# 1 Functionalities of the Project

This project is the essential part of a navigation system. It reads in either a directed graph or an undirected graph G with n vertices and m edges from a file specified by the command-line (with proper arguments). It then takes corresponding actions for given instructions from stdin. Besides the Stop instruction, valid instructions include

- (i) graph printing instruction (PrintADJ)
- (ii) path computation instructions (SinglePair and SingleSource)
- (iii) length/path printing instructions (PrintLength and PrintPath)

Both SinglePair and SingleSource path computations should have worst-case time complexity  $O((m+n)\log n)$ . Path printing should have worst-case time complexity O(n). Length printing should have worst-case time complexity O(1). Memory should be allocated when needed, and released when it is no longer needed. Memory leaks should be avoided.

# 2 Modular Design

For modular design, you need to write the following modules:

- a module for various data structures, with header file named data\_structures.h
- a module for **min-heap**, with header file named **heap.h** and implementation file named **heap.cpp**
- a module for stack, with header file named stack.h and implementation file named stack.cpp
- a module for **graph algorithms**, with header file named **graph.h** and implementation file named **graph.cpp**
- a module for utilities, with header file named util.h and implementation file named util.cpp
- and the **main program**, with header file named **main.h** and implementation file named **main.cpp**

Your project should only use basic C++ libraries to compile your implementation to produce the executable PJ3. To ensure that, the following standard Makefile will be used to grade your project.

```
EXEC = PJ3
CC = g++
CFLAGS = -c - Wall
$(EXEC) :main.o util.o stack.o heap.o graph.o
        $(CC) -o $(EXEC) main.o util.o heap.o graph.o stack.o
       :main.cpp main.h data_structures.h util.h stack.h heap.h graph.h
main.o
        $(CC) $(CFLAGS) main.cpp
       :util.cpp util.h data_structures.h
util.o
        $(CC) $(CFLAGS) util.cpp
stack.o :stack.cpp stack.h data_structures.h
        $(CC) $(CFLAGS) stack.cpp
       :heap.cpp heap.h data_structures.h
heap.o
        $(CC) $(CFLAGS) heap.cpp
graph.o :graph.cpp graph.h data_structures.h stack.h heap.h
        $(CC) $(CFLAGS) graph.cpp
clean
        rm *.o $(EXEC)
```

Given that your project will be compile using the above Makefile, you have to name the files exactly as specified.

## 3 Data Structures

For this project, you need to implement graph representation using adjacency lists, a priority queue (min-heap), a stack, and the graph algorithms related to Dijkstra's shortest path algorithm. This section provides some data structures that may give you a head start with the project. You should not copy and paste these data structures. However, you can write similar ones after studying them. It should be your own work.

### 3.1 VERTEX

You need to have a data structure for vertices in the graph. Our algorithms also use a color system on vertices. The following is a part of the codes that I wrote. Note that the definition of COLOR in the following is NOT provided.

```
typedef struct TAG_VERTEX{
   int       index;
   COLOR    color;
   double       key;
   int       pi;
   int       position;
}VERTEX;
typedef VERTEX *pVERTEX;
```

Here the field index is the index of the corresponding vertex. It does not change. The fields key is the length of the *current best path from the source* computed. The field position is used to record the **position of the vertex in the min-heap array**. You will find this very handy when DecreaseKey operations are needed. I use the key field (rather than the d field) to reuse my codes for the min-heap.

Here is a sample usage of the data type VERTEX.

```
pVERTEX *V;
// V is a pointer to pointer to VERTEX

V = (pVERTEX *) calloc(n+1, sizeof(pVERTEX));
// Now you can make reference to V[1], but not to V[1]->index

for (int i=1; i<=n; i++){
    V[i] = (VERTEX *) calloc(1, sizeof(VERTEX));
    // Now you can make reference to V[1]->index
}
```

Please note that illegal memory access is the main cause of segmentation fault.

