

Given Enough Eyeballs, All Bugs Are Shallow?

Revisiting Eric Raymond with Bug Bounty Programs

Thomas Maillart*

University of Geneva, Geneva, Switzerland

Mingyi Zhao

Snap Inc., USA

Jens Grossklags

Technical University Munich, Germany

John Chuang

University of California, Berkeley, USA

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Bug bounty programs offer a modern way for organizations to crowdsource their software security, and for security researchers to be fairly rewarded for the vulnerabilities they find. However, little is known on the incentives set by bug bounty programs – how they drive engagement and new bug discoveries. This article provides an empirical investigation of the strategic interactions among the managers and participants of bug bounty programs, as well as the intermediation by bug bounty platforms. We find that for a given bug bounty program, each security researcher can only expect to discover a bounded number of bugs. This result offers a validation step to a theory brought forth early on by Brady et al. [1], which proposes that each security researcher inspecting a software piece offers a unique environment of skills and mindset, which is prone to the discovery of bugs that others may not be able to uncover. Bug bounty programs indeed benefit from the engagement of large crowds of researchers. Conversely, security researchers benefit greatly from searching bugs in multiple bug bounty programs. We find however that, following a strong front-loading effect, newly launched programs attract researchers, at the

expense of older programs: the probability of finding bugs decays as $\sim 1/t^{0.4}$ after the launch of a program, even though bugs found later yield on average higher reward. Our results lead to us to formulate 3 recommendations for organizing bug bounty programs and platforms: (i) organize enrollment, mobility and renewal of security researchers across bounty programs, (ii) feature and organize programs for front-loading, and (iii) organize fluid market transactions to reduce uncertainty and thus, reduce incentives for security researchers to sell on the black market.

* thomas.maillart@unige.ch

I. INTRODUCTION

On March 2nd, 2016, the Pentagon announced the launch of its first *bug bounty* program [2]. From this point on, one of the most paranoid organizations in the world would offer incentives to hackers to break into its systems and report found vulnerabilities for a reward. Although bug bounty programs have mushroomed in the last few years, this audacious announcement by a prominent defense administration may set a precedent, if not a standard, for the future of cybersecurity practice.

Software security has long been recognized as a challenging computational problem [3] that often requires human intelligence. However, given the complexity of modern computer systems, human intelligence at the individual level is no longer sufficient. Instead, organizations are turning to tap the wisdom of crowds [4] to improve their security. Software security is not alone. Other disciplines have similarly turned to mobilizing people at scale to tackle their hard problems, such as sorting galaxies in astronomy [5], folding proteins in biology [6], recognizing words from low quality book scans [7], and addressing outstanding mathematics problems [8, 9]. These examples involve different aspects of human intelligence, ranging from pattern recognition (e.g., Captcha [7]) to higher abstraction levels (e.g., mathematical conjectures [8, 9]). It is not clear what kind of intelligence is necessary to find bugs and vulnerabilities in software, but it generally requires a high level of programming proficiency coupled with *hacking skills* – out-of-the-box thinking to find unintended uses for a software.

From hedonist pleasure to reputation building, to activism, motivations and incentives for hacking have evolved over time [10]. Among these, reputation and monetary incentives are increasingly put in place to entice security researchers to hunt for bugs. Bug bounty programs and the online platforms help set such incentives [11–14], while facilitating communication and transactions between security researchers and software editors. It however remains unclear how current mechanism designs and incentive structures will influence the long-term success of bounty programs. A better understanding of bug discovery mechanisms [1, 15, 16], and a better characterization of the utility functions of security researchers, organizations launching bug bounty programs and bug bounty platforms, will help shape the way bug bounty programs evolve in the future.

In this study, we investigate a public data set of 35 public bug bounty programs from the *HackerOne* website. We find that with each vulnerability discovered within a bounty program, the probability of finding the next vulnerability in the program decreases more rapidly than the corresponding increase in payoff. Therefore, security researchers rationally switch to newly launched bounty programs at the expense of existing ones. This switching phenomenon has already been found in [14]. Here, we characterize it further, by quantifying how incentives evolve as more vulnerabilities get discovered in a program, and how researchers benefit in the long term by switching to newly launched programs. Our results help better understand the mechanisms associated with bug discovery, as they provide a validation step of the theory proposed in [1], and they help formulate concrete recommendations for the organization of both bug bounty programs and the online platforms supporting them.

This article is organized as follows. Related research is presented in Section II. Important features of the data set are detailed in Section III. We introduce the main mechanism driving vulnerability discovery in Section IV. Results are presented and discussed in Sections V and VI, respectively. We offer concluding remarks in Section VII.

II. BACKGROUND

Software reliability is an age-old problem [3, 17, 18]. Early empirical work on software bug discovery dates back to the time of UNIX systems [19], and over the years, numerous models for vulnerability discovery have been developed (see [16, 20] for some contemporary approaches). As early as in 1989, it was recognized that the time to achieve a given level of software reliability is inversely proportional to the desired failure frequency level [3]. For example, in order to achieve a 10^{-9} probability of failure, a software routine should be tested 10^9 times. Actually, the random variable $P(T > t) = 1/t$ corresponds to the Zipf's law [21, 22], which diverges as the random variable sample increases (i.e., no statistical moment is defined). Thus, there will always be software vulnerabilities to be discovered as long as enough resources can be provided to find them.

Taking an evolutionary perspective brings additional insights. Finding bugs is comparable

to the survival process involved in the selection of species: Defects are like genes, which get expressed under the pressure of environment changes. Brady et al. [1] have shown that software testing follows the principle of entropy maximization, which preserves *genetic variability* and thus, removes only the minimum possible number of bugs, following the exploration of use cases (the software environment). With her out-of-the-box – *hacker minded* – thinking, the security researcher is precisely good about envisioning a broad range of possible use cases, which may reveal a software defect (i.e., program crash) or an unintended behavior.

