# Chem277B: Machine Learning Algorithms

# Homework assignment #6: Clustering

```
In [168...
         import numpy as np
          import pandas as pd
          import math
          import matplotlib.pyplot as plt
          import torch
          import torch.nn as nn
          import torch.optim as optim
          from sklearn.model selection import train test split, KFold
          import warnings
          from sklearn.cluster import DBSCAN
          from sklearn import cluster, datasets, mixture
          from sklearn.preprocessing import StandardScaler
          from itertools import cycle, islice
          from pylab import *
          import seaborn as sns
         np.random.seed(0)
         sns.set()
```

#### 1. KMeans.

(a) By normalizing the data and visualizing their correlation, I noticed that all three types are correlated by features C and D. In addition, amides and ethers are correlated by features C and C, but phenols are not correlated by these two features.

```
In [169... compounds = pd.read_csv('compounds.csv')

Out[169]:

A B C D type

O 6.4 2.9 4.3 1.3 amide

1 5.7 4.4 1.5 0.4 phenol

2 6.7 3.0 5.2 2.3 ether

3 5.8 2.8 5.1 2.4 ether

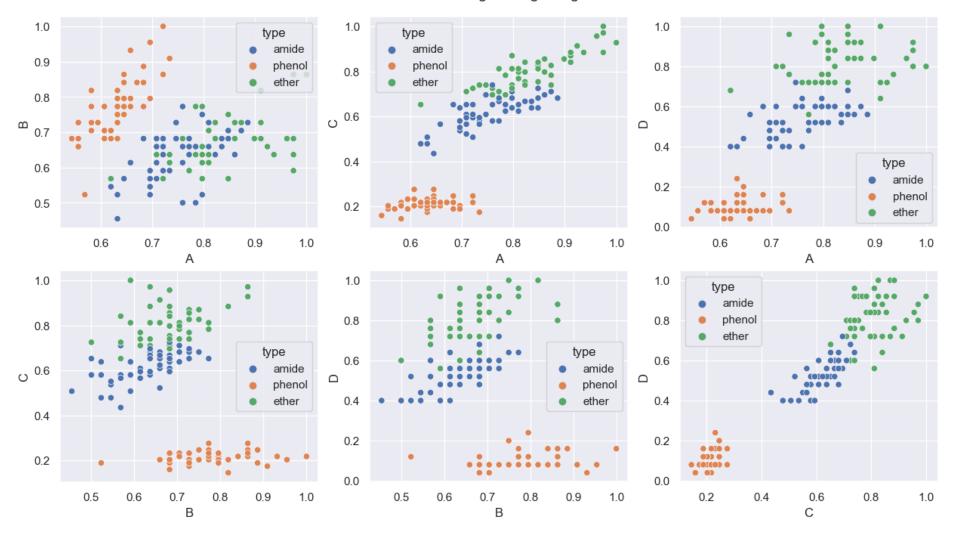
4 6.4 3.2 5.3 2.3 ether
```

```
In [170... compounds.loc[:,'A':'D'].max(axis=0)
                7.9
Out[170]:
                4.4
          C
                6.9
          D
                2.5
          dtype: float64
In [171... compounds.loc[:,'A':'D'] = compounds.loc[:,'A':'D'] / compounds.loc[:,'A':'D'].max(axis=0)
          compounds.head()
Out[171]:
                   Α
                            В
                                     С
                                          D
                                              type
           0 0.810127 0.659091 0.623188 0.52
                                             amide
           1 0.721519 1.000000 0.217391 0.16 phenol
           2 0.848101 0.681818 0.753623 0.92
                                              ether
           3 0.734177 0.636364 0.739130 0.96
                                              ether
           4 0.810127 0.727273 0.768116 0.92
                                              ether
In [172... fig, axes = plt.subplots(2, 3, figsize=(15,8))
          fig.suptitle('Correlation Among Testing Reagents', y=0.93)
          sns.scatterplot(ax=axes[0,0], data = compounds, x='A', y='B', hue='type')
          sns.scatterplot(ax=axes[0,1], data = compounds, x='A', y='C', hue='type')
          sns.scatterplot(ax=axes[0,2], data = compounds, x='A', y='D', hue='type')
          sns.scatterplot(ax=axes[1,0], data = compounds, x='B', y='C', hue='type')
          sns.scatterplot(ax=axes[1,1], data = compounds, x='B', y='D', hue='type')
          sns.scatterplot(ax=axes[1,2], data = compounds, x='C', y='D', hue='type')
```

<AxesSubplot: xlabel='C', ylabel='D'>

Out[172]:

#### **Correlation Among Testing Reagents**



(b) I have finished the KMeans clustering codes as shown below. I also chose K = 2, 3, 4 and generated 3 new columns in the compounds dataframe. After visualizing the codes, I noticed that K = 2 is actually the best clustering because each cluster is very distant apart from the other in all the correlation graphs.

```
In [173... class KMeans():
    def __init__(self, K, maximum_iters=100):
        # K: number of clusters to be created
        # distance matrix is Eucledian distance
        self.K = K
        self.maximum_iters = maximum_iters

    def cluster(self, input_points):
        """ Do KMeans clustering
        input_points: np.array shape(ndata, nfeatures).
```

```
Each feature is assumed to be normalized within range of [0,1]
    centroids = np.random.random((self.K, input points.shape[1]))
    assignments = np.zeros(input points.shape[0], dtype = np.int32)
    new assignments = self.create new assignments(centroids, input points)
    # restart if run into bad initialization
    # Comment out this part for Q1.(d)
    if len(np.unique(new assignments)) < self.K:</pre>
        return self.cluster(input points)
    n iters = 1
    while (new assignments != assignments).any() and n iters < self.maximum iters:</pre>
        ### Compute the centroid given new assignment ###
        centroids = np.array([input points[new assignments == k].mean(axis=0) for \
                             k in range(self.K)])
        assignments = new assignments
        ### Update the assignment with current centroids ###
        new assignments = self.create new assignments(centroids, input points)
        if len(np.unique(new assignments))< self.K:</pre>
            warnings.warn('At least one centroid vanishes')
        n iters += 1
        if n iters == self.maximum iters:
            print("Warning: Maximum number of iterations reached!")
    return new assignments
def create new assignments(self, centroids, data points):
    """ Assign each datapoint to its nearest centroid.
    centroid: 2d array of the current centroid for each cluster
    data points: 2d arrays recording the features of each data point.
    0.00
    ###Compute the distances that stores the Eucledian distances between each datapoints and the centroid ###
    #shape (ndata,ncentroid)
    distances = np.sqrt(((data points[:, np.newaxis, :] - centroids)**2).sum(axis = -1))
    new assignments = np.argmin(distances, axis=-1)
    return new assignments
```

```
In [174... compounds_ndarray = np.array(compounds.loc[:,'A':'D'])
   KMeans_2 = KMeans(2, maximum_iters=100)
   compounds['type_2'] = KMeans_2.cluster(compounds_ndarray)
   KMeans_3 = KMeans(3, maximum_iters=100)
   compounds['type_3'] = KMeans_3.cluster(compounds_ndarray)
   KMeans_4 = KMeans(4, maximum_iters=100)
   compounds['type_4'] = KMeans_4.cluster(compounds_ndarray)
   compounds.head()
```

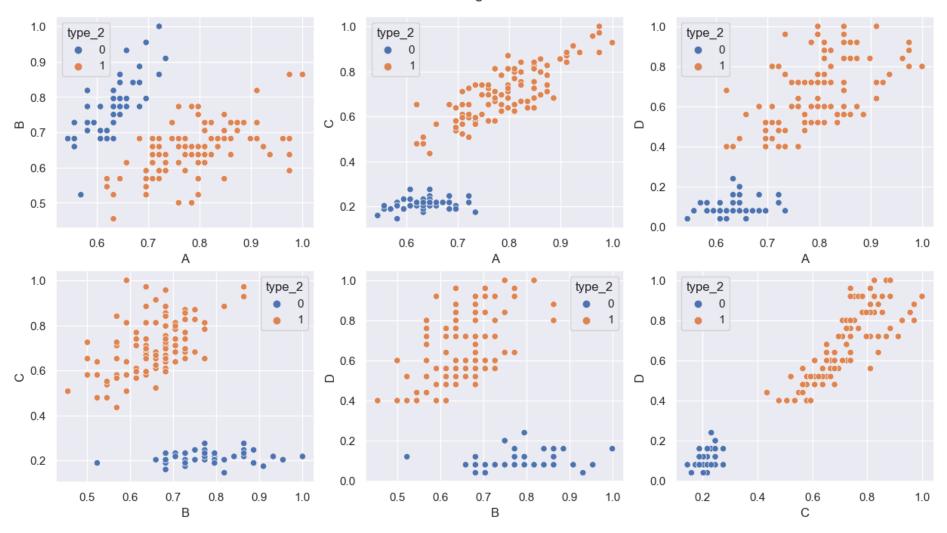
```
0 0.810127 0.659091 0.623188 0.52
                                                               2
                                             amide
                                                        1
                                                                      3
           1 0.721519 1.000000 0.217391 0.16 phenol
                                                               0
                                                       0
                                                                      0
           2 0.848101 0.681818 0.753623 0.92
                                                        1
                                                               1
                                                                      2
                                              ether
           3 0.734177 0.636364 0.739130 0.96
                                                                      2
                                              ether
                                                        1
                                                               1
           4 0.810127 0.727273 0.768116 0.92
                                              ether
                                                        1
                                                               1
                                                                      2
In [175... fig, axes = plt.subplots(2, 3, figsize=(15,8))
          fig.suptitle('KMeans Clustering with K=2 Clusters', y=0.93)
          sns.scatterplot(ax=axes[0,0], data = compounds, x='A', y='B', hue='type 2')
          sns.scatterplot(ax=axes[0,1], data = compounds, x='A', y='C', hue='type 2')
          sns.scatterplot(ax=axes[0,2], data = compounds, x='A', y='D', hue='type 2')
          sns.scatterplot(ax=axes[1,0], data = compounds, x='B', y='C', hue='type 2')
          sns.scatterplot(ax=axes[1,1], data = compounds, x='B', y='D', hue='type 2')
          sns.scatterplot(ax=axes[1,2], data = compounds, x='C', y='D', hue='type 2')
          <AxesSubplot: xlabel='C', ylabel='D'>
Out[175]:
```