### 3.2 EDGE

You need to have a data structure for nodes on the adjacency lists of the graph. I wrote the following in my implementation.

```
typedef struct TAG_NODE{
   int index;
   int u;
   int v;
   double w;
   TAG_NODE *next;
}NODE;
typedef NODE *pNODE;
```

Here the field index is the index of the edge. The field w is the weight of the corresponding edge. The fields u and v correspond to the two end vertices of this edge.

The usage of the NODE data type is similar to that of VERTEX.

### 3.3 MIN-HEAP

In Project 2, you have implemented the min-heap data structure, where the HEAP data structure contains the fields capacity (of type int), size (of type int), and H (of type int \*). In this project, you need to modify it so that H is of type ELEMENT \*\*. The data structure ELEMENT contains only one required field: key (of type double).

To partially re-use your implementation of Project 2, you can use the following:

Because VERTEX has a field named key (of type double), your earlier implementations of min-heap should work as usual. Note that you can make reference to the four other fields defined in VERTEX, and in ELEMENT.

In this project, the elements of the heap array should be pointers to objects of type VERTEX. To reuse codes with minimal modification, I used the following in my implementation.

### 3.4 STACK

In order to print out the computed path from a source node s to a destination node t, we start from the destination node to trace out the path using the predecessor field. This will trace out the path in reverse order. In order to print the path in correct order, we need to use a stack. The elements of the stack should contain information (or pointers to information) about the corresponding vertices on the path.

# 4 Shortest Path Algorithm

For improved efficiency, you should implement the following version of Dijkstra's shortest s-t path algorithm.

```
Dijkstra-ST(G, w, s, t)
01: FOR v=1 TO n {
02:
         V[v]->index
                          = v;
         V[v] \rightarrow key
03:
                          = infinity;
         iq<-[v]V
                          = NULL;
04:
05:
         V[v]->color
                          = WHITE;
         V[v]->position = 0;
06:
```

```
07: }
08: Create empty min-heap pHeap;
09: Set the key of s to 0, and the color of s to GRAY;
10: Insert s into pHeap;
11: WHILE pHeap->size > 0 {
12:
        u = ExtractMin(pHeap);
        IF (u == t) THEN STOP;
13:
        FOR each v on ADJ[u] {
14:
            IF v is WHITE {
15:
                Set the color of v to GRAY;
16:
                Update v's key, pi; // Relax(u, v, w);
16:
                Insert v into pHeap;
17:
            }ELSE IF v is GRAY {
18:
19:
                Relax(u, v, w);
                Call DecreaseKey if nexessary; // Using the position field of v
20:
            }
21:
22:
        }
23:
        Color u BLACK;
24: }
```

For single-pair shortest path, both **s** and **t** are in  $\{1, 2, ..., n\}$ . For single-source shortest paths, **s** is in  $\{1, 2, ..., n\}$ , **t** is set to -1.

## 5 Valid Executions

A valid execution of your project has the following form:

```
./PJ3 <InputFile> <GraphType> <Flag>
where
```

- PJ3 is the executable file of your project,
- <InputFile> should be the exact name of the input file,
- <GraphType> should be substituted by either DirectedGraph or UndirectedGraph,
- <Flag> is either 1 or 0.

Your program should check whether the execution is valid. If the execution is not valid, your program should print out the following message to stderr and stop.

```
Usage: ./PJ3 <InputFile> <GraphType> <Flag>
```

Note that your program should not crash when the execution is not valid.

# 6 Flow of the Project

# 6.1 Read in the Graph and Build the Adjacency Lists

Upon a valid execution, your program should open the input file (specified by argv[1]) and read in the graph. The format of the input file is the following. The first line contains two positive integers, representing the number of vertices n and number of edges m, respectively. Each of the next m lines has the following format:

## edgeIndex u v w(u, v)

where u is the start vertex of edge (u, v), v is the end vertex of edge (u, v), w(u, v) is the weight of edge (u, v), and edgeIndex is the index of edge (u, v). Your program should read in edgeIndex, u, and v as int, and read in w(u, v) as double. For undirected graphs, each edge still has two vertices but the order is not important.

