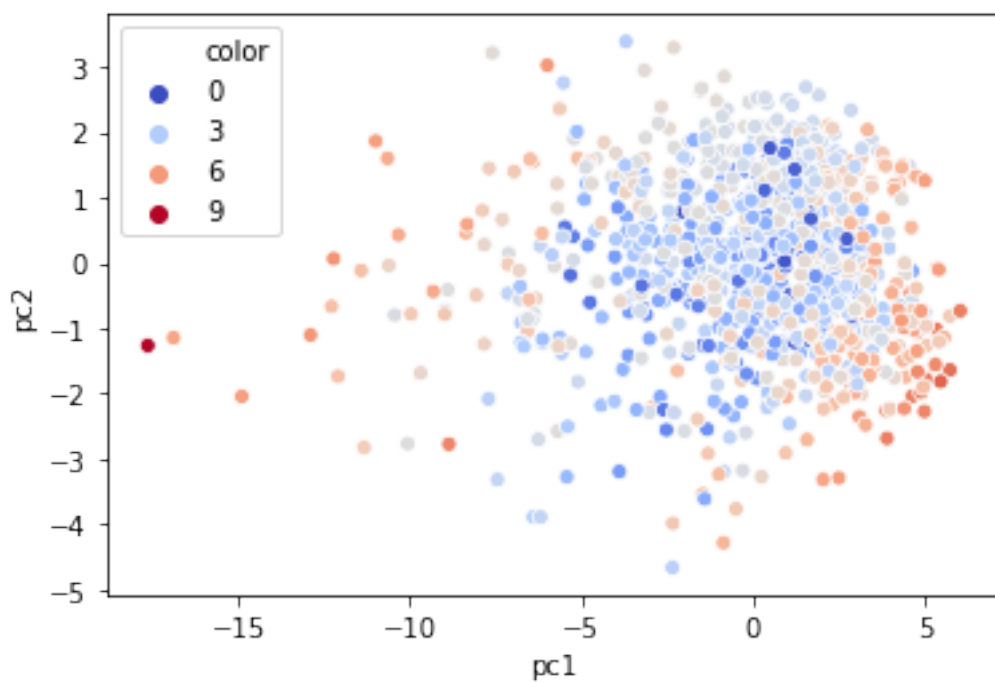


0.1 Question 2d

Create a 2D scatterplot of the first two principal components of `mid1_grades_centered_scaled`. Use `colorize_midterm_data` to add a color column to `mid1_2d_1st_2_pcs`. Your code will be very similar to the code from problems 2a and 2b.

```
In [53]: u_2d, s_2d, vt_2d = np.linalg.svd(mid1_grades_centered_scaled,full_matrices=True)
mid1_2d_1st_2_pcs = mid1_2d_1st_2_pcs = pd.DataFrame((u_2d[:, :2] @ np.diag(s[:2])), columns =
sns.scatterplot(data = colorize_midterm_data(mid1_2d_1st_2_pcs), x = "pc1", y = "pc2", hue = "
```