type type\_2 type\_3 type\_4

Out[174]:

Α

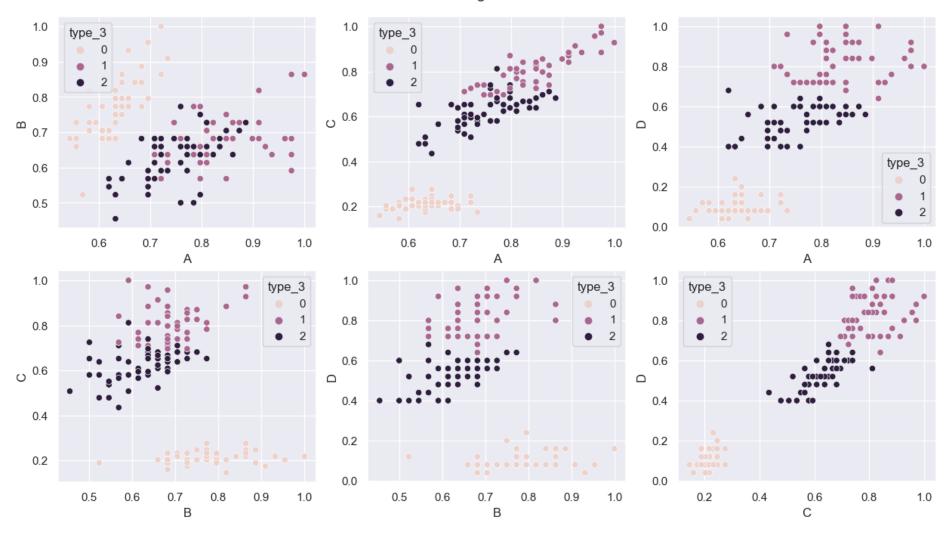
# KMeans Clustering with K=2 Clusters



```
In [176... fig, axes = plt.subplots(2, 3, figsize=(15,8))
    fig.suptitle('KMeans Clustering with K=3 Clusters', y=0.93)
    sns.scatterplot(ax=axes[0,0], data = compounds, x='A', y='B', hue='type_3')
    sns.scatterplot(ax=axes[0,1], data = compounds, x='A', y='C', hue='type_3')
    sns.scatterplot(ax=axes[0,2], data = compounds, x='A', y='D', hue='type_3')
    sns.scatterplot(ax=axes[1,0], data = compounds, x='B', y='C', hue='type_3')
    sns.scatterplot(ax=axes[1,1], data = compounds, x='B', y='D', hue='type_3')
    sns.scatterplot(ax=axes[1,2], data = compounds, x='C', y='D', hue='type_3')
```

