max-x_min), x_max + 0.3*(x_max-x_min))
    plt.ylim(y_min, y_max)
    plt.show()
```

▼ Test Case 1: OR

```
# DO NOT EDIT THIS CELL
# RUN THIS CELL
```

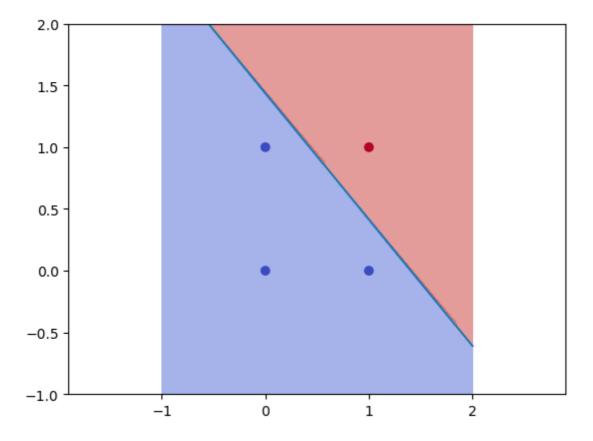


Your output must be similar to the following:



▼ Test Case 2: AND

```
# DO NOT EDIT THIS CELL
# RUN THIS CELL
import matplotlib.pyplot as plt
import numpy as np
```

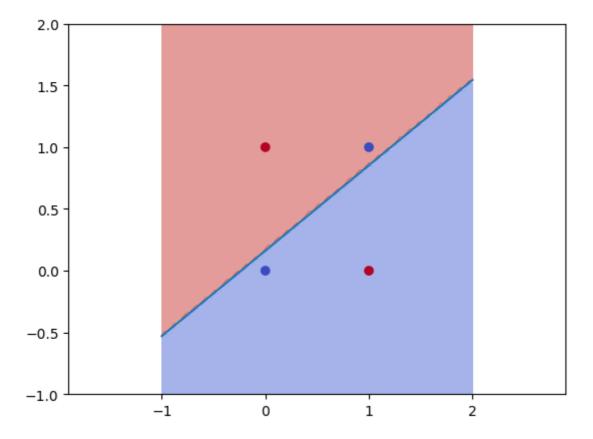


Your output must be similar to the following:



▼ Test Case 3: XOR

```
# DO NOT EDIT THIS CELL
# RUN THIS CELL
import matplotlib.pyplot as plt
import numpy as np
```



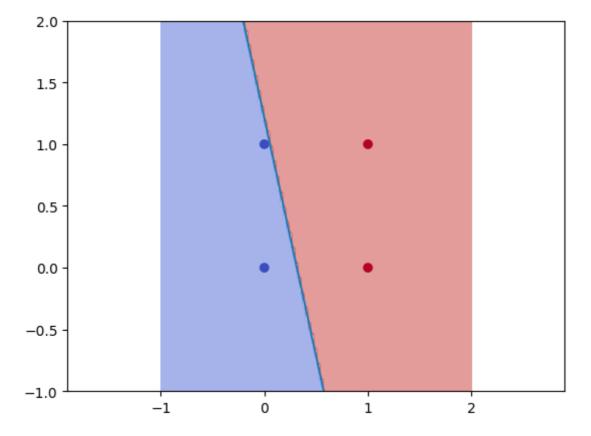
Your output must be similar to the following:



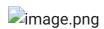
▼ Test Case 4: Right

```
# DO NOT EDIT THIS CELL
# RUN THIS CELL
import matplotlib.pyplot as plt
import numpy as np
X = [[1,0,0], [1,0,1], [1,1,0], [1,1,1]]
```

```
y = [-1, -1, 1, 1]
```



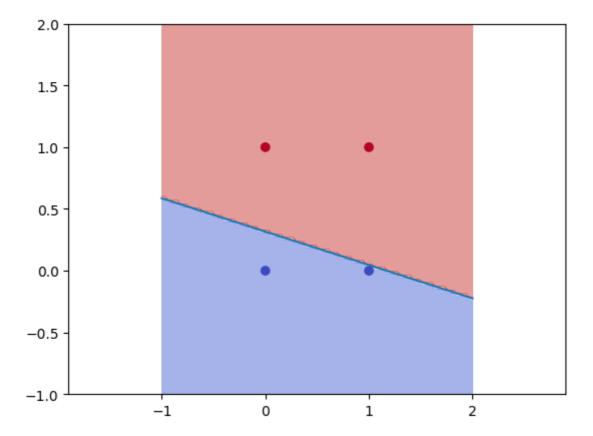
Your output must be similar to the following:



▼ Test Case 5: Upper