After knowing the values of n and m, your program should dynamically allocate memory for an array of n pointers to objects of type VERTEX. Let us call this array V. Then for each i = 1, 2, ..., n, V[i] is a pointer to an object for vertex i. Your program should dynamically allocate memory for an array of n adjacency lists. Let us call this array ADJ. Then for each i = 1, 2, ..., n, ADJ[i] is a pointer to NODE. Note that NODE has a field next. Therefore ADJ[i] is a pointer to the adjacency list of vertex i.

While reading the graph from argv[1] edge by edge, the adjacency lists are populated accordingly. Note that dynamic memory allocation is needed for each node (corresponding to an edge) on the adjacency lists.

Let (u, v) be the edge newly read in from the file argv[1]. If the graph is directed and flag is 1, insert the corresponding node for edge (u, v) at the rear of ADJ[u]. If the graph is directed and flag is 0, insert the corresponding node for edge (u, v) at the front of ADJ[u]. If the graph is undirected and flag is 1, insert a corresponding node for edge (u, v) at the rear of ADJ[u], and insert a corresponding node for edge (v, u) at the rear of ADJ[v]. If the graph is undirected and flag is 0, insert a corresponding node for edge (u, v) at the front of ADJ[u], and insert a corresponding node for edge (v, u) at the front of ADJ[u], and insert a corresponding node for edge (v, u) at the front of ADJ[v]. After all m edges are read in, your program should close the file argv[1].

# 6.2 Initialize the Priority Queue (min-heap) and the Stack

Your program should initialize a min-heap of capacity n and a stack of capacity n. Dynamic memory allocations are required for the min-heap and the stack. The heap will be used in the execution of Dijkstra's path finding algorithm. The stack will be used to output a path from a given source vertex to a given destination vertex.

# 6.3 Loop over the Instructions

Your program should expect the following instructions from stdin and act accordingly:

## (a) Stop

On reading Stop, the program stops.

### (b) PrintADJ

On reading the PrintADJ instruction, your program should do the following:

- (b-i) Print the adjacency lists of the input graph to stdout. Refer to posted test cases for output format.
- (b-ii) Wait for the next instruction from stdin.

## (c) SinglePair <source> <destination>

where  $\langle \text{source} \rangle$  and  $\langle \text{destination} \rangle$  are two integers in the set  $\{1, 2, ..., n\}$ . This is one of the two *path computation* instructions. On reading the SinglePair instruction, your program should do the following:

- (c-i) Apply the variant of Dijkstra's algorithm (as taught in class and stated in the lecture slides) to compute a shortest path from <source> to <destination>. In particular, for each  $i \in \{1, 2, ..., n\}$ , the algorithm should compute the final values of  $V[i] \rightarrow key$  and  $V[i] \rightarrow \pi$ . If <destination> is reachable from <source>,  $V[destination] \rightarrow key$  is the weight of a shortest path from <source> to <destination>, and  $V[destination] \rightarrow \pi$  is the predecessor of <destination> on the computed shortest path from <source> to <destination>. If <destination> is not reachable from <source>,  $V[i] \rightarrow \pi$  is nil, and  $V[i] \rightarrow key$  is DBL\_MAX (defined in the header file <cfloat>).
- (c-ii) Wait for the next instruction from stdin.

## (d) SingleSource <source>

where  $\langle \text{source} \rangle$  is an integer in the set  $\{1, 2, ..., n\}$ . This is the other path computation instruction. On reading the SingleSource instruction, your program should do the following:

- (d-i) Apply Dijkstra's algorithm to compute shortest paths from  $\langle source \rangle$  to all vertices that are reachable from  $\langle source \rangle$ . In particular, for each  $i \in \{1, 2, ..., n\}$ , the algorithm should compute the final values of  $V[i] \langle key \rangle$  and  $V[i] \langle \pi \rangle$ . If vertex i is reachable from  $\langle source \rangle$ ,  $V[i] \langle key \rangle$  is the length of a shortest path from  $\langle source \rangle$  to i, and  $V[i] \langle \pi \rangle$  is the predecessor of i on the computed shortest path from  $\langle source \rangle$  to i. If vertex i is not reachable from  $\langle source \rangle$ ,  $V[i] \langle \pi \rangle$  is nil, and  $V[i] \langle key \rangle$  is DBL\_MAX.
- (d-ii) Wait for the next instruction from stdin.