Out[176]: <AxesSubplot: xlabel='C', ylabel='D'>

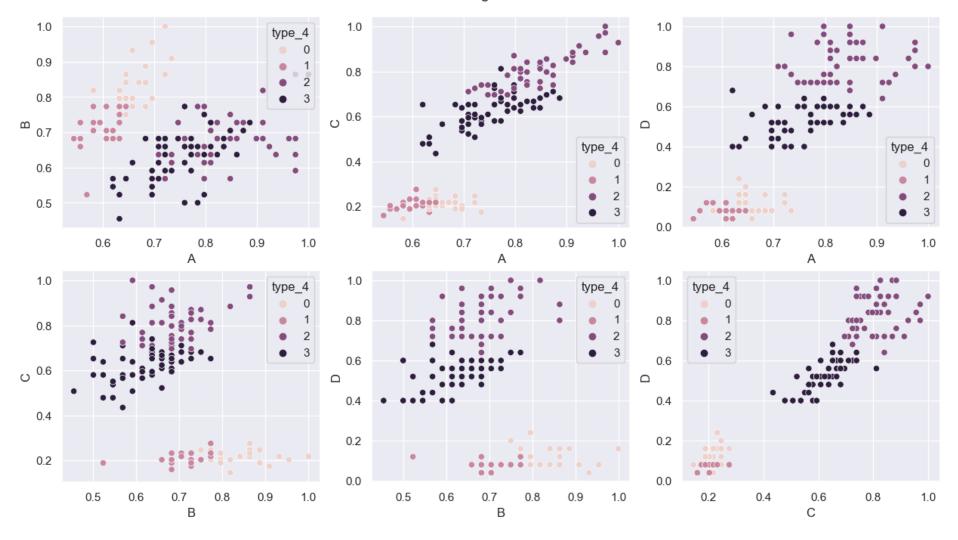
### KMeans Clustering with K=3 Clusters



```
fig, axes = plt.subplots(2, 3, figsize=(15,8))
fig.suptitle('KMeans Clustering with K=4 Clusters', y=0.93)
sns.scatterplot(ax=axes[0,0], data = compounds, x='A', y='B', hue='type_4')
sns.scatterplot(ax=axes[0,1], data = compounds, x='A', y='C', hue='type_4')
sns.scatterplot(ax=axes[0,2], data = compounds, x='A', y='D', hue='type_4')
sns.scatterplot(ax=axes[1,0], data = compounds, x='B', y='C', hue='type_4')
sns.scatterplot(ax=axes[1,1], data = compounds, x='B', y='D', hue='type_4')
sns.scatterplot(ax=axes[1,2], data = compounds, x='C', y='D', hue='type_4')
```

Out[177]: <AxesSubplot: xlabel='C', ylabel='D'>

# KMeans Clustering with K=4 Clusters



(c) I ran the provided validation function on the K=3 clustering and the true label. The clustering is pretty close to the original labeling, giving the following results:

Class 0 - ether: 46 out of 50 are classified correctly

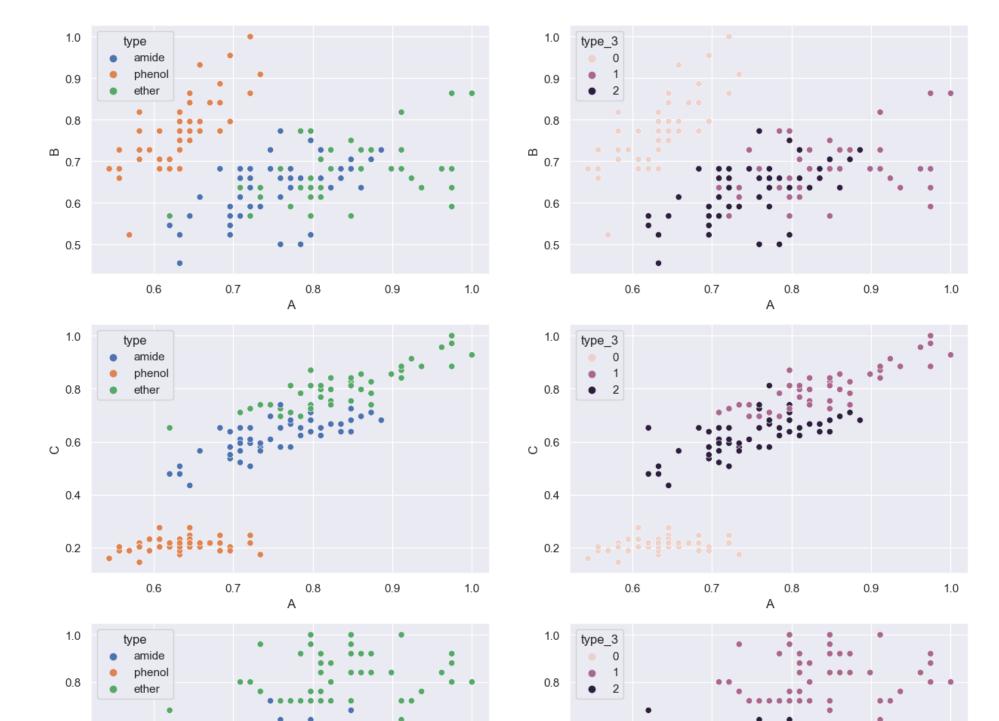
Class 1 - phenol: 50 out of 50 are classified correctly