Software solutions have been developed to systematically detect software inconsistencies and thus potential bugs (e.g., Coverity, FindBugs, SLAM, Astree, to name a few). However, to date, no systematic algorithmic approach has been found to detect and remove bugs at a speed that would keep pace with software evolution and expansion. Thus, human intelligence is still considered as one of the most efficient ways to explore novel use case scenarios – by manual code inspection or with the help of bug testing software – in which a software may not behave in the intended way.

Management techniques and governance approaches have been developed to help software developers and security researchers in their review tasks, starting with pair programming [23]. To protect against cyber-criminals, it is also fashionable to hire *ethical hackers*, who have a mindset similar to potential attackers, to probe the security of computer systems [24–26]. The policy of full disclosure, originating from the hacking and open source communities, has played a significant role in software security by forcing software owners to acknowledge and fix vulnerabilities discovered and published by independent researchers [27]. The full-disclosure model has evolved into responsible disclosure, a standard practice where the security researcher agrees to allow a period of time for the vulnerability to be patched before publishing the details of the uncovered flaw. In most of these successful human-driven approaches, there is a knowledge-sharing component, either between two programmers sitting together in front of a screen, ethical hackers hired to probe the weaknesses of a computer system, or the broader community being exposed to open source code and publicly disclosed software vulnerabilities [28]. Thus, Eric Raymond’s famous quote “Given enough eyeballs, all bugs are shallow” [29] tends to hold, even though in practice things are

often slightly more complicated [30].

One way to gather enough eyeballs is to resort to the larger crowd of security researchers. For this purpose, bug bounty programs and vulnerability *markets* have emerged in recent years to facilitate the trading of bugs and vulnerabilities. These two-sided markets provide economic incentives to support the transfer of knowledge from security researchers to software organizations [31], as they help simultaneously harness the wisdom of crowds and to reveal the security level of organizations through a competitive incentive mechanism [32]. Nonetheless, the efficiency of bug bounty programs has been questioned on both theoretical [33, 34] and empirical grounds [35, 36].

Building on previous work by Schechter [32], Andy Ozment [37] theorized that the most efficient mechanisms are not markets *per se*, but rather auction systems [38]. In a nutshell, the proposed (monopsonistic) auction mechanism implies an initial reward $R(t = t_0) = R_0$, which increases linearly with time. If a bug is reported more than once, only the first reporter receives the reward. Therefore, security researchers have an incentive to submit a vulnerability early (before other researchers submit the same bug), but not too early, so that they can maximize their payoff $R(t) = R_0 + \epsilon \times t$ with ϵ the linear growth factor, which is meant to compensate for the increasing difficulty of finding each new bug. However, setting the right incentive structure $\{R_0, \epsilon\}$ is non-trivial given uncertainties in the amount of work needed, the level of competition (e.g., the number of researchers enrolled) in the bug bounty program [39], or the nature and likelihood of overlap between two submissions by different researchers. Nevertheless, bug bounty programs have emerged as a tool used by many software organizations, with a range of heterogeneous incentive schemes [12]. For instance, some bug bounty programs include no monetary rewards [13]. Meanwhile, dedicated platforms have been launched to act as trusted third parties in charge of clearing transactions between organizations and security researchers. These platforms also assist organizations in the design and deployment of their own program. One of the leading platforms is HackerOne which runs public and private programs for organizations across a wide range of business sectors. A subset of the private and public programs award bounties, while other bug bounty programs capitalize on incentives associated with reputation building, which is an important motivation driver in the hacker community [40]. These programs report bounty awards on

their company program pages on the HackerOne website. Previous research has investigated vulnerability trends, response and resolve behaviors, as well as reward structures of participating organizations [13, 14]. In particular, it was found that a considerable number of organizations experienced diminishing trends for the number of reported vulnerabilities, even as the monetary incentives exhibit a significantly positive correlation with the number of vulnerabilities reported [14].

III. DATA

The data were collected from the public part of the HackerOne website. From 35 public bounty programs, we collected the rewards received by security researchers (in US dollars), with their timestamps (45 other public bounty programs do not disclose detailed information on rewards, and the number of private programs is not disclosed). Since HackerOne started its platform in December 2013, new public programs have been launched roughly every two months, following an essentially memoryless Poisson process ($\lambda = 57$ days, $p < 0.001$ and $R^2 > 0.99$). Figure 1A shows the timeline of the 9 most active programs with at least 90 valid (i.e., rewarded) bug discoveries, as of February 15, 2016. When a new program is launched, we observe an initial peak within weeks after launch, which accounts for the majority of discoveries. Following the initial surge of vulnerability discoveries, bounty awards become less frequent following a decay function with long-memory, following a robust power law decay $\sim t^\alpha$ with $\alpha = -0.40(4)$ ($p < 0.001$ and $R^2 = 0.79$; fit of the time series obtained using ordinary least square regression as described in [42]) at the aggregate level and over all 35 bounty programs (see Figure 1B). Some programs depart from this averaged trend: For instance Twitter exhibits a steady, almost constant, bug discovery rate and VKontakte exhibits its peak activity months after the initial launch. These peculiar behaviors may be attributed to program tuning and marketing, to sudden change of media exposure or even to fundamental differences of program comparative fitness, for which we do not have specific information.