### (e) PrintLength <s> <t>

where  $\langle s \rangle$  and  $\langle t \rangle$  are two integers in the set  $\{1, 2, ..., n\}$ . This is the only *length printing* instruction. This instruction is valid if and only if  $\langle s \rangle$  is the same as  $\langle source \rangle$  in the most recent path computation instruction, and  $\langle t \rangle$  is the same as  $\langle destination \rangle$  in case the most recent path computation instruction is a SinglePair instruction.

On reading a valid PrintLength instruction, your program should do the following:

(e-i) If your program has computed a shortest <s> to <t> path in the most recent path computation, print the length of the computed path to stdout. Refer to posted test cases for output format.

If your program has not computed a shortest <s> to <t> path in the most recent path computation, print the following to stdout:

There is no path from <s> to <t>.

In the above, <s> and <t> should be replaced by their given values. Refer to posted test cases for output format.

(e-ii) Wait for the next instruction from stdin.

### (f) PrintPath <s> <t>

where  $\langle s \rangle$  and  $\langle t \rangle$  are two integers in the set  $\{1, 2, ..., n\}$ . This is the only path printing instruction. This instruction is valid if and only if  $\langle s \rangle$  is the same as  $\langle source \rangle$  in the most recent path computation instruction, and  $\langle t \rangle$  is the same as  $\langle destination \rangle$  in case the most recent path computation instruction is a SinglePair instruction.

On reading a valid PrintPath instruction, your program should do the following:

(f-i) If your program has computed a shortest <s> to <t> path in the most recent path computation, print the computed path to stdout. Refer to posted test cases for output format.

If your program has not computed a shortest <s> to <t> path in the most recent path computation, print the following to stdout:

There is no path from <s> to <t>.

In the above, <s> and <t> should be replaced by their given values. Refer to posted test cases for output format.

(f-ii) Wait for the next instruction from stdin.

#### (g) Invalid instruction

On reading an invalid instruction, your program should do the following:

(g-i) Write the following to stderr:

Invalid instruction.

(g-ii) Wait for the next instruction from stdin.

# 7 Format of the Input File

Refer to Section 6.1 and the posted test cases for the format of the input file. While w(u, v) may look like an int in the input file, it should be read in as double.

# 8 Format of the Output

Since the autograder on Gradescope uses the Linux diff function to compare your output with the expected output, your output has to match the expected output exactly. It is your responsibility to make sure that your output matches the expected output, with the aid of the posted test cases. The following are some general guidelines to help you.

## 8.1 Output Integers to stdout

All integers (to stdout) should be printed using the %d format. Refer to the posted test cases.

## 8.2 Output Floating Point Numbers to stdout

Edge weights (to stdout) should be printed using the %4.21f format when printing the adjacency lists (for easy debugging). In all other places, doubles (to stdout) should be printed using the %8.21f format. Refer to the posted test cases.

# 8.3 Output Strings (possibly with numerical values) to stdout

Refer to the posted test cases for strings printed to stdout. Keep in mind the rules in Section 8.1 (for int) and Section 8.2 (for double).

## 8.4 Output to stderr

While the autograder does not test the messages written to stderr, your program should output meaningful messages with sufficient information when a warning or error message should be written to stderr.

# 9 Submission

You should submit your project to Gradescope via the link on Canvas. Submit all header files and implementation files. You should put your name and ASU ID at the top of each of the header files and the implementation files, as a comment.

The instructor and the TAs will offer more help to this project early on, and will not answer emails/questions near the project due date that are clearly in the very early stage of the project. So, please manage your time, and start working on this project today.

You should not use Gradescope and the autograder on Gradescope as a debugger. The main purpose of the test cases are for you to get familiar with the output format. It is suggested to use a similar shell script to test your program on <code>general.asu.edu</code>. You also need to submit to Gradescope early enough to avoid last-minute surprises.