Class 2 - amide: 48 out of 49 are classified correctly

When I visualized the results using Seaborn, I think the KMeans clustering is actually better than the true labeling, especially for correlations between A & D, B & D and C & D.

```
In [178... def validate(y hat,y):
              """print accuracy of prediction for each class for the compounds dataset
             yhat: np.array shape(ndata). Your prediction of classes
             y: np.array of str shape(ndata). data labels / groudn truths.
              # correct classification
              compounds = np.unique(y) # should be ['amide', 'phenol', 'ether'] for compounds dataset
              clusters =[np.where((y==c)) for c in compounds]
             pred class = np.unique(y hat)
              #remove -1 for noise point in DBSCAN
             pred class= np.delete(pred class,np.where(pred class==-1))
              assert len(pred class) == len(compounds), f'y hat has less or more than {len(compounds)} classes:{pred class}'
             for i in range(3):
                 #loop over solutions
                 counts=[]
                 scores=[]
                 for j in range(3):
                      #loop over clusters of true assignments
                      sol i= np.where((y hat==pred class[i]))
                     counts.append(len(np.intersect1d(sol i, clusters[j])))
                      scores.append(counts[-1]/len(clusters[j]))
                 idx = np.argmax(scores)
                 print(f'Class {pred class[i]} - {compounds[idx]}: {counts[idx]} out \
          of {np.count nonzero(clusters[idx])} are classified correctly')
In [179... validate(compounds['type 3'], compounds['type'])
         Class 0 - phenol: 50 out of 50 are classified correctly
         Class 1 - ether: 46 out of 50 are classified correctly
         Class 2 - amide: 48 out of 49 are classified correctly
In [180...] fig, axes = plt.subplots(6, 2, figsize=(15,30))
         fig.suptitle('K=3 Cluster Comparison with True Label', y=0.93)
          sns.scatterplot(ax=axes[0,0], data = compounds, x='A', y='B', hue='type')
          sns.scatterplot(ax=axes[0,1], data = compounds, x='A', y='B', hue='type 3')
          sns.scatterplot(ax=axes[1,0], data = compounds, x='A', y='C', hue='type')
          sns.scatterplot(ax=axes[1,1], data = compounds, x='A', y='C', hue='type 3')
          sns.scatterplot(ax=axes[2,0], data = compounds, x='A', y='D', hue='type')
          sns.scatterplot(ax=axes[2,1], data = compounds, x='A', y='D', hue='type 3')
          sns.scatterplot(ax=axes[3,0], data = compounds, x='B', y='C', hue='type')
          sns.scatterplot(ax=axes[3,1], data = compounds, x='B', y='C', hue='type 3')
          sns.scatterplot(ax=axes[4,0], data = compounds, x='B', y='D', hue='type')
          sns.scatterplot(ax=axes[4,1], data = compounds, x='B', y='D', hue='type 3')
          sns.scatterplot(ax=axes[5,0], data = compounds, x='C', y='D', hue='type')
          sns.scatterplot(ax=axes[5,1], data = compounds, x='C', y='D', hue='type 3')
```

Out[180]: <AxesSubplot: xlabel='C', ylabel='D'>



(d) I encountered bad initialization and received a lot of warning signs, including Maximum number of iterations reached and warnings.warn('At least one centroid vanishes'). I think it means that one or more of the initial K centroids are too far away from all data points, hence resulting in empty cluster(s). So in this case the algorithm just keeps running until it reaches the maximum number of iterations. But the faraway centroids will not be updated with new data points, which causes the centroids to remain in the initial distant positions.

Therefore, it is important to check whether all K clusters have at least one data point assigned to them. If not, we need to restart the clustering with a new set of randomly initialized centroids.