The power law decay observed here is reminiscent of the the long-established $\sim 1/\tau^1$ law of bug discovery in software testing [3]. This similitude is interesting even though bug bounties programs don't provide direct information regarding software reliability. The difference of

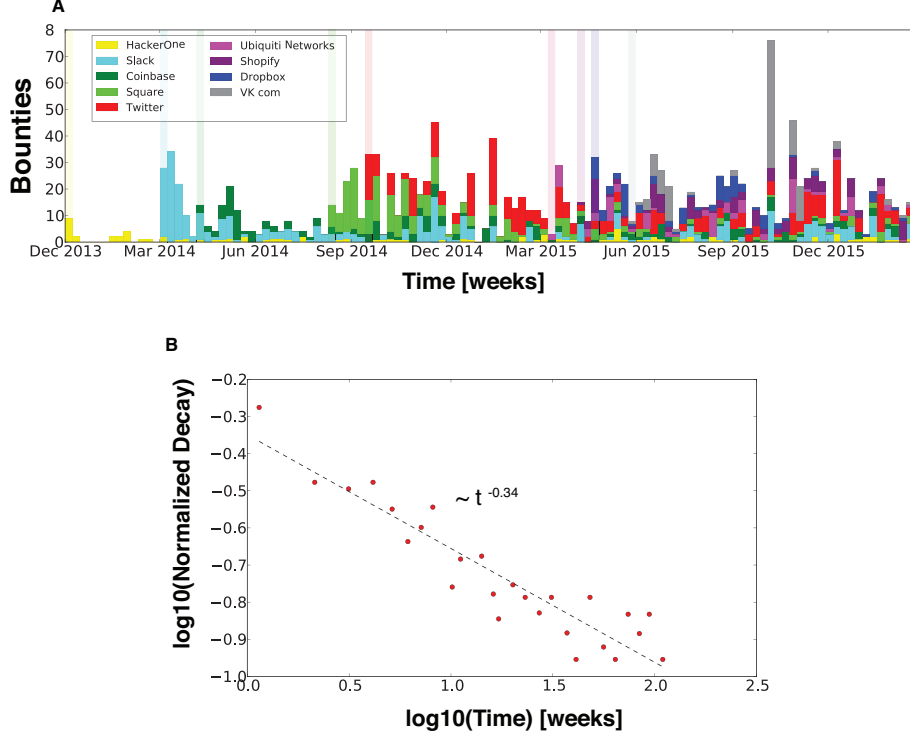


FIG. 1. **A.** Weekly vulnerability discoveries for the 9 most active programs (with at least 90 bug discoveries as of February 15, 2016). The light colored vertical bars represent the start of the program, occurring when the first bounty is awarded. Most programs exhibit an initial shock, followed by a decay of discoveries, which is characterized at the aggregate level by a long-memory process (panel **B**) characterized by a power law decay $\sim t^\alpha$ with $\alpha = -0.40(4)$ ($p < 0.001$ and $R^2 = 0.79$, obtained by ordinary least square fitting). Each data point in the figure is the median of normalized vulnerability numbers of all 35 programs considered in this study.

exponent ($\alpha \approx 0.4$ instead of 1), may stem from long-memory processes associated with human behaviors and human timing effects, which correspond to task priority queueing and a rationalize use of time as non-storable scarce resource [42]. Long-memory processes observed in collective human behaviors such as those observed on Figure 1B may also be associated with critical cascades of productive events [43]. The intuition is that each security researcher will generate a cascade of bug discoveries (of size the total number of bugs discovered by this person, which is a random variable across all researchers), and by her activity, each researcher will influence and attract other researchers, hence generating cascades of joining and of bug discoveries, which precise mechanisms are beyond the scope of the present paper.

Here, we don't consider the human timing effects encompassing delays, effort, processing time, influence. We only consider incremental valid bug discovery and reporting by security researchers.

IV. METHOD

Bug bounty programs work on the premise that humans as a crowd are efficient at searching and finding bugs. Their mere existence is a *de facto* recognition that market approaches for bug and security vulnerabilities discovery involving large pools of security researchers bring efficiency, beyond in-house security. Bug bounty programs signal that organizations are ready to complement their vertical cost-effective security operations with market approaches, which are traditionally perceived as less cost-effective, yet more adaptive [44]. Brady et al. [1] have early on offered a hint for the existence of such markets for bugs: according to their proposed theory, each researcher has slightly different skills and mindset. When a security researcher tests a software piece, by choosing the inputs, she offers a unique operational environment. This environment is prone to the discovery of new bugs, which may have not be seen by other researchers with their own environment. The proposed theory by Brady et al. [1] intrinsically justifies the existence of bug bounty programs structures as markets, which provide the necessary diversity to account for the highly uncertain risk horizon of bug discovery. Here, we develop a quantitative method to formalize a mechanism and to test the theory proposed in [1]. This validation step shall help provide organizational design insights for bug bounty programs.

For that, we investigate the interplay between the vulnerability discovery process and the cumulative reward distributed to security researchers within and across 35 public bounty programs hosted on HackerOne. When a bug bounty program starts, it attracts a number of security researchers, who in turn submit bugs. Subsequent bug discoveries get increasingly difficult for each researcher individual, and to some extent for all researchers together. The difficulties faced by security researchers can be technical. It can also be the result of insufficient or conflicting incentives. Here, we develop and test a model, which accounts for technical difficulties and insufficient incentives together. We further address conflicting incentives by measuring the effect of newly launched bug bounty program on incumbent

programs.