# 11 Examples and Test Cases

Test cases will be posted on Canvas shortly. The following is the content of the input file network01.txt, which is a directed graph with n = 8 and m = 14.

14 8 6 1

This graph is illustrated in Figure 1. You are highly encouraged to debug your program using this directed graph.

The following is the content of the input file network02.txt, which is an undirected graph with n = 8 and m = 11.

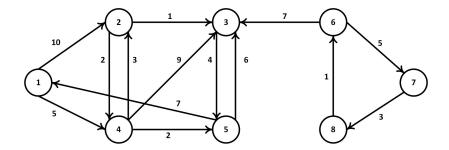


Figure 1: Directed graph  $G_1$  contained in the file network01.txt

This graph is illustrated in Figure 2. You are highly encouraged to debug your program using this undirected graph.

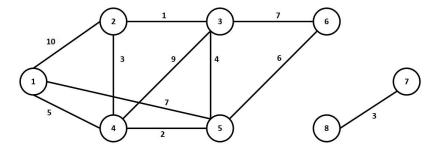


Figure 2: Undirected graph  $G_2$  contained in the file network02.txt

Some examples are presented in the following subsections. I used the shell script run with the following content

#### #!/bin/bash

./Execution < Instructions > Output.txt

as sample executions for given files Execution and Instructions to generate these examples.

# 11.1 Example 1

The content of Execution is

# #!/bin/bash

./PJ3 network01.txt DirectedGraph 1

The content of Instructions is

### PrintADJ

Stop

The content of the produced Output.txt is

```
ADJ[1]:-->[1 2: 10.00]-->[1 4: 5.00]

ADJ[2]:-->[2 3: 1.00]-->[2 4: 2.00]

ADJ[3]:-->[3 5: 4.00]

ADJ[4]:-->[4 2: 3.00]-->[4 3: 9.00]-->[4 5: 2.00]

ADJ[5]:-->[5 1: 7.00]-->[5 3: 6.00]

ADJ[6]:-->[6 3: 7.00]-->[6 7: 5.00]

ADJ[7]:-->[7 8: 3.00]

ADJ[8]:-->[8 6: 1.00]
```

Please note that the nodes are inserted at the rear of the adjacency list.

# 11.2 Example 2

The content of Execution is

## #!/bin/bash

./PJ3 network01.txt DirectedGraph 0

The content of Instructions is

### PrintADJ

Stop

The content of the produced Output.txt is

```
ADJ[1]:-->[1 4: 5.00]-->[1 2: 10.00]

ADJ[2]:-->[2 4: 2.00]-->[2 3: 1.00]

ADJ[3]:-->[3 5: 4.00]

ADJ[4]:-->[4 5: 2.00]-->[4 3: 9.00]-->[4 2: 3.00]

ADJ[5]:-->[5 3: 6.00]-->[5 1: 7.00]

ADJ[6]:-->[6 7: 5.00]-->[6 3: 7.00]

ADJ[7]:-->[7 8: 3.00]

ADJ[8]:-->[8 6: 1.00]
```

Please note that the nodes are inserted at the front of the adjacency list.

## 11.3 Example 3

```
The content of Execution is
```

### #!/bin/bash

./PJ3 network02.txt UndirectedGraph 1

The content of Instructions is

### PrintADJ

Stop

The content of produced Output.txt is

```
ADJ[1]:-->[1 2: 10.00]-->[1 4: 5.00]-->[1 5: 7.00]

ADJ[2]:-->[2 1: 10.00]-->[2 3: 1.00]-->[2 4: 3.00]

ADJ[3]:-->[3 2: 1.00]-->[3 4: 9.00]-->[3 5: 4.00]-->[3 6: 7.00]

ADJ[4]:-->[4 1: 5.00]-->[4 2: 3.00]-->[4 3: 9.00]-->[4 5: 2.00]

ADJ[5]:-->[5 1: 7.00]-->[5 3: 4.00]-->[5 4: 2.00]-->[5 6: 6.00]

ADJ[6]:-->[6 3: 7.00]-->[6 5: 6.00]

ADJ[7]:-->[7 8: 3.00]
```