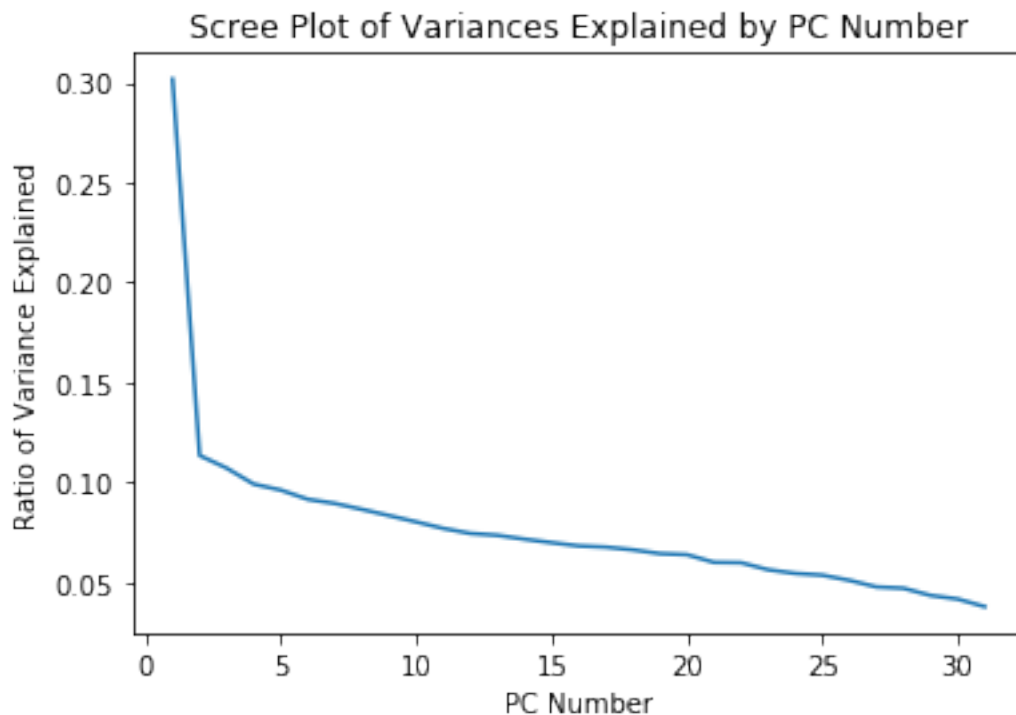
0.2 Question 2e

If you compute the fraction of the variance captured by this 2D scatter plot, you'll see it's only 17%, roughly 12% by the 1st PC, and roughly 5% by the 2nd PC. **In the cell below, create a scree plot showing the fraction of the variance explained by PC #i using the data from 2d.**

Informally, we can say that our midterm scores matrix has a high rank. More formally, we can say that a rank 2 approximation only captures a small fraction of the variance, and thus the data are not particularly amenable to 2D PCA scatterplotting.

```
In [54]: varianceSrs = (s_2d**2) / sum(s**2)
plt.plot(np.arange(1,32),varianceSrs)
plt.xlabel("PC Number")
plt.ylabel("Ratio of Variance Explained")
plt.title("Scree Plot of Variances Explained by PC Number")
```

```
Out[54]: Text(0.5, 1.0, 'Scree Plot of Variances Explained by PC Number')
```



Unfortunately, we have two problems:

1. There is a lot of overplotting, with only 27 distinct dots. This means that at least some states voted exactly alike in these elections.
2. We don't know which state is which, because the points are unlabeled.

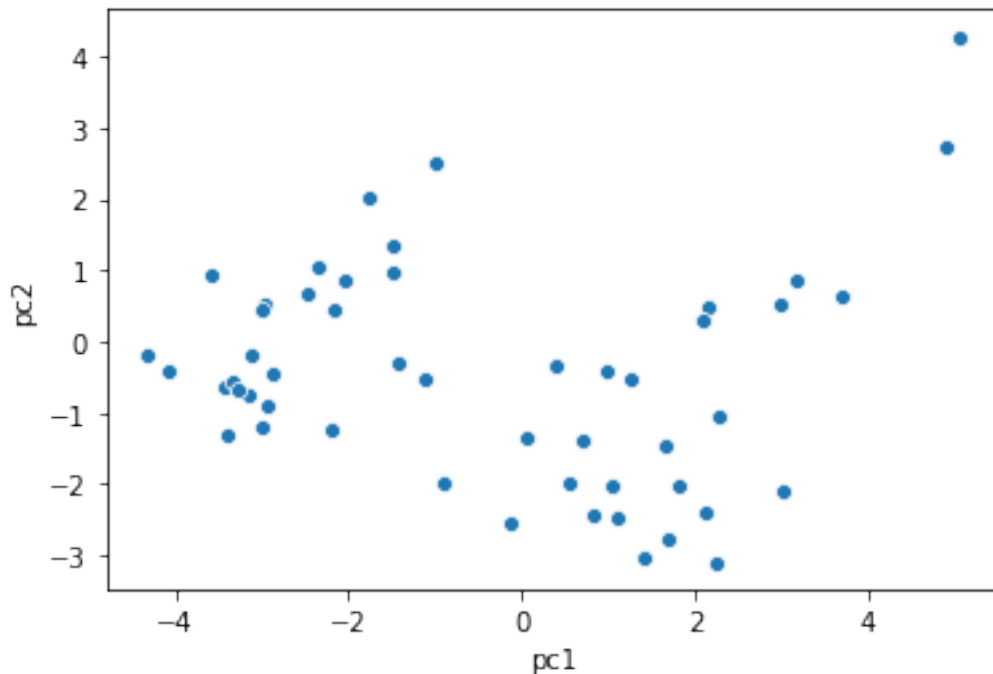
Let's start by addressing problem 1.

In the cell below, create a new dataframe `first_2_pcs_jittered` with a small amount of random noise added to each principal component. In this same cell, create a scatterplot.

The amount of noise you add should not significantly affect the appearance of the plot, it should simply serve to separate overlapping observations.