I found the following possible solutions: 1. KMeans++, which choose initial centroids uniformly from the dataset to make sure thei will be assigned data points. 2. Instead of K centroids, we choose 2K or 3K centroids and discard the empty centroids to keep K centroids with data points assigned.

```
In [181...

class KMeans_4():
    def __init__(self, K, maximum_iters=100):
        # K: number of clusters to be created
        # distance matrix is Eucledian distance
        self.K = K
        self.maximum_iters = maximum_iters

def cluster(self, input_points):
    """ Do KMeans clustering
        input_points: np.array shape(ndata, nfeatures).
        Each feature is assumed to be normalized within range of [0,1]
    """
    centroids = np.random.random((self.K, input_points.shape[1]))
    assignments = np.zeros(input_points.shape[0], dtype = np.int32)
    new_assignments = self.create_new_assignments(centroids, input_points)
```

```
# restart if run into bad initialization
                  # Comment out this part for Q1.(d)
                    if len(np.unique(new assignments)) < self.K:</pre>
                        return self.cluster(input points)
                  n iters = 1
                  while (new assignments != assignments).any() and n iters < self.maximum iters:</pre>
                      ### Compute the centroid given new assignment ###
                      centroids = np.array([input points[new assignments == k].mean(axis=0) for \
                                            k in range(self.K)])
                      assignments = new assignments
                      ### Update the assignment with current centroids ###
                      new assignments = self.create new assignments(centroids, input points)
                      if len(np.unique(new assignments))< self.K:</pre>
                          warnings.warn('At least one centroid vanishes')
                      n iters += 1
                      if n iters == self.maximum iters:
                          print("Warning: Maximum number of iterations reached!")
                  return new assignments
              def create new assignments(self, centroids, data points):
                  """ Assign each datapoint to its nearest centroid.
                  centroid: 2d array of the current centroid for each cluster
                  data points: 2d arrays recording the features of each data point.
                  ###Compute the distances that stores the Eucledian distances between each datapoints and the centroid ###
                  #shape (ndata,ncentroid)
                  distances = np.sqrt(((data points[:, np.newaxis, :] - centroids)**2).sum(axis = -1))
                  new assignments = np.argmin(distances, axis=-1)
                  return new assignments
In [182... KMeans 4 1 = KMeans 4(4, maximum iters=100)
          compounds['type 4 1'] = KMeans 4 1.cluster(compounds ndarray)
          KMeans 4 2 = KMeans 4(4, maximum iters=100)
          compounds['type 4 2'] = KMeans 4 2.cluster(compounds ndarray)
          KMeans 4 3 = KMeans 4(4, \text{ maximum iters}=100)
          compounds['type 4 3'] = KMeans 4 3.cluster(compounds ndarray)
          KMeans 4\ 4 = \text{KMeans } 4(4, \text{maximum iters}=100)
          compounds['type 4 4'] = KMeans 4 4.cluster(compounds ndarray)
          KMeans 4 5 = KMeans 4(4, \text{ maximum iters}=100)
          compounds['type 4 5'] = KMeans 4 5.cluster(compounds ndarray)
          compounds.head()
```

```
Warning: Maximum number of iterations reached!
/var/folders/pk/syhj1001491bwlx124c6hv h0000gn/T/ipykernel 17298/3366918875.py:25: RuntimeWarning: Mean of empty slice.
 centroids = np.array([input points[new assignments == k].mean(axis=0) for \
/opt/miniconda3/envs/qm-tools/lib/python3.10/site-packages/numpy/core/ methods.py:181: RuntimeWarning: invalid value en
countered in true divide
 ret = um.true divide(
/var/folders/pk/syhj1001491bwlx124c6hv h0000gn/T/ipykernel 17298/3366918875.py:31: UserWarning: At least one centroid v
anishes
 warnings.warn('At least one centroid vanishes')
/var/folders/pk/syhj1001491bwlx124c6hv h0000gn/T/ipykernel 17298/3366918875.py:25: RuntimeWarning: Mean of empty slice.
 centroids = np.array([input points[new assignments == k].mean(axis=0) for \
/opt/miniconda3/envs/qm-tools/lib/python3.10/site-packages/numpy/core/ methods.py:181: RuntimeWarning: invalid value en
countered in true divide
 ret = um.true divide(
/var/folders/pk/syhj1001491bwlx124c6hv h0000gn/T/ipykernel 17298/3366918875.py:31: UserWarning: At least one centroid v
anishes
 warnings.warn('At least one centroid vanishes')
/var/folders/pk/syhj1001491bwlx124c6hv h0000gn/T/ipykernel 17298/3366918875.py:25: RuntimeWarning: Mean of empty slice.
  centroids = np.array([input points[new assignments == k].mean(axis=0) for \
/opt/miniconda3/envs/qm-tools/lib/python3.10/site-packages/numpy/core/ methods.py:181: RuntimeWarning: invalid value en
countered in true divide
 ret = um.true divide(
/var/folders/pk/syhj1001491bwlx124c6hv h0000gn/T/ipykernel 17298/3366918875.py:31: UserWarning: At least one centroid v
anishes
 warnings.warn('At least one centroid vanishes')
/var/folders/pk/syhj1001491bwlx124c6hv h0000gn/T/ipykernel 17298/3366918875.py:25: RuntimeWarning: Mean of empty slice.
 centroids = np.array([input points[new assignments == k].mean(axis=0) for \
/opt/miniconda3/envs/qm-tools/lib/python3.10/site-packages/numpy/core/ methods.py:181: RuntimeWarning: invalid value en
countered in true divide
 ret = um.true divide(
/var/folders/pk/syhj1001491bwlx124c6hv h0000qn/T/ipykernel 17298/3366918875.py:31: UserWarning: At least one centroid v
anishes
 warnings.warn('At least one centroid vanishes')
/var/folders/pk/syhj1001491bwlx124c6hv h0000gn/T/ipykernel 17298/3366918875.py:25: RuntimeWarning: Mean of empty slice.
  centroids = np.array([input points[new assignments == k].mean(axis=0) for \
/opt/miniconda3/envs/qm-tools/lib/python3.10/site-packages/numpy/core/ methods.py:181: RuntimeWarning: invalid value en
countered in true divide
 ret = um.true divide(
/var/folders/pk/syhj1001491bwlx124c6hv h0000qn/T/ipykernel 17298/3366918875.py:31: UserWarning: At least one centroid v
anishes
 warnings.warn('At least one centroid vanishes')
```