## 11.4 Example 4

The content of Execution is

#### #!/bin/bash

./PJ3 network02.txt UndirectedGraph 0

The content of Instructions is

### PrintADJ

Stop

The content of produced Output.txt is

```
ADJ[1]:-->[1 5: 7.00]-->[1 4: 5.00]-->[1 2: 10.00]

ADJ[2]:-->[2 4: 3.00]-->[2 3: 1.00]-->[2 1: 10.00]

ADJ[3]:-->[3 6: 7.00]-->[3 5: 4.00]-->[3 4: 9.00]-->[3 2: 1.00]

ADJ[4]:-->[4 5: 2.00]-->[4 3: 9.00]-->[4 2: 3.00]-->[4 1: 5.00]

ADJ[5]:-->[5 6: 6.00]-->[5 4: 2.00]-->[5 3: 4.00]-->[5 1: 7.00]

ADJ[6]:-->[6 5: 6.00]-->[6 3: 7.00]

ADJ[7]:-->[7 8: 3.00]

ADJ[8]:-->[8 7: 3.00]
```

## 11.5 Example 5

The content of Execution is

#!/bin/bash

./PJ3 network01.txt DirectedGraph 1

The content of Instructions is

SinglePair 1 3

PrintPath 1 3

Stop

The content of the produced Output.txt is

The shortest path from 1 to 3 is:

 $[1: 0.00] \longrightarrow [4: 5.00] \longrightarrow [2: 8.00] \longrightarrow [3: 9.00].$ 

## 11.6 Example 6

The content of Execution is

#!/bin/bash

./PJ3 network01.txt DirectedGraph 0

The content of Instructions is

SinglePair 1 3

PrintPath 1 3

Stop

The content of the produced Output.txt is

The shortest path from 1 to 3 is:

 $[1: 0.00] \longrightarrow [4: 5.00] \longrightarrow [2: 8.00] \longrightarrow [3: 9.00].$ 

# 11.7 Example 7

The content of Execution is

#!/bin/bash

./PJ3 network01.txt DirectedGraph 0

The content of Instructions is

SinglePair 1 6

PrintPath 1 6

Stop

The content of the produced Output.txt is

There is no path from 1 to 6.

## 11.8 Example 8

```
The content of Execution is
#!/bin/bash
./PJ3 network02.txt UndirectedGraph 0
The content of Instructions is
SinglePair 1 3
PrintPath 1 3
Stop
SingleSource 1
SinglePair 1 3
The content of the produced Output.txt is
The shortest path from 1 to 3 is:
       0.00]-->[4:
                       5.00]-->[2:
                                       8.00]-->[3:
Γ1:
                                                       9.00].
```

## 11.9 Example 9

The content of Execution is

```
#!/bin/bash
./PJ3 network02.txt UndirectedGraph 0
```

The content of Instructions is

```
SinglePair 1 8
PrintPath 1 8
Stop
SingleSource 1
SinglePair 1 3
```

The content of the produced Output.txt is

There is no path from 1 to 8.

# 11.10 Example 10

The content of Execution is

```
#!/bin/bash
./PJ3 network01.txt DirectedGraph 0
```

The content of Instructions is

```
SingleSource 1
PrintPath 1 5
PrintPath 1 8
Stop
SingleSource 1
SinglePair 1 3
The content of the produced Output.txt is
The shortest path from 1 to 5 is:
[1:
       0.00] --> [4:
                      5.00]-->[5:
                                      7.00].
There is no path from 1 to 8.
        Example 11
11.11
The content of Execution is
#!/bin/bash
./PJ3 network01.txt DirectedGraph 0
The content of Instructions is
SingleSource 1
PrintLength 1 5
PrintLength 1 8
Stop
SingleSource 1
SinglePair 1 3
The content of the produced Output.txt is
The length of the shortest path from 1 to 5 is:
                                                      7.00
There is no path from 1 to 8.
11.12
         Example 12
The content of Execution is
#!/bin/bash
./PJ3 network02.txt UndirectedGraph 0
The content of Instructions is
SingleSource 1
```