Hint: See the pairplot from the intro to question 2 for an example of how to introduce noise.

```
In [78]: first_2_pcs_jittered = first_2_pcs + np.random.normal(-0.35, 0.45, size = (len(first_2_pcs), 2))
sns.scatterplot(data = first_2_pcs_jittered, x = "pc1", y = "pc2");
```



Give an example of a cluster of states that vote a similar way. Does the composition of this cluster surprise you? If you're not familiar with U.S. politics, it's fine to just say 'No, I'm not surprised because I don't know anything about U.S. politics.'

California, New Mexico, and Connecticut appear to vote a similar way. I am not surprised since these are democrat states.

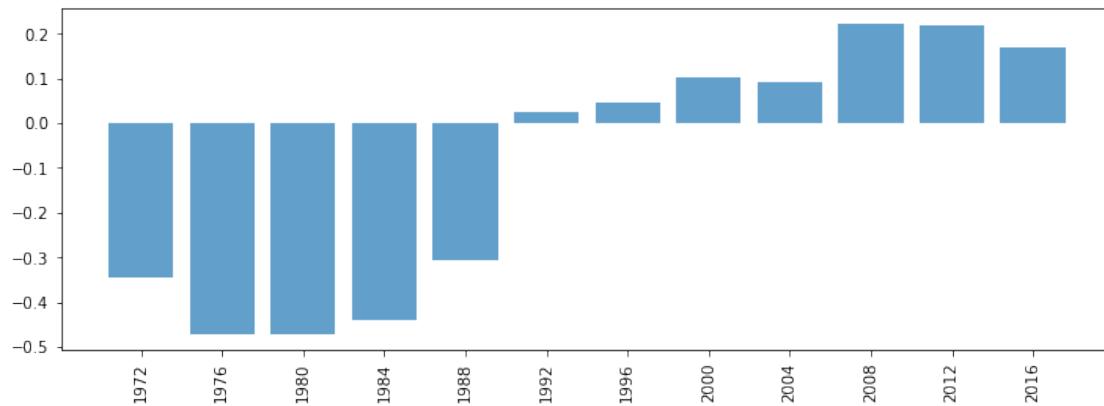
In the cell below, write down anything interesting that you observe by looking at this plot. You will get credit for this as long as you write something reasonable that you can take away from the plot.

Something interesting I observed is that New York and California appeared to vote differently. Usually these states seem to vote for democratic candidates, so it was surprising to see their difference.

In the cell below, plot the the 2nd row of V^T .

Hint: You are just copying and pasting code from the cell above and then changing one number.

```
In [81]: with plt.rc_context({"figure.figsize": (12, 4)}):  
         plot_pc(list(df_1972_to_2016.columns), vt_q3, 1);
```



0.3 Question 3i

Using your plots from question 3h as well as the original table, give a description of what it means to have a relatively large positive value for **pc1** (right side of the 2D scatter plot), and what it means to have a relatively large positive value for **pc2** (top side of the 2D scatter plot).

In other words, what is generally true about a state with relatively large positive value for **pc1**? For a large positive value for **pc2**?

Note: **pc2** is pretty hard to interpret, and the staff doesn't really have a consensus on what it means either. We'll be nice when grading.

Note: Principal components beyond the first are often hard to interpret (but not always; see question 1 earlier in this homework).

From the first plot, we see that all the PC1 values are negative, and this suggests that there is a negative relationship to the PC1 line. On the second plot from 3h, we see PC2 values rise from negative to positive values when measured across the PC1 values. So, we can see and deduce that the deviation of PC2 from PC1 changes as time passes.

0.4 Question 3j

To get a better sense of whether our 2D scatterplot captures the whole story, create a scree plot for this data. On the y-axis plot the fraction of the total variance captured by the i th principal component. You should see that the first two principal components capture much more of the variance than we were able to capture when using the Data 100 Midterm 1 data. It is partially for this reason that the 2D scatter plot was so much more useful for this dataset.

Hint: Your code will be very similar to the scree plot from problem 1d. Be sure to label your axes appropriately!

```
In [82]: plt.plot(np.arange(1, len(s_q3) + 1), (np.square(s_q3)/sum(np.square(s_q3))))  
         plt.xlabel('PC Number')  
         plt.ylabel('Ratio of Variance Explained')  
         plt.title("Scree Plot of Variances Explained by PC Number (Elections Dataset)")
```

```
Out[82]: Text(0.5, 1.0, 'Scree Plot of Variances Explained by PC Number (Elections Dataset)')
```