Starting from an initial probability of discovering the first vulnerability $P(k=0) = 1$, the probability to find a second bug, is a fraction of the former probability: $P_{k+1} = \beta * P_k$ with β a constant strictly smaller than one. The probability that no more discovery will be made after k steps is given by $P_k = \beta^k(1 - \beta)$. Conversely, starting from the initial reward $R_0 = R(k=0)$, the subsequent reward $R_1 = \Lambda_1 \cdot R_0$, and further additional reward $R_2 = \Lambda_2 \Lambda_1 \cdot R_0$. After n steps, the total reward is the sum of all past rewards:

$$R_n = R_0 \sum_{k=1}^n \Lambda_1 \dots \Lambda_k. \quad (1)$$

Thus, R_n is the recurrence solution of the Kesten map ($R_n = \Lambda_n R_{n-1} + R_0$) [45, 46]: As soon as amplification occurs (technically, some of the factors Λ_k are larger than 1), the distribution of rewards is a power law, whose exponent μ is a function of β and of the distribution of the factors Λ_k . In the case where all factors are equal to Λ , this model predicts three possible regimes for the distribution of rewards (for a given program): thinner than exponential for $\Lambda < 1$, exponential for $\Lambda = 1$, and power law for $\Lambda > 1$ with exponent $\mu = |\ln \beta| / \ln \Lambda$ (see Appendix). The expected payoff of vulnerability discovery is given by,

$$U_k = P_k \times R_k, \quad (2)$$

with both P_k and R_k random variables respectively determined by β and Λ . Because U is a multiplication of diverging probability and reward components, its nature is reminiscent of the St. Petersburg paradox (or St. Petersburg lottery), proposed first by the Swiss Mathematician Nicolas Bernoulli in 1713, and later formalized by his brother Daniel in 1738 [47]. The St. Petersburg paradox states the problem of decision-making when both the probability and the reward are diverging when $k \rightarrow \infty$: A player has a chance to toss a fair coin at each stage of the game. The pot starts at two and is doubled every time a head appears. The first time a tail appears, the game ends and the player wins whatever is in the pot. Thus the player wins two if a tail appears on the first toss, four if a head appears on the first toss and a tail on the second, eight if a head appears on the first two tosses and a tail on the third, and so on. The main interest of Bernoulli was to determine how much a player would be ready to pay for this game, and he found that very

few people would like to play this game even though the expected utility increases (in the simplest case proposed by Bernoulli, $U_n = \sum_{k=0}^n U_k = n$) [47]. The situation of a security researcher differs from the St. Petersburg lottery as bug search costs are incurred at every step. Since these costs influence the probability to find an additional bug the cost can be integrated in P_k . We could assume equivalently that costs are integrated into the utility as $U_k^* = U_k - c_k$. Here, we don't factor these costs because their exact nature is largely undetermined and our data don't offer a reliable proxy. The security researcher may also decide to stop searching for bugs in a program, at any time k . This is equivalent to setting $P_{k+1} = 0$.

The expected payoff U_k therefore determines the incentive structure for security researchers, given that the bounty program manager can tune R_0 and in some cases, the manager may also set Λ . The utility function may also incorporate non-monetary incentives, such as reputation: Finding a long series of bugs may signal some fitness for a bug bounty program and as thus, create a permanent job opportunity [48]. Similarly, discovery of a rare bug that no other researcher has found before has a strong signaling effect, which can help build a career. However, these strategies are high-risk high-return, therefore they carry additional fame. In the next section, we will calibrate our model to the bug discovery process associated with 35 bounty programs publicly documented on the HackerOne platform.

V. RESULTS

The discovery process in a bug bounty program is driven by the probability to find an additional bug given that k bugs have already been discovered, and program managers aim to maximize B_c , the total number of bugs found. Our results show that the number of bugs discovered is a super-linear function of security researchers who have enrolled in the program (see Figure 2A). While bug bounty programs benefit from the work of a large number of researchers, researchers overall benefit from diversifying their efforts across programs (see Figure 3C). This benefit is particularly tangible regarding the cumulative reward they can extract from their bug hunting activity. In particular, we illustrate how researchers take the strategic decision to enroll in a newly launched program, at the expense of existing ones they have formerly been involved in.

A. Security researcher enrollment determines the success of a bug bounty program

As presented on Figure 2A, we find that the number B_c of bug discovered scales as $B_c \sim h^\alpha$ with $\alpha = 1.10(3)$ and h the number of security researchers enrolled in a program. Since $\alpha > 1$, a bounty program benefits in a super-linear fashion from the enrollment of more researchers. This result is reminiscent of productive bursts and critical cascades of contributions in open source software development [43]: Each enrollment (i.e., *mother* event) initiates a cascade of bug discoveries (i.e., *daughter* events). Here, each cascade stems from a single security researcher (with some exceptions researchers mostly search bugs alone) and the nature of these cascades is captured at the aggregate level by their size as a random variable. As shown on Figure 2B, the distribution of bounty discoveries per researcher and per program follows a power law tail $P(X > x) \sim 1/x^\gamma$ with $\gamma = 1.63(7)$. The first moment of the distribution (i.e., the mean) is however well-defined (as a result of $\gamma > 1$). Moreover, we observe an upper cut-off of the tail with $x_{max} \approx 40$ bounties. Thus, each enrollment of a security researcher in a program provides a statistically bounded amount of new bug discoveries.

B. Security researchers are incentivized to diversify their contributions across bug bounty programs

For security researchers, the main metric is the expected cumulative payoff earned from the accumulation of bounty awards over all programs. This expected payoff is governed by the probability to find a given number of bugs and their associated payoff, as discussed in Section IV. To fully understand the incentive mechanisms at work, we consider 3 perspectives: (i) the expected cumulative down-payment made by bug bounty program managers (see Figure 3A), the expected cumulative payoff from the viewpoint of a security researcher for (ii) one program (see Figure 3B), and for (iii) all programs (see Figure 3C).