PrintPath 1 5 PrintPath 1 8

SingleSource 1 SinglePair 1 3

Stop

```
The content of the produced Output.txt is
```

```
The shortest path from 1 to 5 is: [1: 0.00] --> [5: 7.00]. There is no path from 1 to 8.
```

## 11.13 Example 13

The content of Execution is

```
#!/bin/bash
./PJ3 network02.txt UndirectedGraph 0
```

The content of Instructions is

```
SingleSource 1
PrintLength 1 5
PrintLength 1 8
Stop
SingleSource 1
SinglePair 1 3
```

The content of the produced Output.txt is

The length of the shortest path from 1 to 5 is: 7.00 There is no path from 1 to 8.

# 11.14 Example 14

The content of Execution is

```
#!/bin/bash
./PJ3 network03.txt DirectedGraph 0
```

The content of Instructions is

```
SingleSource 1
PrintPath 1 2
PrintPath 1 3
PrintPath 1 4
PrintPath 1 5
PrintPath 1 6
PrintPath 1 7
PrintPath 1 8
PrintPath 1 9
Stop
```

The content of the produced Output.txt is

```
The shortest path from 1 to 2 is:
Γ1:
       0.00] --> [2:
                       9.931.
The shortest path from 1 to 3 is:
Γ1:
       0.00]-->[3:
                       1.36].
The shortest path from 1 to 4 is:
Γ1:
       0.00]-->[3:
                       1.36]-->[4:
                                        1.76].
The shortest path from 1 to 5 is:
       0.00] \longrightarrow [3:
                       1.36] --> [4:
                                        1.76] --> [5:
                                                       4.18].
The shortest path from 1 to 6 is:
                                                       4.18]-->[6:
Γ1:
       0.00]-->[3:
                       1.36] --> [4:
                                        1.76]-->[5:
                                                                        9.10].
The shortest path from 1 to 7 is:
                       1.36]-->[4:
                                       1.76]-->[5: 4.18]-->[6:
       0.00]-->[3:
                                                                        9.10]-->[7:
                                                                                       23.51].
The shortest path from 1 to 8 is:
[1:
       0.00] -->[2:
                       9.93]-->[8:
                                      12.69].
The shortest path from 1 to 9 is:
Γ1:
       0.00] -->[2:
                       9.93]-->[8:
                                      12.69]-->[9:
                                                      19.88].
```

## 11.15 Example 15

The content of Execution is

#!/bin/bash

./PJ3 network03.txt DirectedGraph 0

The content of Instructions is

SingleSource 1000 PrintPath 1000 1010 Stop

The content of produced Output.txt is

The shortest path from 1000 to 1010 is:

[1000: 0.00] --> [1004: 1.24] --> [1006: 3.54] --> [1010: 7.15].

# 11.16 Example 16

The content of Execution is

#!/bin/bash

./PJ3 network01.txt DirectedGraph 2

The content of Instructions is

PrintADJ

Stop

The file Output.txt is empty. The following message is written to stderr.

Usage: ./PJ3 <InputFile> <GraphType> <Flag>

## 11.17 Example 17

The content of Execution is

#!/bin/bash

./PJ3 network01.txt DirectedGraph 0

The content of Instructions is

PrintPath 1 3

Stop

The file Output.txt is empty. The following is written to stderr.

Error: Invalid instruction.

# 11.18 Example 18

The content of Execution is

#!/bin/bash

./PJ3 network01.txt DirectedGraph 0

The content of Instructions is

SingleSource 1

PrintPath 1 2

PrintPath 2 3

PrintPath 1 8

SingleSource 2

PrintPath 1 2

PrintPath 2 5

Stop

The content of produced Output.txt is

The shortest path from 1 to 2 is:

 $[1: 0.00] \longrightarrow [4: 5.00] \longrightarrow [2: 8.00].$ 

There is no path from 1 to 8.

The shortest path from 2 to 5 is:

 $[2: 0.00] \longrightarrow [4: 2.00] \longrightarrow [5: 4.00].$ 

Good Luck!