:		Α	В	С	D	type	type_2	type_3	type_4	type_4_1	type_4_2	type_4_3	type_4_4	type_4_5
	0	0.810127	0.659091	0.623188	0.52	amide	1	2	3	1	1	1	0	1
	1	0.721519	1.000000	0.217391	0.16	phenol	0	0	0	1	1	1	0	1
	2	0.848101	0.681818	0.753623	0.92	ether	1	1	2	1	1	1	0	1
	3	0.734177	0.636364	0.739130	0.96	ether	1	1	2	1	1	1	0	1
	4	0.810127	0.727273	0.768116	0.92	ether	1	1	2	1	1	1	0	1

# 2. DBSCAN.

Out[182]:

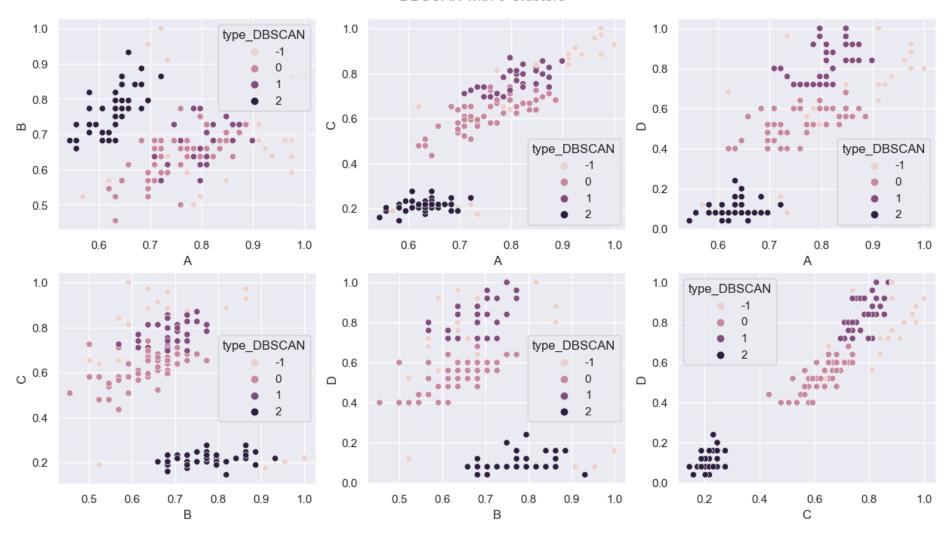
(a) I tried to adjust the eps and min\_samples hyperparameters. Apparently there's no easy way to remove all noisy points. In the end with eps=0.9 and min\_samples = 5, I acquired the following 3+1 clusters, with 3 clusters and 1 noisy cluster.

With the set hyperparameters, I have altogether 103 core points, 26 border points, and 21 noise points.