```
# DO NOT EDIT THIS CELL
# RUN THIS CELL
import matplotlib.pyplot as plt
import numpy as np

X = [[1,0,0], [1,0,1], [1,1,0], [1,1,1]]
y = [-1, 1, -1, 1]
```



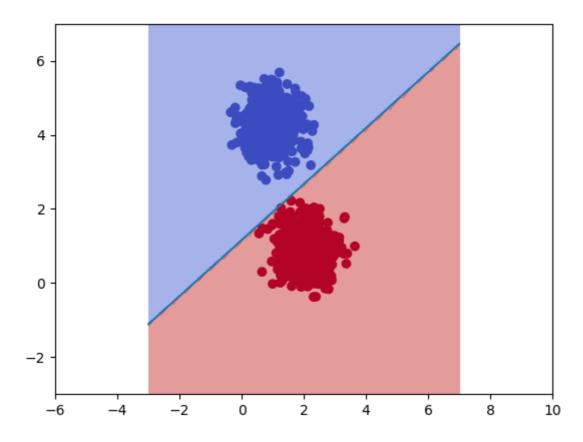
Your output must be similar to the following:



▼ Test Case 6: Two Clusters

```
# DO NOT EDIT THIS CELL
# RUN THIS CELL
import matplotlib.pyplot as plt
from sklearn.datasets import make_blobs
import random
```

Xs, ys = make_blobs(n_samples=1000, n_features=2, centers=2, cluster_std=0.5, rando
Xs1 = np.hstack((np.ones((Xs.shape[0],1)), Xs))



Your output must be similar to the following:

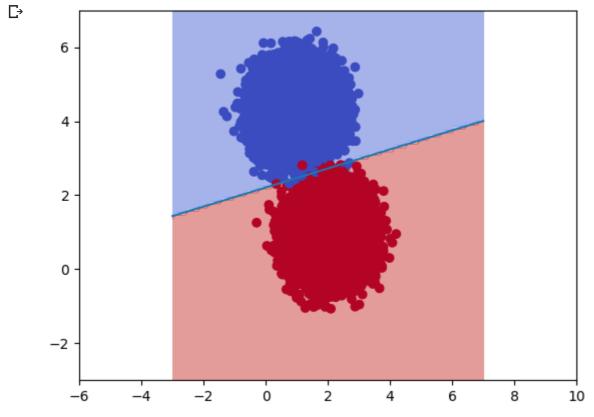


▼ Test Case 7: Two Big Clusters

```
# DO NOT EDIT THIS CELL
# RUN THIS CELL
import matplotlib.pyplot as plt
from sklearn.datasets import make_blobs
import random
```

```
import time
```

```
Xs, ys = make_blobs(n_samples=100000, n_features=2, centers=2, cluster_std=0.5, ran
Xs1 = np.hstack((np.ones((Xs.shape[0],1)), Xs))
# choose random value to start
random.seed(2)
theta = [1, random.random(), random.random()]
X = Xs1.tolist()
y = (np.where(ys = 1, 1, -1)).tolist()
start = time.time()
w = minimize_stochastic(perceptron_error,
                        perceptron_error_gradient,
                        Χ,
                        у,
                        theta,
                        0.1)
end = time.time()
shade_decision_region(X, y, w, x_min=-3, x_max=7, y_min=-3, y_max=7)
lapse = end - start
total = 10
weight = 1.5
grace = 100.0
my_point = int(total / (weight ** (lapse // grace)))
print(f'Total time taken : {lapse} seconds')
print(f'My point is {my_point}')
```



Total time taken : 120.93883180618286 seconds My point is 6

Your output must be similar to the following:



Ethics:

If you cheat, you will get negatgive of the total points. If the homework total is 22 and you cheat, you get -22.

What to submit

- · Run all cells after restarting the kernel
- Goto "File -> Print Preview"
- · Print the page as pdf
- Pdf file name must be in a form of: homework_3_홍길동_202200001.pdf
- · Submit the pdf file in google classroom
- · No late homeworks will be accepted
- Your homework will be graded on the basis of correctness, performance, and programming skills