The average cumulative down-payment per program exhibits a super-linear scaling as $\sim k^{1.27}$ ($p < 0.001$, $R^2 > 0.99$), while the frequency of bugs P_k is only slightly upwards trended, increasing as $\sim k^{0.13}$ ($p < 0.001$, $R^2 = 0.40$). The expected down-payment by bug

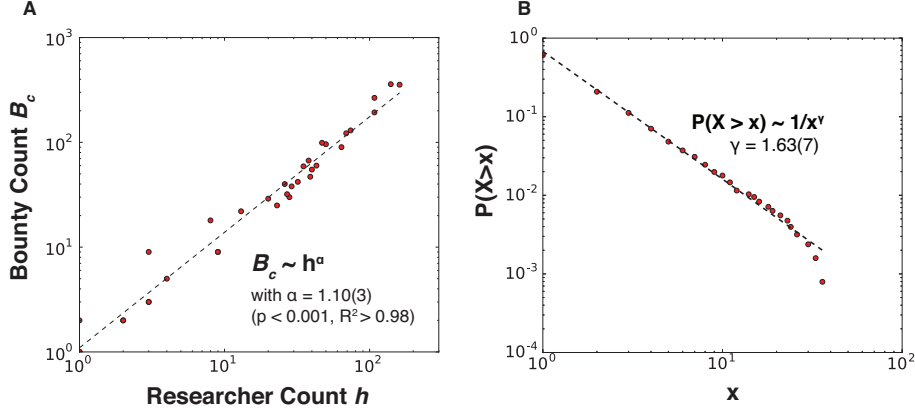


FIG. 2. **A.** The number of bounty discoveries per program B_c scales as h^α with $\alpha = 1.10(3)$ and h the number of security researchers enrolled in a program (fit and confidence interval were obtained by ordinary least squares of the logarithm of researcher and bounty counts). Since $\alpha > 1$, a bounty program benefits in a super-linear fashion to the enrollment of more researchers. **B.** The tail distribution of bounty discoveries per researcher per program follows a power law distribution $P(X > x) \sim 1/x^\gamma$ with $1 < \gamma = 1.63(7) < 2$ (obtained by maximum likelihood estimation and confidence interval bootstrapping, following [21, 50]). The distribution is therefore relatively well bounded (with the first moment being well-defined). Furthermore, we observe an upper cut-off of the tail with $x_{max} \approx 400$ bounties. Thus, from **A.** and **B.** combined, we find that the number of vulnerabilities is mainly driven by the number of researchers enrolled in programs.

bounty program managers therefore scales as $\sim k^{1.40}$. This is a considerable super-linear increase (as $k \rightarrow \infty$), which casts questions on the long-term sustainability of bug bounty programs.

From the security researcher's viewpoint and her expected payoff from a single bug bounty program, the increase of average cumulative reward ($R_k \sim k^{1.40}$) does not offset the fast decay of probability ($P_k \sim k^{-1.85}$) to find a vulnerability of rank k . The expected payoff therefore follows $U_k \sim k^{-0.45}$, which clearly does not bring high incentives to explore in depth a bug bounty program. It is important to note however, that the bug bounty manager cannot fix P_k , which is a genuine feature of bug discovery by humans. To maintain positive individual incentives, the manager should set an incremental reward such that $R_k \sim k^\alpha$ with $\alpha > 1.40$, which in turn would worsen the down-payment function both in terms of incremental expenditures and in exploration of bugs with higher ranks. This approach does

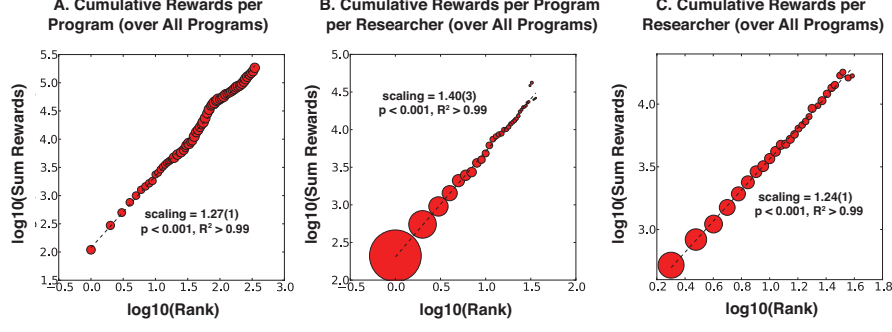


FIG. 3. **A.** (Log-)binned cumulative down-payment per program over all public programs on the HackerOne platform, scales as $R_k \sim k^{1.27}$ ($p < 0.001$, $R^2 > 0.99$), with k the rank. Each log-bin shows the mean value and the circle sizes depict the number of values in each bin (i.e., the rank frequency). The super-linear *scaling* relationship between the cumulative reward and the rank shows that reward increases as a function of k . However, the frequency of vulnerabilities P_k is only slightly upwards trended increasing as $\sim k^{0.13}$ ($p < 0.001$, $R^2 = 0.40$). **B.** Considering the opposite figure from the viewpoint of researcher's expected payoff when enrolling in a single bug bounty program, the super-linear effect is much stronger ($R_k \sim k^{1.40}$ with $p < 0.001$ and $R^2 > 0.99$). However, the frequency decays following a power law of the form $P_k \sim k^{-1.85}$ ($p < 0.001$, $R^2 = 0.97$). **C.** Over all bug bounty programs, security researchers have another expected payoff: the reward scaling is smaller ($R_k \sim k^{1.24}$ with $p < 0.001$, $R^2 > 0.99$), yet the frequency of bug discoveries decays much slower as a function of rank $P_k \sim k^{-1.05}$ ($p < 0.001$, $R^2 = 0.85$).

not consider possible individual human hard limits preventing finding additional bugs, which would drive iterative costs c_k sufficiently high as k gets large. In that latter case, setting higher reward incentives would have no effect.

Security researchers tend to switch from one bounty program to another program [13, 14]. The strategy can be assimilated to portfolio diversification [51]. Over all bug bounty programs, security researchers have another much more favorable expected payoff: The reward scaling is smaller ($R_k \sim k^{1.24}$ with $p < 0.001$, $R^2 > 0.99$), yet the frequency of bug discoveries decays much slower as a function of rank $P_k \sim k^{-1.05}$ ($p < 0.001$, $R^2 = 0.85$). Therefore, over all bounty programs, security researchers have an increasing, yet marginally decreasing, incentive to explore higher ranks as $U_k \sim k^{0.19}$. In a nutshell, security researchers

have an incentive to keep searching for bugs on a large variety of bug bounty programs.

C. Influence of newly launched programs on researcher behaviors

As security researchers weigh their strategic choice to switch their attention from one program to another, the time factor is determinant because the expected payoff is dependent on the current vulnerability rank, which maps into the time dimension (i.e, the duration between two discoveries is drawn from a characteristic random variable, which is not considered here). While a researcher may decide to switch at any time, the most obvious moment is when a new program is being launched: Incentives shift suddenly, and security researchers may decide to abandon older programs at the expense of the new program with fresh bug discovery opportunities. However, a number of factors may influence their decision: The reputation of the organization launching the program (it brings more fame to submit a bug to e.g., Twitter compared to a less famous organization), the amount of reward, and the relative time between an old program and the newest one. To encompass the effects of new public bug bounty programs on incumbent programs, we aim to test 3 hypotheses:

- **H1:** An existing bounty program will receive less reports when more new programs are launched,
- **H2:** An existing bounty program will receive less reports when bounty rewards provided by newly launched programs is higher,
- **H3:** The number of newly launched programs has a larger impact on the contribution to older programs.

We specify a simple ordinary least square (OLS) regression model as follows:

$$V_{it} = \beta_0 + \beta_1 dP_t + \beta_2 T_{it} + \beta_3 A_{it} + \beta_4 B_{it} + \epsilon_{it}. \quad (3)$$

V_{it} is the number of vulnerability reports received by bounty program i in the month t . dP_t is the number of new programs launched in month t . Hypothesis **H1** predicts that its coefficient (β_1) is negative. T_{it} is the number of months since bounty program i launched. We consider two control variables that could influence researcher's decision [14]. We first incorporate A_i the log of the Alexa rank, which measures web traffic as a proxy of popularity

for organization i . B_i is the log of the average amount of bounty paid per bug by bounty program i . Both A_i and B_i are assumed to remain constant over time. Finally, ϵ_{it} is the unobservable error term. In models **2-4**, we extend the basic model (model **1**) to further study competition occurring between bounty programs. These alternative specifications include:

- **Average bounty of newly launched programs:** Intuitively, if new programs offer higher rewards, they should attract more researchers from existing programs. We calculate the average bounty for all new programs in month t as NB_t in models **2-4**.
- **Interaction between dP_t and T_{it} :** Conceivably, the effect of new programs on existing programs depends on certain characteristics of the latter, such as age. In particular, we ask if a new entrant has more negative effects on older programs compared to younger programs? To examine this, we consider an interaction term between the number of new programs (dP_t) and the age of the program (T_{it}) in models **3-4**. Hypothesis H3 predicts that its coefficient is negative.
- **Program fixed effect:** To better control for program-specific, time-invariant characteristics, e.g., the reputation among researchers, we add program fixed effect in model **4**. The addition of this fixed effect allows us to examine how bug discovery changes over time within each program i .

The regression results are shown in Table I. Consistent with our prediction in Hypothesis **H1**, the coefficient of dP_t is negative and statistically significant in all 4 specifications. *Ceteris paribus*, the launch of new programs reduces the number of vulnerabilities reported to existing programs. In other words, the entry of new programs indeed attracts researcher’s attention away from existing programs, which is consistent with the fast decreasing expected payoff for individuals searching bugs for a specific program. Also, the average bounty paid by new programs ($B_{new,t}$) has a negative effect on existing programs as well, but the coefficient is only significant in model **4**. Again this result is consistent with the theory and Hypothesis **H2**, as researchers have a higher incentive to switch to new programs, if they have more low-hanging fruits and higher bounty.

TABLE I. Regression results.

	(1)	(2)	(3)	(4)
VARIABLES	V_{it}	V_{it}	V_{it}	V_{it}
dP_t	-1.235*** (0.305)	-1.350*** (0.327)	-2.310*** (0.603)	-1.236** (0.515)
A_i	-23.61*** (2.140)	-23.72*** (2.156)	-23.72*** (2.152)	-7.188** (3.473)
B_i	16.64*** (1.311)	16.56*** (1.315)	16.75*** (1.339)	-7.414 (5.698)
T_{it}	-0.690 (0.426)	-0.658 (0.427)	-3.312*** (1.239)	-3.758*** (1.128)
$B_{new,t}$		-0.0445 (0.0280)	-0.0312 (0.0277)	-0.0321* (0.0184)
$T_{it} \times dP_t$			0.106** (0.0431)	0.0755* (0.0406)
Constant	160.2*** (16.12)	170.4*** (18.80)	190.3*** (23.17)	136.5*** (26.17)
Observations	1,212	1,212	1,212	1,212
R-squared	0.314	0.316	0.319	0.647
Program FE	No	No	No	Yes

Robust standard errors in parentheses

*** p<0.01, ** p<0.05, * p<0.1

The interaction coefficients for term $T_{it} \times dP_t$ in models **3** and **4** are positive and statistically significant, so they do not support Hypothesis **H3**. The result shows that the impact of newly launched programs depends on the age of the existing programs: Compared to younger programs, the negative impact of dP_t is smaller for programs with a longer history, i.e., those with larger T_{it} . At first sight, this results may look at odds with the fact that individual expected payoff from a specific program decreases as a function of rank k , and

presumably the older a program the more likely it has a high rank. Thus, the switching effect should be stronger. Perhaps our OLS regression model is limited in the sense that it does account for the absolute activity (which decreases very slowly as $t \rightarrow \infty$, as shown on Figure 1B), instead of the variation rate. Consistent with previous research [14], the regression results also show that a program with higher reputation (A_i) or higher bounty (B_i) is associated with more bugs received in a month. The regression results also show that a program with longer age (T_{it}) is associated with less bugs found. This observation corresponds to the power law decay of bug submission observed following a program launch (c.f., Figure 1B).

VI. DISCUSSION

Finding bugs in software code is one of the oldest and toughest problems in software engineering [3]. While algorithm-based approaches have been developed over the years [20], human verification has remained a prime way for bug hunting. While resorting to the crowd for finding bugs is not new [52], bug bounty programs have recently been promoted by the emergence of bug bounty platforms. Here, we have studied incentive mechanisms across 35 bug bounty programs on HackerOne, one of such platforms. Our results show that the number of discovered bugs and vulnerabilities in a bounty program is super-linearly associated with the number of security researchers. However, the distribution of bugs found per researcher per program is bounded: in a given bug bounty program, the marginal probability of finding additional bugs is decreasing rapidly. On the contrary, security researchers have high incentive to switch among multiple bug bounty programs. We find indeed that each newly launched program has a negative effect on submissions to incumbent bug bounty programs. Furthermore, controlling specifically for monetary incentives, we find that the reward amount for valid bugs in newly launched programs has a negative effect on the number of bug submissions to incumbent programs.

We find quantitative evidence for the incentive mechanisms associated with bug discovery by crowds of security researchers, and help draw practical organization design recommendations for bug bounty platforms such as HackerOne, as well as for organizations managing bug bounty programs.

Our results provide an essential validation step to the theory formulated by Brady et al. [1]. No single security researcher is able to find most bugs in one program. On the contrary, a good bug bounty program involves submissions from a diverse crowd of security researchers. Borrowing to the formulation by Brady et al. of software security as a phenomenon of evolutionary pressure dictated by environmental changes, we shall propose that any additional security researcher involved in a bug bounty program brings a unique combination of skills and mindset, which is at least partially different from all other researchers. This unique perspective is comparable to a slightly changing environment for the software piece under scrutiny, which brings unique opportunities for each security researcher, regardless of the opportunity level of other researchers focused on the same software piece. Yet because people cannot easily change their skills and mindset, once the opportunity has been exploited, finding additional bugs gets much harder, hence pushing toward other opportunities, such as newly launched bug bounty programs.

The intrinsic limited capability by each single security researcher to find a large number of bugs for a specific program (i.e., on a specific software piece) carries a strong justification for the existence of bug bounty programs as a tool for engaging a large and diverse crowd of security researchers, beyond internalized software testing and security research teams. While we do not prescribe here on the seniority and trustworthiness level of the security crowd targeted and engaged in a specific program, we may however discuss the *Uber* bug bounty program launched in 2016 [48]. This organization has designed its program as a way to select and hire a hand *security czars* from a larger crowd. Although there is certainly nothing wrong with hiring a security expert in an opportunistic manner, our results rather suggest that systematically using bug bounty programs for hiring purpose may reveal counter-productive on the long term. Security researchers will be likely to tune their expectations and behaviors toward getting a job. The approach implemented by Uber may reduce engagement of researchers who don't expect to get a job offer. Thus, it could limit the involvement of a larger crowd and its renewal, as more permanent security positions get filled.

The strategy followed by Uber for its bug bounty program is also interesting from a

theoretical perspective: Uber is following a well-known strategy first described by Ronald Coase [44], which prescribes that if an organization has repeated interactions on the market with the same counterpart – or *ceteris paribus* a similar counterpart, then the organization is better off internalizing the resource in order to avoid repeated transaction costs. Hence, Uber considers that security researchers as *substitute goods*, while our results and actually the mere existence of bug bounty programs, rather demonstrate that security researchers are *complements*, at least partially. The distinction between substitutes and complements regarding security researchers brings a fundamental justification for the existence and the future development of bug bounty programs as market places for trading bugs and vulnerabilities [11].

Yet, the organization designs of bug bounties programs and online platforms supporting them are still pretty much empirical. The validation step performed here provide additional theoretical insights. On the one hand, these insights shall be useful to formulate recommendations. On the other hand, they help identify blind spots, which will deserve future theoretical and empirical research efforts. We propose 3 major recommendations that may significantly improve the efficiency of bug bounty programs and the online platforms hosting them, as well as maximize the engagement of security researchers.

1. *Encourage enrollment, mobility and renewal*

Bug bounty programs shall encourage mobility by devoting resources to the recruitment of security researchers who were not previously involved in the program, rather than making effort to keep security researchers who have already well performed engaged. Mobility increases chances to find security researchers with genuine skills and mindset, who in turn will find additional bugs. Similarly, bug bounty platforms have the possibility to encourage mobility across bug bounty programs. We have found that mobility across programs already exists, in particular mobility from old to newly launched programs. We also advocate the active recruitment of new security researchers by both bug bounty programs and platforms. For example, the bug bounty platform may feature older programs to security researchers who have recently enrolled on the platform.