Compared to KMeans, DBSCAN seems less flexible and less effective. It results in a lot of noise points that can't be defined. With the compounds dataset, I prefer KMeans.

```
In [183... compounds DBSCAN = compounds.loc[:,'A':'D'].values
         db = DBSCAN(eps=0.09, min_samples=5)
         clustering = db.fit(compounds DBSCAN)
         # Cluster labels for each point in the dataset given to fit(). Noisy samples are given the label -1.
         clustering.labels
         array([0, -1,
                                    2, -1,
                                          1, 0,
                                                   1,
                                                       0, -1, -1,
Out[183]:
                        2, 2, 1, -1, 1, 2, 1,
                                                   2,
                                                      2,
                                                          2, 1, -1,
                                           0, -1, 1,
                                                      2,
                                                              1,
                                                          0,
                                0, -1,
                                          1, 2,
                                                   2,
                                                          2,
                                                              0,
                                                       0,
                                           2,
                                              1,
                                                   0,
                                                       0,
                                                          0,
                                                              0,
                                           2, 2,
                                                      2, 1,
                                    0, -1,
                                                   2,
                                                              1,
                                                   2,
                                                       2, -1,
                                                              0,
                                    2,
                                       2,
                                           0, -1,
                                                      2, 1,
                -1, 2, 2, 2, 0, -1, -1, 1, 0, 1,
                                                              0, 1, 0, 1, -1,
                 2, 0, 2, 0, 1, 2, 0, 2, 0, 2, 1, 0, 0])
In [184... # Indices of core samples.
         clustering.core sample indices
```

```
array([ 0,
                       2,
                            4,
                                 5,
                                      7,
                                           8,
                                               9, 10, 13, 14, 15, 17, 18,
Out[184]:
                           21, 24,
                                     25,
                                          26, 27, 28, 29, 31, 32,
                           40, 41, 43, 44,
                                              45, 46, 47, 54,
                                                                  55,
                                                                       57,
                  59, 60, 61, 62, 63, 65, 66, 67, 69, 71, 72, 73, 74,
                 75, 76, 77, 78, 79, 81, 82, 83, 84, 85, 89,
                 93, 99, 101, 103, 104, 105, 106, 107, 108, 109, 111, 112, 114,
                 115, 116, 117, 118, 120, 121, 122, 126, 128, 129, 130, 131, 132,
                 133, 134, 136, 137, 139, 141, 142, 143, 145, 146, 148, 149])
In [185... # Number of core samples.
         len(clustering.core sample indices )
Out[185]:
In [186... compounds['type DBSCAN'] = clustering.labels
         fig, axes = plt.subplots(2, 3, figsize=(15,8))
         fig.suptitle('DBSCAN with 3 Clusters', y=0.93)
         sns.scatterplot(ax=axes[0,0], data = compounds, x='A', y='B', hue='type DBSCAN')
         sns.scatterplot(ax=axes[0,1], data = compounds, x='A', y='C', hue='type DBSCAN')
         sns.scatterplot(ax=axes[0,2], data = compounds, x='A', y='D', hue='type DBSCAN')
         sns.scatterplot(ax=axes[1,0], data = compounds, x='B', y='C', hue='type DBSCAN')
         sns.scatterplot(ax=axes[1,1], data = compounds, x='B', y='D', hue='type DBSCAN')
         sns.scatterplot(ax=axes[1,2], data = compounds, x='C', y='D', hue='type DBSCAN')
          <AxesSubplot: xlabel='C', ylabel='D'>
Out[186]:
```



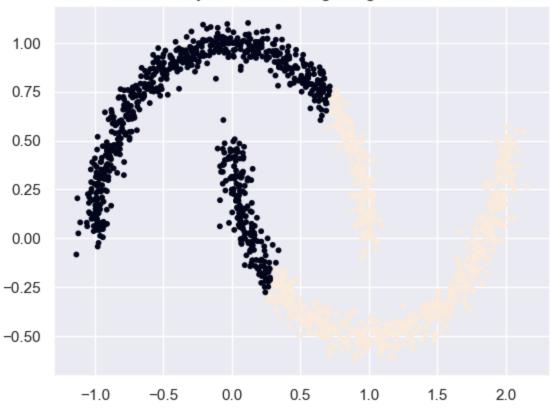
103 26 21

(b) In the case of noisy moon dataset, DBSCAN work much better than KMeans.

```
In [198... # Clustering the noisy moon dataset using KMeans
K_moon = KMeans(2, maximum_iters=100)
moon_clustering_k = K_moon.cluster(X)
moon_clustering_k
plt.scatter(X[:, 0], X[:, 1], s=10,c=moon_clustering_k)
plt.title('Noisy Moon Clustering using KMeans')
```

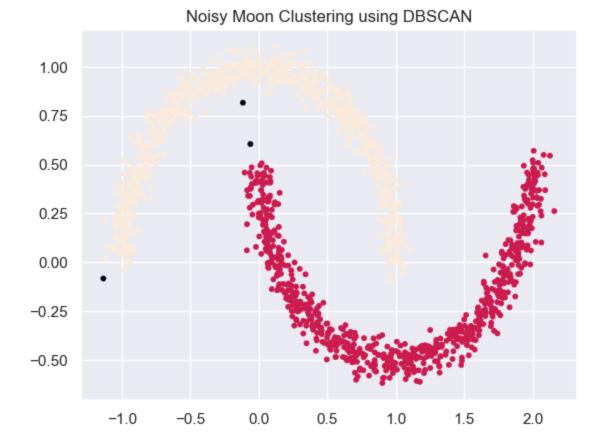
Out[198]: Text(0.5, 1.0, 'Noisy Moon Clustering using KMeans')

### Noisy Moon Clustering using KMeans



```
In [203... # Clustering the noisy moon dataset using DBSCAN
db_moon = DBSCAN(eps=0.1, min_samples=10)
clustering_moon = db_moon.fit(X)
# Cluster labels for each point in the dataset given to fit(). Noisy samples are given the label -1.
clustering_moon.labels_
plt.scatter(X[:, 0], X[:, 1], s=10,c=clustering_moon.labels_)
plt.title('Noisy Moon Clustering using DBSCAN')
```

Out[203]: Text(0.5, 1.0, 'Noisy Moon Clustering using DBSCAN')



In [ ]: