

Solutions:**1.****(1) Pseudocode function:**

```

bool balancedBracketProblem(string a)
{
    //step1 : check every character in the string and solve the question by stack ADT
    for (each character ch in the string)
    {
        if (ch is a left bracket(e.g. "(", "[", "{"))
            aStack.push(char);
        else if (ch is a right bracket(e.g. ")", "]", "}"))
        {
            if (aStack.peek() == the same type of its left bracket(e.g. "(", "[", "{"))
                aStack.pop();
            else // the left bracket doesn't match the right bracket ==> invalid
            {
                cout << "The string is Invalid !!!";
                return false;
            }
        }
    }

    //step2 : check if there are any left brackets left in the stack
    if(aStack.isEmpty() == true)
    {
        cout << "The string is Valid !!!";
        return true;
    }
    else // still exists at least one left bracket in the stack ==> invalid
    {
        cout << "The string is Invalid !!!";
        return false;
    }
}

```

(2) Simulate:

***stack ADT will be implemented as: **Stack [a (bottom), b, c (top)**

(a)

start : **aStack [**

```

step1 : read in "[ " ==> aStack [ "[ "
step2 : read in "( " ==> aStack [ "[ ", "( "
step3 : read in " ) ", pop "( " out ==> aStack [ "[ "
step4 : read in "{ " ==> aStack [ "[ ", "{ "
step5 : read in " } ", pop "{ " out ==> aStack [ "[ "

```

step6 : read in “ (” ==> **aStack** [“ [” , “ (”
 step7 : read in “) ” , pop “ (” out ==> **aStack** [“ [”
 step8 : read in “] ” , pop “ [” ==> **aStack** [

end : **aStack** [

result : aStack is empty at the end so it is valid, **cout << "The string is Valid !!!"** and **return true**

(b)

start : **aStack** [

step1 : read in “ (” ==> **aStack** [“ (”
 step2 : read in “ (” ==> **aStack** [“ (” , “ (”
 step3 : read in “) ” , pop “ (” out ==> **aStack** [“ (”
 step4 : read in “ { ” ==> **aStack** [“ (” , “ { ”
 step5 : read in “ (” ==> **aStack** [“ (” , “ { ” , “ (”
 step6 : read in “ [” ==> **aStack** [“ (” , “ { ” , “ (” , “ [”
 step7 : read in “] ” , pop “ [” out ==> **aStack** [“ (” , “ { ” , “ (”
 step8 : read in “) ” , pop “ (” out ==> **aStack** [“ (” , “ { ”
 step9 : read in “ } ” , pop “ { ” out ==> **aStack** [“ (”
 step9 : read in “) ” , pop “ (” out ==> **aStack** [

end : **aStack** [

result : aStack is empty at the end so it is valid, **cout << "The string is Valid !!!"** and **return true**

2.

(a)

start : **aStack** [; postfixExp

step1 : read in “a”, append to postfixExp
 step2 : read in “+” ==> **aStack** [“+”
 step3 : read in “b”, append to postfixExp
 step4 : read in “-”, append “+” to postfixExp, pop “+” out ==> **aStack** [“-”
 step5 : read in “c”, append to postfixExp
 step6 : append “-” to postfixExp, pop “-” out ==> **aStack** [

end : **aStack** [

result : postfixExp = ab+c-

(b)

start : **aStack** [; postfixExp

step1 : read in “(” ==> **aStack** [“(”
 step2 : read in “a”, append to postfixExp
 step3 : read in “+” ==> **aStack** [“(” , “+”
 step4 : read in “b”, append to postfixExp
 step5 : read in “)”, append “+” to postfixExp, pop “+” and “(” out ==> **aStack** [“*”
 step6 : read in “*” ==> **aStack** [“*”
 step7 : read in “(” ==> **aStack** [“*” , “(”
 step8 : read in “c”, append to postfixExp
 step9 : read in “-” ==> **aStack** [“*” , “(” , “-”

step10 : read in "d", append to postfixExp
 step11 : read in ")", append "-" to postfixExp, pop "-" and "(" out ==> **aStack** ["*"]
 step12 : append "*" to postfixExp, pop "*" out ==> **aStack** []