2. *Feature major changes for front-loading*

The launch of a new bug bounty program is a unique moment that attracts a large number of security researchers. Yet front-loading may also be organized when a software piece received a major update with higher probability of finding bugs. Bug bounty program managers are encouraged to feature significant changes in the codebase, to help security researchers focus on issues they have not been exposed previously. Organizing engagement in order to match demand with supply is a token of fairness for security researchers who may appreciate to be guided to windows of opportunity. This approach may also help the bug bounty program manager to steer the attention of security researchers toward more pressing security issues. Front-loading can also be organized with a temporary bug bounty reward increase. Additionally, dynamic adaptation of incentives can help manage contingencies associated with the management of submissions, for instance by reducing reward during a temporary overload.

3. *Organize fluid and low-transaction cost markets*

One overarching concern with trading bugs and vulnerabilities is the temptation by security researchers to consider selling their bugs on the black market. One way is to streamline transactions costs associated with bug submission and reward operations. Encouraging mobility without providing market fluidity indeed exposes to the risk that more bugs get submitted more often on the black market. Our recommendation is reminiscent of the strategy followed by *Apple Inc.*: by offering cheap enough online music, easy to download on *iTunes*, Apple Inc. was able to capture most of the online music black market, such as on *Napster*. Bug bounty programs face similar challenges and opportunities to capture a larger market share by reducing transaction costs and alleviating uncertainties associated with being involved on the black market.

Our recommendations stem directly from the validation step performed. They show the importance of having a clear view of the theoretical and empirical underpinnings of the mechanisms of bug bounty programs and of platforms organizing them. Mobility, front-loading and fluidity may be organized either through top-down bureaucracy or by setting

market incentives right. The relative advantages bureaucracy and market organizations shall be further studied. Our recommendations for designing bug bounty programs, apply indistinctly to public and private bug bounties. Private bug bounty programs however face additional effort to encourage enrollment, mobility, renewal and front-loading, while at the same time curating the security researchers invited to participate in the private program.

Our study would benefit from additional empirical research using data which is currently not available from public sources. First, our study is limited by the impossibility to estimate the resource costs that security researchers bear when searching for bugs (e.g., time spent). This information would help further test and understand our theory and results which show that it exists physical limitations regarding the possibility for an individual to find an arbitrarily large number of bugs. Information on the cost functions would also bring further insights on refined expected utility functions by security researchers, in particular the distinction between expected monetary rewards and effort devoted to reputation seeking.

We may also further question how bug bounty program operations impact the motivation of researchers: For example, bug bounty programs may be temporarily overloaded with submissions [13, 14] associated with priority queueing and contingent delays [42]. Delays and contingencies, such as timing and discounting effects, contribute to increase transaction costs and uncertainties for security researchers. Deeper understanding of the dynamics associated with bug bounty program operations may help establish a benchmark on the performance of organization designs and their implementations.

Finally, there is evidence that security researchers specialize: researchers typically have specialized skills and unique mindset. The competitive environment associated with bug bounty programs reinforces incentives to specialize. Two types of specialization exist in bug bounty programs: program-specific and bug-specific [13, 14]. *Program-specific* specialization is associated with the knowledge, experience and skill of finding vulnerabilities in websites and software products in one particular program. Since specialization is relatively unique to the program, a specialized researcher has less options regarding switching between programs. *Vulnerability-specific* specialization is associated with knowledge and skills of a particular type of vulnerability, which can exist in many different products. Researchers with

vulnerability-specific specialization have stronger incentive to explore different bug bounty programs. Specialization must be accounted for when implementing organization design recommendations. In some circumstances, it may be desirable to attract a crowd of diverse yet specialized security researchers. Depending on the specialization required, targeting specific security researchers may however restrict the diversity of the resource pool. Specialization is also associated with the concept of “skills and mindset”, which we have introduced here to explain the observed hard limits regarding the number of bugs a single researcher can find. This notion deserves a thorough definition, as well as theory and empirical testing.

VII. CONCLUSION

In this paper, we have investigated how crowds of security researchers hunt software vulnerabilities and how they report to bug bounty programs on dedicated online platforms. Consistent with the famous adage “Given enough eyeballs, all bugs are shallow” by Eric Raymond [29], we have found that security researchers face challenging difficulties when trying to uncover large numbers of bugs in a same bounty program: the super-linear reward increase for each new bug found does not counterbalance the sharply decreasing probability of finding new bugs by the same person. This result is consistent with the theory proposed by Brady et al. on maximized entropy of bug discovery as an evolutionary process following adaptation to changing environments [1]: each security researcher tests software within an environment bounded by her skills and mindset. This result brings a fundamental justification for the existence of markets for bugs, beyond internalized security operations and research: bug bounty programs offer a way to capitalize on these diverse *environments* provided by the involvement of many security researchers. Yet difficulties for researchers to find large numbers of bugs in one bug bounty program bring incentives for mobility across programs. In particular, we find that the launch of new bug bounty programs has a negative effect on incumbent programs regarding bug submissions. We thus propose 3 organization design recommendations. First, enrollment, mobility and renewal shall be encouraged across bug bounty programs as well as across bug bounty platforms. Second, bug bounty program managers shall feature major changes in the codebase and get organized for front-loading, in order to help security researchers focus on outstanding issues. Finally, recognizing that

market structures are probably a prime way to mobilize large crowds of researchers, we recommend to organize fluid market transactions, in order to reduce as much as possible uncertainties for security researchers.

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