end : **aStack** []
 result : postfixExp = ab+cd-*

(c)
 start : **aStack** []; postfixExp

step1 : read in "(" ==> **aStack** ["("]
 step2 : read in "a", append to postfixExp
 step3 : read in "*" ==> **aStack** ["(", "*"]
 step4 : read in "(" ==> **aStack** ["(", "*", "("]
 step5 : read in "b", append to postfixExp
 step6 : read in "*" ==> **aStack** ["(", "*", "(", "*"]
 step7 : read in "c", append to postfixExp
 step8 : read in ")", append "*" to postfixExp, pop "*" and "(" out ==> **aStack** ["(", "*"]
 step9 : read in ")", append "*" to postfixExp, pop "*" and "(" out ==> **aStack** []
 step10 : read in "-" ==> **aStack** ["-"]
 step11 : read in "d", append to postfixExp
 step12 : read in "+", append "-" to postfix, pop "-" out ==> **aStack** ["+"]
 step13 : read in "e", append to postfixExp
 step14 : read in "/" ==> **aStack** ["+", "/"]
 step15 : read in "f", append to postfixExp
 step16 : append "/" to postfixExp, pop "/" out ==> **aStack** ["+"]
 step17 : append "+" to postfixExp, pop "+" out ==> **aStack** []

end : **aStack** []
 result : postfixExp = abc**d-ef/+

(d)
 start : **aStack** []; postfixExp

step1 : read in "a", append to postfixExp
 step2 : read in "/" ==> **aStack** ["/"]
 step3 : read in "(" ==> **aStack** ["/", "("]
 step5 : read in "b", append to postfixExp
 step6 : read in "-" ==> **aStack** ["/", "(", "-"]
 step7 : read in "c", append to postfixExp
 step8 : read in ")", append "-" to postfixExp, pop "-" and "(" out ==> **aStack** ["/"]
 step9 : read in "+", append "/" to postfixExp, pop "/" out ==> **aStack** ["+"]
 step10 : read in "(" ==> **aStack** ["+", "("]
 step11 : read in "d", append to postfixExp
 step12 : read in "+" ==> **aStack** ["+", "(", "+"]
 step13 : read in "e", append to postfixExp
 step14 : read in ")", append "+" to postfixExp, pop "+" and "(" out ==> **aStack** ["+"]
 step15 : read in "*" ==> **aStack** ["+", "*"]
 step16 : read in "f", append to postfixExp
 step17 : append "*" to postfixExp, pop "*" out ==> **aStack** ["+"]
 step18 : append "+" to postfixExp, pop "+" out ==> **aStack** []

end : **aStack** [
result : postfixExp = abc-/de+f*+

(e)

start : **aStack** []; postfixExp

step1 : read in "(" ==> **aStack** ["("
step2 : read in "(" ==> **aStack** ["(", "("
step3 : read in "a", append to postfixExp
step4 : read in "+" ==> **aStack** ["(", "(", "+"
step5 : read in "b", append to postfixExp
step6 : read in ")", append "+" to postfixExp, pop "+" and "(" out ==> **aStack** ["("
step7 : read in "*" ==> **aStack** ["(", "*"]
step8 : read in "c", append to postfixExp
step9 : read in "-", append "*" to postfixExp, pop "*" out ==> **aStack** ["(", "-"
step10 : read in "(" ==> **aStack** ["(", "- ", "("
step11 : read in "d", append to postfixExp
step12 : read in "-" ==> **aStack** ["(", "- ", "(", "-"
step13 : read in "e", append to postfixExp
step14 : read in ")", append "-" to postfixExp, pop "-" and "(" out ==> **aStack** ["(", "-"
step15 : read in ")", append "-" to postfixExp, pop "-" and "(" out ==> **aStack** ["
step16 : read in "*" ==> **aStack** ["*"]
step17 : read in "(" ==> **aStack** ["*", "("
step18 : read in "f", append to postfixExp
step19 : read in "+" ==> **aStack** ["*", "(", "+"
step20 : read in "g", append to postfixExp
step21 : read in ")", append "+" to postfixExp, pop "+" and "(" out ==> **aStack** ["*"]
step22 : append "*" to postfixExp, pop "*" out ==> **aStack** [

end : **aStack** [
result : postfixExp = ab+c*de- fg+*

(f)

start : **aStack** []; postfixExp

step1 : read in "a", append to postfixExp
step2 : read in "+" ==> **aStack** ["+"]
step3 : read in "(" ==> **aStack** ["+", "("
step4 : read in "b", append to postfixExp
step5 : read in "*" ==> **aStack** ["+", "(", "*"]
step6 : read in "c", append to postfixExp
step7 : read in "/", append "*" to postfixExp, pop "*" out ==> **aStack** ["+", "(", "/"]
step8 : read in "d", append to postfixExp
step9 : read in ")", append "/" to postfixExp, pop "/" and "(" out ==> **aStack** ["+"]
step10 : read in "-", append "+" to postfixExp, pop "+" out ==> **aStack** ["-"
step11 : read in "e", append to postfixExp
step12 : append "-" to postfixExp, pop "-" out ==> **aStack** [

end : **aStack** [
result : postfixExp = abc*d/+e-